We can assume $U \leq n$ after sorting.

1. build segment tree on id, and record the maximum room size in each interval. $O(n \log n)$.

2. vEB tree. $O(n \log \log n)$.

References