1. DP. let g[i][j] denote the maximum floor we can detect using i moves and j eggs.

$$\begin{cases} g[i][j] = g[i-1][j-1] + g[i-1][j] + 1 \ (i,j>1) \\ g[1][j] = 1 \end{cases}$$

 $O(\sqrt{n})$.

国家集训队2004论文集: 朱晨光《优化,再优化! --从《鹰蛋》一题浅析对动态规划算法的优化》 https://wenku.baidu.com/view/286731b765ce05087632131b.html

2. use generating functions to optimize the calculation for g. $g[i][j] = \sum_{k=0}^{j} {j \choose k} - 1$. this algorithm is actually for a more general problem: 1893: Ural EE see https://blog.csdn.net/limboman/article/details/53366049

References