1. Stack and simulation, repeatedly take gcd. $O(n \log U)$ or $O(n + \sqrt{U} \operatorname{polylog} U)$.