divide and conquer, compare the middle elements of two arrays, and recurse. $O(\log(n+m))$.

in general, finding the t-th largest element in the union of k sorted array with respective sizes $n_1, \ldots, n_k$ takes time:

1. $O(\sum_{i=1}^{k} \log n_i)$ [1] (and its erratum [2]).

output sensitive version: $O(k + \sum_{i=1}^{k} \log(t_i + 1))$, where t_i is the number of items of the i-th list within the t-th largest elements [3].

https://cstheory.stackexchange.com/questions/20944/select-in-union-of-sorted-arrays-already-known/20955#20955.

2. let $p = \min\{k, t\}$, the running time is $\Theta(k + p \log \frac{t}{p})$ [4].

i.e. if $t \geq k$, $O(k \log \frac{t}{k})$. if $t < k$, $O(k)$.

References

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