This is the (continuous) line set cover problem. The problem is NP-hard, and there are FPT algorithms [1].

References

[1] Stefan Langerman and Pat Morin. Covering things with things. Discrete & Computational Geometry, $33(4):717-729,\ 2005.$