Reduce to predecessor search. For addRange, merge intervals by enumerating them, an amortized analysis shows there are only $O(n)$ pred searches. $O(n \cdot \text{pred}(n))$.

References