If  $n = \prod_i p_i^{q_i}$ , then the number of prime factors (not distinct) is  $\sum_i q_i$ , and the number of nice divisors is  $\prod_i q_i$ . Greedily use 2 and 3.  $O(\log n)$ .

## References