1. DP. $O(n^2)$.
2. $O(n)$. [1].

References

[1] Daxin Zhu and Xiaodong Wang. An optimal algorithm for a computer game in linear time. In *International Conference on Smart Computing & Communication*, 2016.