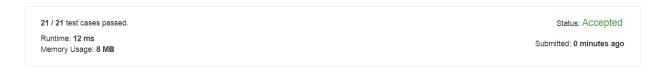
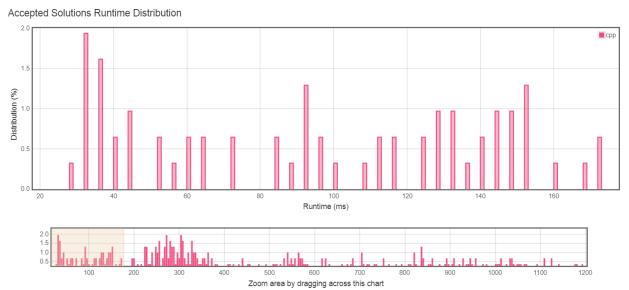
We can reduce the problem to 2D LIS. Let r[i] denote the rank of a[i] in array b (a minor issue is when $\exists j$ s.t. a[i] = b[j]), then the problem is equivalent to find the longest increasing subsequence in a, where a[i] can be followed by a[j] if a[i] < a[j] and we can change $a[i+1,\ldots,j-1]$ to elements in b, which is equivalent to $r[j] - r[i] \ge j - i - 1$, i.e. $r[j] - j \ge r[i] - i - 1$ (the -1 shouldn't affect much). cite? Similar to the 1D LIS solution, we can dynamically maintain a set of disjoint staircase structures in 2D, where the i-th staircase represents the points with LIS length i ending at it. $O(\frac{\log n}{\log \log n})$ using dynamic planar orthogonal point location [1].





Runtime: $12\ ms$, faster than 100.00% of C++ online submissions for Make Array Strictly Increasing.

Memory Usage: 8 MB, less than 100.00% of C++ online submissions for Make Array Strictly Increasing.

References

[1] Timothy M Chan and Konstantinos Tsakalidis. Dynamic planar orthogonal point location in sublogarithmic time. In 34th International Symposium on Computational Geometry (SoCG 2018). Schloss Dagstuhl-Leibniz-Zentrum fuer Informatik, 2018.