optimize DP by binary search. $O(n \log n)$.

lower bound: $\Omega(n \log n)$ in comparison-based model [1].

References

[1] Michael L Fredman. On computing the length of longest increasing subsequences. Discrete Mathematics, 11(1):29-35, 1975.