This is [HAOI2009]求回文串. Reduce to counting inversions https://leetcode-cn.com/problems/minimum-number-of-moves-to-make-palindrome/solution/de-dao-hui-wen-chuan-de-zui-shao-cao-zuo-nnis/. $O(n \log n)$ or $O(n\sqrt{\log n})$.