1. algorithm

#include <algorithm> #include <numeric>

Algo	Params	Funcion
sort, stable_sort	f, 1	ordena el intervalo
nth_element	f, nth, l	void ordena el n-esimo, y
		particiona el resto
fill, fill_n	f, l / n, elem	void llena [f, l) o [f,
		f+n) con elem
lower_bound, upper_bound	f, l, elem	it al primer / ultimo donde se
		puede insertar elem para que
		quede ordenada
binary_search	f, l, elem	bool esta elem en [f, l)
copy	f, l, resul	hace resul+ i =f+ $i \forall i$
find, find_if, find_first_of	f, l, elem	it encuentra i \in [f,l) tq. i=elem,
	/ pred / f2, l2	$\operatorname{pred}(i), i \in [f2, l2)$
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, l, f2, l2	busca $[f2,l2) \in [f,l)$
replace_if	f, l, old	cambia old / pred(i) por new
	/ pred, new	
reverse	f, 1	da vuelta
partition, stable_partition	f, l, pred	pred(i) ad, !pred(i) atras
min_element, max_element	f, l, [comp]	it min, max de [f,l]
lexicographical_compare	f1,l1,f2,l2	bool con [f1,l1]; $[f2,l2]$
next/prev_permutation	f,l	deja en [f,l) la perm sig, ant
set_intersection,	f1, l1, f2, l2, res	[res,) la op. de conj
set_difference, set_union,		
set_symmetric_difference,		
push_heap, pop_heap,	f, l, e / e /	mete/saca e en heap [f,l),
make_heap		hace un heap de [f,l)
is_heap	f,l	bool es [f,l) un heap
accumulate	f,l,i,[op]	$T = \sum /\text{oper de [f,l)}$
inner_product	f1, l1, f2, i	$T = i + [f1, 11) \cdot [f2, \dots)$
partial_sum	f, l, r, [op]	$r+i = \sum /oper de [f,f+i] \forall i \in [f,l)$
builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
_builtin_popcount	unsigned int	Cant. de 1's en x.
builtin_parity	unsigned int	1 si x es par, 0 si es impar.
builtin_XXXXXXII	unsigned ll	= pero para long long's.

2. Estructuras

2.1. RMQ (static)

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: LVL \geq ceil(logn); Usar [] para llenar arreglo y luego build().

```
1 struct RMQ{
     #define LVL 10
     tipo vec[LVL] [1<<(LVL+1)];
     tipo &operator[](int p){return vec[0][p];}
     tipo get(int i, int j) {//intervalo [i,j)
       int p = 31-__builtin_clz(j-i);
       return min(vec[p][i],vec[p][j-(1<<p)]);
7
    }
8
    void build(int n) {//O(nlogn)
       int mp = 31-__builtin_clz(n);
      forn(p, mp) forn(x, n-(1 << p))
11
         vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
    }};
13
```

2.2. RMQ (dynamic)

```
1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
        sobre el rango [i, j).
2 #define MAXN 100000
   #define operacion(x, y) max(x, y)
   const int neutro=0;
   struct RMQ{
     int sz;
     tipo t[4*MAXN];
     tipo &operator[](int p){return t[sz+p];}
     void init(int n){//O(nlgn)
       sz = 1 \ll (32-\_builtin\_clz(n));
10
       forn(i, 2*sz) t[i]=neutro;
11
     }
12
     void updall(){//0(n)}
13
       dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);}
14
     tipo get(int i, int j){return get(i,j,1,0,sz);}
15
     tipo get(int i, int j, int n, int a, int b){\frac{1}{0}}
16
       if(j<=a || i>=b) return neutro;
17
       if(i<=a && b<=j) return t[n];
18
       int c=(a+b)/2;
19
```

```
return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
                                                                                          if(j<=a || i>=b) return neutro;
20
                                                                                  28
                                                                                          push(n, a, b);//corrige el valor antes de usarlo
                                                                                  29
^{21}
     void set(int p, tipo val){//0(lgn)
                                                                                          if(i<=a && b<=j) return t[n];</pre>
                                                                                  30
^{22}
       for(p+=sz; p>0 && t[p]!=val;){
                                                                                          int c=(a+b)/2;
23
                                                                                  31
         t[p]=val;
                                                                                          return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
24
                                                                                  32
         p/=2;
25
                                                                                  33
         val=operacion(t[p*2], t[p*2+1]);
                                                                                        Elem get(int i, int j){return get(i,j,1,0,sz);}
26
                                                                                  34
                                                                                        //altera los valores en [i, j) con una alteración de val
                                                                                  35
27
     }
                                                                                        void alterar(Alt val, int i, int j, int n, int a, int b)\frac{1}{0(\lg n)}
28
                                                                                  36
                                                                                          push(n, a, b);
   }rmq;
                                                                                          if(j<=a || i>=b) return;
   //Usage:
                                                                                  38
31 | cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall();
                                                                                          if(i<=a && b<=j){
                                                                                  39
                                                                                            dirty[n]+=val;
                                                                                  40
2.3. RMQ (lazy)
                                                                                           push(n, a, b);
                                                                                            return:
                                                                                  42
                                                                                          }
1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
                                                                                          int c=(a+b)/2;
        sobre el rango [i, j).
                                                                                          alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
   typedef int Elem; //Elem de los elementos del arreglo
                                                                                          t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
   typedef int Alt;//Elem de la alteracion
                                                                                  46
   #define operacion(x,y) x+y
                                                                                  47
                                                                                        void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
   const Elem neutro=0; const Alt neutro2=0;
                                                                                   49 | }rmq;
   #define MAXN 100000
   struct RMQ{
                                                                                  2.4. RMQ (persistente)
     int sz:
8
     Elem t[4*MAXN]:
     Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem
                                                                                   typedef int tipo;
10
     Elem &operator[](int p){return t[sz+p];}
                                                                                     tipo oper(const tipo &a, const tipo &b){
11
     void init(int n){//O(nlgn)
                                                                                          return a+b;
                                                                                   3
12
       sz = 1 \ll (32-\_builtin\_clz(n));
                                                                                     }
                                                                                   4
13
       forn(i, 2*sz) t[i]=neutro;
                                                                                     struct node{
14
       forn(i, 2*sz) dirty[i]=neutro2;
                                                                                        tipo v; node *1,*r;
15
                                                                                       node(tipo v):v(v), 1(NULL), r(NULL) {}
16
     void push(int n, int a, int b){//propaga el dirty a sus hijos
                                                                                          node(node *1, node *r) : 1(1), r(r){
                                                                                   8
17
       if(dirty[n]!=0){
                                                                                              if(!1) v=r->v;
                                                                                   9
18
         t[n]+=dirty[n]*(b-a);//altera el nodo
                                                                                              else if(!r) v=l->v;
19
                                                                                  10
                                                                                              else v=oper(1->v, r->v);
         if(n<sz){
                                                                                  11
20
           dirty[2*n]+=dirty[n];
                                                                                          }
                                                                                  12
^{21}
           dirty[2*n+1]+=dirty[n];
                                                                                     }:
                                                                                  13
22
         }
                                                                                     node *build (tipo *a, int tl, int tr) {//modificar para que tome tipo a
23
         dirty[n]=0;
                                                                                       if (tl+1==tr) return new node(a[tl]);
24
                                                                                       int tm=(tl + tr)>>1:
       }
                                                                                  16
25
     }
                                                                                       return new node(build(a, tl, tm), build(a, tm, tr));
                                                                                  17
26
     Elem get(int i, int j, int n, int a, int b){\frac{1}{0}}
                                                                                  18 | }
```

```
node *update(int pos, int new_val, node *t, int tl, int tr){
     if (tl+1==tr) return new node(new_val);
20
     int tm=(tl+tr)>>1;
21
     if(pos < tm) return new node(update(pos, new_val, t->1, tl, tm), t->r)
^{22}
     else return new node(t->1, update(pos, new_val, t->r, tm, tr));
23
^{24}
   tipo get(int 1, int r, node *t, int tl, int tr){
25
       if(l==tl && tr==r) return t->v;
26
     int tm=(t1 + tr)>>1;
27
       if(r<=tm) return get(1, r, t->1, t1, tm);
28
       else if(1>=tm) return get(1, r, t->r, tm, tr);
29
     return oper(get(1, tm, t->1, t1, tm), get(tm, r, t->r, tm, tr));
31 | }
```

2.5. Fenwick Tree

```
1 //For 2D threat each column as a Fenwick tree, by adding a nested for in
        each operation
2 struct Fenwick{
     static const int sz=1000001;
     tipo t[sz];
4
     void adjust(int p, tipo v){//valid with p in [1, sz), O(lgn)
5
       for(; p<sz; p+=(p&-p)) t[p]+=v; }
6
     tipo sum(int p){//cumulative sum in [1, p], O(lgn)
7
       tipo s=0:
8
       for(; p; p-=(p&-p)) s+=t[p];
9
       return s;
10
11
     tipo sum(int a, int b){return sum(b)-sum(a-1);}
12
     //get largest value with cumulative sum less than or equal to x;
13
     //for smallest, pass x-1 and add 1 to result
14
     int getind(tipo x) {//O(lgn)
15
         int idx = 0, mask = N;
16
         while(mask && idx < N) {</pre>
17
           int t = idx + mask;
18
         if(x >= tree[t])
19
             idx = t, x -= tree[t];
20
           mask >>= 1;
21
22
         return idx;
23
     }};
24
```

2.6. Union Find

```
1 | struct UnionFind{
    vector<int> f;//the array contains the parent of each node
    void init(int n){f.clear(); f.insert(f.begin(), n, -1);}
3
    int comp(int x){return (f[x]=-1?x:f[x]=comp(f[x]));}//0(1)
4
    bool join(int i, int j) {
5
      bool con=comp(i)==comp(j);
6
      if(!con) f[comp(i)] = comp(j);
7
      return con:
8
    }};
9
```

2.7. Disjoint Intervals

```
bool operator (const ii &a, const ii &b) {return a.fst <b.fst;}
  //Stores intervals as [first, second]
   //in case of a collision it joins them in a single interval
   struct disjoint_intervals {
     set<ii>> segs;
     void insert(ii v) {//O(lgn)
       if(v.snd-v.fst==0.) return;//0J0
       set<ii>>::iterator it,at;
8
9
       at = it = segs.lower_bound(v);
       if (at!=segs.begin() && (--at)->snd >= v.fst)
10
         v.fst = at->fst, --it;
11
       for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))</pre>
12
         v.snd=max(v.snd, it->snd);
13
       segs.insert(v);
14
15
<sub>16</sub> | };
```

2.8. RMQ (2D)

```
1 struct RMQ2D{
     static const int sz=1024;
     RMQ t[sz];
3
     RMQ &operator[](int p){return t[sz/2+p];}
4
     void build(int n, int m){\frac{1}{0}}(nm)
       forr(y, sz/2, sz/2+m)
6
         t[y].build(m);
7
       forr(y, sz/2+m, sz)
8
         forn(x, sz)
9
           t[y].t[x]=0;
10
       dforn(y, sz/2)
```

bint(11 x=0){

forn(i, LMAX){

x/=BASE;

if (x) l=i+1;

n[i]=x %BASE:

1=1;

}

bint(string x){

}

7

8

9

10

11

12 13

14

15

```
forn(x, sz)
                                                                                           l=(x.size()-1)/BASEXP+1:
12
           t[y].t[x]=max(t[y*2].t[x], t[y*2+1].t[x]);
                                                                                               fill(n, n+LMAX, 0);
                                                                                   18
13
     }
                                                                                   19
14
     void set(int x, int y, tipo v){//0(lgm.lgn)}
                                                                                   20
15
       v + = sz/2;
                                                                                   21
16
       t[v].set(x, v);
17
                                                                                   22
                                                                                               }
       while(v/=2)
                                                                                   23
18
         t[y].set(x, max(t[y*2][x], t[y*2+1][x]));
                                                                                           }
19
     }
20
     //O(lgm.lgn)
21
     int get(int x1, int y1, int x2, int y2, int n=1, int a=0, int b=sz/2){
                                                                                   27
22
       if(y2<=a || y1>=b) return 0;
23
                                                                                   28
       if(y1<=a && b<=y2) return t[n].get(x1, x2);
                                                                                   29
24
       int c=(a+b)/2:
                                                                                   30
25
       return max(get(x1, y1, x2, y2, 2*n, a, c),
                                                                                   31
26
            get(x1, y1, x2, y2, 2*n+1, c, b));
                                                                                        }
                                                                                    32
27
    }
                                                                                       };
28
                                                                                   33
29
   //Example to initialize a grid of M rows and N columns:
                                                                                         bint c:
   RMQ2D rmq;
  forn(i, M)
32
    forn(j, N)
33
       cin >> rmq[i][j];
34
35 rmq.build(N, M);
                                                                                   41
2.9. Big Int
                                                                                       {
  #define BASEXP 6
                                                                                    44
   #define BASE 1000000
                                                                                        bint c;
                                                                                   45
   #define LMAX 1000
   struct bint{
       int 1;
5
       11 n[LMAX];
6
```

```
ll r=1;
           forn(i, sz(x)){
               n[i / BASEXP] += r * (x[x.size()-1-i]-'0');
               r*=10; if (r==BASE)r=1;
       void out(){
       cout << n[1-1];
       dforn(i, l-1) printf("%6.61lu", n[i]);//6=BASEXP!
    void invar(){
      fill(n+1, n+LMAX, 0);
       while(1>1 && !n[1-1]) 1--;
   bint operator+(const bint&a, const bint&b){
      c.1 = max(a.1, b.1);
      11 q = 0;
      forn(i, c.1) q += a.n[i]+b.n[i], c.n[i]=q %BASE, q/=BASE;
      if(q) c.n[c.l++] = q;
       c.invar();
       return c;
   pair<br/><br/>bint, bool> lresta(const bint& a, const bint& b) // c = a - b
      c.1 = max(a.1, b.1);
      11 q = 0;
      forn(i, c.l) q += a.n[i]-b.n[i], c.n[i]=(q+BASE) %BASE, q=(q+BASE)/
           BASE-1:
       c.invar():
       return make_pair(c, !q);
52 bint& operator-= (bint& a, const bint& b){return a=lresta(a, b).first;}
  bint operator- (const bint&a, const bint&b) {return lresta(a, b).first;}
  bool operator< (const bint&a, const bint&b){return !lresta(a, b).second
55 | bool operator <= (const bint&a, const bint&b) {return lresta(b, a).second
bool operator==(const bint&a, const bint&b){return a <= b && b <= a;}
```

```
bint operator*(const bint&a, ll b){
                                                                                                  dforn(j, rm.l) rm.n[j+1] = rm.n[j];
                                                                                  99
                                                                                                  rm.n[0] = a.n[i]:
       bint c;
                                                                                  100
58
                                                                                                  rm.l++;
       11 q = 0;
                                                                                  101
59
       forn(i, a.1) q += a.n[i]*b, c.n[i] = q BASE, q/=BASE;
                                                                                              }
                                                                                  102
60
                                                                                              11 q = rm.n[b.1] * BASE + rm.n[b.1-1];
       c.1 = a.1:
                                                                                  103
61
       while(q) c.n[c.l++] = q %BASE, q/=BASE;
                                                                                              ll u = q / (b.n[b.l-1] + 1);
62
                                                                                  104
       c.invar();
                                                                                              ll v = q / b.n[b.l-1] + 1;
                                                                                  105
                                                                                              while (u < v-1){
       return c;
64
                                                                                                  11 m = (u+v)/2;
65
                                                                                  107
   bint operator*(const bint&a, const bint&b){
                                                                                                  if (b*m \le rm) u = m;
       bint c;
                                                                                                  else v = m;
67
                                                                                  109
       c.1 = a.1+b.1;
68
                                                                                  110
       fill(c.n, c.n+b.1, 0);
                                                                                              c.n[i]=u:
                                                                                  111
       forn(i, a.1){
                                                                                              rm-=b*u:
                                                                                  112
70
           11 a = 0:
                                                                                          }
                                                                                  113
71
           forn(j, b.l) q += a.n[i]*b.n[j]+c.n[i+j], c.n[i+j] = q BASE, q
                                                                                        c.l=a.l;
                                                                                  114
72
                                                                                          c.invar();
                                                                                  115
                                                                                          return make_pair(c, rm);
           c.n[i+b.1] = q;
                                                                                  116
73
       }
                                                                                  117
74
       c.invar();
                                                                                      bint operator/(const bint&a, const bint&b){return ldiv(a, b).first;}
75
       return c;
                                                                                  bint operator %(const bint&a, const bint&b) {return ldiv(a, b).second;}
76
77
                                                                                   2.10. Modnum
   pair<bint, ll> ldiv(const bint& a, ll b){// c = a / b ; rm = a % b
78
     bint c;
79
                                                                                   1 struct mnum{
     11 \text{ rm} = 0;
80
                                                                                        static const tipo mod=12582917;
     dforn(i, a.1){
81
                                                                                        tipo v;
               rm = rm * BASE + a.n[i];
82
                                                                                        mnum(tipo v=0): v(v mod) {}
               c.n[i] = rm / b;
83
                                                                                        mnum operator+(mnum b){return v+b.v;}
               rm %= b;
84
                                                                                        mnum operator-(mnum b){return v>=b.v? v-b.v : mod-b.v+v;}
       }
85
                                                                                        mnum operator*(mnum b){return v*b.v;}
       c.1 = a.1;
86
                                                                                        mnum operator^(int n){
       c.invar();
87
                                                                                          if(!n) return 1;
       return make_pair(c, rm);
88
                                                                                          return n\%2? (*this)^(n/2)*(this) : (*this)^(n/2);}
                                                                                   10
89
                                                                                  11 };
   bint operator/(const bint&a, ll b){return ldiv(a, b).first;}
   11 operator %(const bint&a, 11 b) {return ldiv(a, b).second;}
                                                                                   2.11. Treap
   pair<br/>bint, bint> ldiv(const bint& a, const bint& b){
     bint c:
                                                                                   typedef int Key;
93
       bint rm = 0;
                                                                                   typedef struct node *pnode;
94
       dforn(i, a.1){
                                                                                   3 struct node{
95
           if (rm.l==1 && !rm.n[0])
96
                                                                                          Key key;
               rm.n[0] = a.n[i];
97
                                                                                          int prior, size;
                                                                                   5
           else{
98
                                                                                          pnode 1,r;
```

```
node(Key key=0, int prior=0): key(key), prior(prior), size(1), 1(0),
                                                                                               root=merge(t1,t3);
7
                                                                                   49
                                                                                           }
            r(0) {}
                                                                                   50
  };
                                                                                           void eraseKey(pnode &t, Key key) {
                                                                                   51
8
   struct treap {
                                                                                               if (!t) return;
                                                                                   52
                                                                                               push(t);
       pnode root;
                                                                                   53
10
       treap(): root(0) {}
                                                                                               if (key == t->key) t=merge(t->1, t->r);
11
       int size(pnode p) { return p ? p->size : 0; }
                                                                                               else if (key < t->key) eraseKey(t->1, key);
                                                                                   55
12
       int size() { return size(root); }
                                                                                               else eraseKey(t->r, key);
13
                                                                                   56
       void push(pnode p) {
                                                                                               pull(t);
                                                                                   57
14
           // modificar y propagar el dirty a los hijos aca(para lazy)
15
       }
                                                                                           void eraseKey(Key key) {eraseKey(root, key);}
                                                                                   59
16
                                                                                           pnode findKey(pnode t, Key key) {
       // Update function and size from children's values
17
                                                                                   60
       void pull(pnode p) {//recalcular valor del nodo aca (para rmq)
                                                                                               if (!t) return 0:
18
                                                                                   61
           p->size = 1 + size(p->1) + size(p->r);
                                                                                               if (key == t->key) return t;
                                                                                   62
19
       }
                                                                                               if (key < t->key) return findKey(t->1, key);
                                                                                   63
20
       pnode merge(pnode 1, pnode r) {
                                                                                               return findKey(t->r, key);
21
           if (!1 || !r) return 1 ? 1 : r;
                                                                                           }
22
                                                                                   65
           push(1), push(r);
                                                                                           pnode findKey(Key key) { return findKey(root, key); }
23
                                                                                           //****POS OPERATIONS*****// No mezclar con las funciones Key
           pnode t:
                                                                                   67
24
           if (1->prior < r->prior) 1->r=merge(1->r, r), t = 1;
                                                                                           //(No funciona con pos:)
25
           else r\rightarrow l=merge(1, r\rightarrow 1), t = r;
                                                                                           void splitSize(pnode t, int sz, pnode &1, pnode &r) {
                                                                                   69
26
           pull(t);
                                                                                               if (!t) return void(1 = r = 0);
                                                                                   70
27
           return t;
                                                                                               push(t);
                                                                                   71
28
                                                                                               if (sz \le size(t->1)) splitSize(t->1, sz, 1, t->1), r = t;
       }//opcional:
                                                                                   72
29
       void merge(treap t) {root = merge(root, t.root), t.root=0;}
                                                                                               else splitSize(t->r, sz - 1 - size(t->l), t->r, r), l = t;
                                                                                   73
30
       //*****KEY OPERATIONS****//
                                                                                               pull(t);
                                                                                   74
31
       void splitKey(pnode t, Key key, pnode &1, pnode &r) {
                                                                                           }
                                                                                   75
32
                                                                                           void insertPos(int pos, Key key) {
           if (!t) return void(1 = r = 0);
                                                                                   76
33
           push(t);
                                                                                               pnode elem = new node(key, rand());
                                                                                   77
34
           if (\text{key} \leftarrow \text{t->key}) splitKey(t->1, key, 1, t->1), r = t;
                                                                                               pnode t1,t2; splitSize(root, pos, t1, t2);
                                                                                   78
35
           else splitKey(t->r, key, t->r, r), l = t;
                                                                                               t1=merge(t1,elem);
                                                                                   79
36
           pull(t);
                                                                                               root=merge(t1,t2);
37
                                                                                   80
       }
                                                                                   81
38
       void insertKey(Key key) {
                                                                                           void erasePos(int pos1, int pos2=-1) {
                                                                                   82
39
                                                                                           if(pos2==-1) pos2=pos1+1;
           pnode elem = new node(key, rand());
                                                                                   83
40
           pnode t1, t2; splitKey(root, key, t1, t2);
                                                                                               pnode t1,t2,t3;
                                                                                   84
41
           t1=merge(t1,elem);
                                                                                               splitSize(root,pos1,t1,t2);
42
                                                                                   85
           root=merge(t1,t2);
                                                                                               splitSize(t2,pos2-pos1,t2,t3);
43
       }
                                                                                               root=merge(t1, t2);
                                                                                   87
44
       void eraseKeys(Key key1, Key key2) {
                                                                                   88
45
           pnode t1,t2,t3;
                                                                                           pnode findPos(pnode t, int pos) {
                                                                                   89
46
           splitKey(root,key1,t1,t2);
                                                                                               if(!t) return 0;
                                                                                   90
47
           splitKey(t2,key2, t2, t3);
                                                                                               if(pos <= size(t->1)) return findPos(t->1, pos);
                                                                                   91
48
```

32

```
return findPos(t->r, pos - 1 - size(t->l));
92
                                                                                    34
93
       Key &operator[](int pos){return findPos(root, pos)->key;}//ojito
94
                                                                                    35
  |};
95
                                                                                    36
                                                                                            }
                                                                                    37
                                                                                       }h;
                                                                                    38
         Convex Hull Trick
   const ll is_query = -(1LL<<62);</pre>
   struct Line {
       ll m, b;
       mutable multiset<Line>::iterator it;
       const Line *succ(multiset<Line>::iterator it) const;
5
       bool operator<(const Line& rhs) const {</pre>
6
           if (rhs.b != is_query) return m < rhs.m;</pre>
                                                                                       struct V{
           const Line *s=succ(it);
8
           if(!s) return 0;
9
           11 x = rhs.m;
                                                                                       };
                                                                                     7
           return b - s -> b < (s -> m - m) * x;
11
                                                                                       set<V> s;
       }
12
                                                                                       void add(V x){
   };
13
   struct HullDynamic : public multiset<Line>{ // will maintain upper hull
                                                                                    11
       for maximum
       bool bad(iterator y) {
15
                                                                                    13
           iterator z = next(y);
16
           if (y == begin()) {
17
                                                                                    15
                if (z == end()) return 0;
18
                                                                                    16
                return y->m == z->m && y->b <= z->b;
19
                                                                                    17
20
                                                                                    18
           iterator x = prev(y);
21
                                                                                         }
                                                                                    19
           if (z == end()) return y->m == x->m && y->b <= x->b;
22
                                                                                          s.insert(x);
                                                                                    20
           return (x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m)
23
                                                                                    21
                );
24
                                                                                    23
       iterator next(iterator y){return ++y;}
^{25}
                                                                                    24
       iterator prev(iterator y){return --y;}
26
       void insert_line(ll m, ll b) {
27
                                                                                           Algos
           iterator y = insert((Line) { m, b });
28
           y->it=y;
29
           if (bad(y)) { erase(y); return; }
30
           while (next(y) != end() && bad(next(y))) erase(next(y));
31
           while (y != begin() && bad(prev(y))) erase(prev(y));
```

```
}
33
       11 eval(ll x) {
           Line l = *lower_bound((Line) { x, is_query });
           return 1.m * x + 1.b;
   const Line *Line::succ(multiset<Line>::iterator it) const{
       return (++it==h.end()? NULL : &*it);}
```

2.13. Gain-Cost Set

```
1 //esta estructura mantiene pairs(beneficio, costo)
 //de tal manera que en el set quedan ordenados
 //por beneficio Y COSTO creciente. (va borrando los que no son optimos)
    int gain, cost;
    bool operator<(const V &b)const{return gain<b.gain;}</pre>
    set<V>::iterator p=s.lower_bound(x);//primer elemento mayor o igual
    if(p!=s.end() && p->cost <= x.cost) return;//ya hay uno mejor
    p=s.upper_bound(x);//primer elemento mayor
    if(p!=s.begin()){//borro todos los peores (<=beneficio y >=costo)
      --p;//ahora es ultimo elemento menor o igual
      while(p->cost >= x.cost){
        if(p==s.begin()){s.erase(p); break;}
        s.erase(p--);
  int get(int gain){//minimo costo de obtener tal ganancia
    set<V>::iterator p=s.lower_bound((V){gain, 0});
    return p==s.end()? INF : p->cost;}
```

3.1. Longest Increasing Subsecuence

1 //Para non-increasing, cambiar comparaciones y revisar busq binaria

```
2 //Given an array, paint it in the least number of colors so that each
       color turns to a non-increasing subsequence.
3 //Solution:Min number of colors=Length of the longest increasing
       subsequence
  int N, a[MAXN];//secuencia v su longitud
   ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
   int p[MAXN];//padres
   vector<int> R;//respuesta
   void rec(int i){
     if(i==-1) return;
     R.push_back(a[i]);
     rec(p[i]);
11
   }
12
   int lis(){//O(nlogn)
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
14
     forn(i, N){
15
       int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
16
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
18
         d[j] = ii(a[i], i);
19
       }
20
     }
21
     R.clear();
22
     dforn(i, N+1) if(d[i].first!=INF){
23
       rec(d[i].second);//reconstruir
24
       reverse(R.begin(), R.end());
25
       return i;//longitud
26
     }
27
     return 0;
28
29
3.2. Manacher
```

```
int d1[MAXN];//d1[i]=long del maximo palindromo impar con centro en i
int d2[MAXN];//d2[i]=analogo pero para longitud par

//0 1 2 3 4
//a a b c c <--d1[2]=3
//a a b b <--d2[2]=2 (estan uno antes)

void manacher(){
  int l=0, r=-1, n=sz(s);
  forn(i, n){
  int k=(i>r? 1 : min(d1[l+r-i], r-i));
  while(i+k<n && i-k>=0 && s[i+k]==s[i-k]) ++k;
```

```
d1[i] = k--:
11
       if(i+k > r) l=i-k, r=i+k;
12
     }
13
     l=0, r=-1;
14
     forn(i, n){
15
       int k=(i>r? 0 : min(d2[1+r-i+1], r-i+1))+1;
16
       while(i+k-1 \le k = 0 \ k \le [i+k-1] == s[i-k]) k++;
17
       d2[i] = --k:
18
       if(i+k-1 > r) l=i-k, r=i+k-1;
19
20
```

3.3. Alpha-Beta prunning

```
1 | 11 alphabeta(State &s, bool player = true, int depth = 1e9, 11 alpha = -
       INF, 11 beta = INF) { //player = true -> Maximiza
       if(s.isFinal()) return s.score;
2
     //~ if (!depth) return s.heuristic();
       vector<State> children;
4
       s.expand(player, children);
5
       int n = children.size();
6
       forn(i, n) {
7
           ll v = alphabeta(children[i], !player, depth-1, alpha, beta);
           if(!player) alpha = max(alpha, v);
9
           else beta = min(beta, v);
10
           if(beta <= alpha) break;</pre>
11
12
       return !player ? alpha : beta;}
13
```

4. Strings

4.1. KMP

```
string T;//cadena donde buscar(where)
 string P;//cadena a buscar(what)
   int b[MAXLEN];//back table
   void kmppre(){//by gabina with love
       int i =0, j=-1; b[0]=-1;
       while(i<sz(P)){</pre>
6
           while(j>=0 && P[i] != P[j]) j=b[j];
7
           i++, j++;
8
           b[i] = j;
9
       }
10
11 |}
```

tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];

15

```
memcpy(sa, tmpsa, sizeof(sa));
12
                                                                                  16
   void kmp(){
                                                                                  17
13
                                                                                     void constructsa(){\frac{}{0} n log n)
       int i=0, j=0;
                                                                                  18
14
       while(i<sz(T)){</pre>
                                                                                       n=sz(s);
15
                                                                                       forn(i, n) sa[i]=i, r[i]=s[i];
           while(j>=0 && T[i]!=P[j]) j=b[j];
16
                                                                                  20
                                                                                       for(int k=1; k<n; k<<=1){
           i++, j++;
17
                                                                                  21
           if(j==sz(P)){
                                                                                         countingSort(k), countingSort(0);
                                                                                  22
18
               printf("P_is_found_at_index_"%d_in_T\n", i-j);
                                                                                         int rank, tmpr[MAX_N];
                                                                                  23
19
                                                                                         tmpr[sa[0]]=rank=0;
               j=b[j];
20
                                                                                  24
           }
                                                                                         forr(i, 1, n)
21
       }
                                                                                            tmpr[sa[i]] = r[sa[i-1]] \&\& r[sa[i]+k] = r[sa[i-1]+k])?
22
                                                                                  26
                                                                                                rank : ++rank;
23
                                                                                          memcpy(r, tmpr, sizeof(r));
                                                                                  27
4.2.
       Trie
                                                                                         if(r[sa[n-1]]==n-1) break:
                                                                                       }
                                                                                  29
  struct trie{
                                                                                     }
                                                                                  30
     map<char, trie> m;
                                                                                     void print(){//for debug
     void add(const string &s, int p=0){
                                                                                       forn(i, n)
       if(s[p]) m[s[p]].add(s, p+1);
4
                                                                                         cout << i << ''' <<
                                                                                  33
     }
5
                                                                                          s.substr(sa[i], s.find( '$', sa[i])-sa[i]) << endl;}
     void dfs(){
6
       //Do stuff
                                                                                  4.4. String Matching With Suffix Array
       forall(it, m)
8
         it->second.dfs();
9
                                                                                   1 //returns (lowerbound, upperbound) of the search
    }
10
                                                                                     ii stringMatching(string P){ //O(sz(P)lgn)
11 | };
                                                                                       int lo=0, hi=n-1, mid=lo;
      Suffix Array (largo, nlogn)
                                                                                       while(lo<hi){
                                                                                         mid=(lo+hi)/2;
                                                                                   5
  #define MAX_N 1000
                                                                                         int res=s.compare(sa[mid], sz(P), P);
                                                                                   6
   #define rBOUND(x) (x<n? r[x] : 0)
                                                                                         if(res>=0) hi=mid;
                                                                                   7
   //sa will hold the suffixes in order.
                                                                                          else lo=mid+1;
                                                                                   8
   int sa[MAX_N], r[MAX_N], n;
                                                                                   9
   string s; //input string, n=sz(s)
                                                                                       if(s.compare(sa[lo], sz(P), P)!=0) return ii(-1, -1);
                                                                                  10
                                                                                       ii ans; ans.fst=lo;
                                                                                  11
6
   int f[MAX_N], tmpsa[MAX_N];
                                                                                       lo=0, hi=n-1, mid;
                                                                                  12
   void countingSort(int k){
                                                                                       while(lo<hi){</pre>
8
                                                                                  13
     zero(f);
                                                                                         mid=(lo+hi)/2;
                                                                                  14
                                                                                         int res=s.compare(sa[mid], sz(P), P);
     forn(i, n) f[rBOUND(i+k)]++;
                                                                                  15
10
     int sum=0:
                                                                                         if(res>0) hi=mid:
                                                                                  16
11
     forn(i, max(255, n)){
                                                                                          else lo=mid+1;
                                                                                  17
12
       int t=f[i]; f[i]=sum; sum+=t;}
13
                                                                                  18
     forn(i, n)
                                                                                       if(s.compare(sa[hi], sz(P), P)!=0) hi--;
                                                                                  19
14
```

ans.snd=hi;

19

20

if(!link){

```
if(!padre) link=this;//es la raiz
     return ans:
                                                                                 21
22 }
                                                                                           else if(!padre->padre) link=padre;//hijo de la raiz
                                                                                 22
                                                                                           else link=padre->get_link()->get_tran(pch);
                                                                                 23
4.5. LCP (Longest Common Prefix)
                                                                                 ^{24}
                                                                                         return link;
                                                                                 25
   //Calculates the LCP between consecutives suffixes in the Suffix Array.
                                                                                 26
    //LCP[i] is the length of the LCP between sa[i] and sa[i-1]
                                                                                       trie* get_tran(int c) {
                                                                                 27
   int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
                                                                                         if(!tran[c])
                                                                                 28
   void computeLCP(){//0(n)}
                                                                                           tran[c] = !padre? this : this->get_link()->get_tran(c);
                                                                                 29
     phi[sa[0]]=-1;
5
                                                                                         return tran[c];
     forr(i, 1, n) phi[sa[i]]=sa[i-1];
6
                                                                                      }
                                                                                 31
     int L=0;
                                                                                      trie *get_nxthoja(){
                                                                                 32
     forn(i, n){
8
                                                                                         if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
                                                                                 33
       if(phi[i]==-1) {PLCP[i]=0; continue;}
9
                                                                                         return nxthoja;
                                                                                 34
       while(s[i+L] == s[phi[i]+L]) L++;
10
                                                                                 35
       PLCP[i]=L:
11
                                                                                      void print(int p){
                                                                                 36
       L=max(L-1, 0);
12
                                                                                         if(idhoja)
                                                                                 37
13
                                                                                           cout << "found," << idhoja << ", , at, position, " << p-szhoja << endl
                                                                                 38
     forn(i, n) LCP[i]=PLCP[sa[i]];
14
15
                                                                                         if(get_nxthoja()) get_nxthoja()->print(p);
       Corasick
                                                                                 40
                                                                                       void matching(const string &s, int p=0){
                                                                                 41
                                                                                         print(p);
                                                                                 42
1
                                                                                         if(p<sz(s)) get_tran(s[p])->matching(s, p+1);
                                                                                 43
   struct trie{
     map<char, trie> next;
3
                                                                                       Geometria
     trie* tran[256];//transiciones del automata
4
     int idhoja, szhoja;//id de la hoja o 0 si no lo es
                                                                                  5.1. Punto
     //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
6
         es hoja
     trie *padre, *link, *nxthoja;
                                                                                  1 struct pto{
7
     char pch;//caracter que conecta con padre
                                                                                       tipo x, v;
8
     trie(): tran(), idhoja(), padre(), link() {}
                                                                                       pto(tipo x=0, tipo y=0):x(x),y(y){}
9
                                                                                      pto operator+(pto a){return pto(x+a.x, y+a.y);}
     void insert(const string &s, int id=1, int p=0){//id>0!!!
10
       if(p<sz(s)){</pre>
                                                                                      pto operator-(pto a){return pto(x-a.x, y-a.y);}
11
         trie &ch=next[s[p]];
                                                                                      pto operator+(tipo a){return pto(x+a, y+a);}
12
                                                                                  6
                                                                                      pto operator*(tipo a){return pto(x*a, y*a);}
         tran[(int)s[p]]=&ch;
13
                                                                                      pto operator/(tipo a){return pto(x/a, y/a);}
         ch.padre=this, ch.pch=s[p];
14
                                                                                      //dot product, producto interno:
         ch.insert(s, id, p+1);
15
                                                                                  9
       }
                                                                                       tipo operator*(pto a){return x*a.x+y*a.y;}
                                                                                 10
16
                                                                                      //module of the cross product or vectorial product:
       else idhoja=id, szhoja=sz(s);
                                                                                 11
17
                                                                                      //if a is less than 180 clockwise from b, a^b>0
18
                                                                                 12
     trie* get_link() {
                                                                                      tipo operator^(pto a){return x*a.y-y*a.x;}
```

13

//returns true if this is at the left side of line gr

22

23

return r;

return pto(INF, INF);

```
bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
15
     bool operator<(const pto &a) const{return x<a.x || (abs(x-a.x)<EPS &&
16
         y<a.y);}
   bool operator==(pto a){return abs(x-a.x)<EPS && abs(y-a.y)<EPS;}
     double norm(){return sqrt(x*x+y*y);}
18
     tipo norm_sq(){return x*x+y*y;}
19
20
   double dist(pto a, pto b){return (b-a).norm();}
   typedef pto vec;
23
   double angle(pto a, pto o, pto b){
     pto oa=a-o, ob=b-o;
     return atan2(oa^ob, oa*ob);}
   //rotate p by theta rads CCW w.r.t. origin (0,0)
   pto rotate(pto p, double theta){
     return pto(p.x*cos(theta)-p.y*sin(theta),
30
        p.x*sin(theta)+p.y*cos(theta));
31
32
33
   //orden total de puntos alrededor de un punto r
   struct Cmp{
35
     pto r;
36
     Cmp(pto _r)\{r = _r;\}
37
     int cuad(const pto &a) const{
38
       if(a.x > 0 \&\& a.y >= 0)return 0;
39
       if(a.x <= 0 && a.y > 0)return 1;
40
       if(a.x < 0 && a.y <= 0)return 2;
41
       if(a.x >= 0 \&\& a.y < 0)return 3;
42
       assert(a.x ==0 && a.y==0);
43
       return -1;
44
45
     bool cmp(const pto&p1, const pto&p2)const{
46
       int c1 = cuad(p1), c2 = cuad(p2);
47
       if(c1==c2){}
48
         return p1.y*p2.x<p1.x*p2.y;
49
       }else{
50
         return c1 < c2:
51
     }}
52
   bool operator()(const pto&p1, const pto&p2) const{
   return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
55
56 };
```

5.2. Line

```
int sgn(ll x){return x<0? -1 : !!x;}</pre>
   struct line{
     line() {}
     double a,b,c;//Ax+By=C
   //pto MUST store float coordinates!
    line(double a, double b, double c):a(a),b(b),c(c){}
    line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
     int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
9
   bool parallels(line 11, line 12){return abs(11.a*12.b-12.a*11.b)<EPS;}
   pto inter(line 11, line 12){//intersection
     double det=11.a*12.b-12.a*11.b;
    if(abs(det) < EPS) return pto(INF, INF); //parallels</pre>
     return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
15 }
5.3. Segment
struct segm{
     pto s,f;
     segm(pto s, pto f):s(s), f(f) {}
     pto closest(pto p) {//use for dist to point
        double 12 = dist_sq(s, f);
        if(12==0.) return s:
6
        double t = ((p-s)*(f-s))/12;
        if (t<0.) return s;//not write if is a line
        else if(t>1.)return f;//not write if is a line
        return s+((f-s)*t);
10
    }
11
     bool inside(pto p){
   return ((s-p)^(f-p))==0 \&\& min(s, f)<*this&&*this<max(s, f);}
   };
14
15
   bool insidebox(pto a, pto b, pto p) {
     return (a.x-p.x)*(p.x-b.x)>-EPS && (a.y-p.y)*(p.y-b.y)>-EPS;
17
18
   pto inter(segm s1, segm s2){
     pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
     if(insidebox(s1.s,s1.f,p) && insidebox(s2.s,s2.f,p))
21
```

```
24 }
5.4. Rectangle
  struct rect{
     //lower-left and upper-right corners
     pto lw, up;
3
  };
4
   //returns if there's an intersection and stores it in r
   bool inter(rect a, rect b, rect &r){
     r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
7
    r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
   //check case when only a edge is common
     return r.lw.x<r.up.x && r.lw.y<r.up.y;</pre>
10
11 }
5.5. Polygon Area
double area(vector<pto> &p){//O(sz(p))
     double area=0;
2
    forn(i, sz(p)) area+=p[i]^p[(i+1) %z(p)];
    //if points are in clockwise order then area is negative
     return abs(area)/2;
6
   //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
  //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
5.6. Circle
  vec perp(vec v){return vec(-v.y, v.x);}
  line bisector(pto x, pto y){
    line l=line(x, y); pto m=(x+y)/2;
     return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
4
   }
5
   struct Circle{
6
     pto o;
7
     double r;
8
     Circle(pto x, pto y, pto z){
9
       o=inter(bisector(x, y), bisector(y, z));
10
       r=dist(o, x);
11
12
     pair<pto, pto> ptosTang(pto p){
13
       pto m=(p+o)/2;
14
```

tipo d=dist(o, m);

```
tipo a=r*r/(2*d);
       tipo h=sqrt(r*r-a*a);
       pto m2=o+(m-o)*a/d;
       vec per=perp(m-o)/d;
       return mkp(m2-per*h, m2+per*h);
20
21
   };
22
   //finds the center of the circle containing p1 and p2 with radius r
   //as there may be two solutions swap p1, p2 to get the other
   bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
           double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
26
           if(det<0) return false;</pre>
27
           c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
28
           return true;
29
30
   #define sqr(a) ((a)*(a))
   #define feq(a,b) (fabs((a)-(b))<EPS)</pre>
   pair<tipo, tipo > ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
     tipo dx = sqrt(b*b-4.0*a*c);
     return make_pair((-b + dx)/(2.0*a), (-b - dx)/(2.0*a));
36
   pair<pto, pto> interCL(Circle c, line 1){
     bool sw=false;
38
     if((sw=feq(0,1.b))){
39
     swap(1.a, 1.b);
40
     swap(c.o.x, c.o.y);
41
42
     pair<tipo, tipo> rc = ecCuad(
43
     sqr(1.a)+sqr(1.b),
44
     2.0*1.a*1.b*c.o.y-2.0*(sqr(1.b)*c.o.x+1.c*1.a),
45
     sqr(1.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(1.c)-2.0*1.c*1.b*c.o.y
46
47
     pair<pto, pto> p( pto(rc.first, (1.c - 1.a * rc.first) / 1.b),
48
               pto(rc.second, (l.c - l.a * rc.second) / l.b) );
49
     if(sw){
50
     swap(p.first.x, p.first.y);
51
     swap(p.second.x, p.second.y);
52
53
54
     return p;
   pair<pto, pto> interCC(Circle c1, Circle c2){
     line 1;
     1.a = c1.o.x-c2.o.x;
```

```
1.b = c1.o.y-c2.o.y;
1.c = (sqr(c2.r)-sqr(c1.r)+sqr(c1.o.x)-sqr(c2.o.x)+sqr(c1.o.y)
-sqr(c2.o.y))/2.0;
return interCL(c1, 1);
}
```

5.7. Point in Poly

```
//checks if v is inside of P, using ray casting
   //works with convex and concave.
   //excludes boundaries, handle it separately using segment.inside()
  bool inPolygon(pto v, vector<pto>& P) {
     bool c = false;
5
     forn(i, sz(P)){
6
       int j=(i+1) \%z(P);
7
      if((P[j].y>v.y) != (P[i].y > v.y) &&
8
     (v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))
         c = !c;
10
     }
11
     return c;
12
13 | }
```

5.8. Convex Check CHECK

```
bool isConvex(vector<int> &p){//O(N)
    int N=sz(p);
    if(N<3) return false;
    bool isLeft=p[0].left(p[1], p[2]);
    forr(i, 1, N)
        if(p[i].left(p[(i+1) M], p[(i+2) M])!=isLeft)
        return false;
    return true; }</pre>
```

5.9. Convex Hull

```
//stores convex hull of P in S, CCW order
void CH(vector<pto>& P, vector<pto>&S){
    S.clear();
    sort(P.begin(), P.end());
    forn(i, sz(P)){
        while(sz(S)>= 2 && S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
        S.pb(P[i]);
    }
    S.pop_back();
```

5.10. Cut Polygon

```
1 //cuts polygon Q along the line ab
2 //stores the left side (swap a, b for the right one) in P
  void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
    P.clear();
    forn(i, sz(Q)){
5
       double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1) \sz(Q)]-a);
       if(left1>=0) P.pb(Q[i]);
7
       if(left1*left2<0)
8
         P.pb(inter(line(Q[i], Q[(i+1) \slashz(Q)]), line(a, b)));
9
    }
10
11 }
```

5.11. Bresenham

```
1 //plot a line approximation in a 2d map
   void bresenham(pto a, pto b){
     pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
     pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
     int err=d.x-d.y;
     while(1){
       m[a.x][a.y]=1;//plot
       if(a==b) break;
       int e2=2*err;
       if(e2 > -d.y){
         err-=d.y, a.x+=s.x;
11
       if(e2 < d.x)
13
         err+= d.x, a.y+= s.y;
    }
14
15 }
```

5.12. Rotate Matrix

1 //rotates matrix t 90 degrees clockwise

```
2 //using auxiliary matrix t2(faster)
  void rotate(){
     forn(x, n) forn(y, n)
       t2[n-y-1][x]=t[x][y];
     memcpy(t, t2, sizeof(t));
7
5.13. Interseccion de Circulos en n3log(n)
  struct event {
       double x; int t;
       event(double xx, int tt) : x(xx), t(tt) {}
       bool operator <(const event &o) const { return x < o.x; }</pre>
5
   typedef vector<Circle> VC;
   typedef vector<event> VE;
   double cuenta(VE &v, double A, double B) {
       sort(v.begin(), v.end());
10
       double res = 0.0, lx = ((v.empty())?0.0:v[0].x);
11
       int contador = 0;
12
       forn(i,sz(v)) {
13
           // interseccion de todos (contador == n), union de todos (
14
               contador > 0).
           // conjunto de puntos cubierto por exacta k Circulos (contador
15
           if (contador == n) res += v[i].x - lx;
16
           contador += v[i].t;
17
           lx = v[i].x;
18
19
       return res;
20
^{21}
   // Primitiva de sqrt(r*r - x*x) como funcion double de una variable x.
22
   inline double primitiva(double x,double r) {
23
       if (x \ge r) return r*r*M_PI/4.0;
24
       if (x \le -r) return -r*r*M_PI/4.0;
25
       double raiz = sqrt(r*r-x*x);
26
       return 0.5 * (x * raiz + r*r*atan(x/raiz));
27
28
```

vector<double> p; p.reserve(v.size() * (v.size() + 2));

 $p.push_back(v[i].c.x + v[i].r);$

double interCircle(VC &v) {

forn(i,sz(v)) {

29

30

31

32

```
p.push_back(v[i].c.x - v[i].r);
33
34
       forn(i,sz(v)) forn(j,i) {
35
           Circle &a = v[i], b = v[j];
36
           double d = (a.c - b.c).norm();
37
           if (fabs(a.r - b.r) < d \&\& d < a.r + b.r) {
                double alfa = acos((sqr(a.r) + sqr(d) - sqr(b.r)) / (2.0 * d)
39
                     * a.r));
                pto vec = (b.c - a.c) * (a.r / d);
                p.pb((a.c + rotate(vec, alfa)).x);
                p.pb((a.c + rotate(vec, -alfa)).x);
42
43
       }
44
       sort(p.begin(), p.end());
       double res = 0.0;
       forn(i,sz(p)-1) {
            const double A = p[i], B = p[i+1];
48
           VE ve; ve.reserve(2 * v.size());
49
           forn(j,sz(v)) {
50
                const Circle &c = v[j];
51
                double arco = primitiva(B-c.c.x,c.r) - primitiva(A-c.c.x,c.r
52
                    );
                double base = c.c.y * (B-A);
53
                ve.push_back(event(base + arco,-1));
54
                ve.push_back(event(base - arco, 1));
55
56
           res += cuenta(ve,A,B);
57
58
       return res;
59
60 }
```

6. Math

6.1. Identidades

```
\sum_{i=0}^{n} {n \choose i} = 2^n
\sum_{i=0}^{n} i {n \choose i} = n * 2^{n-1}
\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}
\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}
\sum_{i=0}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6}
\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2}+1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}
\sum_{i=0}^{n} i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^{n} i\right]^2
```

```
\sum_{i=0}^{n} i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}
\sum_{i=0}^{n} i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_k}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}
r = e - v + k + 1
Teorema de Pick: (Area, puntos interiores y puntos en el borde)
A = I + \frac{B}{2} - 1
```

6.2. Ec. Caracteristica

```
\begin{aligned} a_0T(n) + a_1T(n-1) + \ldots + a_kT(n-k) &= 0 \\ p(x) = a_0x^k + a_1x^{k-1} + \ldots + a_k \\ \text{Sean } r_1, r_2, \ldots, r_q \text{ las raíces distintas, de mult. } m_1, m_2, \ldots, m_q \\ T(n) &= \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij} n^j r_i^n \\ \text{Las constantes } c_{ij} \text{ se determinan por los casos base.} \end{aligned}
```

6.3. Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
    comb[i][0]=comb[i][i]=1;
    forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1]) MOD;
}

ll lucas (ll n, ll k, int p){ //Calcula (n,k) %p teniendo comb[p][p]
    precalculado.
    ll aux = 1;
    while (n + k){
        aux = (aux * comb[n %p][k %p]) %p;
        n/=p, k/=p;
    }
    return aux;
}
```

6.4. Exp. de Numeros Mod.

6.5. Exp. de Matrices y Fibonacci en log(n)

```
struct M22{ // |a b|
tipo a,b,c,d;// |c d|
```

```
M22 operator*(const M22 &p) const {
    return (M22){a*p.a+b*p.c, a*p.b+b*p.d, c*p.a+d*p.c,c*p.b+d*p.d};}
};
M22 operator^(const M22 &p, int n){
    if(!n) return (M22){1, 0, 0, 1};//identidad
    M22 q=p^(n/2); q=q*q;
    return n%2? p * q : q;}

11 fibo(ll n){//calcula el fibonacci enesimo
    M22 mat=(M22){0, 1, 1, 1}^n;
    return mat.a*f0+mat.b*f1;//f0 y f1 son los valores iniciales
}
```

6.6. Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)$$

6.7. Funciones de primos

```
1 | 11 numPrimeFactors (11 n) {
     11 \text{ rta} = 0;
     map<ll, ll> f=fact(n);
     forall(it, f) rta += it->second:
     return rta:
6
   11 numDiffPrimeFactors (11 n){
     ll rta = 0;
     map<ll,11> f=fact(n);
     forall(it, f) rta += 1;
11
     return rta;
12
13
14
   11 sumPrimeFactors (ll n){
     ll rta = 0;
16
     map<ll, ll> f=fact(n);
17
     forall(it, f) rta += it->first;
18
     return rta:
19
20
21
22 | 11 numDiv (11 n) {
```

if (b % 2 == 1) x = (x+y) % c;

```
ll rta = 1;
                                                                                           y = (y*2) \% c;
23
     map<ll,ll> f=fact(n);
                                                                                           b /= 2;
                                                                                    8
^{24}
     forall(it, f) rta *= (it->second + 1);
25
                                                                                    9
     return rta;
                                                                                         return x % c;
26
                                                                                    10
                                                                                   11
27
28
   ll sumDiv (ll n){
                                                                                       ll expmod (ll b, ll e, ll m){\frac{1}{0}} \log b
29
     ll rta = 1;
                                                                                        if(!e) return 1;
30
     map<ll,ll> f=fact(n);
                                                                                        11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
31
     forall(it, f) rta *= ((11)pow((double)it->first, it->second + 1.0)-1)
                                                                                        return e %2? mulmod(b,q,m) : q;
32
         / (it->first-1);
                                                                                   17
     return rta;
33
                                                                                    18
                                                                                       bool es_primo_prob (ll n, int a)
34
                                                                                   20
35
   ll eulerPhi (ll n){ // con criba: O(lg n)
                                                                                         if (n == a) return true:
                                                                                   21
36
     11 \text{ rta} = n;
                                                                                        11 s = 0, d = n-1;
37
                                                                                         while (d \% 2 == 0) s++, d/=2;
     map<ll,ll> f=fact(n);
38
     forall(it, f) rta -= rta / it->first;
39
                                                                                   24
     return rta:
                                                                                         11 x = expmod(a,d,n);
                                                                                   25
40
                                                                                         if ((x == 1) \mid | (x+1 == n)) return true;
41
                                                                                   27
42
   11 eulerPhi2 (11 n){ // 0 (sqrt n)
                                                                                        forn (i, s-1){
                                                                                        x = mulmod(x, x, n);
     11 r = n;
44
     forr (i,2,n+1){
                                                                                          if (x == 1) return false;
45
       if ((ll)i*i > n)
                                                                                           if (x+1 == n) return true;
                                                                                   31
46
         break;
                                                                                   32
47
       if (n \% i == 0){
                                                                                         return false;
                                                                                   33
48
         while (n\% == 0) n/=i;
                                                                                   34
49
         r -= r/i;
50
       }}
                                                                                       bool rabin (ll n){ //devuelve true si n es primo
51
     if (n != 1)
                                                                                         if (n == 1) return false;
52
                                                                                        const int ar[] = \{2,3,5,7,11,13,17,19,23\};
       r=r/n;
53
                                                                                        forn (i.9)
     return r:
                                                                                   39
54
                                                                                           if (!es_primo_prob(n,ar[j]))
55 }
                                                                                             return false:
                                                                                   41
6.8. Phollard's Rho (rolando)
                                                                                         return true:
                                                                                    42
                                                                                       }
                                                                                   43
1 | ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
                                                                                      ll rho(ll n){
2
                                                                                           if( (n & 1) == 0 ) return 2;
3 | 11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %, and minimize overfloor
                                                                                          11 x = 2 , y = 2 , d = 1;
    11 x = 0, y = a\%;
                                                                                           ll c = rand() % n + 1;
    while (b > 0){
                                                                                   48
5
                                                                                           while( d == 1){
```

n/=criba[n];

19

```
x = (mulmod(x, x, n) + c) n;
50
                                                                                  20
           y = (mulmod(y, y, n) + c) %n;
                                                                                        if(n>1) ret[n]++;
                                                                                  21
51
           y = (mulmod(y, y, n) + c) %n;
                                                                                        return ret;
                                                                                  22
52
           if(x - y \ge 0) d = gcd(x - y, n);
                                                                                   23
53
           else d = gcd(y - x, n);
54
                                                                                   24
       }
                                                                                      map<11,11> f3;
55
                                                                                      void fact3(11 n){ //O (lg n)^3. un solo numero
       return d;
56
                                                                                          if (n == 1) return;
57 |}
                                                                                          if (rabin(n))
       Criba
                                                                                              f3[n]++;
                                                                                          else{
   #define MAXP 80000 //no necesariamente primo
                                                                                              11 \text{ aux} = \text{rho(n)};
   int criba[MAXP+1];
                                                                                              fact3(aux); fact3(n/aux);
                                                                                   32
   void crearcriba(){
                                                                                          }
     int w[] = \{4,2,4,2,4,6,2,6\};
                                                                                        if(n>1) f3[n]++;
    for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
                                                                                        return;
                                                                                   35
    for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
                                                                                      }
                                                                                   36
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
                                                                                   37
    for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])</pre>
                                                                                      //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
      for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
                                                                                      void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::
10
                                                                                          iterator it, ll n=1){
                                                                                          if(it==f.begin()) divs.clear();
6.10. Factorizacion
                                                                                          if(it==f.end()) {
                                                                                   41
Sea n = \prod p_i^{k_i}, fact(n) genera un map donde a cada p_i le asocia su k_i
                                                                                              if(n>1) divs.pb(n);
                                                                                              return;
1 //factoriza bien numeros hasta MAXP^2
                                                                                   43
                                                                                          }
  map<ll,ll> fact(ll n){ //0 (cant primos)
                                                                                   44
                                                                                          ll p=it->fst, k=it->snd; ++it;
     map<11,11> ret;
                                                                                   45
                                                                                          forn(_, k+1)
    forall(p, primos){
                                                                                              divisores(f, divs, it, n), n*=p;
       while(!(n %*p)){
                                                                                   47
                                                                                   48 }
         ret[*p]++;//divisor found
6
         n/=*p;
       }
8
                                                                                   6.11. GCD
     }
9
     if(n>1) ret[n]++;
10
                                                                                   tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
     return ret;
11
12
                                                                                   6.12. Extended Euclid
13
   //factoriza bien numeros hasta MAXP
   map<11,11> fact2(11 n){ //0 (lg n)
                                                                                   void extendedEuclid (ll a, ll b) \{ //a * x + b * y = d \}
                                                                                       if (!b) { x = 1; y = 0; d = a; return;}
     map<11,11> ret;
16
     while (criba[n]){
                                                                                        extendedEuclid (b, a%);
17
       ret[criba[n]]++;
                                                                                        11 x1 = y;
18
                                                                                   4
```

11 y1 = x - (a/b) * y;

return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}

12

```
x = x1; y = y1;
7 |}
                                                                                        tipo a = mcd(q, o.q);
                                                                                 14
                                                                                 15
6.13. LCM
                                                                                      frac operator*(frac o){
                                                                                 16
                                                                                 17
tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
                                                                                 18
                                                                                      frac operator/(frac o){
                                                                                 19
6.14. Inversos
  #define MAXMOD 15485867
  | 11 inv[MAXMOD];//inv[i]*i=1 mod MOD
                                                                                 23
  void calc(int p){\frac{}{0}}
                                                                                 24 | };
    inv[1]=1;
4
    forr(i, 2, p) inv[i]= p-((p/i)*inv[p%i])%;
5
                                                                                 6.17. Polinomio
6
  int inverso(int x){\frac{1}{0(\log x)}}
7
                                                                                  1 struct poly {
    return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
     return expmod(x, MOD-2);//si mod es primo
9
                                                                                 3
10 }
                                                                                        poly() {}
6.15. Simpson
                                                                                        return sz(c); }
  double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
                                                                                 7
     double area=0, h=(b-a)/n, fa=f(a), fb;
                                                                                 8
2
    forn(i, n){
                                                                                 9
3
                                                                                 10
       fb=f(a+h*(i+1));
4
                                                                                 11
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
5
                                                                                 12
    }
6
                                                                                            return poly(res);
                                                                                 13
     return area*h/6.:}
                                                                                 14
6.16. Fraction
                                                                                 15
                                                                                 16
   tipo mcd(tipo a, tipo b){return a?mcd(b%, a):b;}
                                                                                 17
  struct frac{
2
                                                                                 18
                                                                                            return poly(res);
     tipo p,q;
                                                                                 19
3
    frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
4
                                                                                 20
                                                                                       tipo eval(tipo v) {
     void norm(){
                                                                                 21
       tipo a = mcd(p,q);
                                                                                        tipo sum = 0;
                                                                                 22
6
       if(a) p/=a, q/=a;
                                                                                 23
       else q=1;
                                                                                        return sum:
                                                                                 24
8
       if (q<0) q=-q, p=-p;}
                                                                                      }
                                                                                 25
9
     frac operator+(const frac& o){
10
                                                                                 26
       tipo a = mcd(q, o.q);
                                                                                 27
11
```

```
frac operator-(const frac& o){
  return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
  tipo a = mcd(q,o.p), b = mcd(o.q,p);
  return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
  tipo a = mcd(q,o.q), b = mcd(o.p,p);
  return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
bool operator<(const frac &o) const{return p*o.q < o.p*q;}</pre>
bool operator==(frac o){return p==o.p&kq==o.q;}
  vector<tipo> c;//guarda los coeficientes del polinomio
  poly(const vector<tipo> &c): c(c) {}
int gr(){//calculates grade of the polynomial
bool isnull() {return c.empty();}
  poly operator+(const poly &o) const {
      int m = sz(c), n = sz(o.c):
      vector<tipo> res(max(m,n));
      forn(i, m) res[i] += c[i];
      forn(i, n) res[i] += o.c[i];
  poly operator*(const poly &o) const {
      int m = sz(c), n = sz(o.c);
      vector<tipo> res(m+n-1);
      forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
  forall(it, c) sum=sum*v + *it;
  //poly contains only a vector<int> c (the coeficients)
//the following function generates the roots of the polynomial
```

28 //it can be easily modified to return float roots

```
set<tipo> roots(){
                                                                                 71 //main function, call this to parse
29
       set<tipo> roots;
                                                                                 poly E(string &s) {
30
       tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
                                                                                      polv e=T(s);
31
       vector<tipo> ps,qs;
                                                                                      if (LAST(s)=='+')\{POP(s); return E(s)+e;\}
32
       forr(p,1,sqrt(a0)+1) if (a0%p==0) ps.pb(p),ps.pb(a0/p);
                                                                                      return e;
33
       forr(q,1,sqrt(an)+1) if (an \% ==0) qs.pb(q),qs.pb(an/q);
                                                                                 76 }
34
       forall(pt,ps)
35
                                                                                 6.18. Ec. Lineales
         forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
36
           tipo root = abs((*pt) / (*qt));
37
           if (eval(root)==0) roots.insert(root);
                                                                                  bool resolver_ev(Mat a, Vec v, Vec &x, Mat &ev){
38
         }
                                                                                      int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
39
       return roots;
                                                                                      vector<int> p; forn(i,m) p.push_back(i);
40
     }
                                                                                      forn(i, rw) {
41
                                                                                        int uc=i, uf=i;
42
   poly interpolate(const vector<tipo> &x, const vector<tipo> &y) {
                                                                                        forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;
43
       int n = sz(x);
44
                                                                                             uc=c:}
       poly p;
                                                                                        if (feq(a[uf][uc], 0)) { rw = i; break; }
45
                                                                                  7
       vector<tipo> aux(2);
                                                                                        forn(j, n) swap(a[j][i], a[j][uc]);
46
                                                                                  8
       forn(i, n) {
                                                                                        swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
47
          double a = y[i] - p.eval(x[i]);
                                                                                         tipo inv = 1 / a[i][i]; //aca divide
48
          forn(j, i) a /= x[i] - x[j];
                                                                                        forr(j, i+1, n) {
49
          poly add(vector<tipo>(1, a));
                                                                                          tipo v = a[j][i] * inv;
50
          forn(j, i) aux[0]=-x[j], aux[1]=1, add = add*aux;
                                                                                          forr(k, i, m) a[j][k]-=v * a[i][k];
51
          p = p + add;
                                                                                          y[j] -= v*y[i];
52
       }
53
       return p;
                                                                                      } // rw = rango(a), aca la matriz esta triangulada
54
                                                                                      forr(i, rw, n) if (!feq(y[i],0)) return false; // checkeo de
55
                                                                                 17
   //the following functions allows parsing an expression like
                                                                                           compatibilidad
   //34+150+4*45
                                                                                      x = vector < tipo > (m, 0);
   //into a polynomial(el numero en funcion de la base)
                                                                                      dforn(i, rw){
                                                                                 19
   #define LAST(s) (sz(s)? s[sz(s)-1] : 0)
                                                                                        tipo s = v[i];
                                                                                 20
   #define POP(s) s.erase(--s.end());
                                                                                        forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
                                                                                 21
  poly D(string &s) {
                                                                                        x[p[i]] = s / a[i][i]; //aca divide
                                                                                 22
    poly d;
                                                                                      }
62
                                                                                 23
     for(int i=0; isdigit(LAST(s)); i++) d.c.push_back(LAST(s)-'0'), POP(s)
                                                                                      ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
63
                                                                                 24
                                                                                      forn(k, m-rw) {
                                                                                 25
     return d;}
                                                                                         ev[k][p[k+rw]] = 1;
64
                                                                                 26
                                                                                        dforn(i, rw){
65
                                                                                 27
   poly T(string &s) {
                                                                                           tipo s = -a[i][k+rw]:
66
                                                                                 28
     polv t=D(s);
                                                                                          forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
67
     if (LAST(s)=='*'){POP(s); return T(s)*t;}
                                                                                           ev[k][p[i]] = s / a[i][i]; //aca divide
                                                                                 30
     return t;
69
                                                                                 31
70 }
                                                                                      }
                                                                                 32
```

15 }

```
return true;
34 }
```

7. Grafos

7.1. Dijkstra

```
#define INF 1e9
   int N;
2
   #define MAX_V 250001
   vector<ii> G[MAX_V];
   //To add an edge use
   #define add(a, b, w) G[a].pb(mkp(w, b))
   ll dijkstra(int s, int t){\frac{}{|V|}}
     priority_queue<ii, vector<ii>, greater<ii> > Q;
9
     vector<ll> dist(N, INF); vector<int> dad(N, -1);
10
     Q.push(mkp(0, s)); dist[s] = 0;
11
     while(sz(Q)){
12
       ii p = Q.top(); Q.pop();
13
       if(p.snd == t) break;
14
       forall(it, G[p.snd])
15
         if(dist[p.snd]+it->first < dist[it->snd]){
16
           dist[it->snd] = dist[p.snd] + it->fst;
17
           dad[it->snd] = p.snd;
18
           Q.push(mkp(dist[it->snd], it->snd));
19
20
     }
21
     return dist[t];
^{22}
     if(dist[t]<INF)//path generator</pre>
23
       for(int i=t; i!=-1; i=dad[i])
24
         printf("%d%c", i, (i==s?'\n':','));
25
26 }
```

7.2. Bellman-Ford

```
vector<ii>G[MAX_N];//ady. list with pairs (weight, dst)
int dist[MAX_N];
void bford(int src){//O(VE)

dist[src]=0;
forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
}
```

```
bool hasNegCycle(){
    forn(j, N) if(dist[j]!=INF) forall(it, G[j])
       if(dist[it->snd]>dist[j]+it->fst) return true;
    //inside if: all points reachable from it->snd will have -INF distance
         (do bfs)
     return false;
13
14 }
7.3. Floyd-Warshall
1 //G[i][j] contains weight of edge (i, j) or INF
2 //G[i][i]=0
   int G[MAX_N] [MAX_N];
   void floyd(){//0(N^3)}
  forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
     G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
   }
7
   bool inNegCycle(int v){
     return G[v][v]<0;}
   //checks if there's a neg. cycle in path from a to b
   bool hasNegCycle(int a, int b){
    forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
       return true:
13
     return false;
14
15 }
7.4. Kruskal
struct Ar{int a,b,w;};
  | bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}
   vector<Ar> E;
   11 kruskal(){
       ll cost=0;
       sort(E.begin(), E.end());//ordenar aristas de menor a mayor
6
       uf.init(n);
7
       forall(it, E){
8
           if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
9
               uf.unir(it->a, it->b)://conectar
10
               cost+=it->w:
11
           }
12
       }
13
       return cost;
14
```

7.5. Prim

```
bool taken[MAXN];
   priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
   void process(int v){
       taken[v]=true;
       forall(e, G[v])
5
           if(!taken[e->second]) pq.push(*e);
6
7
8
   11 prim(){
9
       zero(taken);
10
       process(0);
11
       11 cost=0;
12
       while(sz(pq)){
13
           ii e=pq.top(); pq.pop();
14
           if(!taken[e.second]) cost+=e.first, process(e.second);
15
       }
16
       return cost;
17
18 }
```

2-SAT + Tarjan SCC

19

```
//We have a vertex representing a var and other for his negation.
   //Every edge stored in G represents an implication. To add an equation
       of the form a | |b, use addor(a, b)
   //MAX=max cant var, n=cant var
  #define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
  vector<int> G[MAX*2];
  //idx[i]=index assigned in the dfs
   //lw[i]=lowest index(closer from the root) reachable from i
  int lw[MAX*2], idx[MAX*2], qidx;
  stack<int> q;
  int qcmp, cmp[MAX*2];
   //verdad[cmp[i]]=valor de la variable i
   bool verdad[MAX*2+1];
12
13
  int neg(int x) { return x>=n? x-n : x+n;}
   void tjn(int v){
15
     lw[v]=idx[v]=++qidx;
16
     q.push(v), cmp[v]=-2;
17
    forall(it, G[v]){
18
       if(!idx[*it] || cmp[*it]==-2){
```

```
if(!idx[*it]) tjn(*it);
20
         lw[v]=min(lw[v], lw[*it]);
21
       }
22
     }
23
     if(lw[v]==idx[v]){
24
       qcmp++;
25
       int x;
26
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
29
30
   //remember to CLEAR G!!!
   bool satisf(){//O(n)
     memset(idx, 0, sizeof(idx)), qidx=0;
     memset(cmp, -1, sizeof(cmp)), qcmp=0;
     forn(i, n){
35
       if(!idx[i]) tjn(i);
36
       if(!idx[neg(i)]) tjn(neg(i));
37
38
     forn(i, n) if(cmp[i] == cmp[neg(i)]) return false;
39
     return true;
41 }
```

Articulation Points

```
1 int N:
   vector<int> G[1000000];
   //V[i]=node number(if visited), L[i]= lowest V[i] reachable from i
   int qV, V[1000000], L[1000000], P[1000000];
   void dfs(int v, int f){
     L[v]=V[v]=++qV;
     forall(it, G[v])
       if(!V[*it]){
         dfs(*it, v);
         L[v] = min(L[v], L[*it]);
         P[v] += L[*it] >= V[v];
11
12
       else if(*it!=f)
13
         L[v]=min(L[v], V[*it]);
14
   }
15
   int cantart() \{ //0(n) \}
16
17
     aV=0:
     zero(V), zero(P);
```

```
dfs(1, 0); P[1]--;
19
     int q=0;
20
     forn(i, N) if(P[i]) q++;
^{21}
   return q;
  |}
23
       Comp. Biconexas y Puentas
struct edge {
     int u, v, comp;
     bool bridge;
   vector<edge> e;
   void addEdge(int u, int v) {
     G[u].pb(sz(e)), G[v].pb(sz(e));
7
     e.pb((edge)\{u,v,-1,false\});
8
9
   //d[i]=id de la dfs
   //b[i]=lowest id reachable from i
   int d[MAXN], b[MAXN], t;
   int nbc;//cant componentes
   int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
   void initDfs(int n) {
     zero(G), zero(comp);
16
     e.clear();
17
     forn(i,n) d[i]=-1;
18
     nbc = t = 0;
19
20
   stack<int> st;
21
   void dfs(int u, int pe) \{//0(n + m)\}
22
     b[u] = d[u] = t++;
23
     comp[u] = (pe != -1);
24
     forall(ne, G[u]) if (*ne != pe){
25
       int v = e[*ne].u ^ e[*ne].v ^ u;
26
       if (d[v] == -1) {
27
         st.push(*ne);
28
         dfs(v,*ne);
29
         if (b[v] > d[u]){
30
           e[*ne].bridge = true; // bridge
31
```

}

int last;

do {

if $(b[v] >= d[u]) \{ // art \}$

32

33

34

35

```
last = st.top(); st.pop();
36
             e[last].comp = nbc;
37
           } while (last != *ne);
38
           nbc++;
39
           comp[u]++;
40
41
         b[u] = min(b[u], b[v]);
42
43
       else if (d[v] < d[u]) \{ // back edge
         st.push(*ne);
         b[u] = min(b[u], d[v]);
46
47
    }
48
49 }
7.9. LCA + Climb
1 //f[v][k] holds the 2^k father of v
   //L[v] holds the level of v
   int N, f[100001][20], L[100001];
   void build(){//f[i][0] must be filled previously, O(nlgn)
     forn(k, 20-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}
   #define lg(x) (31-__builtin_clz(x))//=floor(log2(x))
   int climb(int a, int d){\frac{1}{0}}
     if(!d) return a;
     dforn(i, lg(L[a])+1)
11
       if(1<<i<=d)
         a=f[a][i], d-=1<<i;
13
       return a;
14
15
   int lca(int a, int b){\frac{1}{0}}
     if(L[a]<L[b]) swap(a, b);</pre>
     a=climb(a, L[a]-L[b]);
     if(a==b) return a;
     dforn(i, lg(L[a])+1)
       if(f[a][i]!=f[b][i])
         a=f[a][i], b=f[b][i];
     return f[a][0];
23
24 }
```

7.10. Heavy Light Decomposition

```
int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
  int dad[MAXN];//dad[v]=padre del nodo v
   void dfs1(int v, int p=-1){//pre-dfs
     dad[v]=p;
4
     treesz[v]=1;
     forall(it, G[v]) if(*it!=p){
       dfs1(*it, v);
       treesz[v]+=treesz[*it];
8
9
10
   int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
   //Las cadenas aparecen continuas en el recorrido!
   int cantcad:
   int homecad[MAXN]://dada una cadena devuelve su nodo inicial
   int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
   void heavylight(int v, int cur=-1){
     if(cur==-1) homecad[cur=cantcad++]=v;
17
     pos[v]=q++;
18
     cad[v]=cur:
19
     int mx=-1;
20
     forn(i, sz(G[v])) if(G[v][i]!=dad[v])
21
       if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;</pre>
22
     if(mx!=-1) heavylight(G[v][mx], cur);
23
     forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
24
       heavylight(G[v][i], -1);
25
26
   //ejemplo de obtener el maximo numero en el camino entre dos nodos
   //RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
    //esta funcion va trepando por las cadenas
   int query(int an, int v){//0(logn)
     //si estan en la misma cadena:
31
     if(cad[an] == cad[v]) return rmq.get(pos[an], pos[v]+1);
32
     return max(query(an, dad[homecad[cad[v]]]),
33
            rmq.get(pos[homecad[cad[v]]], pos[v]+1));
34
35 }
        Centroid Decomposition
```

```
typedef pair<int,int> ii;
1 int n,szt[100100],letter[100100];
 bool taken[100100];
 vector<int> G[100100];
5
```

```
void calcsz(int v, int p) {
     szt[v] = 1;
     forall(it,G[v]) if (*it!=p && !taken[*it])
       calcsz(*it,v), szt[v]+=szt[*it];
   }
10
11
   void centroid(int v, int lvl=0, int tam=-1) {
    if(tam==-1) calcsz(v, -1), tam=szt[v];
    forall(it, G[v]) if(!taken[*it] && szt[*it]>=tam/2)
14
       {szt[v]=0; centroid(*it, lvl, tam); return;}
15
     taken[v]=true;
16
     letter[v]=lvl;
17
     forall(it, G[v]) if(!taken[*it])
18
19
       centroid(*it, lvl+1, -1);
20 }
7.12. Euler Cycle
```

```
int n,m,ars[MAXE], eq;
vector<int> G[MAXN];//fill G,n,m,ars,eq
3 list<int> path;
   int used[MAXN];
   bool usede[MAXE];
   queue<list<int>::iterator> q;
   int get(int v){
     while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
     return used[v];
10
   void explore(int v, int r, list<int>::iterator it){
11
     int ar=G[v][get(v)]; int u=v^ars[ar];
12
     usede[ar]=true;
13
     list<int>::iterator it2=path.insert(it, u);
14
     if(u!=r) explore(u, r, it2);
15
     if(get(v)<sz(G[v])) q.push(it);</pre>
16
   }
17
   void euler(){
     zero(used), zero(usede);
19
     path.clear():
20
     q=queue<list<int>::iterator>();
21
     path.push_back(0); q.push(path.begin());
22
     while(sz(q)){
23
       list<int>::iterator it=q.front(); q.pop();
24
       if(used[*it] < sz(G[*it])) explore(*it, *it, it);</pre>
25
```

vector<int> no(n);

vector<vector<int> > comp(n);

31

32

ly[i] = 0;

lx[i] = *max_element(mt[i], mt[i]+n); }

15

```
forn(u, n) comp[u].pb(no[u] = u);
26
     reverse(path.begin(), path.end());
                                                                                      for (weight cost = 0; ;) {
                                                                                 34
27
                                                                                         vector<int> prev(n, -1);
28
                                                                                 35
   void addEdge(int u, int v){
                                                                                         vector<weight> mcost(n, INF);
29
                                                                                 36
     G[u].pb(eq), G[v].pb(eq);
                                                                                         forn(j,n) if (j != r) forall(e,h[j])
30
                                                                                           if (no[e->src] != no[j])
     ars[eq++]=u^v;
31
32 | }
                                                                                             if (e->w < mcost[ no[j] ])</pre>
                                                                                               mcost[ no[j] ] = e->w, prev[ no[j] ] = no[e->src];
7.13. Chu-liu
                                                                                         vector< vector<int> > next(n);
                                                                                         forn(u,n) if (prev[u] >= 0)
                                                                                          next[ prev[u] ].push_back(u);
void visit(graph &h, int v, int s, int r,
                                                                                 43
                                                                                         bool stop = true;
     vector<int> &no, vector< vector<int> > &comp,
                                                                                 44
                                                                                         vector<int> mark(n):
     vector<int> &prev, vector< vector<int> > &next, vector<weight> &mcost,
                                                                                 45
                                                                                         forn(u,n) if (u != r && !mark[u] && !comp[u].empty()) {
     vector<int> &mark, weight &cost, bool &found) {
                                                                                           bool found = false:
                                                                                 47
     if (mark[v]) {
5
                                                                                           visit(h, u, u, r, no, comp, prev, next, mcost, mark, cost, found);
       vector<int> temp = no;
6
                                                                                           if (found) stop = false;
       found = true;
7
                                                                                         }
       do {
                                                                                 50
8
                                                                                         if (stop) {
         cost += mcost[v]:
                                                                                           forn(u,n) if (prev[u] >= 0) cost += mcost[u];
         v = prev[v];
                                                                                           return cost;
         if (v != s) {
           while (comp[v].size() > 0) {
12
                                                                                      }
             no[comp[v].back()] = s;
                                                                                 55
13
                                                                                 56 }
             comp[s].push_back(comp[v].back());
14
             comp[v].pop_back();
15
                                                                                 7.14. Hungarian
16
17
       } while (v != s);
                                                                                  1 #define MAXN 256
18
       forall(j,comp[s]) if (*j != r) forall(e,h[*j])
                                                                                    #define INFTO 0x7f7f7f7f
19
         if (no[e->src] != s) e->w -= mcost[ temp[*i] ];
                                                                                    int n;
20
     }
                                                                                     int mt[MAXN] [MAXN]; // Matriz de costos (X * Y)
21
     mark[v] = true;
                                                                                    int xy[MAXN], yx[MAXN]; // Matching resultante (X->Y, Y->X)
22
     forall(i,next[v]) if (no[*i] != no[v] && prev[no[*i]] == v)
                                                                                    int lx[MAXN], ly[MAXN], slk[MAXN], slkx[MAXN], prv[MAXN];
23
       if (!mark[no[*i]] || *i == s)
                                                                                    char S[MAXN], T[MAXN];
^{24}
         visit(h, *i, s, r, no, comp, prev, next, mcost, mark, cost, found)
                                                                                     void updtree(int x) {
25
                                                                                      forn(y, n) if (lx[x] + ly[y] - mt[x][y] < slk[y]) {
                                                                                         slk[y] = lx[x] + ly[y] - mt[x][y];
                                                                                 10
26
   weight minimumSpanningArborescence(const graph &g, int r) {
                                                                                         slkx[v] = x:
                                                                                 11
27
       const int n=sz(g);
                                                                                    } }
                                                                                 12
28
                                                                                    int hungar(){//Matching maximo de mayor costo en grafos dirigidos (N^3)
     graph h(n);
29
     forn(u,n) forall(e,g[u]) h[e->dst].pb(*e);
                                                                                      forn(i, n) {
30
```

```
memset(xy, -1, sizeof(xy));
17
     memset(yx, -1, sizeof(yx));
18
     forn(m, n) {
19
       memset(S, 0, sizeof(S));
20
       memset(T, 0, sizeof(T));
21
       memset(prv, -1, sizeof(prv));
22
       memset(slk, 0x7f, sizeof(slk));
23
       queue<int> q;
^{24}
   #define bpone(e, p) { q.push(e); prv[e] = p; S[e] = 1; updtree(e); }
25
       forn(i, n) if (xy[i] == -1) { bpone(i, -2); break; }
26
       int x=0, y=-1;
27
       while (y==-1) {
28
         while (!q.empty() && y==-1) {
29
           x = q.front(); q.pop();
30
           forn(j, n) if (mt[x][j] == lx[x] + ly[j] && !T[j]) {
31
             if (yx[j] == -1) \{ y = j; break; \}
32
             T[i] = 1;
33
             bpone(yx[j], x);
34
           }
35
36
         if (y!=-1) break;
37
         int dlt = INFTO;
38
         forn(j, n) if (!T[j]) dlt = min(dlt, slk[j]);
39
         forn(k, n) {
40
           if (S[k]) lx[k] = dlt;
41
           if (T[k]) ly [k] += dlt;
42
           if (!T[k]) slk[k] -= dlt;
43
44
         forn(j, n) if (!T[j] && !slk[j]) {
45
           if (yx[i] == -1) {
46
             x = slkx[j]; y = j; break;
47
           } else {
48
             T[i] = 1;
49
             if (!S[yx[j]]) bpone(yx[j], slkx[j]);
50
           }
51
         }
52
       }
53
       if (v!=-1) {
54
         for(int p = x; p != -2; p = prv[p]) {
55
           yx[y] = p;
56
           int ty = xy[p]; xy[p] = y; y = ty;
57
58
       } else break;
59
```

```
60 }
61 int res = 0;
62 forn(i, n) res += mt[i][xy[i]];
63 return res;
64 }
```

8. Network Flow

8.1. Dinic

```
int nodes, src, dest;
   int dist[MAX], q[MAX], work[MAX];
   struct Edge {
     int to, rev;
     11 f, cap;
     Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap)
   };
8
   vector<Edge> G[MAX];
11
   // Adds bidirectional edge
   void addEdge(int s, int t, ll cap){
     G[s].push_back(Edge(t, G[t].size(), 0, cap));
     G[t].push_back(Edge(s, G[s].size()-1, 0, 0));
15
16
17
   bool dinic_bfs() {
     fill(dist, dist + nodes, -1);
19
     dist[src] = 0;
20
     int qt = 0;
21
     q[qt++] = src;
22
     for (int qh = 0; qh < qt; qh++) {
23
       int u = q[qh];
24
       forall(e, G[u]){
25
         int v = e \rightarrow to;
26
         if(dist[v]<0 \&\& e->f < e->cap){
27
           dist[v]=dist[u]+1;
28
           q[qt++]=v;
29
         }
30
31
    }
32
```

```
return dist[dest] >= 0;
33
   }
34
35
   ll dinic_dfs(int u, ll f) {
36
     if (u == dest) return f;
37
     for (int &i = work[u]; i < (int) G[u].size(); i++) {</pre>
38
       Edge &e = G[u][i];
39
       if (e.cap <= e.f) continue;</pre>
40
       int v = e.to;
41
       if (dist[v] == dist[u] + 1) {
42
         11 df = dinic_dfs(v, min(f, e.cap - e.f));
43
         if (df > 0) {
44
           e.f += df:
45
           G[v][e.rev].f -= df;
46
           return df;
47
         }
48
       }
49
     }
50
     return 0;
51
52
53
   11 maxFlow(int _src, int _dest) {//O(V^2 E)
     src = _src;
55
     dest = _dest;
56
     11 result = 0;
57
     while (dinic_bfs()) {
58
       fill(work, work + nodes, 0);
59
       while(ll delta = dinic_dfs(src, INF))
60
         result += delta;
61
     }
62
63
     // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1
64
         forman el min cut
65
     return result;
66
67 | }
8.2. Konig
1 // asume que el dinic YA ESTA tirado
  // asume que nodes-1 y nodes-2 son la fuente y destino
int match[maxnodes]; // match[v] = u si u-v esta en el matching, -1 si v
       no esta matcheado
```

```
int s[maxnodes]; // numero de la bfs del koning
  queue<int> kq;
6 // s[e] %2==1 o si e esta en V1 y s[e] ==-1-> lo agarras
   void koning() {//O(n)
     forn(v,nodes-2) s[v] = match[v] = -1;
     forn(v,nodes-2) forall(it,g[v]) if (it->to < nodes-2 && it->f>0)
       { match[v]=it->to; match[it->to]=v;}
     forn(v,nodes-2) if (match[v]==-1) \{s[v]=0; kq.push(v);\}
11
     while(!kq.empty()) {
12
       int e = kq.front(); kq.pop();
       if (s[e] %2==1) {
14
         s[match[e]] = s[e]+1;
         kq.push(match[e]);
       } else {
18
         forall(it,g[e]) if (it->to < nodes-2 && s[it->to]==-1) {
19
           s[it->to] = s[e]+1;
20
           kq.push(it->to);
         }
23
    }
24
25 }
```

8.3. Edmonds Karp's

```
1 #define MAX V 1000
   #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
   map<int, int> G[MAX_V];//limpiar esto
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   int f, p[MAX_V];
   void augment(int v, int minE){
    if(v==SRC) f=minE;
11
     else if(p[v]!=-1){
12
       augment(p[v], min(minE, G[p[v]][v]));
13
       G[p[v]][v]=f, G[v][p[v]]+=f;
14
    }
15
   }
16
17 | ll maxflow(){//0(VE^2)
    11 Mf=0;
18
```

```
do{
19
       f=0;
20
       char used[MAX_V]; queue<int> q; q.push(SRC);
21
       zero(used), memset(p, -1, sizeof(p));
^{22}
       while(sz(q)){
23
         int u=q.front(); q.pop();
24
         if(u==SNK) break;
25
         forall(it, G[u])
26
           if(it->snd>0 && !used[it->fst])
27
              used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
28
       }
29
       augment(SNK, INF);
30
       Mf+=f:
31
     }while(f);
32
     return Mf;
33
34 | }
```

8.4. Push-Relabel O(N3)

```
1 #define MAX V 1000
  int N://valid nodes are [0...N-1]
   #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
  map<int, int> G[MAX_V];
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   11 excess[MAX_V];
   int height[MAX_V], active[MAX_V], count[2*MAX_V+1];
   queue<int> Q;
12
   void enqueue(int v) {
13
     if (!active[v] && excess[v] > 0) active[v]=true, Q.push(v); }
14
   void push(int a, int b) {
15
     int amt = min(excess[a], ll(G[a][b]));
16
     if(height[a] <= height[b] || amt == 0) return;</pre>
17
     G[a][b]-=amt, G[b][a]+=amt;
18
     excess[b] += amt. excess[a] -= amt:
19
     enqueue(b);
20
21
   void gap(int k) {
22
     forn(v, N){
23
       if (height[v] < k) continue;
24
```

```
count[height[v]]--;
25
       height[v] = max(height[v], N+1);
26
       count[height[v]]++;
27
       enqueue(v);
28
     }
29
30
   void relabel(int v) {
31
     count[height[v]]--;
     height[v] = 2*N;
33
     forall(it, G[v])
34
       if(it->snd)
35
         height[v] = min(height[v], height[it->fst] + 1);
36
     count[height[v]]++;
37
     enqueue(v);
39
   ll maxflow() \{//0(V^3)
     zero(height), zero(active), zero(count), zero(excess);
     count[0] = N-1;
     count[N] = 1:
43
     height[SRC] = N;
     active[SRC] = active[SNK] = true;
     forall(it, G[SRC]){
       excess[SRC] += it->snd;
47
       push(SRC, it->fst);
48
     }
49
     while(sz(Q)) {
50
       int v = Q.front(); Q.pop();
51
       active[v]=false;
52
     forall(it, G[v]) push(v, it->fst);
53
     if(excess[v] > 0)
54
       count[height[v]] == 1? gap(height[v]):relabel(v);
55
     }
56
     ll mf=0:
57
     forall(it, G[SRC]) mf+=G[it->fst][SRC];
     return mf:
59
60 }
8.5. Min-cost Max-flow
struct edge {
     int u, v;
     ll cap, cost, flow;
     ll rem() { return cap - flow; }
```

```
<sub>5</sub> | };
  int n://numero de nodos
   vector<int> G[MAXN];
   vector<edge> e;
   void addEdge(int u, int v, ll cap, ll cost) {
     G[u].pb(si(e)); e.pb((edge){u,v,cap,cost,0});
     G[v].pb(si(e)); e.pb((edge){v,u,0,-cost,0});
12
   11 pot[MAXN], dist[MAXN], pre[MAXN], cap[MAXN];
13
   11 mxFlow, mnCost;
   void flow(int s, int t) {
     fill(pot, pot+n, 0);
     mxFlow=mnCost=0;
     while(1){
18
       fill(dist, dist+n, INF); dist[s] = 0;
19
       fill(pre, pre+n, -1); pre[s]=0;
20
       fill(cap, cap+n, 0); cap[s] = INF;
21
       priority_queue<pair<11,int> > q; q.push(mkp(0,s));
22
       while (!q.empty()) {
23
         pair<ll,int> top = q.top(); q.pop();
24
         int u = top.second, d = -top.first;
25
         if (u == t) break;
26
         if (d > dist[u]) continue;
27
         forn(i,si(G[u])) {
28
           edge E = e[G[u][i]];
29
           int c = E.cost + pot[u] - pot[E.v];
30
           if (E.rem() && dist[E.v] > dist[u] + c) {
31
             dist[E.v] = dist[u] + c;
32
             pre[E.v] = G[u][i];
33
             cap[E.v] = min(cap[u], E.rem());
34
             q.push(mkp(-dist[E.v], E.v));
35
36
         }
37
38
       if (pre[t] == -1) break;
39
       forn(u,n)
40
         if (dist[u] == INF) pot[u] = INF;
41
         else pot[u] += dist[u];
42
       mxFlow +=cap[t];
43
       mnCost +=cap[t]*pot[t];
44
       for (int v = t; v != s; v = e[pre[v]].u) {
45
         e[pre[v]].flow += cap[t];
46
         e[pre[v]^1].flow -= cap[t];
47
```

```
48 | }
49 | }
50 |}
```

9. Ayudamemoria

Cant. decimales

```
#include <iomanip>
cout << setprecision(2) << fixed;</pre>
```

Rellenar con espacios(para justificar)

```
#include <iomanip>
cout << setfill('u') << setw(3) << 2 << endl;</pre>
```

Leer hasta fin de linea

```
#include <sstream>
//hacer cin.ignore() antes de getline()
while(getline(cin, line)){
   istringstream is(line);
   while(is >> X)
   cout << X << """;
   cout << endl;
}</pre>
```

Aleatorios

```
#define RAND(a, b) (rand() %(b-a+1)+a)
rand(time(NULL));
```

Doubles Comp.

```
const double EPS = 1e-9;
x == y <=> fabs(x-y) < EPS
x > y <=> x > y + EPS
x >= y <=> x > y - EPS
```

Limites

```
#include timits>
numeric_limits<T>
::max()
::min()
::epsilon()
```

Muahaha

```
1 | #include <signal.h>
void divzero(int p){
   while(true);}
  void segm(int p){
   exit(0);}
  //in main
signal(SIGFPE, divzero);
s signal(SIGSEGV, segm);
Mejorar velocidad
i lios::sync_with_stdio(false);
Mejorar velocidad 2
1 //Solo para enteros positivos
2 inline void Scanf(int& a){
  char c = 0;
   while(c<33) c = getc(stdin);</pre>
    while(c>33) a = a*10 + c - '0', c = getc(stdin);
7 }
Leer del teclado
freopen("/dev/tty", "a", stdin);
Iterar subconjunto
1 | for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
File setup
1 //tambien se pueden usar comas: {a, x, m, l}
touch {a..l}.in; tee {a..l}.cpp < template.cpp
```