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1. algorithm

#include <algorithm> #include <numeric>

Algo	Params	Funcion
sort, stable_sort	f, l	ordena el intervalo
nth_element	f, nth, l	void ordena el n-esimo, y
		particiona el resto
fill, fill_n	f, l / n, elem	void llena [f, l) o [f,
		f+n) con elem
lower_bound, upper_bound	f, l, elem	it al primer / ultimo donde se
		puede insertar elem para que
		quede ordenada
binary_search	f, l, elem	bool esta elem en [f, l)
copy	f, l, resul	hace $resul+i=f+i \ \forall i$
find, find_if, find_first_of	f, l, elem	it encuentra i \in [f,l) tq. i $=$ elem,
	/ pred / f2, l2	$pred(i), i \in [f2,l2)$
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, l, f2, l2	busca $[f2,l2) \in [f,l)$
replace, replace_if	f, l, old	cambia old / pred(i) por new
	/ pred, new	
reverse	f, 1	da vuelta
partition, stable_partition	f, l, pred	pred(i) ad, !pred(i) atras
min_element, max_element	f, l, [comp]	$it \min, \max de [f,l]$
$lexicographical_compare$	f1,l1,f2,l2	bool con [f1,l1];[f2,l2]
$next/prev_permutation$	f,l	deja en [f,l) la perm sig, ant
set_intersection,	f1, l1, f2, l2, res	[res,) la op. de conj
set_difference, set_union,		
set_symmetric_difference,		
push_heap, pop_heap,	f, l, e / e /	mete/saca e en heap [f,l),
make_heap		hace un heap de [f,l)
is_heap	f,l	bool es [f,l) un heap
accumulate	f,l,i,[op]	$T = \sum /\text{oper de [f,l)}$
$inner_product$	f1, l1, f2, i	$T = i + [f1, l1) \cdot [f2,)$
partial_sum	f, l, r, [op]	$r+i = \sum /oper de [f,f+i] \forall i \in [f,l)$
_builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
_builtin_popcount	unsigned int	Cant. de 1's en x.
_builtin_parity	unsigned int	1 si x es par, 0 si es impar.
$_{-}$ builtin $_{-}$ XXXXXXII	unsigned ll	= pero para long long's.

2. Estructuras

2.1. RMQ (static)

Dado un arreglo y una operación asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restricción: LVL ≥ ceil(logn); Usar [] para llenar arreglo y luego build().

```
1 | struct RMQ{
     #define LVL 10
2
     tipo vec[LVL] [1<<(LVL+1)];
     tipo &operator[](int p){return vec[0][p];}
     tipo get(int i, int j) {//intervalo [i,j)
5
       int p = 31-_builtin_clz(j-i);
6
       return min(vec[p][i],vec[p][j-(1<<p)]);</pre>
7
     }
8
     void build(int n) {//O(nlogn)
9
       int mp = 31-__builtin_clz(n);
10
       forn(p, mp) forn(x, n-(1<<p))
11
         vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
12
     }
13
14 };
```

2.2. RMQ (dynamic)

```
1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
        sobre el rango [i, j).
   #define MAXN 100000
   #define operacion(x, y) max(x, y)
   const int neutro=0;
   struct RMQ{
5
     int sz;
6
     tipo t[4*MAXN];
7
     tipo &operator[](int p){return t[sz+p];}
8
     void init(int n){//O(nlgn)
9
       sz = 1 \ll (32-\_builtin\_clz(n));
10
       forr(i, sz, 2*sz) t[i]=neutro;
11
12
     void updall(){//0(n)}
13
       dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);}
14
     tipo get(int i, int j){return get(i,j,1,0,sz);}
15
     tipo get(int i, int j, int n, int a, int b)\frac{1}{0}
16
       if(j<=a || i>=b) return neutro;
17
       if(i<=a && b<=j) return t[n];
18
```

```
int c=(a+b)/2:
19
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
20
21
     void set(int p, tipo val){//O(lgn)
22
       for(p+=sz; p>0 && t[p]!=val;){
23
         t[p]=val;
24
         p/=2;
25
         val=operacion(t[p*2], t[p*2+1]);
26
27
    }
   }rmq;
29
   //Usage:
31 | cin >> n; rmg.init(n); forn(i, n) cin >> rmg[i]; rmg.updall();
                            2.3. RMQ (lazy)
1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
        sobre el rango [i, j).
typedef int Elem;//Elem de los elementos del arreglo
   typedef int Alt;//Elem de la alteracion
   #define operacion(x,y) x+y
   const Elem neutro=0; const Alt neutro2=0;
   #define MAXN 100000
   struct RMO{
     int sz:
     Elem t[4*MAXN]:
     Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem
10
     Elem &operator[](int p){return t[sz+p];}
11
     void init(int n){//O(nlgn)
12
       sz = 1 \ll (32-\_builtin\_clz(n));
13
       forr(i, sz, 2*sz) t[i]=neutro;
14
       forn(i, 2*sz) dirty[i]=neutro2;
15
16
     void push(int n, int a, int b){//propaga el dirty a sus hijos
17
       if(dirty[n]!=0){
18
         t[n]+=dirty[n]*(b-a);//altera el nodo
19
         if(n<sz){
20
           dirty[2*n]+=dirty[n];
21
           dirty[2*n+1]+=dirty[n];
22
         }
23
         dirty[n]=0;
24
25
    }
26
```

```
Elem get(int i, int j, int n, int a, int b){\frac{1}{0}}
27
       if(j<=a || i>=b) return neutro;
28
       push(n, a, b);//corrige el valor antes de usarlo
29
       if(i<=a && b<=j) return t[n];</pre>
30
       int c=(a+b)/2;
31
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
32
33
     Elem get(int i, int j){return get(i,j,1,0,sz);}
34
     //altera los valores en [i, j) con una alteracion de val
35
     void alterar(Alt val, int i, int j, int n, int a, int b)\{//0(lgn)\}
36
       push(n, a, b);
37
       if(j<=a || i>=b) return;
38
       if(i<=a && b<=j){
39
         dirty[n]+=val;
         push(n, a, b);
41
         return;
42
       }
43
       int c=(a+b)/2;
44
       alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
45
       t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
46
     }
47
     void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
  |}rmq;
49
```

2.4. Fenwick Tree

```
//For 2D threat each column as a Fenwick tree, by adding a nested for in
        each operation
  struct Fenwick{
     static const int sz=1000001;
     tipo t[sz];
4
     void adjust(int p, tipo v){//valid with p in [1, sz), O(lgn)
       for(; p<sz; p+=(p&-p)) t[p]+=v; }</pre>
6
     tipo sum(int p){//cumulative sum in [1, p], O(lgn)
       tipo s=0;
8
       for(; p; p-=(p&-p)) s+=t[p];
9
       return s;
10
11
     tipo sum(int a, int b){return sum(b)-sum(a-1);}
12
     //get largest value with cumulative sum less than or equal to x;
13
     //for smallest, pass x-1 and add 1 to result
14
     int getind(tipo x) {//0(lgn)
15
         int idx = 0, mask = N;
16
```

```
while(mask && idx < N) {
17
            int t = idx + mask;
18
          if(x >= tree[t])
19
               idx = t, x -= tree[t];
20
            mask >>= 1;
21
22
          return idx;
23
     }
24
<sub>25</sub> };
```

2.5. Union Find

```
struct UnionFind{
vector<int> f;//the array contains the parent of each node
void init(int n){f.clear(); f.insert(f.begin(), n, -1);}
int comp(int x){return (f[x]==-1?x:f[x]=comp(f[x]));}//0(1)
bool join(int i, int j) {
   bool con=comp(i)==comp(j);
   if(!con) f[comp(i)] = comp(j);
   return con;
}
return con;
}
```

2.6. Disjoint Intervals

```
bool operator (const ii &a, const ii &b) {return a.fst <b.fst;}
   //Stores intervals as [first, second]
   //in case of a collision it joins them in a single interval
   struct disjoint_intervals {
     set<ii>> segs;
5
     void insert(ii v) {//O(lgn)
6
       if(v.snd-v.fst==0.) return;//0J0
7
       set<ii>>::iterator it.at:
8
       at = it = segs.lower_bound(v);
9
       if (at!=segs.begin() && (--at)->snd >= v.fst)
10
         v.fst = at->fst, --it;
11
       for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))</pre>
         v.snd=max(v.snd, it->snd);
13
       segs.insert(v):
14
15
<sub>16</sub> | };
```

2.7. RMQ (2D)

```
1 | struct RMQ2D{
                                                                                          11 n[LMAX];
                                                                                   6
     static const int sz=1024;
                                                                                          bint(11 x=0){
2
                                                                                   7
     RMQ t[sz];
                                                                                              1=0;
3
     RMQ &operator[](int p){return t[sz/2+p];}
                                                                                              forn(i, LMAX){
4
     void build(int n, int m){\frac{1}{0}}
                                                                                                   n[i]=x BASE;
       forr(v, sz/2, sz/2+m)
                                                                                                   x/=BASE;
                                                                                   11
         t[v].build(m);
                                                                                                  1+=!!x||!i;
                                                                                   12
       forr(y, sz/2+m, sz)
                                                                                              }
                                                                                   13
8
         forn(x, sz)
                                                                                          }
9
                                                                                   14
           t[v].t[x]=0;
                                                                                          bint(string x){
10
       dforn(y, sz/2)
                                                                                          l=(x.size()-1)/BASEXP+1;
11
                                                                                   16
         forn(x, sz)
                                                                                              fill(n, n+LMAX, 0);
12
                                                                                   17
           t[y].t[x]=max(t[y*2].t[x], t[y*2+1].t[x]);
                                                                                              ll r=1:
13
                                                                                   18
     }
                                                                                              forn(i, sz(x)){
                                                                                   19
14
     void set(int x, int y, tipo v){//O(lgm.lgn)
                                                                                                  n[i / BASEXP] += r * (x[x.size()-1-i]-'0');
15
       v + = sz/2:
                                                                                                   r*=10; if(r==BASE)r=1;
                                                                                   21
16
       t[y].set(x, v);
                                                                                              }
17
                                                                                   22
                                                                                          }
       while(y/=2)
18
         t[y].set(x, max(t[y*2][x], t[y*2+1][x]));
                                                                                          void out(){
19
     }
                                                                                          cout << n[l-1];
20
                                                                                          dforn(i, l-1) printf("%6.61lu", n[i]);//6=BASEXP!
     //0(lgm.lgn)
                                                                                   26
21
     int get(int x1, int y1, int x2, int y2, int n=1, int a=0, int b=sz/2){
22
                                                                                   27
       if(y2<=a || y1>=b) return 0;
                                                                                        void invar(){
                                                                                   28
23
       if(y1<=a && b<=y2) return t[n].get(x1, x2);
                                                                                          fill(n+1, n+LMAX, 0);
                                                                                   29
24
       int c=(a+b)/2;
                                                                                          while(1>1 && !n[1-1]) 1--;
                                                                                   30
25
       return max(get(x1, y1, x2, y2, 2*n, a, c),
                                                                                       }
                                                                                   31
26
            get(x1, y1, x2, y2, 2*n+1, c, b));
                                                                                   32
27
     }
                                                                                      bint operator+(const bint&a, const bint&b){
28
                                                                                        bint c;
                                                                                   34
29
   //Example to initialize a grid of M rows and N columns:
                                                                                          c.1 = max(a.1, b.1);
   RMQ2D rmq;
                                                                                          11 q = 0;
31
                                                                                   36
  forn(i, M)
                                                                                          forn(i, c.1) q += a.n[i]+b.n[i], c.n[i]=q %BASE, q/=BASE;
    forn(j, N)
                                                                                          if(q) c.n[c.l++] = q;
33
       cin >> rmq[i][j];
                                                                                          c.invar():
35 | rmq.build(N, M);
                                                                                          return c;
                                                                                   40
                               2.8. Big Int
                                                                                      pair<br/>bint, bool> lresta(const bint& a, const bint& b) // c = a - b
                                                                                      {
                                                                                   43
                                                                                        bint c;
1 #define BASEXP 6
                                                                                   44
                                                                                          c.1 = max(a.1, b.1);
  #define BASE 1000000
                                                                                          11 q = 0;
  #define LMAX 1000
                                                                                          forn(i, c.1) q += a.n[i]-b.n[i], c.n[i]=(q+BASE) %BASE, q=(q+BASE)/
  struct bint{
                                                                                   47
                                                                                              BASE-1;
       int 1;
5
```

```
c.invar():
48
       return make_pair(c, !q);
49
50
   bint& operator-= (bint& a, const bint& b){return a=lresta(a, b).first;}
   bint operator- (const bint&a, const bint&b){return lresta(a, b).first;}
   bool operator (const bint&a, const bint&b) {return !lresta(a, b).second
   bool operator<= (const bint&a, const bint&b){return lresta(b, a).second
   bool operator==(const bint&a, const bint&b){return a <= b && b <= a;}
   bint operator*(const bint&a, ll b){
       bint c;
57
       11 q = 0;
58
       forn(i, a.l) q += a.n[i]*b, c.n[i] = q \text{BASE}, q/=BASE};
59
       c.1 = a.1:
60
       while(q) c.n[c.l++] = q \text{ $\beta$ASE}, q/=BASE;
61
       c.invar();
62
       return c;
63
64
   bint operator*(const bint&a, const bint&b){
65
       bint c;
66
       c.1 = a.1+b.1;
67
       fill(c.n, c.n+b.1, 0);
68
       forn(i, a.1){
69
           11 q = 0;
70
           forn(j, b.1) q += a.n[i]*b.n[j]+c.n[i+j], c.n[i+j] = q BASE, q
71
               /=BASE;
           c.n[i+b.1] = q;
72
       }
73
       c.invar();
74
       return c;
75
76
   pair<br/>
\frac{1}{c} = \frac{a}{b}; rm = a %b
77
     bint c:
78
     11 \text{ rm} = 0:
79
     dforn(i, a.1){
80
               rm = rm * BASE + a.n[i];
81
               c.n[i] = rm / b:
82
               rm %= b;
83
84
       c.1 = a.1;
85
       c.invar();
86
       return make_pair(c, rm);
87
```

```
88 | }
   bint operator/(const bint&a, ll b){return ldiv(a, b).first;}
   11 operator%(const bint&a, 11 b){return ldiv(a, b).second;}
   pair<bint, bint> ldiv(const bint& a, const bint& b){
     bint c;
92
        bint rm = 0;
93
        dform(i, a.1){
94
            if (rm.l==1 && !rm.n[0])
95
                rm.n[0] = a.n[i];
96
            else{
97
                dforn(j, rm.l) rm.n[j+1] = rm.n[j];
98
                rm.n[0] = a.n[i];
99
                rm.l++:
100
            }
101
            ll q = rm.n[b.1] * BASE + rm.n[b.1-1];
102
            ll u = q / (b.n[b.l-1] + 1);
            ll v = q / b.n[b.l-1] + 1;
104
            while (u < v-1){
                11 m = (u+v)/2:
106
                if (b*m \le rm) u = m;
                else v = m;
108
109
            c.n[i]=u;
110
            rm-=b*u;
111
       }
112
      c.l=a.l;
113
        c.invar();
114
        return make_pair(c, rm);
115
116
   bint operator/(const bint&a, const bint&b){return ldiv(a, b).first;}
bint operator %(const bint&a, const bint&b) {return ldiv(a, b).second;}
                               2.9. Modnum
```

```
struct mnum{
static const tipo mod=12582917;
tipo v;
mnum(tipo v=0): v(v mod) {}
mnum operator+(mnum b){return v+b.v;}
mnum operator-(mnum b){return v>=b.v? v-b.v : mod-b.v+v;}
mnum operator*(mnum b){return v*b.v;}
mnum operator^(int n){
if(!n) return 1;
```

```
return n \% ? (*this)^(n/2) * (this) : (*this)^(n/2);}
                                                                                              pull(t);
                                                                                   38
11 };
                                                                                          }
                                                                                   39
                                                                                          void insertKey(Key key) {
                                                                                   40
                                2.10. Treap
                                                                                               pnode elem = new node(key, rand());
                                                                                   41
                                                                                              pnode t1, t2; splitKey(root, key, t1, t2);
                                                                                   42
                                                                                               t1=merge(t1,elem);
   typedef int Key;
                                                                                   43
                                                                                               root=merge(t1,t2);
                                                                                   44
                                                                                   45
   typedef struct node *pnode;
                                                                                          void eraseKeys(Key key1, Key key2) {
   struct node{
                                                                                               pnode t1,t2,t3;
       Kev kev;
                                                                                               splitKey(root,key1,t1,t2);
                                                                                   48
       int prior, size;
                                                                                               splitKey(t2,key2, t2, t3);
       pnode l,r;
                                                                                   49
                                                                                               root=merge(t1,t3);
       node(Key key=0, int prior=0): key(key), prior(prior), size(1), 1(0),
                                                                                   50
            r(0) {}
                                                                                   51
                                                                                          void eraseKey(pnode &t, Key key) {
                                                                                   52
9
                                                                                               if (!t) return;
                                                                                   53
   struct treap {
10
                                                                                               push(t);
       pnode root;
11
                                                                                              if (key == t->key) t=merge(t->1, t->r);
       treap(): root(0) {}
12
                                                                                              else if (key < t->key) eraseKey(t->1, key);
       int size(pnode p) { return p ? p->size : 0; }
                                                                                   56
       int size() { return size(root); }
                                                                                               else eraseKey(t->r, key);
                                                                                               pull(t);
       void push(pnode p) {
                                                                                   58
15
                                                                                          }
           // modificar y propagar el dirty a los hijos aca(para lazy)
                                                                                   59
16
                                                                                          void eraseKey(Key key) {eraseKey(root, key);}
       }
                                                                                   60
17
                                                                                          pnode findKey(pnode t, Key key) {
       // Update function and size from children's values
                                                                                   61
18
                                                                                               if (!t) return 0;
       void pull(pnode p) {//recalcular valor del nodo aca (para rmq)
                                                                                   62
19
                                                                                               if (key == t->key) return t;
           p->size = 1 + size(p->1) + size(p->r);
                                                                                   63
20
                                                                                              if (key < t->key) return findKey(t->1, key);
                                                                                   64
21
                                                                                              return findKey(t->r, key);
       pnode merge(pnode 1, pnode r) {
                                                                                   65
22
           if (!1 || !r) return 1 ? 1 : r;
                                                                                   66
23
                                                                                          pnode findKey(Key key) { return findKey(root, key); }
                                                                                   67
           push(1), push(r);
24
                                                                                          //****POS OPERATIONS*****// No mezclar con las funciones Key
                                                                                   68
           pnode t;
25
                                                                                          //(No funciona con pos:)
           if (1->prior < r->prior) 1->r=merge(1->r, r), t = 1;
                                                                                   69
26
                                                                                          void splitSize(pnode t, int sz, pnode &1, pnode &r) {
           else r\rightarrow l=merge(1, r\rightarrow 1), t = r;
                                                                                   70
27
                                                                                              if (!t) return void(1 = r = 0);
           pull(t);
                                                                                   71
28
                                                                                               push(t);
                                                                                   72
           return t;
29
                                                                                               if (sz \le size(t->1)) splitSize(t->1, sz, 1, t->1), r = t;
                                                                                   73
       }//opcional:
30
                                                                                              else splitSize(t->r, sz - 1 - size(t->l), t->r, r), l = t;
       void merge(treap t) {root = merge(root, t.root), t.root=0;}
                                                                                   74
31
                                                                                               pull(t):
       //*****KEY OPERATIONS*****//
                                                                                   75
32
       void splitKey(pnode t, Key key, pnode &1, pnode &r) {
                                                                                   76
33
                                                                                          void insertPos(int pos, Key key) {
           if (!t) return void(1 = r = 0);
34
                                                                                              pnode elem = new node(key, rand());
                                                                                   78
35
                                                                                               pnode t1,t2; splitSize(root, pos, t1, t2);
                                                                                   79
           if (\text{key} \le \text{t->key}) splitKey(t->1, key, 1, t->1), r = t;
36
                                                                                               t1=merge(t1,elem);
           else splitKey(t->r, key, t->r, r), l = t;
                                                                                   80
37
```

```
root=merge(t1,t2);
81
       }
82
       void erasePos(int pos1, int pos2=-1) {
83
       if(pos2==-1) pos2=pos1+1;
84
           pnode t1,t2,t3;
85
           splitSize(root,pos1,t1,t2);
86
           splitSize(t2,pos2-pos1,t2,t3);
87
           root=merge(t1, t2);
88
       }
89
       pnode findPos(pnode t, int pos) {
90
           if(!t) return 0;
91
           if(pos <= size(t->1)) return findPos(t->1, pos);
92
           return findPos(t->r, pos - 1 - size(t->l));
93
       }
94
       Key &operator[](int pos){return findPos(root, pos)->key;}//ojito
95
96 |};
```

2.11. Gain-Cost Set

```
//esta estructura mantiene pairs(beneficio, costo)
   //de tal manera que en el set quedan ordenados
   //por beneficio Y COSTO creciente. (va borrando los que no son optimos)
   struct V{
     int gain, cost;
     bool operator<(const V &b)const{return gain<b.gain;}</pre>
6
7
   set<V> s;
8
   void add(V x){
     set<V>::iterator p=s.lower_bound(x);//primer elemento mayor o igual
10
     if(p!=s.end() && p->cost <= x.cost) return;//ya hay uno mejor
11
     p=s.upper_bound(x);//primer elemento mayor
12
     if(p!=s.begin()){//borro todos los peores (<=beneficio y >=costo)
13
       --p;//ahora es ultimo elemento menor o igual
14
       while(p->cost >= x.cost){
15
         if(p==s.begin()){s.erase(p); break;}
16
         s.erase(p--);
17
18
     }
19
     s.insert(x);
20
21
   int get(int gain){//minimo costo de obtener tal ganancia
22
     set<V>::iterator p=s.lower_bound((V){gain, 0});
23
     return p==s.end()? INF : p->cost;}
24
```

3. Algos

3.1. Longest Increasing Subsecuence

```
1 //Para non-increasing, cambiar comparaciones y revisar busq binaria
2 //Given an array, paint it in the least number of colors so that each
       color turns to a non-increasing subsequence.
3 //Solution:Min number of colors=Length of the longest increasing
       subsequence
4 int N, a[MAXN];//secuencia y su longitud
   ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
   int p[MAXN];//padres
   vector<int> R;//respuesta
   void rec(int i){
     if(i==-1) return;
     R.push_back(a[i]);
10
     rec(p[i]);
11
12
   int lis(){//O(nlogn)
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
14
     forn(i, N){
15
       int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
16
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
18
         d[i] = ii(a[i], i);
19
       }
20
     }
21
     R.clear();
22
     dforn(i, N+1) if(d[i].first!=INF){
23
       rec(d[i].second);//reconstruir
24
       reverse(R.begin(), R.end());
25
       return i;//longitud
26
     }
27
     return 0;
28
29 }
```

3.2. Manacher

```
1  //0 1 2 3 4
2  //a a b c c <--d1[2]=3
3  //a a b b <--d2[2]=2 (estan uno antes)
4  void manacher(){
5  int l=0, r=-1, n=sz(s);</pre>
```

```
forn(i, n){
6
       int k=(i>r? 1 : min(d1[l+r-i], r-i));
7
       while(i+k<n && i-k>=0 && s[i+k]==s[i-k]) ++k;
8
       d1[i] = k--;
9
       if(i+k > r) l=i-k, r=i+k;
10
     }
11
     l=0, r=-1;
12
     forn(i, n){
13
       int k=(i>r? 0 : min(d2[1+r-i+1], r-i+1))+1;
14
       while(i+k-1 \le k = 0 \& s[i+k-1] == s[i-k]) k++;
15
       d2[i] = --k;
16
       if(i+k-1 > r) l=i-k, r=i+k-1;
17
     }
18
```

4. Strings

4.1. KMP

```
string T;//cadena donde buscar(where)
   string P;//cadena a buscar(what)
   int b[MAXLEN];//back table
   void kmppre(){//by gabina with love
       int i =0, j=-1; b[0]=-1;
5
       while(i<sz(P)){</pre>
6
            while(j>=0 && P[i] != P[j]) j=b[j];
7
            i++, j++;
8
            b[i] = j;
9
       }
10
11
12
   void kmp(){
13
       int i=0, j=0;
14
       while(i<sz(T)){</pre>
15
            while(j>=0 && T[i]!=P[j]) j=b[j];
16
           i++, j++;
17
            if(j==sz(P)){
18
                printf("Puisufounduatuindexu/duinuT\n", i-j);
19
                j=b[j];
20
            }
21
       }
^{22}
23 }
```

4.2. Trie

```
struct trie{
     map<char, trie> m;
2
     void add(const string &s, int p=0){
       if(s[p]) m[s[p]].add(s, p+1);
    }
5
     void dfs(){
       //Do stuff
       forall(it, m)
         it->second.dfs();
    }
10
11 | };
                  4.3. Suffix Array (corto, nlog2n)
 pair<int, int> sf[MAXN];
  bool comp(int lhs, int rhs) {return sf[lhs] < sf[rhs];}
   struct SuffixArray {
     //sa guarda los indices de los sufijos ordenados
       int sa[MAXN], r[MAXN];
5
       void init(const char *a, int n) {
6
7
           forn(i, n) r[i] = a[i];
           for(int m = 1; m < n; m <<= 1) {
8
         forn(i, n) sa[i]=i, sf[i] = make_pair(r[i], i+m<n? r[i+m]:-1);</pre>
               stable_sort(sa, sa+n, comp);
               r[sa[0]] = 0;
11
               forr(i, 1, n) r[sa[i]] = sf[sa[i]] != sf[sa[i - 1]] ? i : r[
12
                   sa[i-1]];
           }
13
14
15 } sa;
                  4.4. Suffix Array (largo, nlogn)
1 #define MAX_N 1000
  #define rBOUND(x) (x<n? r[x] : 0)
   //sa will hold the suffixes in order.
  int sa[MAX_N], r[MAX_N], n;
   string s; //input string, n=sz(s)
   void countingSort(int k){
    int f[MAX_N], tmpsa[MAX_N];
     zero(f);
     forn(i, n) f[rBOUND(i+k)]++;
10
     int sum=0;
11
```

```
forn(i, max(255, n)){
12
       int t=f[i]; f[i]=sum; sum+=t;}
13
     forn(i, n)
14
       tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
15
     memcpy(sa, tmpsa, sizeof(sa));
16
17
   void constructsa(){\frac{1}{0} \text{ n}}
     n=sz(s);
19
     forn(i, n) sa[i]=i, r[i]=s[i];
20
     for(int k=1; k<n; k<<=1){
21
       countingSort(k), countingSort(0);
22
       int rank, tmpr[MAX_N];
23
       tmpr[sa[0]]=rank=0:
24
       forr(i, 1, n)
25
         tmpr[sa[i]] = r[sa[i-1]] \&\& r[sa[i]+k] = r[sa[i-1]+k])?
26
             rank: ++rank:
       memcpy(r, tmpr, sizeof(r));
27
       if(r[sa[n-1]]==n-1) break;
28
     }
29
30
   void print(){//for debug
31
    forn(i, n)
32
       cout << i << ',,' <<
33
       s.substr(sa[i], s.find( '$', sa[i])-sa[i]) << endl;}
34
```

4.5. String Matching With Suffix Array

```
//returns (lowerbound, upperbound) of the search
   ii stringMatching(string P){ //O(sz(P)lgn)
     int lo=0, hi=n-1, mid=lo;
     while(lo<hi){</pre>
4
       mid=(lo+hi)/2;
5
       int res=s.compare(sa[mid], sz(P), P);
6
       if(res>=0) hi=mid;
       else lo=mid+1;
8
9
     if(s.compare(sa[lo], sz(P), P)!=0) return ii(-1, -1);
10
     ii ans: ans.fst=lo:
11
     lo=0, hi=n-1, mid;
12
     while(lo<hi){
13
       mid=(lo+hi)/2:
14
       int res=s.compare(sa[mid], sz(P), P);
15
       if(res>0) hi=mid;
16
```

```
else lo=mid+1:
17
18
     if(s.compare(sa[hi], sz(P), P)!=0) hi--;
19
     ans.snd=hi;
20
     return ans;
21
22 | }
                4.6. LCP (Longest Common Prefix)
1 //Calculates the LCP between consecutives suffixes in the Suffix Array.
   //LCP[i] is the length of the LCP between sa[i] and sa[i-1]
   int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
   void computeLCP(){//0(n)}
     phi[sa[0]]=-1;
     forr(i, 1, n) phi[sa[i]]=sa[i-1];
     int L=0;
     forn(i, n){
8
       if(phi[i]==-1) {PLCP[i]=0; continue;}
9
       while(s[i+L]==s[phi[i]+L]) L++;
10
       PLCP[i]=L:
11
       L=max(L-1, 0);
12
13
     forn(i, n) LCP[i]=PLCP[sa[i]];
14
15 }
                             4.7. Corasick
1
   struct trie{
     map<char, trie> next;
     trie* tran[256];//transiciones del automata
     int idhoja, szhoja;//id de la hoja o 0 si no lo es
     //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
6
```

trie *padre, *link, *nxthoja;

trie &ch=next[s[p]];

tran[(int)s[p]]=&ch;

ch.insert(s, id, p+1);

ch.padre=this, ch.pch=s[p];

if(p < sz(s)){

8

10

11

12

13

14

15

16

char pch;//caracter que conecta con padre

trie(): tran(), idhoja(), padre(), link() {}

void insert(const string &s, int id=1, int p=0){//id>0!!!

```
else idhoja=id, szhoja=sz(s);
17
18
     trie* get_link() {
19
       if(!link){
20
         if(!padre) link=this;//es la raiz
21
         else if(!padre->padre) link=padre;//hijo de la raiz
22
         else link=padre->get_link()->get_tran(pch);
23
       }
24
       return link;
25
26
     trie* get_tran(int c) {
27
       if(!tran[c])
28
         tran[c] = !padre? this : this->get_link()->get_tran(c);
29
       return tran[c];
30
31
     trie *get_nxthoja(){
32
       if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
33
       return nxthoja;
34
     }
35
     void print(int p){
36
       if(idhoja)
37
         cout << "found" << idhoja << "LUatuposition" << p-szhoja << endl
38
       if(get_nxthoja()) get_nxthoja()->print(p);
39
40
     void matching(const string &s, int p=0){
41
       print(p);
42
       if(p<sz(s)) get_tran(s[p])->matching(s, p+1);
43
                                  Geometría
```

#define EPS 1e-9

5.1. Punto

```
struct pto{
tipo x, y;
pto(tipo x=0, tipo y=0):x(x),y(y){}

pto operator+(pto a){return pto(x+a.x, y+a.y);}

pto operator-(pto a){return pto(x-a.x, y-a.y);}

pto operator+(tipo a){return pto(x+a, y+a);}

pto operator*(tipo a){return pto(x*a, y*a);}

pto operator/(tipo a){return pto(x/a, y/a);}
```

```
//dot product, producto interno:
9
     tipo operator*(pto a){return x*a.x+y*a.y;}
10
     //module of the cross product or vectorial product:
11
     //if a is less than 180 clockwise from b, a^b>0
     tipo operator^(pto a){return x*a.y-y*a.x;}
13
     //returns true if this is at the left side of line qr
14
     bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
15
     bool operator<(const pto &a) const{return x<a.x || (abs(x-a.x)<EPS &&
16
         v<a.v);}
   bool operator==(pto a){return abs(x-a.x) < EPS && abs(y-a.y) < EPS;}
     double norm(){return sqrt(x*x+y*y);}
     tipo norm_sq(){return x*x+y*y;}
19
   }:
20
   double dist(pto a, pto b){return (b-a).norm();}
   typedef pto vec;
23
   double angle(pto a, pto o, pto b){
24
     vec oa=a-o, ob=b-o;
25
     return acos((oa*ob) / sqrt(oa.norm_sq()*ob.norm_sq()));}
26
27
   //rotate p by theta rads CCW w.r.t. origin (0,0)
   pto rotate(pto p, double theta){
     return pto(p.x*cos(theta)-p.y*sin(theta),
30
        p.x*sin(theta)+p.v*cos(theta));
31
32 }
                                 5.2. Line
1 struct line{
     line() {}
     double a,b,c;//Ax+By=C
   //pto MUST store float coordinates!
    line(double a, double b, double c):a(a),b(b),c(c){}
    line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
   };
   bool parallels(line 11, line 12){return abs(l1.a*l2.b-l2.a*l1.b)<EPS;}</pre>
   pto inter(line 11, line 12){//intersection
     double det=11.a*12.b-12.a*11.b;
     if(abs(det) < EPS) return pto(INF, INF); //parallels
     return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
13 }
                              5.3. Segment
```

```
struct segm{
     pto s,f;
                                                                                    5
2
     segm(pto s, pto f):s(s), f(f) {}
                                                                                    6
                                                                                      }
3
     pto closest(pto p) {//use for dist to point
        double 12 = dist_sq(s, f);
        if(12==0.) return s;
        double t = ((p-s)*(f-s))/12;
        if (t<0.) return s;//not write if is a line
8
        else if(t>1.)return f;//not write if is a line
9
        return s+((f-s)*t);
10
     }
11
     bool inside(pto p){
12
                                                                                      }
                                                                                    5
   return ((s-p)^(f-p))==0 \&\& min(s, f)<*this&&*this<max(s, f);}
                                                                                    6
14
                                                                                        pto o;
15
                                                                                         double r:
   bool insidebox(pto a, pto b, pto p) {
     return (a.x-p.x)*(p.x-b.x)>-EPS && (a.y-p.y)*(p.y-b.y)>-EPS;
17
                                                                                   10
18
                                                                                   11
   pto inter(segm s1, segm s2){
19
                                                                                   12
     pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
20
                                                                                        }
                                                                                   13
     if(insidebox(s1.s,s1.f,p) && insidebox(s2.s,s2.f,p))
21
                                                                                   14
         return r;
22
                                                                                   15
     return pto(INF, INF);
23
                                                                                   16
24 }
                              5.4. Rectangle
                                                                                   18
                                                                                   19
   struct rect{
                                                                                   20
     //lower-left and upper-right corners
                                                                                   21
     pto lw, up;
3
                                                                                   ^{22}
4
                                                                                   23
   //returns if there's an intersection and stores it in r
   bool inter(rect a, rect b, rect &r){
     r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
     r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
                                                                                   27
   //check case when only a edge is common
                                                                                   28
     return r.lw.x<r.up.x && r.lw.y<r.up.y;</pre>
                                                                                   29
11 }
                                                                                   30
                                                                                   31 }
                                 Polygon Area
   double area(vector<tipo> &p)\{//0(sz(p))\}
     double area=0;
2
     forn(i, sz(p)) area+=p[i]^p[(i+1) %z(p)];
```

```
//if points are in clockwise order then area is negative
    return abs(area)/2;
  //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
_{8} //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
                              5.6. Circle
vec perp(vec v){return vec(-v.y, v.x);}
  line bisector(pto x, pto y){
    line l=line(x, y); pto m=(x+y)/2;
    return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
  struct Circle{
   //circle determined by three points, uses line
    Circle(pto x, pto y, pto z){
      o=inter(bisector(x, y), bisector(y, z));
      r=dist(o, x);
    pair<pto, pto> ptosTang(pto p){
      pto m=(p+o)/2;
      tipo d=dist(o, m);
      tipo a=r*r/(2*d);
      tipo h=sqrt(r*r-a*a);
      pto m2=o+(m-o)*a/d;
      vec per=perp(m-o)/d;
      return mkp(m2-per*h, m2+per*h);
  //finds the center of the circle containing p1 and p2 with radius r
   //as there may be two solutions swap p1, p2 to get the other
  bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
          double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
          if(det<0) return false:
          c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
          return true;
                          5.7. Point in Poly
1 //checks if v is inside of P, using ray casting
2 //works with convex and concave.
```

```
//excludes boundaries, handle it separately using segment.inside()
bool inPolygon(pto v, vector<pto>& P) {
   bool c = false;
   forn(i, sz(P)){
      int j=(i+1) %sz(P);
      if((P[j].y>v.y) != (P[i].y > v.y) &&
      (v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))
      c = !c;
   }
   return c;
}
</pre>
```

5.8. Convex Check CHECK

```
bool isConvex(vector<int> &p){//O(N)

int N=sz(p);

if(N<3) return false;

bool isLeft=p[0].left(p[1], p[2]);

forr(i, 1, N)

if(p[i].left(p[(i+1) %), p[(i+2) %))!=isLeft)

return false;

return true; }</pre>
```

5.9. Convex Hull

```
//stores convex hull of P in S, CCW order
   void CH(vector<pto>& P, vector<pto> &S){
     S.clear();
3
     sort(P.begin(), P.end());
4
     forn(i, sz(P)){
       while(sz(S) \ge 2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
       S.pb(P[i]);
7
     }
8
     S.pop_back();
9
     int k=sz(S);
10
     dforn(i, sz(P)){
11
       while(sz(S) \ge k+2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back
12
           ();
       S.pb(P[i]);
13
     }
     S.pop_back();
16 }
```

5.10. Cut Polygon

```
//cuts polygon Q along the line ab
//stores the left side (swap a, b for the right one) in P
void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
    P.clear();
    forn(i, sz(Q)){
        double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1) %z(Q)]-a);
        if(left1>=0) P.pb(Q[i]);
        if(left1*left2<0)
        P.pb(inter(line(Q[i], Q[(i+1) %z(Q)]), line(a, b)));
    }
}</pre>
```

5.11. Bresenham

```
1 //plot a line approximation in a 2d map
void bresenham(pto a, pto b){
     pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
    pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
     int err=d.x-d.y;
     while(1){
       m[a.x][a.y]=1;//plot
       if(a==b) break;
       int e2=2*err;
       if(e2 > -d.y){
         err-=d.v, a.x+=s.x;
11
       if(e2 < d.x)
         err+= d.x, a.y+= s.y;
13
    }
14
15 }
```

5.12. Rotate Matrix

```
//rotates matrix t 90 degrees clockwise
//using auxiliary matrix t2(faster)
void rotate(){
forn(x, n) forn(y, n)
t2[n-y-1][x]=t[x][y];
memcpy(t, t2, sizeof(t));
}
```

6. Math

6.1. Identidades

$$\sum_{i=0}^{n} \binom{n}{i} = 2^{n}$$

$$\sum_{i=0}^{n} i \binom{n}{i} = n * 2^{n-1}$$

$$\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^{n} i^{2} = \frac{n(n+1)(2n+1)}{6} = \frac{n^{3}}{3} + \frac{n^{2}}{2} + \frac{n}{6}$$

$$\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2} + 1)(n+1)$$
(doubles) \rightarrow Sino ver caso impar y par
$$\sum_{i=0}^{n} i^{3} = \left(\frac{n(n+1)}{2}\right)^{2} = \frac{n^{4}}{4} + \frac{n^{3}}{2} + \frac{n^{2}}{4} = \left[\sum_{i=1}^{n} i\right]^{2}$$

$$\sum_{i=0}^{n} i^{4} = \frac{n(n+1)(2n+1)(3n^{2} + 3n - 1)}{30} = \frac{n^{5}}{5} + \frac{n^{4}}{2} + \frac{n^{3}}{3} - \frac{n}{30}$$

$$\sum_{i=0}^{n} i^{p} = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_{k}}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}$$

6.2. Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
   comb[i][0]=comb[i][i]=1;
   forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1]) MOD;
}

ll lucas (ll n, ll k, int p){ //Calcula (n,k) %p teniendo comb[p][p]
        precalculado.
   ll aux = 1;
   while (n + k){
```

```
aux = (aux * comb[n\%][k\%]) \%;
       n/=p, k/=p;
10
11
     return aux;
12
13 }
                    6.3. Exp. de Numeros Mod.
  int expmod (int b, int e) \frac{1}{0} \log b
     if(!e) return 1;
    11 q= expmod(b,e/2); q=(q*q) MOD;
    return e %2? (b * q) MOD : q;
5 }
          6.4. Exp. de Matrices y Fibonacci en log(n)
1 struct M22{
                   // |a b|
     tipo a,b,c,d;// |c|d|
     M22 operator*(const M22 &p) const {
       return (M22){a*p.a+b*p.c, a*p.b+b*p.d, c*p.a+d*p.c,c*p.b+d*p.d};}
5
   M22 operator (const M22 &p, int n){
6
     if(!n) return (M22){1, 0, 0, 1};//identidad
     M22 q=p^(n/2); q=q*q;
     return n %2? p * q : q;}
   11 fibo(ll n){//calcula el fibonacci enesimo
11
     M22 \text{ mat}=(M22)\{0, 1, 1, 1\}^n;
12
     return mat.a*f0+mat.b*f1;//f0 y f1 son los valores iniciales
13
14 }
                          Teorema Chino del Resto
                      6.6.
                           Funciones de primos
```

```
1 ll numPrimeFactors (ll n){
2    ll rta = 0;
3    map<ll,ll> f=fact(n);
4    forall(it, f) rta += it->second;
5    return rta;
```

```
6 | }
7
   11 numDiffPrimeFactors (11 n){
8
     11 rta = 0;
9
     map<ll,ll> f=fact(n);
     forall(it, f) rta += 1;
     return rta;
12
13
14
   11 sumPrimeFactors (11 n){
15
     ll rta = 0;
     map<ll,ll> f=fact(n);
     forall(it, f) rta += it->first;
     return rta;
19
20
21
   11 numDiv (ll n){
22
     ll rta = 1;
23
     map<ll,ll> f=fact(n);
24
     forall(it, f) rta *= (it->second + 1);
25
     return rta;
26
27
28
   ll sumDiv (ll n){
29
     ll rta = 1;
30
     map<ll,ll> f=fact(n);
31
     forall(it, f) rta *= ((ll)pow((double)it->first, it->second + 1.0)-1)
32
         / (it->first-1);
     return rta;
33
34
35
   11 eulerPhi (ll n){ // con criba: O(lg n)
     11 \text{ rta} = n:
37
     map<11,11> f=fact(n);
38
     forall(it, f) rta -= rta / it->first;
39
     return rta;
40
41
42
   11 eulerPhi2 (11 n){ // 0 (sqrt n)
43
     11 r = n;
44
     forr (i,2,n+1){
45
       if ((11)i*i > n)
46
         break;
47
```

```
if (n \% i == 0){
         while (n\% == 0) n/=i;
49
         r = r/i;
       }}
     if (n != 1)
      r=r/n;
     return r;
55 }
                          6.7. Phollard's Rho
1 | 11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %c, and minimize overfloor
    11 x = 0, y = a\%;
     while (b > 0){
       if (b \% 2 == 1) x = (x+y) \% c;
       y = (y*2) \% c;
       b /= 2;
6
     return x % c;
8
9
10
   ll pollard_rho (ll n){
11
     int i = 0, k = 2;
    11 x = 3, y = 3;
     while (1){
14
      i++;
15
      x = (mulmod (x,x,n) + n - 1) %n;
      ll d = gcd (abs(y-x), n);
       if (d != 1 && d != n) return d;
       if (i == k) v = x, k*=2;
19
     }
20
   }
21
   int main(){
23
    11 n = 2063512844981574047LL;
24
    ll ans = pollard_rho (n);
    if (ans > n / ans) ans = n / ans;
     printf ("%ldu%ld\n", ans, n / ans);
       return 0;
29 }
```

6.8. Criba

#define MAXP 80000 //no necesariamente primo

```
1 int criba[MAXP+1];
   vector<int> primos;
   void buscarprimos(){
4
     int sq=sqrt(MAXP)+1;
     forr(p, 2, MAXP+1) if(!criba[p]){
       primos.push_back(p);
       if(p \le sq)
8
         for(int m=p*p; m<=MAXP; m+=p)//borro los multiplos de p</pre>
9
           if(!criba[m])criba[m]=p;
10
     }
11
  |}
12
```

6.9. Factorizacion

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```
//factoriza bien numeros hasta MAXP^2
   map<ll,ll> fact(ll n){ //0 (cant primos)
     map<ll,ll> ret;
     forall(p, primos){
       while(!(n \(\frac{1}{2}\)\)){
5
         ret[*p]++;//divisor found
6
         n/=*p;
7
       }
8
     }
9
     if(n>1) ret[n]++;
     return ret;
11
12
13
    //factoriza bien numeros hasta MAXP
   map<11,11> fact2(11 n){ //0 (1g n)}
     map<11,11> ret;
16
     while (criba[n]){
17
       ret[criba[n]]++;
18
       n/=criba[n];
19
20
     if(n>1) ret[n]++;
     return ret;
22
23 | }
```

6.10. GCD

```
tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
```

6.11. LCM

```
1 | tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
                              6.12. Inversos
   #define MAXMOD 15485867
   ll inv[MAXMOD];//inv[i]*i=1 mod MOD
   void calc(int p){\frac{}{0}}
     inv[1]=1:
     forr(i, 2, p) inv[i] = p-((p/i)*inv[p\%i])\%;
6
   int inverso(int x){\frac{1}{0}(\log x)}
     return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
     return expmod(x, MOD-2);//si mod es primo
9
10 }
                             6.13. Simpson
   double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
     double area=0, h=(b-a)/n, fa=f(a), fb;
     forn(i, n){
       fb=f(a+h*(i+1)):
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
6
     return area*h/6.;}
                              6.14. Fraction
1 struct frac{
     tipo p.q:
     frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
     tipo mcd(tipo a, tipo b){return a?mcd(b %a, a):b;}
     void norm(){
5
       tipo a = mcd(p,q);
6
       if(a) p/=a, q/=a;
       else q=1;
       if (q<0) q=-q, p=-p;}
     frac operator+(const frac& o){
10
       tipo a = mcd(q, o.q);
11
       return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
12
     frac operator-(const frac& o){
13
       tipo a = mcd(q, o.q);
14
       return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
15
```

```
frac operator*(frac o){
    tipo a = mcd(q,o.p), b = mcd(o.q,p);
    return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}

frac operator/(frac o){
    tipo a = mcd(q,o.q), b = mcd(o.p,p);
    return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}

bool operator<(const frac &o) const{return p*o.q < o.p*q;}
    bool operator==(frac o){return p==o.p&&q==o.q;}

};</pre>
```

6.15. Polinomio

```
#define MAX_GR 20
   struct poly {
     tipo p[MAX_GR];//guarda los coeficientes del polinomio
     poly(){zero(p);}
4
     int gr(){//calculates grade of the polynomial
5
       dforn(i,MAX_GR) if(p[i]) return i;
6
       return 0; }
7
     bool isnull() {return gr()==0 && !p[0];}
8
     poly operator+(poly b) {// - is analogous
       poly c=THIS;
10
       forn(i,MAX_GR) c.p[i]+=b.p[i];
11
       return c;
12
     }
13
     poly operator*(poly b) {
14
       poly c;
15
       forn(i,MAX_GR) forn(k,i+1) c.p[i]+=p[k]*b.p[i-k];
16
       return c;
17
18
     tipo eval(tipo v) {
19
       tipo sum = 0;
20
       dforn(i, MAX_GR) sum=sum*v + p[i];
21
       return sum;
^{22}
     }
23
     //the following function generates the roots of the polynomial
24
    //it can be easily modified to return float roots
^{25}
     set<tipo> roots(){
26
       set<tipo> roots;
27
       tipo a0 = abs(p[0]), an = abs(p[gr()]);
28
       vector<tipo> ps,qs;
29
       forr(p,1,sqrt(a0)+1) if (a0 \% ==0) ps.pb(p),ps.pb(a0/p);
30
       forr(q,1,sqrt(an)+1) if (an)(q=0) qs.pb(q),qs.pb(an/q);
31
```

```
forall(pt,ps)
32
         forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
33
           tipo root = abs((*pt) / (*qt));
34
           if (eval(root)==0) roots.insert(root);
35
         }
36
       return roots;
37
38
   };
39
   //the following functions allows parsing an expression like
   //34+150+4*45
   //into a polynomial(el numero en funcion de la base)
   #define LAST(s) (sz(s)? s[sz(s)-1] : 0)
   #define POP(s) s.erase(--s.end()):
   poly D(string &s) {
     poly d;
     for(int i=0; isdigit(LAST(s)); i++) d.p[i]=LAST(s)-'0', POP(s);
     return d;}
49
   poly T(string &s) {
50
     polv t=D(s);
     if (LAST(s)=='*')\{POP(s); return T(s)*t;\}
52
     return t;
53
54
   //main function, call this to parse
   poly E(string &s) {
     polv e=T(s);
     if (LAST(s)=='+')\{POP(s); return E(s)+e;\}
     return e;
59
60 }
```

7. Grafos

7.1. Dijkstra

```
#define INF 1e9
int N;
#define MAX_V 250001
vector<ii>> G[MAX_V];
//To add an edge use
#define add(a, b, w) G[a].pb(mkp(w, b))

ll dijkstra(int s, int t){//O(|E| log |V|)
priority_queue<ii, vector<ii>> greater<ii>> Q;
```

```
7 }
     vector<ll> dist(N, INF); vector<int> dad(N, -1);
10
     Q.push(mkp(0, s)); dist[s] = 0;
11
     while(sz(Q)){
12
       ii p = Q.top(); Q.pop();
13
       if(p.snd == t) break;
14
       forall(it, G[p.snd])
15
         if(dist[p.snd]+it->first < dist[it->snd]){
                                                                                   13
16
           dist[it->snd] = dist[p.snd] + it->fst;
                                                                                   14
17
           dad[it->snd] = p.snd;
                                                                                   15 }
18
           Q.push(mkp(dist[it->snd], it->snd));
19
         }
20
     }
21
     return dist[t]:
22
     if(dist[t]<INF)//path generator</pre>
23
                                                                                      vector<Ar> E;
       for(int i=t; i!=-1; i=dad[i])
                                                                                      ll kruskal(){
         printf("%d%c", i, (i==s?'\n':','));
25
                                                                                          11 cost=0:
26 }
                                                                                   6
                           7.2. Bellman-Ford
                                                                                   7
                                                                                   8
  vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
                                                                                   9
  int dist[MAX N]:
                                                                                   10
   void bford(int src){//O(VE)
                                                                                   11
     dist[src]=0:
                                                                                              }
                                                                                   12
4
     forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                   13
5
       dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
6
                                                                                   14
                                                                                   15 }
7
8
   bool hasNegCycle(){
     forn(j, N) if(dist[j]!=INF) forall(it, G[j])
10
       if(dist[it->snd]>dist[j]+it->fst) return true;
11
     //inside if: all points reachable from it->snd will have -INF distance
12
         (do bfs)
                                                                                   4
     return false;
13
                                                                                   5
14 | }
                                                                                   6
                          7.3. Floyd-Warshall
                                                                                      }
                                                                                   7
   //G[i][j] contains weight of edge (i, j) or INF
                                                                                      ll prim(){
                                                                                   9
   //G[i][i]=0
                                                                                   10
  int G[MAX_N] [MAX_N];
                                                                                  11
   void floyd(){//0(N^3)}
                                                                                          11 cost=0;
                                                                                   12
  forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
                                                                                  13
     G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
                                                                                  14
```

```
bool inNegCycle(int v){
    return G[v][v]<0;}
  //checks if there's a neg. cycle in path from a to b
  bool hasNegCycle(int a, int b){
   forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
      return true;
    return false;
                             7.4. Kruskal
struct Ar{int a,b,w;};
 bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}
      sort(E.begin(), E.end());//ordenar aristas de menor a mayor
      uf.init(n);
      forall(it, E){
          if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
              uf.unir(it->a, it->b)://conectar
              cost+=it->w:
      return cost;
                              7.5. Prim
 bool taken[MAXN];
  priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
  void process(int v){
      taken[v]=true;
      forall(e, G[v])
          if(!taken[e->second]) pq.push(*e);
      zero(taken);
      process(0);
      while(sz(pq)){
          ii e=pq.top(); pq.pop();
```

```
if(!taken[e.second]) cost+=e.first, process(e.second);
                                                                                         if(!idx[i]) tjn(i);
15
                                                                                  36
                                                                                         if(!idx[neg(i)]) tjn(neg(i));
       }
16
                                                                                 37
       return cost;
17
                                                                                  38
18 }
                                                                                       forn(i, n) if(cmp[i] == cmp[neg(i)]) return false;
                                                                                  39
                                                                                       return true;
                      7.6. 2-SAT + Tarjan SCC
                                                                                  41 }
                                                                                                         7.7. Articulation Points
   //We have a vertex representing a var and other for his negation.
   //Every edge stored in G represents an implication. To add an equation
                                                                                  1 int N;
       of the form a | |b, use addor(a, b)
                                                                                     vector<int> G[1000000];
   //MAX=max cant var, n=cant var
                                                                                     //V[i]=node number(if visited), L[i]= lowest V[i] reachable from i
   #define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
                                                                                     int qV, V[1000000], L[1000000], P[1000000];
   vector<int> G[MAX*2];
                                                                                     void dfs(int v, int f){
   //idx[i]=index assigned in the dfs
                                                                                      L[v]=V[v]=++qV;
   //lw[i]=lowest index(closer from the root) reachable from i
                                                                                       forall(it, G[v])
   int lw[MAX*2], idx[MAX*2], qidx;
                                                                                         if(!V[*it]){
   stack<int> q;
                                                                                           dfs(*it, v);
                                                                                  9
   int qcmp, cmp[MAX*2];
                                                                                           L[v] = min(L[v], L[*it]);
   //verdad[cmp[i]]=valor de la variable i
                                                                                           P[v] += L[*it] >= V[v];
                                                                                 11
   bool verdad[MAX*2+1];
                                                                                         }
                                                                                  12
                                                                                         else if(*it!=f)
                                                                                  13
   int neg(int x) { return x>=n? x-n : x+n;}
                                                                                           L[v]=min(L[v], V[*it]);
                                                                                  14
   void tjn(int v){
15
                                                                                     }
                                                                                  15
     lw[v]=idx[v]=++qidx;
16
                                                                                     int cantart(){ //O(n)
     q.push(v), cmp[v]=-2;
17
                                                                                       qV=0;
                                                                                 17
     forall(it, G[v]){
18
                                                                                       zero(V), zero(P);
                                                                                  18
       if(!idx[*it] || cmp[*it]==-2){
19
                                                                                      dfs(1, 0); P[1]--;
                                                                                  19
         if(!idx[*it]) tjn(*it);
20
                                                                                       int q=0;
                                                                                 20
         lw[v]=min(lw[v], lw[*it]);
21
                                                                                      forn(i, N) if(P[i]) q++;
22
                                                                                     return q;
     }
23
                                                                                  23 }
     if(lw[v]==idx[v]){
24
                                                                                                    7.8. Comp. Biconexas y Puentas
       qcmp++;
25
       int x;
26
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
                                                                                  1 struct edge {
27
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
                                                                                       int u,v, comp;
28
                                                                                       bool bridge;
                                                                                  3
29
                                                                                     }:
                                                                                  4
30
    //remember to CLEAR G!!!
                                                                                     vector<edge> e;
31
   bool satisf(){//O(n)
                                                                                     void addEdge(int u, int v) {
32
                                                                                      G[u].pb(sz(e)), G[v].pb(sz(e));
     memset(idx, 0, sizeof(idx)), qidx=0;
33
     memset(cmp, -1, sizeof(cmp)), qcmp=0;
                                                                                       e.pb((edge)\{u,v,-1,false\});
                                                                                  8
34
     forn(i, n){
                                                                                  9 | }
35
```

```
//d[i]=id de la dfs
   //b[i]=lowest id reachable from i
   int d[MAXN], b[MAXN], t;
   int nbc;//cant componentes
   int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
   void initDfs(int n) {
     zero(G), zero(comp);
16
     e.clear();
17
     forn(i,n) d[i]=-1;
18
     nbc = t = 0;
19
20
   stack<int> st;
   void dfs(int u, int pe) \{//0(n + m)\}
     b[u] = d[u] = t++;
23
     comp[u] = (pe != -1);
24
     forall(ne, G[u]) if (*ne != pe){
25
       int v = e[*ne].u ^ e[*ne].v ^ u;
26
       if (d[v] == -1) {
27
         st.push(*ne);
28
         dfs(v,*ne);
29
         if (b[v] > d[u]){
30
            e[*ne].bridge = true; // bridge
31
         }
32
         if (b[v] >= d[u]) \{ // art \}
33
           int last;
34
           do {
35
              last = st.top(); st.pop();
36
              e[last].comp = nbc;
37
           } while (last != *ne);
38
           nbc++;
39
            comp[u]++;
40
41
         b[u] = min(b[u], b[v]);
42
       }
43
       else if (d[v] < d[u]) \{ // back edge
44
         st.push(*ne);
45
         b[u] = min(b[u], d[v]);
46
47
     }
48
49 }
```

7.9. LCA + Climb

```
1 //f[v][k] holds the 2^k father of v
2 //L[v] holds the level of v
   int N, f[100001][20], L[100001];
   void build(){//f[i][0] must be filled previously, O(nlgn)
     forn(k, 20-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}
   #define lg(x) (31-__builtin_clz(x))//=floor(log2(x))
   int climb(int a, int d){\frac{1}{0(lgn)}}
     if(!d) return a;
     dforn(i, lg(L[a])+1)
11
       if(1<<i<=d)
12
         a=f[a][i], d-=1<<i;
13
       return a;
14
15
   int lca(int a, int b){\frac{1}{0}}
     if(L[a]<L[b]) swap(a, b);</pre>
     a=climb(a, L[a]-L[b]);
18
     if(a==b) return a;
19
     dforn(i, lg(L[a])+1)
       if(f[a][i]!=f[b][i])
21
         a=f[a][i], b=f[b][i];
22
     return f[a][0];
23
24 }
```

8. Network Flow

8.1. Dinic

```
int nodes, src, dest;
int dist[MAX], q[MAX], work[MAX];

struct Edge {
   int to, rev;
   ll f, cap;
   Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap)
   {}
};

vector<Edge> G[MAX];

// Adds bidirectional edge
void addEdge(int s, int t, ll cap){
```

```
G[s].push_back(Edge(t, G[t].size(), 0, cap));
     G[t].push_back(Edge(s, G[s].size()-1, 0, 0));
15
   }
16
17
   bool dinic_bfs() {
     fill(dist, dist + nodes, -1);
19
     dist[src] = 0;
20
     int qt = 0;
21
     q[qt++] = src;
^{22}
     for (int qh = 0; qh < qt; qh++) {
23
       int u = q[qh];
24
       forall(e, G[u]){
25
         int v = e \rightarrow to:
26
         if(dist[v]<0 \&\& e->f < e->cap){
27
            dist[v]=dist[u]+1;
28
            q[qt++]=v;
29
         }
30
       }
31
32
     return dist[dest] >= 0;
33
34
35
   ll dinic_dfs(int u, ll f) {
36
     if (u == dest) return f;
37
     for (int &i = work[u]; i < (int) G[u].size(); i++) {</pre>
38
       Edge &e = G[u][i];
39
       if (e.cap <= e.f) continue;</pre>
40
       int v = e.to;
41
       if (dist[v] == dist[u] + 1) {
42
         11 df = dinic_dfs(v, min(f, e.cap - e.f));
43
         if (df > 0) {
44
            e.f += df:
45
            G[v][e.rev].f -= df;
46
            return df:
47
         }
48
       }
49
     }
50
     return 0;
51
52
53
   11 maxFlow(int _src, int _dest) {//O(V^2 E)
54
     src = _src;
55
     dest = _dest;
```

```
11 result = 0;
while (dinic_bfs()) {
    fill(work, work + nodes, 0);
    while(ll delta = dinic_dfs(src, INF))
    result += delta;
}
return result;
}
```

8.2. Edmonds Karp's

```
1 #define MAX_V 1000
   #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
   map<int, int> G[MAX_V];//limpiar esto
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   int f, p[MAX_V];
   void augment(int v, int minE){
    if(v==SRC) f=minE;
     else if(p[v]!=-1){
       augment(p[v], min(minE, G[p[v]][v]));
13
       G[p[v]][v]=f, G[v][p[v]]+=f;
14
     }
15
16
   11 maxflow(){//0(VE^2)
     11 Mf=0;
18
     do{
19
       f=0;
20
       char used[MAX_V]; queue<int> q; q.push(SRC);
21
       zero(used), memset(p, -1, sizeof(p));
22
       while(sz(q)){
23
         int u=q.front(); q.pop();
24
         if(u==SNK) break;
25
         forall(it, G[u])
26
           if(it->snd>0 && !used[it->fst])
27
             used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
28
29
       augment(SNK, INF);
30
       Mf+=f:
31
     }while(f);
32
```

```
return Mf;
34 }
                            8.3. Push-Relabel
   #define MAX V 1000
   int N;//valid nodes are [0...N-1]
   #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
   map<int, int> G[MAX_V];
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   11 excess[MAX_V];
   int height[MAX_V], active[MAX_V], count[2*MAX_V+1];
   queue<int> Q;
   void enqueue(int v) {
13
     if (!active[v] && excess[v] > 0) active[v]=true, Q.push(v); }
   void push(int a, int b) {
     int amt = min(excess[a], ll(G[a][b]));
     if(height[a] <= height[b] || amt == 0) return;</pre>
17
     G[a][b]-=amt, G[b][a]+=amt;
18
     excess[b] += amt, excess[a] -= amt;
19
     enqueue(b);
20
21
   void gap(int k) {
22
     forn(v, N){
23
       if (height[v] < k) continue;</pre>
24
       count[height[v]]--;
25
       height[v] = max(height[v], N+1);
26
       count[height[v]]++;
27
       enqueue(v);
28
29
```

height[v] = min(height[v], height[it->fst] + 1);

30

31

32

33

34

35

36

37

void relabel(int v) {

height[v] = 2*N;

forall(it, G[v])

if(it->snd)

enqueue(v);

count[height[v]]--;

count[height[v]]++;

```
39 }
   ll maxflow() {//O(V^3)
     zero(height), zero(active), zero(count), zero(excess);
41
     count[0] = N-1;
42
     count[N] = 1;
43
    height[SRC] = N;
44
     active[SRC] = active[SNK] = true;
45
     forall(it, G[SRC]){
46
       excess[SRC] += it->snd;
       push(SRC, it->fst);
49
     while(sz(Q)) {
50
       int v = Q.front(); Q.pop();
51
       active[v]=false:
52
    forall(it, G[v]) push(v, it->fst);
53
     if(excess[v] > 0)
       count[height[v]] == 1? gap(height[v]):relabel(v);
    }
56
    ll mf=0:
57
    forall(it, G[SRC]) mf+=G[it->fst][SRC];
    return mf;
60 }
                             Avudamemoria
                                 Límites
1 | #include <climits> //INT_MIN, LONG_MAX, ULLONG_MAX, etc.
                            Cant. decimales
 #include <iomanip>
cout << setprecision(2) << fixed;</pre>
               Rellenar con espacios(para justificar)
 1 | #include <iomanip>
cout << setfill(''') << setw(3) << 2 << endl;
                        Leer hasta fin de línea
1 #include <sstream>
//hacer cin.ignore() antes de getline()
3 while(getline(cin, line)){
```

```
istringstream is(line);
       while(is >> X)
5
         cout << X << "";
6
       cout << endl;</pre>
8
                               Aleatorios
1 | #define RAND(a, b) (rand() %(b-a+1)+a)
srand(time(NULL));
                           Doubles Comp.
 const double EPS = 1e-9;
  x == y \iff fabs(x-y) \iff EPS
_3 | x > y <=> x > y + EPS
_4 | x >= y <=> x > y - EPS
                                Límites
  #include <limits>
 numeric limits<T>
    ::max()
    ::min()
    ::epsilon()
                               Muahaha
 #include <signal.h>
  void divzero(int p){
    while(true);}
  void segm(int p){
    exit(0);}
5
  //in main
  signal(SIGFPE, divzero);
8 signal(SIGSEGV, segm);
                          Mejorar velocidad
i lios::sync_with_stdio(false);
                         Mejorar velocidad 2
1 //Solo para enteros positivos
inline void Scanf(int& a){
```

```
char c = 0;
while(c<33) c = getc(stdin);
a = 0;
while(c>33) a = a*10 + c - '0', c = getc(stdin);

Leer del teclado

Leer del teclado

File setup

//tambien se pueden usar comas: {a, x, m, 1}
for i in {a. k}; do cp template.cpp $i.cpp && touch $i.in; done
```