Let n denote the number of steps and let m denote the array length.

- 1. DP.  $O(n \cdot \min(n, m))$ .
- 2. If we cannot stay in the same place: DP, the answer is

$$\binom{n}{n/2} - \sum_{i \geq 1} \left( \binom{n}{n/2 - (i-1)m - (2i-1)} - \binom{n}{n/2 + im + 2i} \right) - \sum_{i \geq 1} \left( \binom{n}{n/2 + im + (2i-1)} - \binom{n}{n/2 - im - 2i} \right).$$

O(n). https://www.zhihu.com/question/346654767/answer/1110765408

Now we can stay in the same place, and the answer is

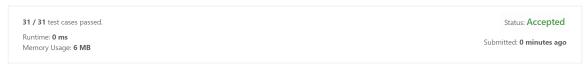
$$\begin{split} \sum_{n' \leq n, \ n' \text{ even}} \binom{n}{n'} \bigg[ \binom{n'}{n'/2} - \sum_{i \geq 1} \left( \binom{n'}{n'/2 - (i-1)(m-1) - (2i-1)} \right) - \binom{n'}{n'/2 + i(m-1) + 2i} \right) \\ - \sum_{i \geq 1} \left( \binom{n'}{n'/2 + i(m-1) + (2i-1)} - \binom{n'}{n'/2 - i(m-1) - 2i} \right) \bigg]. \end{split}$$

We can compute the solution in  $O(n \cdot \frac{n}{m})$  time, by preprocessing factorial mod p and its inverse, then each binomial can be computed in O(1) time.

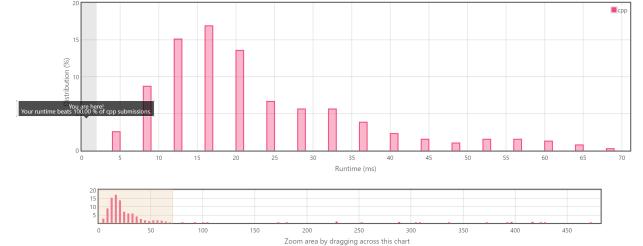
If  $m \leq \sqrt{n}$ , use the first algorithm, otherwise use the second algorithm.  $O(n\sqrt{n})$ .

## Number of Ways to Stay in the Same Place After Some Steps

## **Submission Detail**







## References