

We can arbitrarily permute the elements in the same connected component (which can be proved by induction). For an element  $x$ , add an edge between  $p$  and  $\frac{x}{p}$ , where  $p$  divides  $x$ . Sort each connected component by counting sort.  $O(U)$ .

## References