

1. offline, reduce to sorting.  $O(\text{sort}(n))$ .
2. reduce to one-dimensional range reporting. static:  $O(1)$  query time [1], dynamic:  $O(\log \log w)$  query time [2]. but the preprocessing time is not faster than sorting.
3. divide into buckets with size  $\Theta(d)$ , and record the minimum and maximum value within *arr2* in each bucket.  $O(n)$ .

## References

- [1] Stephen Alstrup, Gerth Brodal, and Theis Rauhe. Optimal static range reporting in one dimension. In *Proceedings of the thirty-third annual ACM symposium on Theory of computing*, pages 476–482, 2001.
- [2] Christian Worm Mortensen, Rasmus Pagh, and Mihai Ptraşcu. On dynamic range reporting in one dimension. In *Proceedings of the thirty-seventh annual ACM symposium on Theory of computing*, pages 104–111, 2005.