

This is the multi-way number partitioning problem, which is NPC.

1. binary search, and let  $f[i][j]$  denote the minimum total time of the  $j$ -th worker can have among valid solutions that use  $j$  workers to finish job subset  $i$ .  $O(2^n \cdot n^2 \log U)$ , and we can assume  $U \leq 2^n$ .
2. let  $f[i][j]$  be a pair of integers, the first integer denote the minimum number of workers needed to finish job subset  $i$ , and the second denote the minimum total time of the last worker.  $O(2^n \cdot n \log U)$ .
3. binary search, suppose we want to decide whether the answer  $\leq mid$ . construct a vector  $A = \langle a_0, \dots, a_{2^n-1} \rangle$ , where  $a_i = 1$  if the subset  $i$  has sum  $\leq mid$ , otherwise  $a_i = 0$ . Use FWT to compute  $A^k$ , and  $ans \leq mid$  iff  $A^k[2^n - 1] > 0$ .  $O(2^n \cdot n \log U)$ .

## References