meet in the middle+hashing: for $i=1,\ldots,n$, store sum of all pairs in $a[1\ldots i-1]$ in the hash table, query sum of -a[i]-a[j] for $j=i+1,\ldots,n$. $O(n^2)$ expected, or $O(n^2\log n)$ deterministic by sorting. for k-sum, the best known algorithm is $O(n^{\lceil d/2 \rceil}/poly \log n)$. can reduce to 2-sum when k is even, or reduce to an unbalanced 3-sum when k is odd.

https://cs.stackexchange.com/questions/2973/generalised-3sum-k-sum-problem

lower bound: no $n^{o(k)}$ algorithm for k-sum, if Strong ETH holds [1].

References

[1] Mihai Pătrașcu and Ryan Williams. On the possibility of faster sat algorithms. In *Proceedings of the twenty-first annual ACM-SIAM symposium on Discrete Algorithms*, pages 1065–1075. SIAM, 2010.