Índice

1. algorithm

#include <algorithm> #include <numeric>

Algo	Params	Funcion
sort, stable_sort	f, l	ordena el intervalo
nth_element	f, nth, l	*void* ordena el n-esimo, y particiona el resto
fill, fill_n	f, l / n, elem	*void* llena [f, l) o [f, f+n) con elem
lower_bound, upper_bound	f, l, elem	*it* al primer / ultimo donde se puede insertar elem para que quede ordenada
binary_search	f, l, elem	*bool* esta elem en [f, l)
copy	f, l, resul	hace resul+i=f+i $\forall i$
find, find_if, find_first_of	f, l, elem / pred / f2, l2	*it* encuentra i $\in$[f,l) tq. i=elem, pred(i), i$\in$[f2,l2)
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, l, f2, l2	busca [f2,l2) $\in$ [f,l)
replace, replace_if	f, l, old / pred, new	cambia old / pred(i) por new
reverse	f, l	da vuelta
partition, stable_partition	f, l, pred	pred(i) ad, !pred(i) atras
min_element, max_element	f, l, [comp]	*it* min, max de [f,l]
lexicographical_compare	f1,l1,f2,l2	*bool* con [f1,l1]¡[f2,l2]
next/prev_permutation	f,l	deja en [f,l) la perm sig, ant
set_intersection, set_difference, set_union, set_symmetric_difference,	f1, l1, f2, l2, res	[res, ...) la op. de conj
push_heap, pop_heap, make_heap	f, l, e / e /	mete/saca e en heap [f,l), hace un heap de [f,l)
is_heap	f,l	*bool* es [f,l) un heap
accumulate	f,l,i,[op]	$T = \sum$/oper de [f,l)
inner_product	f1, l1, f2, i	T = i + [f1, l1) . [f2, ...)
partial_sum	f, l, r, [op]	r+i = $\sum$/oper de [f,f+i] $\forall i \in$[f,l)
__builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
__builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
__builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
__builtin_popcount	unsigned int	Cant. de 1's en x.
__builtin_parity	unsigned int	1 si x es par, 0 si es impar.
__builtin_XXXXXXll	unsigned ll	= pero para long long's.

2. Estructuras

2.1. RMQ (static)

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: LVL $\geq$ ceil(logn); Usar [ ] para llenar arreglo y luego build().

```
struct RMQ{
  #define LVL 10
  tipo vec[LVL][1<<(LVL+1)];
  tipo &operator[](int p){return vec[0][p];}
  tipo get(int i, int j) {//intervalo [i,j)
    int p = 31-__builtin_clz(j-i);
    return min(vec[p][i],vec[p][j-(1<<p)]);
  }
  void build(int n) {//O(nlogn)
    int mp = 31-__builtin_clz(n);
    forn(p, mp) forn(x, n-(1<<p))
      vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
  }
};
```

2.2. RMQ (dynamic)

```
//Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
    sobre el rango [i, j).
#define MAXN 100000
#define operacion(x, y) max(x, y)
const int neutro=0;
struct RMQ{
  int sz;
  tipo t[4*MAXN];
  tipo &operator[](int p){return t[sz+p];}
  void init(int n){//O(nlgn)
    sz = 1 << (32-__builtin_clz(n));
    forn(i, 2*sz) t[i]=neutro;
  }
  void updall(){//O(n)
    dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);}
  tipo get(int i, int j){return get(i,j,1,0,sz);}
  tipo get(int i, int j, int n, int a, int b){//O(lgn)
    if(j<=a || i>=b) return neutro;
    if(i<=a && b<=j) return t[n];
```

```
    int c=(a+b)/2;
    return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
  }
  void set(int p, tipo val){//O(lgn)
    for(p+=sz; p>0 && t[p]!=val;){
      t[p]=val;
      p/=2;
      val=operacion(t[p*2], t[p*2+1]);
    }
  }
}rmq;
//Usage:
cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall();
```

2.3. RMQ (lazy)

```
//Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera
    sobre el rango [i, j).
typedef int Elem;//Elem de los elementos del arreglo
typedef int Alt;//Elem de la alteracion
#define operacion(x,y) x+y
const Elem neutro=0; const Alt neutro2=0;
#define MAXN 100000
struct RMQ{
  int sz;
  Elem t[4*MAXN];
  Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem
  Elem &operator[](int p){return t[sz+p];}
  void init(int n){//O(nlgn)
    sz = 1 << (32-__builtin_clz(n));
    forn(i, 2*sz) t[i]=neutro;
    forn(i, 2*sz) dirty[i]=neutro2;
  }
  void push(int n, int a, int b){//propaga el dirty a sus hijos
    if(dirty[n]!=0){
      t[n]+=dirty[n]*(b-a);//altera el nodo
      if(n<sz){
        dirty[2*n]+=dirty[n];
        dirty[2*n+1]+=dirty[n];
      }
      dirty[n]=0;
    }
  }
  Elem get(int i, int j, int n, int a, int b){//O(lgn)
    if(j<=a || i>=b) return neutro;
    push(n, a, b);//corrige el valor antes de usarlo
    if(i<=a && b<=j) return t[n];
    int c=(a+b)/2;
    return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
  }
  Elem get(int i, int j){return get(i,j,1,0,sz);}
  //altera los valores en [i, j) con una alteracion de val
  void alterar(Alt val, int i, int j, int n, int a, int b){//O(lgn)
    push(n, a, b);
    if(j<=a || i>=b) return;
    if(i<=a && b<=j){
      dirty[n]+=val;
      push(n, a, b);
      return;
    }
    int c=(a+b)/2;
    alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
    t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
  }
  void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
}rmq;
```

2.4. Fenwick Tree

```
//For 2D threat each column as a Fenwick tree, by adding a nested for in
    each operation
struct Fenwick{
  static const int sz=1000001;
  tipo t[sz];
  void adjust(int p, tipo v){//valid with p in [1, sz), O(lgn)
    for(; p<sz; p+=(p&-p)) t[p]+=v; }
  tipo sum(int p){//cumulative sum in [1, p], O(lgn)
    tipo s=0;
    for(; p; p-=(p&-p)) s+=t[p];
    return s;
  }
  tipo sum(int a, int b){return sum(b)-sum(a-1);}
  //get largest value with cumulative sum less than or equal to x;
  //for smallest, pass x-1 and add 1 to result
  int getind(tipo x) {//O(lgn)
      int idx = 0, mask = N;
```

```
      while(mask && idx < N) {
        int t = idx + mask;
      if(x >= tree[t])
          idx = t, x -= tree[t];
        mask >>= 1;
      }
      return idx;
  }
};
```

2.5. Union Find

```
struct UnionFind{
  vector<int> f;//the array contains the parent of each node
  void init(int n){f.clear(); f.insert(f.begin(), n, -1);}
  int comp(int x){return (f[x]==-1?x:f[x]=comp(f[x]));}//O(1)
  bool join(int i, int j) {
    bool con=comp(i)==comp(j);
    if(!con) f[comp(i)] = comp(j);
    return con;
  }
};
```

2.6. Disjoint Intervals

```
bool operator< (const ii &a, const ii &b) {return a.fst<b.fst;}
//Stores intervals as [first, second]
//in case of a collision it joins them in a single interval
struct disjoint_intervals {
  set<ii> segs;
  void insert(ii v) {//O(lgn)
    if(v.snd-v.fst==0.) return;//OJO
    set<ii>::iterator it,at;
    at = it = segs.lower_bound(v);
    if (at!=segs.begin() && (--at)->snd >= v.fst)
      v.fst = at->fst, --it;
    for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))
      v.snd=max(v.snd, it->snd);
    segs.insert(v);
  }
};
```

2.7. RMQ (2D)

```
struct RMQ2D{
  static const int sz=1024;
  RMQ t[sz];
  RMQ &operator[](int p){return t[sz/2+p];}
  void build(int n, int m){//O(nm)
    forr(y, sz/2, sz/2+m)
      t[y].build(m);
    forr(y, sz/2+m, sz)
      forn(x, sz)
        t[y].t[x]=0;
    dforn(y, sz/2)
      forn(x, sz)
        t[y].t[x]=max(t[y*2].t[x], t[y*2+1].t[x]);
  }
  void set(int x, int y, tipo v){//O(lgm.lgn)
    y+=sz/2;
    t[y].set(x, v);
    while(y/=2)
      t[y].set(x, max(t[y*2][x], t[y*2+1][x]));
  }
  //O(lgm.lgn)
  int get(int x1, int y1, int x2, int y2, int n=1, int a=0, int b=sz/2){
    if(y2<=a || y1>=b) return 0;
    if(y1<=a && b<=y2) return t[n].get(x1, x2);
    int c=(a+b)/2;
    return max(get(x1, y1, x2, y2, 2*n, a, c),
         get(x1, y1, x2, y2, 2*n+1, c, b));
  }
};
//Example to initialize a grid of M rows and N columns:
RMQ2D rmq;
forn(i, M)
  forn(j, N)
    cin >> rmq[i][j];
rmq.build(N, M);
```

2.8. Big Int

```
#define BASEXP 6
#define BASE 1000000
#define LMAX 1000
struct bint{
    int l;
```

```
    ll n[LMAX];
    bint(ll x=0){
        l=1;
        forn(i, LMAX){
            if (x) l=i+1;
            n[i]=x%BASE;
            x/=BASE;

        }
    }
    bint(string x){
    l=(x.size()-1)/BASEXP+1;
        fill(n, n+LMAX, 0);
        ll r=1;
        forn(i, sz(x)){
            n[i / BASEXP] += r * (x[x.size()-1-i]-'0');
            r*=10; if(r==BASE)r=1;
        }
    }
    void out(){
    cout << n[l-1];
    dforn(i, l-1) printf("%6.6llu", n[i]);//6=BASEXP!
  }
  void invar(){
    fill(n+l, n+LMAX, 0);
    while(l>1 && !n[l-1]) l--;
  }
};
bint operator+(const bint&a, const bint&b){
  bint c;
    c.l = max(a.l, b.l);
    ll q = 0;
    forn(i, c.l) q += a.n[i]+b.n[i], c.n[i]=q %BASE, q/=BASE;
    if(q) c.n[c.l++] = q;
    c.invar();
    return c;
}
pair<bint, bool> lresta(const bint& a, const bint& b)   // c = a - b
{
  bint c;
    c.l = max(a.l, b.l);
    ll q = 0;
    forn(i, c.l) q += a.n[i]-b.n[i], c.n[i]=(q+BASE) %BASE, q=(q+BASE)/
        BASE-1;
    c.invar();
    return make_pair(c, !q);
}
bint& operator-= (bint& a, const bint& b){return a=lresta(a, b).first;}
bint operator- (const bint&a, const bint&b){return lresta(a, b).first;}
bool operator< (const bint&a, const bint&b){return !lresta(a, b).second
    ;}
bool operator<= (const bint&a, const bint&b){return lresta(b, a).second
    ;}
bool operator==(const bint&a, const bint&b){return a <= b && b <= a;}
bint operator*(const bint&a, ll b){
    bint c;
    ll q = 0;
    forn(i, a.l) q += a.n[i]*b, c.n[i] = q %BASE, q/=BASE;
    c.l = a.l;
    while(q) c.n[c.l++] = q %BASE, q/=BASE;
    c.invar();
    return c;
}
bint operator*(const bint&a, const bint&b){
    bint c;
    c.l = a.l+b.l;
    fill(c.n, c.n+b.l, 0);
    forn(i, a.l){
        ll q = 0;
        forn(j, b.l) q += a.n[i]*b.n[j]+c.n[i+j], c.n[i+j] = q %BASE, q
            /=BASE;
        c.n[i+b.l] = q;
    }
    c.invar();
    return c;
}
pair<bint, ll> ldiv(const bint& a, ll b){// c = a / b ; rm = a % b
  bint c;
  ll rm = 0;
  dforn(i, a.l){
            rm = rm * BASE + a.n[i];
            c.n[i] = rm / b;
            rm %= b;
    }
    c.l = a.l;
```

```
    c.invar();
    return make_pair(c, rm);
}
bint operator/(const bint&a, ll b){return ldiv(a, b).first;}
ll operator%(const bint&a, ll b){return ldiv(a, b).second;}
pair<bint, bint> ldiv(const bint& a, const bint& b){
  bint c;
    bint rm = 0;
    dforn(i, a.l){
        if (rm.l==1 && !rm.n[0])
            rm.n[0] = a.n[i];
        else{
            dforn(j, rm.l) rm.n[j+1] = rm.n[j];
            rm.n[0] = a.n[i];
            rm.l++;
        }
        ll q = rm.n[b.l] * BASE + rm.n[b.l-1];
        ll u = q / (b.n[b.l-1] + 1);
        ll v = q /  b.n[b.l-1] + 1;
        while (u < v-1){
            ll m = (u+v)/2;
            if (b*m <= rm) u = m;
            else v = m;
        }
        c.n[i]=u;
        rm-=b*u;
    }
  c.l=a.l;
    c.invar();
    return make_pair(c, rm);
}
bint operator/(const bint&a, const bint&b){return ldiv(a, b).first;}
bint operator%(const bint&a, const bint&b){return ldiv(a, b).second;}
```

2.9. Modnum

```
struct mnum{
  static const tipo mod=12582917;
  tipo v;
  mnum(tipo v=0): v(v%mod) {}
  mnum operator+(mnum b){return v+b.v;}
  mnum operator-(mnum b){return v>=b.v? v-b.v : mod-b.v+v;}
  mnum operator*(mnum b){return v*b.v;}
  mnum operator^(int n){
    if(!n) return 1;
    return n%2? (*this)^(n/2)*(this) : (*this)^(n/2);}
};
```

2.10. Treap

```
typedef int Key;

typedef struct node *pnode;
struct node{
    Key key;
    int prior, size;
    pnode l,r;
    node(Key key=0, int prior=0): key(key), prior(prior), size(1), l(0),
         r(0) {}
};
struct treap {
    pnode root;
    treap(): root(0) {}
    int size(pnode p) { return p ? p->size : 0; }
    int size() { return size(root); }
    void push(pnode p) {
        // modificar y propagar el dirty a los hijos aca(para lazy)
    }
    // Update function and size from children's values
    void pull(pnode p) {//recalcular valor del nodo aca (para rmq)
        p->size = 1 + size(p->l) + size(p->r);
    }
    pnode merge(pnode l, pnode r) {
        if (!l || !r) return l ? l : r;
        push(l), push(r);
        pnode t;
        if (l->prior < r->prior) l->r=merge(l->r, r), t = l;
        else r->l=merge(l, r->l), t = r;
        pull(t);
        return t;
    }//opcional:
    void merge(treap t) {root = merge(root, t.root), t.root=0;}
    //*****KEY OPERATIONS*****//
    void splitKey(pnode t, Key key, pnode &l, pnode &r) {
        if (!t) return void(l = r = 0);
        push(t);
```

```
        if (key <= t->key) splitKey(t->l, key, l, t->l), r = t;
        else splitKey(t->r, key, t->r, r), l = t;
        pull(t);
    }
    void insertKey(Key key) {
        pnode elem = new node(key, rand());
        pnode t1, t2; splitKey(root, key, t1, t2);
        t1=merge(t1,elem);
        root=merge(t1,t2);
    }
    void eraseKeys(Key key1, Key key2) {
        pnode t1,t2,t3;
        splitKey(root,key1,t1,t2);
        splitKey(t2,key2, t2, t3);
        root=merge(t1,t3);
    }
    void eraseKey(pnode &t, Key key) {
        if (!t) return;
        push(t);
        if (key == t->key) t=merge(t->l, t->r);
        else if (key < t->key) eraseKey(t->l, key);
        else eraseKey(t->r, key);
        pull(t);
    }
    void eraseKey(Key key) {eraseKey(root, key);}
    pnode findKey(pnode t, Key key) {
        if (!t) return 0;
        if (key == t->key) return t;
        if (key < t->key) return findKey(t->l, key);
        return findKey(t->r, key);
    }
    pnode findKey(Key key) { return findKey(root, key); }
    //*****POS OPERATIONS*****// No mezclar con las funciones Key
    //(No funciona con pos:)
    void splitSize(pnode t, int sz, pnode &l, pnode &r) {
        if (!t) return void(l = r = 0);
        push(t);
        if (sz <= size(t->l)) splitSize(t->l, sz, l, t->l), r = t;
        else splitSize(t->r, sz - 1 - size(t->l), t->r, r), l = t;
        pull(t);
    }
    void insertPos(int pos, Key key) {
        pnode elem = new node(key, rand());
        pnode t1,t2; splitSize(root, pos, t1, t2);
        t1=merge(t1,elem);
        root=merge(t1,t2);
    }
    void erasePos(int pos1, int pos2=-1) {
    if(pos2==-1) pos2=pos1+1;
        pnode t1,t2,t3;
        splitSize(root,pos1,t1,t2);
        splitSize(t2,pos2-pos1,t2,t3);
        root=merge(t1, t2);
    }
    pnode findPos(pnode t, int pos) {
        if(!t) return 0;
        if(pos <= size(t->l)) return findPos(t->l, pos);
        return findPos(t->r, pos - 1 - size(t->l));
    }
    Key &operator[](int pos){return findPos(root, pos)->key;}//ojito
};
```

3. Algos

3.1. Longest Increasing Subsecuence

```
//Para non-increasing, cambiar comparaciones y revisar busq binaria
//Given an array, paint it in the least number of colors so that each
    color turns to a non-increasing subsequence.
//Solution:Min number of colors=Length of the longest increasing
    subsequence
int N, a[MAXN];//secuencia y su longitud
ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
int p[MAXN];//padres
vector<int> R;//respuesta
void rec(int i){
  if(i==-1) return;
  R.push_back(a[i]);
  rec(p[i]);
}
int lis(){//O(nlogn)
  d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
  forn(i, N){
    int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
    if (d[j-1].first < a[i]&&a[i] < d[j].first){
      p[i]=d[j-1].second;
```

```
      d[j] = ii(a[i], i);
    }
  }
  R.clear();
  dforn(i, N+1) if(d[i].first!=INF){
    rec(d[i].second);//reconstruir
    reverse(R.begin(), R.end());
    return i;//longitud
  }
  return 0;
}
```

3.2. Manacher

```
int d1[MAXN];//d1[i]=long del maximo palindromo impar con centro en i
int d2[MAXN];//d2[i]=analogo pero para longitud par
//0 1 2 3 4
//a a b c c <--d1[2]=3
//a a b b <--d2[2]=2 (estan uno antes)
void manacher(){
  int l=0, r=-1, n=sz(s);
  forn(i, n){
    int k=(i>r? 1 : min(d1[l+r-i], r-i));
    while(i+k<n && i-k>=0 && s[i+k]==s[i-k]) ++k;
    d1[i] = k--;
    if(i+k > r) l=i-k, r=i+k;
  }
  l=0, r=-1;
  forn(i, n){
    int k=(i>r? 0 : min(d2[l+r-i+1], r-i+1))+1;
    while(i+k-1<n && i-k>=0 && s[i+k-1]==s[i-k]) k++;
    d2[i] = --k;
    if(i+k-1 > r) l=i-k, r=i+k-1;
  }
```

4. Strings

4.1. KMP

```
string T;//cadena donde buscar(where)
string P;//cadena a buscar(what)
int b[MAXLEN];//back table
void kmppre(){//by gabina with love
    int i =0, j=-1; b[0]=-1;
    while(i<sz(P)){
        while(j>=0 && P[i] != P[j]) j=b[j];
        i++, j++;
        b[i] = j;
    }
}

void kmp(){
    int i=0, j=0;
    while(i<sz(T)){
        while(j>=0 && T[i]!=P[j]) j=b[j];
        i++, j++;
        if(j==sz(P)){
            printf("P is found at index %d in T\n", i-j);
            j=b[j];
        }
    }
}
```

4.2. Trie

```
struct trie{
  map<char, trie> m;
  void add(const string &s, int p=0){
    if(s[p]) m[s[p]].add(s, p+1);
  }
  void dfs(){
    //Do stuff
    forall(it, m)
      it->second.dfs();
  }
};
```

4.3. Suffix Array (largo, nlogn)

```
#define MAX_N 1000
#define rBOUND(x) (x<n? r[x] : 0)
//sa will hold the suffixes in order.
int sa[MAX_N], r[MAX_N], n;
string s; //input string, n=sz(s)

int f[MAX_N], tmpsa[MAX_N];
void countingSort(int k){
```

```
  zero(f);
  forn(i, n) f[rBOUND(i+k)]++;
  int sum=0;
  forn(i, max(255, n)){
    int t=f[i]; f[i]=sum; sum+=t;}
  forn(i, n)
    tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
  memcpy(sa, tmpsa, sizeof(sa));
}
void constructsa(){//O(n log n)
  n=sz(s);
  forn(i, n) sa[i]=i, r[i]=s[i];
  for(int k=1; k<n; k<<=1){
    countingSort(k), countingSort(0);
    int rank, tmpr[MAX_N];
    tmpr[sa[0]]=rank=0;
    forr(i, 1, n)
      tmpr[sa[i]]=(r[sa[i]]==r[sa[i-1]] && r[sa[i]+k]==r[sa[i-1]+k] )?
          rank : ++rank;
    memcpy(r, tmpr, sizeof(r));
    if(r[sa[n-1]]==n-1) break;
  }
}
void print(){//for debug
  forn(i, n)
    cout << i << ' ␣' <<
    s.substr(sa[i], s.find( '$', sa[i])-sa[i]) << endl;}
```

4.4. String Matching With Suffix Array

```
//returns (lowerbound, upperbound) of the search
ii stringMatching(string P){ //O(sz(P)lgn)
  int lo=0, hi=n-1, mid=lo;
  while(lo<hi){
    mid=(lo+hi)/2;
    int res=s.compare(sa[mid], sz(P), P);
    if(res>=0) hi=mid;
    else lo=mid+1;
  }
  if(s.compare(sa[lo], sz(P), P)!=0) return ii(-1, -1);
  ii ans; ans.fst=lo;
  lo=0, hi=n-1, mid;
  while(lo<hi){
    mid=(lo+hi)/2;
    int res=s.compare(sa[mid], sz(P), P);
    if(res>0) hi=mid;
    else lo=mid+1;
  }
  if(s.compare(sa[hi], sz(P), P)!=0) hi--;
  ans.snd=hi;
  return ans;
}
```

4.5. LCP (Longest Common Prefix)

```
//Calculates the LCP between consecutives suffixes in the Suffix Array.
//LCP[i] is the length of the LCP between sa[i] and sa[i-1]
int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
void computeLCP(){//O(n)
  phi[sa[0]]=-1;
  forr(i, 1, n) phi[sa[i]]=sa[i-1];
  int L=0;
  forn(i, n){
    if(phi[i]==-1) {PLCP[i]=0; continue;}
    while(s[i+L]==s[phi[i]+L]) L++;
    PLCP[i]=L;
    L=max(L-1, 0);
  }
  forn(i, n) LCP[i]=PLCP[sa[i]];
}
```

4.6. Corasick

```

struct trie{
  map<char, trie> next;
  trie* tran[256];//transiciones del automata
  int idhoja, szhoja;//id de la hoja o 0 si no lo es
  //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
      es hoja
  trie *padre, *link, *nxthoja;
  char pch;//caracter que conecta con padre
  trie(): tran(),  idhoja(), padre(), link() {}
  void insert(const string &s, int id=1, int p=0){//id>0!!!
    if(p<sz(s)){
      trie &ch=next[s[p]];
      tran[(int)s[p]]=&ch;
```

```
      ch.padre=this, ch.pch=s[p];
      ch.insert(s, id, p+1);
    }
    else idhoja=id, szhoja=sz(s);
  }
  trie* get_link() {
    if(!link){
      if(!padre) link=this;//es la raiz
      else if(!padre->padre) link=padre;//hijo de la raiz
      else link=padre->get_link()->get_tran(pch);
    }
    return link;
  }
  trie* get_tran(int c) {
    if(!tran[c])
      tran[c] = !padre? this : this->get_link()->get_tran(c);
    return tran[c];
  }
  trie *get_nxthoja(){
    if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
    return nxthoja;
  }
  void print(int p){
    if(idhoja)
      cout << "found " << idhoja << "  at position " << p-szhoja << endl
          ;
    if(get_nxthoja()) get_nxthoja()->print(p);
  }
  void matching(const string &s, int p=0){
    print(p);
    if(p<sz(s)) get_tran(s[p])->matching(s, p+1);
```

5. Geometria

#define EPS 1e-9

5.1. Punto

```
struct pto{
  tipo x, y;
  pto(tipo x=0, tipo y=0):x(x),y(y){}
  pto operator+(pto a){return pto(x+a.x, y+a.y);}
  pto operator-(pto a){return pto(x-a.x, y-a.y);}
  pto operator+(tipo a){return pto(x+a, y+a);}
  pto operator*(tipo a){return pto(x*a, y*a);}
  pto operator/(tipo a){return pto(x/a, y/a);}
  //dot product, producto interno:
  tipo operator*(pto a){return x*a.x+y*a.y;}
  //module of the cross product or vectorial product:
  //if a is less than 180 clockwise from b, a^b>0
  tipo operator^(pto a){return x*a.y-y*a.x;}
  //returns true if this is at the left side of line qr
  bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
  bool operator<(const pto &a) const{return x<a.x || (abs(x-a.x)<EPS &&
      y<a.y);}
bool operator==(pto a){return abs(x-a.x)<EPS && abs(y-a.y)<EPS;}
  double norm(){return sqrt(x*x+y*y);}
  tipo norm_sq(){return x*x+y*y;}
};
double dist(pto a, pto b){return (b-a).norm();}
typedef pto vec;

double angle(pto a, pto o, pto b){
  pto oa=a-o, ob=b-o;
  return atan2(oa^ob, oa*ob);}

//rotate p by theta rads CCW w.r.t. origin (0,0)
pto rotate(pto p, double theta){
  return pto(p.x*cos(theta)-p.y*sin(theta),
      p.x*sin(theta)+p.y*cos(theta));
}

//orden total de puntos alrededor de un punto r
struct Cmp{
  pto r;
  Cmp(pto _r){r = _r;}
  int cuad(const pto &a) const{
    if(a.x > 0 && a.y >= 0)return 0;
    if(a.x <= 0 && a.y > 0)return 1;
    if(a.x < 0 && a.y <= 0)return 2;
    if(a.x >= 0 && a.y < 0)return 3;
    assert(a.x ==0 && a.y==0);
    return -1;
  }
  bool cmp(const pto&p1, const pto&p2)const{
    int c1 = cuad(p1), c2 = cuad(p2);
```

```
    if(c1==c2){
      return p1.y*p2.x<p1.x*p2.y;
    }else{
      return c1 < c2;
  }}
bool operator()(const pto&p1, const pto&p2) const{
return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
}
};
```

5.2. Line

```
struct line{
  line() {}
  double a,b,c;//Ax+By=C
//pto MUST store float coordinates!
  line(double a, double b, double c):a(a),b(b),c(c){}
  line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
};
bool parallels(line l1, line l2){return abs(l1.a*l2.b-l2.a*l1.b)<EPS;}
pto inter(line l1, line l2){//intersection
  double det=l1.a*l2.b-l2.a*l1.b;
  if(abs(det)<EPS) return pto(INF, INF);//parallels
  return pto(l2.b*l1.c-l1.b*l2.c, l1.a*l2.c-l2.a*l1.c)/det;
}
```

5.3. Segment

```
struct segm{
  pto s,f;
  segm(pto s, pto f):s(s), f(f) {}
  pto closest(pto p) {//use for dist to point
     double l2 = dist_sq(s, f);
     if(l2==0.) return s;
     double t =((p-s)*(f-s))/l2;
     if (t<0.) return s;//not write if is a line
     else if(t>1.)return f;//not write if is a line
     return s+((f-s)*t);
  }
  bool inside(pto p){
return ((s-p)^(f-p))==0 && min(s, f)<*this&&*this<max(s, f);}
};

bool insidebox(pto a, pto b, pto p) {
  return (a.x-p.x)*(p.x-b.x)>-EPS && (a.y-p.y)*(p.y-b.y)>-EPS;
}
pto inter(segm s1, segm s2){
  pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
  if(insidebox(s1.s,s1.f,p) && insidebox(s2.s,s2.f,p))
      return r;
  return pto(INF, INF);
}
```

5.4. Polygon Area

```
double area(vector<pto> &p){//O(sz(p))
  double area=0;
  forn(i, sz(p)) area+=p[i]^p[(i+1)%sz(p)];
  //if points are in clockwise order then area is negative
  return abs(area)/2;
}
//Area ellipse = M_PI*a*b where a and b are the semi axis lengths
//Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
```

5.5. Circle

```
vec perp(vec v){return vec(-v.y, v.x);}
line bisector(pto x, pto y){
  line l=line(x, y); pto m=(x+y)/2;
  return line(-l.b, l.a, -l.b*m.x+l.a*m.y);
}
struct Circle{
  pto o;
  double r;
  Circle(pto x, pto y, pto z){
    o=inter(bisector(x, y), bisector(y, z));
    r=dist(o, x);
  }
  pair<pto, pto> ptosTang(pto p){
    pto m=(p+o)/2;
    tipo d=dist(o, m);
    tipo a=r*r/(2*d);
    tipo h=sqrt(r*r-a*a);
    pto m2=o+(m-o)*a/d;
    vec per=perp(m-o)/d;
    return mkp(m2-per*h, m2+per*h);
  }
};
```

```
//finds the center of the circle containing p1 and p2 with radius r
//as there may be two solutions swap p1, p2 to get the other
bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
        double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
        if(det<0) return false;
        c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
        return true;
}
#define sqr(a) ((a)*(a))
#define feq(a,b) (fabs((a)-(b))<EPS)
pair<tipo, tipo> ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
  tipo dx = sqrt(b*b-4.0*a*c);
  return make_pair((-b + dx)/(2.0*a),(-b - dx)/(2.0*a));
}
pair<pto, pto> interCL(Circle c, line l){
  bool sw=false;
  if((sw=feq(0,l.b))){
  swap(l.a, l.b);
  swap(c.o.x, c.o.y);
  }
  pair<tipo, tipo> rc = ecCuad(
  sqr(l.a)+sqr(l.b),
  2.0*l.a*l.b*c.o.y-2.0*(sqr(l.b)*c.o.x+l.c*l.a),
  sqr(l.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(l.c)-2.0*l.c*l.b*c.o.y
  );
  pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
            pto(rc.second, (l.c - l.a * rc.second) / l.b) );
  if(sw){
  swap(p.first.x, p.first.y);
  swap(p.second.x, p.second.y);
  }
  return p;
}
pair<pto, pto> interCC(Circle c1, Circle c2){
  line l;
  l.a = c1.o.x-c2.o.x;
  l.b = c1.o.y-c2.o.y;
  l.c = (sqr(c2.r)-sqr(c1.r)+sqr(c1.o.x)-sqr(c2.o.x)+sqr(c1.o.y)
  -sqr(c2.o.y))/2.0;
  return interCL(c1, l);
}
```

5.6. Point in Poly

```
//checks if v is inside of P, using ray casting
//works with convex and concave.
//excludes boundaries, handle it separately using segment.inside()
bool inPolygon(pto v, vector<pto>& P) {
  bool c = false;
  forn(i, sz(P)){
    int j=(i+1)%sz(P);
    if((P[j].y>v.y) != (P[i].y > v.y) &&
  (v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))
      c = !c;
  }
  return c;
}
```

5.7. Convex Check CHECK

```
bool isConvex(vector<int> &p){//O(N)
  int N=sz(p);
  if(N<3) return false;
  bool isLeft=p[0].left(p[1], p[2]);
  forr(i, 1, N)
    if(p[i].left(p[(i+1)%N], p[(i+2)%N])!=isLeft)
      return false;
  return true; }
```

5.8. Convex Hull

```
//stores convex hull of P in S, CCW order
void CH(vector<pto>& P, vector<pto> &S){
  S.clear();
  sort(P.begin(), P.end());
  forn(i, sz(P)){
    while(sz(S)>= 2 && S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
    S.pb(P[i]);
  }
  S.pop_back();
  int k=sz(S);
  dforn(i, sz(P)){
    while(sz(S) >= k+2 && S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back
        ();
    S.pb(P[i]);
  }
```

```
  S.pop_back();
}
```

5.9. Cut Polygon

```
//cuts polygon Q along the line ab
//stores the left side (swap a, b for the right one) in P
void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
  P.clear();
  forn(i, sz(Q)){
    double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)%sz(Q)]-a);
    if(left1>=0) P.pb(Q[i]);
    if(left1*left2<0)
      P.pb(inter(line(Q[i], Q[(i+1)%sz(Q)]), line(a, b)));
  }
}
```

5.10. Bresenham

```
//plot a line approximation in a 2d map
void bresenham(pto a, pto b){
  pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
  pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
  int err=d.x-d.y;
  while(1){
    m[a.x][a.y]=1;//plot
    if(a==b) break;
    int e2=2*err;
    if(e2 > -d.y){
      err-=d.y, a.x+=s.x;
    if(e2 < d.x)
      err+= d.x, a.y+= s.y;
  }
}
```

5.11. Interseccion de Circulos en n3log(n)

```
struct event {
    double x; int t;
    event(double xx, int tt) : x(xx), t(tt) {}
    bool operator <(const event &o) const { return x < o.x; }
};
typedef vector<Circle> VC;
typedef vector<event> VE;
int n;
double cuenta(VE &v, double A,double B) {
    sort(v.begin(), v.end());
    double res = 0.0, lx = ((v.empty())?0.0:v[0].x);
    int contador = 0;
    forn(i,sz(v)) {
        // interseccion de todos (contador == n), union de todos (
            contador > 0),
        // conjunto de puntos cubierto por exacta k Circulos (contador
            == k)
        if (contador == n) res += v[i].x - lx;
        contador += v[i].t;
        lx = v[i].x;
    }
    return res;
}
// Primitiva de sqrt(r*r - x*x) como funcion double de una variable x.
inline double primitiva(double x,double r) {
    if (x >= r) return r*r*M_PI/4.0;
    if (x <= -r) return -r*r*M_PI/4.0;
    double raiz = sqrt(r*r-x*x);
    return 0.5 * (x * raiz + r*r*atan(x/raiz));
}
double interCircle(VC &v) {
    vector<double> p; p.reserve(v.size() * (v.size() + 2));
    forn(i,sz(v)) {
        p.push_back(v[i].c.x + v[i].r);
        p.push_back(v[i].c.x - v[i].r);
    }
    forn(i,sz(v)) forn(j,i) {
        Circle &a = v[i], b = v[j];
        double d = (a.c - b.c).norm();
        if (fabs(a.r - b.r) < d && d < a.r + b.r) {
            double alfa = acos((sqr(a.r) + sqr(d) - sqr(b.r)) / (2.0 * d
                * a.r));
            pto vec = (b.c - a.c) * (a.r / d);
            p.pb((a.c + rotate(vec, alfa)).x);
            p.pb((a.c + rotate(vec, -alfa)).x);
        }
    }
    sort(p.begin(), p.end());
    double res = 0.0;
    forn(i,sz(p)-1) {
```

```
        const double A = p[i], B = p[i+1];
        VE ve; ve.reserve(2 * v.size());
        forn(j,sz(v)) {
            const Circle &c = v[j];
            double arco = primitiva(B-c.c.x,c.r) - primitiva(A-c.c.x,c.r
                );
            double base = c.c.y * (B-A);
            ve.push_back(event(base + arco,-1));
            ve.push_back(event(base - arco, 1));
        }
        res += cuenta(ve,A,B);
    }
    return res;
}
```

6. Math

6.1. Identidades

$$\sum_{i=0}^{n} \binom{n}{i} = 2^n$$

$$\sum_{i=0}^{n} i\binom{n}{i} = n * 2^{n-1}$$

$$\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6}$$

$$\sum_{i=0}^{n} i(i-1) = \frac{8}{6}(\frac{n}{2})(\frac{n}{2}+1)(n+1)$$

(doubles) → Sino ver caso impar y par

$$\sum_{i=0}^{n} i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^{n} i\right]^2$$

$$\sum_{i=0}^{n} i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$$

$$\sum_{i=0}^{n} i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_k}{p-k+1}\binom{p}{k}(n+1)^{p-k+1}$$

6.2. Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
  comb[i][0]=comb[i][i]=1;
  forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1])%MOD;
}

ll lucas (ll n, ll k, int p){ //Calcula (n,k)%p teniendo comb[p][p]
    precalculado.
  ll aux = 1;
  while (n + k){
    aux = (aux * comb[n%p][k%p]) %p;
    n/=p, k/=p;
  }
  return aux;
}
```

6.3. Exp. de Numeros Mod.

```
ll expmod (ll b, ll e, ll m){//O(log b)
  if(!e) return 1;
  ll q= expmod(b,e/2,m); q=(q*q)%m;
  return e%2? (b * q)%m : q;
}
```

6.4. Exp. de Matrices y Fibonacci en log(n)

```
struct M22{      // |a b|
  tipo a,b,c,d;// |c d|
  M22 operator*(const M22 &p) const {
    return (M22){a*p.a+b*p.c, a*p.b+b*p.d, c*p.a+d*p.c,c*p.b+d*p.d};}
};
M22 operator^(const M22 &p, int n){
  if(!n) return (M22){1, 0, 0, 1};//identidad
  M22 q=p^(n/2); q=q*q;
  return n%2? p * q : q;}

ll fibo(ll n){//calcula el fibonacci enesimo
  M22 mat=(M22){0, 1, 1, 1}^n;
  return mat.a*f0+mat.b*f1;//f0 y f1 son los valores iniciales
}
```

6.5. Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)^{-1}_{m_j} * \prod_{i=1, i \neq j}^{n} m_i)$$

6.6. Funciones de primos

```
ll numPrimeFactors (ll n){
  ll rta = 0;
  map<ll,ll> f=fact(n);
  forall(it, f) rta += it->second;
  return rta;
}

ll numDiffPrimeFactors (ll n){
  ll rta = 0;
  map<ll,ll> f=fact(n);
  forall(it, f) rta += 1;
  return rta;
}

ll sumPrimeFactors (ll n){
  ll rta = 0;
  map<ll,ll> f=fact(n);
  forall(it, f) rta += it->first;
  return rta;
}

ll numDiv (ll n){
  ll rta = 1;
  map<ll,ll> f=fact(n);
  forall(it, f) rta *= (it->second + 1);
  return rta;
}

ll sumDiv (ll n){
  ll rta = 1;
  map<ll,ll> f=fact(n);
  forall(it, f) rta *= ((ll)pow((double)it->first, it->second + 1.0)-1)
      / (it->first-1);
  return rta;
}

ll eulerPhi (ll n){ // con criba: O(lg n)
  ll rta = n;
  map<ll,ll> f=fact(n);
  forall(it, f) rta -= rta / it->first;
  return rta;
}

ll eulerPhi2 (ll n){ // O (sqrt n)
  ll r = n;
  forr (i,2,n+1){
    if ((ll)i*i > n)
      break;
    if (n % i == 0){
      while (n%i == 0) n/=i;
      r -= r/i;
    }}
  if (n != 1)
    r-= r/n;
  return r;
}
```

6.7. Phollard's Rho (rolando)

```
ll mulmod (ll a, ll b, ll c) { //returns (a*b)%c, and minimize overfloor
  ll x = 0, y = a%c;
  while (b > 0){
    if (b % 2 == 1) x = (x+y) % c;
    y = (y*2) % c;
    b /= 2;
  }
  return x % c;
}

bool es_primo_prob (ll n, int a)
{
  if (n == a) return true;
  ll s = 0,d = n-1;
  while (d % 2 == 0) s++,d/=2;

  ll x = expmod(a,d,n);
  if ((x == 1) || (x+1 == n)) return true;

```

```
  forn (i, s-1){
    x = (x*x)%n;
    if (x == 1) return false;
    if (x+1 == n) return true;
  }
  return false;
}

bool miller_rabin (ll n){ //devuelve true si n es primo
  if (n == 1) return false;
  const int ar[] = {2,3,5,7,11,13,17,19,23};
  forn (j,9)
    if (!es_primo_prob(n,ar[j]))
      return false;
  return true;
}

ll pollard_rho (ll n, ll c=1){
  int i = 0, k = 2;
  ll x = 3, y = 3;
  if(c>=n) return -1;//FAILURE
  //~ if(c!=1) dprint(c);
  while (1){
    i++;
    x = (mulmod (x,x,n) + c) % n;
    ll d = gcd (abs(y-x), n);
    if(d==n) return pollard_rho(n, c+1);
    if (d != 1) return d;
    if (i == k) y = x, k*=2;
  }
}

ll brent(ll n){
    srand(time(NULL));
        if (n%2 == 0)
                return 2;
        ll y = rand()%(n-1)+1, c = rand()%(n-1)+1, m = rand()%(n-1)+1;
        ll g,r,q,x,k,ys;
        g = r = q = 1;
        while (g==1){
                x = y;
                forn (i,r)
                     y = ((y*y)%n+c)%n;
                k = 0;
                while (k<r && g==1){
                        ys = y;
                        forn (i,min(m,r-k)){
                                y = ((y*y)%n+c)%n;
                                q = q*(x-y)%n;
                }
                        g = gcd(q,n);
                        k = k + m;
          }
                r = r*2;
      }
        if (g==n){
                while (true){
                        ys = ((ys*ys)%n+c)%n;
                        g = gcd(abs(x-ys),n);
                        if (g>1)
                              break;
          }
        }

        return g;
}
```

6.8. Criba

```
#define MAXP 80000  //no necesariamente primo
int criba[MAXP+1];
vector<int> primos;
void buscarprimos(){
  int sq=sqrt(MAXP)+1;
  forr(p, 2, MAXP+1) if(!criba[p]){
    primos.push_back(p);
    if(p<=sq)
      for(int m=p*p; m<=MAXP; m+=p)//borro los multiplos de p
        if(!criba[m])criba[m]=p;
  }
}
```

6.9. Factorizacion

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```
//factoriza bien numeros hasta MAXP^2
map<ll,ll> fact(ll n){ //0 (cant primos)
```

```
  map<ll,ll> ret;
  forall(p, primos){
    while(!(n%*p)){
      ret[*p]++;//divisor found
      n/=*p;
    }
  }
  if(n>1) ret[n]++;
  return ret;
}

//factoriza bien numeros hasta MAXP
map<ll,ll> fact2(ll n){ //O (lg n)
  map<ll,ll> ret;
  while (criba[n]){
    ret[criba[n]]++;
    n/=criba[n];
  }
  if(n>1) ret[n]++;
  return ret;
}
```

6.10. GCD

```
tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
```

6.11. Extended Euclid

```
void extendedEuclid (ll a, ll b){ //a * x + b * y = d
  if (!b) { x = 1; y = 0; d = a; return;}
  extendedEuclid (b, a%b);
  ll x1 = y;
  ll y1 = x - (a/b) * y;
  x = x1; y = y1;
}
```

6.12. LCM

```
tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
```

6.13. Inversos

```
#define MAXMOD 15485867
ll inv[MAXMOD];//inv[i]*i=1 mod MOD
void calc(int p){//O(p)
  inv[1]=1;
  forr(i, 2, p) inv[i]= p-((p/i)*inv[p%i])%p;
}
int inverso(int x){//O(log x)
  return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
  return expmod(x, MOD-2);//si mod es primo
}
```

6.14. Simpson

```
double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
  double area=0, h=(b-a)/n, fa=f(a), fb;
  forn(i, n){
    fb=f(a+h*(i+1));
    area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
  }
  return area*h/6.;}
```

6.15. Fraction

```
tipo mcd(tipo a, tipo b){return a?mcd(b%a, a):b;}
struct frac{
  tipo p,q;
  frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
  void norm(){
    tipo a = mcd(p,q);
    if(a) p/=a, q/=a;
    else q=1;
    if (q<0) q=-q, p=-p;}
  frac operator+(const frac& o){
    tipo a = mcd(q,o.q);
    return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
  frac operator-(const frac& o){
    tipo a = mcd(q,o.q);
    return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
  frac operator*(frac o){
    tipo a = mcd(q,o.p), b = mcd(o.q,p);
    return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
  frac operator/(frac o){
    tipo a = mcd(q,o.q), b = mcd(o.p,p);
    return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
  bool operator<(const frac &o) const{return p*o.q < o.p*q;}
```

```
  bool operator==(frac o){return p==o.p&&q==o.q;}
};
```

6.16. Polinomio

```
struct poly {
    vector<tipo> c;//guarda los coeficientes del polinomio
    poly(const vector<tipo> &c): c(c) {}
    poly() {}
  int gr(){//calculates grade of the polynomial
    return sz(c); }
  bool isnull() {return c.empty();}
    poly operator+(const poly &o) const {
        int m = sz(c), n = sz(o.c);
        vector<tipo> res(max(m,n));
        forn(i, m) res[i] += c[i];
        forn(i, n) res[i] += o.c[i];
        return poly(res);
    }
    poly operator*(const poly &o) const {
        int m = sz(c), n = sz(o.c);
        vector<tipo> res(m+n-1);
        forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
        return poly(res);
    }
  tipo eval(tipo v) {
    tipo sum = 0;
    forall(it, c) sum=sum*v + *it;
    return sum;
  }
  //the following function generates the roots of the polynomial
//it can be easily modified to return float roots
  set<tipo> roots(){
    set<tipo> roots;
    tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
    vector<tipo> ps,qs;
    forr(p,1,sqrt(a0)+1) if (a0%p==0) ps.pb(p),ps.pb(a0/p);
    forr(q,1,sqrt(an)+1) if (an%q==0) qs.pb(q),qs.pb(an/q);
    forall(pt,ps)
      forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
        tipo root = abs((*pt) / (*qt));
        if (eval(root)==0) roots.insert(root);
      }
    return roots;
  }
};
poly interpolate(const vector<tipo> &x, const vector<tipo> &y) {
    int n = sz(x);
    poly p;
    vector<tipo> aux(2);
    forn(i, n) {
       double a = y[i] - p.eval(x[i]);
       forn(j, i) a /= x[i] - x[j];
       poly add(vector<tipo>(1, a));
       forn(j, i) aux[0]=-x[j], aux[1]=1, add = add*aux;
       p = p + add;
    }
    return p;
}
//the following functions allows parsing an expression like
//34+150+4*45
//into a polynomial(el numero en funcion de la base)
#define LAST(s) (sz(s)? s[sz(s)-1] : 0)
#define POP(s) s.erase(--s.end());
poly D(string &s) {
  poly d;
  for(int i=0; isdigit(LAST(s)); i++) d.c.push_back(LAST(s)-'0'), POP(s)
      ;
  return d;}

poly T(string &s) {
  poly t=D(s);
  if (LAST(s)=='*'){POP(s); return T(s)*t;}
  return t;
}
//main function, call this to parse
poly E(string &s) {
  poly e=T(s);
  if (LAST(s)=='+'){POP(s); return E(s)+e;}
  return e;
}
```

7. Grafos

7.1. Dijkstra

```cpp
#define INF 1e9
int N;
#define MAX_V 250001
vector<ii> G[MAX_V];
//To add an edge use
#define add(a, b, w) G[a].pb(mkp(w, b))

ll dijkstra(int s, int t){//O(|E| log |V|)
  priority_queue<ii, vector<ii>, greater<ii> > Q;
  vector<ll> dist(N, INF); vector<int> dad(N, -1);
  Q.push(mkp(0, s)); dist[s] = 0;
  while(sz(Q)){
    ii p = Q.top(); Q.pop();
    if(p.snd == t) break;
    forall(it, G[p.snd])
      if(dist[p.snd]+it->first < dist[it->snd]){
        dist[it->snd] = dist[p.snd] + it->fst;
        dad[it->snd] = p.snd;
        Q.push(mkp(dist[it->snd], it->snd));
      }
  }
  return dist[t];
  if(dist[t]<INF)//path generator
    for(int i=t; i!=-1; i=dad[i])
      printf("%d%c", i, (i==s?'\n':' '));
}
```

7.2. Bellman-Ford

```cpp
vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
int dist[MAX_N];
void bford(int src){//O(VE)
  dist[src]=0;
  forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
    dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
}

bool hasNegCycle(){
  forn(j, N) if(dist[j]!=INF) forall(it, G[j])
    if(dist[it->snd]>dist[j]+it->fst) return true;
  //inside if: all points reachable from it->snd will have -INF distance
      (do bfs)
  return false;
}
```

7.3. Floyd-Warshall

```cpp
//G[i][j] contains weight of edge (i, j) or INF
//G[i][i]=0
int G[MAX_N][MAX_N];
void floyd(){//O(N^3)
forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
  G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
}
bool inNegCycle(int v){
  return G[v][v]<0;}
//checks if there's a neg. cycle in path from a to b
bool hasNegCycle(int a, int b){
  forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
    return true;
  return false;
}
```

7.4. Kruskal

```cpp
struct Ar{int a,b,w;};
bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}
vector<Ar> E;
ll kruskal(){
    ll cost=0;
    sort(E.begin(), E.end());//ordenar aristas de menor a mayor
    uf.init(n);
    forall(it, E){
        if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
            uf.unir(it->a, it->b);//conectar
            cost+=it->w;
        }
    }
    return cost;
}
```

7.5. Prim

```cpp
bool taken[MAXN];
priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
void process(int v){
    taken[v]=true;
```

```
    forall(e, G[v])
        if(!taken[e->second]) pq.push(*e);
}

ll prim(){
    zero(taken);
    process(0);
    ll cost=0;
    while(sz(pq)){
        ii e=pq.top(); pq.pop();
        if(!taken[e.second]) cost+=e.first, process(e.second);
    }
    return cost;
}
```

7.6. 2-SAT + Tarjan SCC

```
//We have a vertex representing a var and other for his negation.
//Every edge stored in G represents an implication. To add an equation
    of the form a||b, use addor(a, b)
//MAX=max cant var, n=cant var
#define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
vector<int> G[MAX*2];
//idx[i]=index assigned in the dfs
//lw[i]=lowest index(closer from the root) reachable from i
int lw[MAX*2], idx[MAX*2], qidx;
stack<int> q;
int qcmp, cmp[MAX*2];
//verdad[cmp[i]]=valor de la variable i
bool verdad[MAX*2+1];

int neg(int x) { return x>=n? x-n : x+n;}
void tjn(int v){
  lw[v]=idx[v]=++qidx;
  q.push(v), cmp[v]=-2;
  forall(it, G[v]){
    if(!idx[*it] || cmp[*it]==-2){
      if(!idx[*it]) tjn(*it);
      lw[v]=min(lw[v], lw[*it]);
    }
  }
  if(lw[v]==idx[v]){
    qcmp++;
    int x;
    do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
    verdad[qcmp]=(cmp[neg(v)]<0);
  }
}
//remember to CLEAR G!!!
bool satisf(){//O(n)
  memset(idx, 0, sizeof(idx)), qidx=0;
  memset(cmp, -1, sizeof(cmp)), qcmp=0;
  forn(i, n){
    if(!idx[i]) tjn(i);
    if(!idx[neg(i)]) tjn(neg(i));
  }
  forn(i, n) if(cmp[i]==cmp[neg(i)]) return false;
  return true;
}
```

7.7. Articulation Points

```
int N;
vector<int> G[1000000];
//V[i]=node number(if visited), L[i]= lowest V[i] reachable from i
int qV, V[1000000], L[1000000], P[1000000];
void dfs(int v, int f){
  L[v]=V[v]=++qV;
  forall(it, G[v])
    if(!V[*it]){
      dfs(*it, v);
      L[v] = min(L[v], L[*it]);
      P[v]+= L[*it]>=V[v];
    }
    else if(*it!=f)
      L[v]=min(L[v], V[*it]);
}
int cantart(){ //O(n)
  qV=0;
  zero(V), zero(P);
  dfs(1, 0); P[1]--;
  int q=0;
  forn(i, N) if(P[i]) q++;
return q;
}
```

7.8. Comp. Biconexas y Puentas

```
struct edge {
  int u,v, comp;
  bool bridge;
};
vector<edge> e;
void addEdge(int u, int v) {
  G[u].pb(sz(e)), G[v].pb(sz(e));
  e.pb((edge){u,v,-1,false});
}
//d[i]=id de la dfs
//b[i]=lowest id reachable from i
int d[MAXN], b[MAXN], t;
int nbc;//cant componentes
int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
void initDfs(int n) {
  zero(G), zero(comp);
  e.clear();
  forn(i,n) d[i]=-1;
  nbc = t = 0;
}
stack<int> st;
void dfs(int u, int pe) {//O(n + m)
  b[u] = d[u] = t++;
  comp[u] = (pe != -1);
  forall(ne, G[u]) if (*ne != pe){
    int v = e[*ne].u ^ e[*ne].v ^ u;
    if (d[v] == -1) {
      st.push(*ne);
      dfs(v,*ne);
      if (b[v] > d[u]){
        e[*ne].bridge = true; // bridge
      }
      if (b[v] >= d[u]){ // art
        int last;
        do {
          last = st.top(); st.pop();
          e[last].comp = nbc;
        } while (last != *ne);
        nbc++;
        comp[u]++;
      }
      b[u] = min(b[u], b[v]);
    }
    else if (d[v] < d[u]) { // back edge
      st.push(*ne);
      b[u] = min(b[u], d[v]);
    }
  }
}
```

7.9. LCA + Climb

```
//f[v][k] holds the 2^k father of v
//L[v] holds the level of v
int N, f[100001][20], L[100001];
void build(){//f[i][0] must be filled previously, O(nlgn)
  forn(k, 20-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}

#define lg(x) (31-__builtin_clz(x))//=floor(log2(x))

int climb(int a, int d){//O(lgn)
  if(!d) return a;
  dforn(i, lg(L[a])+1)
    if(1<<i<=d)
      a=f[a][i], d-=1<<i;
    return a;
}
int lca(int a, int b){//O(lgn)
  if(L[a]<L[b]) swap(a, b);
  a=climb(a, L[a]-L[b]);
  if(a==b) return a;
  dforn(i, lg(L[a])+1)
    if(f[a][i]!=f[b][i])
      a=f[a][i], b=f[b][i];
  return f[a][0];
}
```

7.10. Heavy Light Decomposition

```
int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
int dad[MAXN];//dad[v]=padre del nodo v
void dfs1(int v, int p=-1){//pre-dfs
  dad[v]=p;
  treesz[v]=1;
  forall(it, G[v]) if(*it!=p){
```

```
    dfs1(*it, v);
    treesz[v]+=treesz[*it];
  }
}
int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
//Las cadenas aparecen continuas en el recorrido!
int cantcad;
int homecad[MAXN];//dada una cadena devuelve su nodo inicial
int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
void heavylight(int v, int cur=-1){
  if(cur==-1) homecad[cur=cantcad++]=v;
  pos[v]=q++;
  cad[v]=cur;
  int mx=-1;
  forn(i, sz(G[v])) if(G[v][i]!=dad[v])
    if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;
  if(mx!=-1) heavylight(G[v][mx], cur);
  forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
    heavylight(G[v][i], -1);
}
//ejemplo de obtener el maximo numero en el camino entre dos nodos
//RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
//esta funcion va trepando por las cadenas
int query(int an, int v){//O(logn)
  //si estan en la misma cadena:
  if(cad[an]==cad[v]) return rmq.get(pos[an], pos[v]+1);
  return max(query(an, dad[homecad[cad[v]]]),
         rmq.get(pos[homecad[cad[v]]], pos[v]+1));
}
```

7.11. Euler Cycle

```
int n,m,ars[MAXE], eq;
vector<int> G[MAXN];//fill G,n,m,ars,eq
list<int> path;
int used[MAXN];
bool usede[MAXE];
queue<list<int>::iterator> q;
int get(int v){
  while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;
  return used[v];
}
void explore(int v, int r, list<int>::iterator it){
  int ar=G[v][get(v)]; int u=v^ars[ar];
  usede[ar]=true;
  list<int>::iterator it2=path.insert(it, u);
  if(u!=r) explore(u, r, it2);
  if(get(v)<sz(G[v])) q.push(it);
}
void euler(){
  zero(used), zero(usede);
  path.clear();
  q=queue<list<int>::iterator>();
  path.push_back(0); q.push(path.begin());
  while(sz(q)){
    list<int>::iterator it=q.front(); q.pop();
    if(used[*it]<sz(G[*it])) explore(*it, *it, it);
  }
  reverse(path.begin(), path.end());
}
void addEdge(int u, int v){
  G[u].pb(eq), G[v].pb(eq);
  ars[eq++]=u^v;
}
```

7.12. Chu-liu

```
struct Ar{
    int src,dst,w;
};
typedef int weight ;
const weight inf=1e9;
typedef vector< vector< Ar > > graph;
void backward_traverse(int v, int s, int r,
graph &gg,
vector<int> &no, vector< vector<int> > &comp,
vector<int> &prev, vector< vector<int> > &next, vector<weight> &mcost,
vector<int> &mark, weight &cost, bool &found) {
    if (mark[v]) {
        vector<int> temp = no;
        found = true;
        do {
            cost += mcost[v];
            v = prev[v];
            if (v != s) {
                while (comp[v].size() > 0) {
```

```
                    no[comp[v].back()] = s;
                    comp[s].push_back(comp[v].back());
                    comp[v].pop_back();
                }
            }
        } while (v != s);

        for (int k = 0; k < sz(comp[s]); ++k) {
            int j = comp[s][k];
            if (j != r)
            for (int l = 0; l < sz(gg[j]); ++l)
            if (no[ gg[j][l].src ] != s)
            gg[j][l].w -= mcost[ temp[j] ];
        }
    }
    mark[v] = true;
    for (int k = 0; k < sz(next[v]); ++k) {
        int i = next[v][k];
        if (no[i] != no[v] && prev[ no[i] ] == v)
        if (!mark[ no[i] ] || i == s)
        backward_traverse(i, s, r, gg,
        no, comp, prev, next, mcost, mark, cost, found);
    }
}
weight minimum_spanning_arborescence(int r, graph &g) {
    const int n = g.size();
    graph gg(n);
    for (int i = 0; i < sz(g); ++i)
    for (int j = 0; j < sz(g[i]); ++j)
      gg[ g[i][j].dst ].push_back( g[i][j] );
    vector<int> no(n);
    vector< vector<int> > comp(n);
    for (int i = 0; i < n; ++i) {
        no[i] = i;
        comp[i].push_back(i);
    }
    weight cost = 0;
    while (1) {
        vector<int> prev(n, -1);
        vector<weight> mcost(n, inf);
        for (int j = 0; j < n; ++j) {
            if (j == r) continue;
            for (int k = 0; k < sz(gg[j]); ++k) {
                int i = gg[j][k].src;
                if (no[i] != no[j]) {
                    if (gg[j][k].w < mcost[ no[j] ]) {
                        mcost[ no[j] ] = gg[j][k].w;
                        prev[ no[j] ] = no[i];
                    }
                }
            }
        }
        vector< vector<int> > next(n);
        for (int i = 0; i < n; ++i)
        if (prev[i] >= 0)
        next[ prev[i] ].push_back( i );

        bool stop = true;
        vector<int> mark(n);
        for (int i = 0; i < n; ++i) {
            if (i == r || mark[i] || comp[i].size() == 0) continue;
            bool found = false;
            backward_traverse(i, i, r, gg,
            no, comp, prev, next, mcost, mark, cost, found);
            if (found) stop = false;
        }
        if (stop) {
            for (int i = 0; i < n; ++i)
              if (prev[i] >= 0)
                cost += mcost[i];
            return cost;
}}}
```

7.13. Hungarian

```
#define MAXN 256
#define INFTO 0x7f7f7f7f
int n;
int mt[MAXN][MAXN]; // Matriz de costos (X * Y)
int xy[MAXN], yx[MAXN]; // Matching resultante (X->Y, Y->X)
int lx[MAXN], ly[MAXN], slk[MAXN], slkx[MAXN], prv[MAXN];
char S[MAXN], T[MAXN];
void updtree(int x) {
  forn(y, n) if (lx[x] + ly[y] - mt[x][y] < slk[y]) {
    slk[y] = lx[x] + ly[y] - mt[x][y];
    slkx[y] = x;
```

```
} }
int hungar(){//Matching maximo de mayor costo en grafos dirigidos (N^3)
  forn(i, n) {
    ly[i] = 0;
    lx[i] = *max_element(mt[i], mt[i]+n); }
  memset(xy, -1, sizeof(xy));
  memset(yx, -1, sizeof(yx));
  forn(m, n) {
    memset(S, 0, sizeof(S));
    memset(T, 0, sizeof(T));
    memset(prv, -1, sizeof(prv));
    memset(slk, 0x7f, sizeof(slk));
    queue<int> q;
#define bpone(e, p) { q.push(e); prv[e] = p; S[e] = 1; updtree(e); }
    forn(i, n) if (xy[i] == -1) { bpone(i, -2); break; }
    int x=0, y=-1;
    while (y==-1) {
      while (!q.empty() && y==-1) {
        x = q.front(); q.pop();
        forn(j, n) if (mt[x][j] == lx[x] + ly[j] && !T[j]) {
          if (yx[j] == -1) { y = j; break; }
          T[j] = 1;
          bpone(yx[j], x);
        }
      }
      if (y!=-1) break;
      int dlt = INFTO;
      forn(j, n) if (!T[j]) dlt = min(dlt, slk[j]);
      forn(k, n) {
        if (S[k]) lx[k] -= dlt;
        if (T[k]) ly[k] += dlt;
        if (!T[k]) slk[k] -= dlt;
      }
      forn(j, n) if (!T[j] && !slk[j]) {
        if (yx[j] == -1) {
          x = slkx[j]; y = j; break;
        } else {
          T[j] = 1;
          if (!S[yx[j]]) bpone(yx[j], slkx[j]);
        }
      }
    }
    if (y!=-1) {
      for(int p = x; p != -2; p = prv[p]) {
        yx[y] = p;
        int ty = xy[p]; xy[p] = y; y = ty;
      }
    } else break;
  }
  int res = 0;
  forn(i, n) res += mt[i][xy[i]];
  return res;
}
```

8. Network Flow

8.1. Dinic

```
int nodes, src, dest;
int dist[MAX], q[MAX], work[MAX];

struct Edge {
  int to, rev;
  ll f, cap;
  Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap)
      {}
};

vector<Edge> G[MAX];

// Adds bidirectional edge
void addEdge(int s, int t, ll cap){
  G[s].push_back(Edge(t, G[t].size(), 0, cap));
  G[t].push_back(Edge(s, G[s].size()-1, 0, 0));
}

bool dinic_bfs() {
  fill(dist, dist + nodes, -1);
  dist[src] = 0;
  int qt = 0;
  q[qt++] = src;
  for (int qh = 0; qh < qt; qh++) {
    int u = q[qh];
    forall(e, G[u]){
      int v = e->to;
      if(dist[v]<0 && e->f < e->cap){
```

```
        dist[v]=dist[u]+1;
        q[qt++]=v;
      }
    }
  }
  return dist[dest] >= 0;
}

ll dinic_dfs(int u, ll f) {
  if (u == dest) return f;
  for (int &i = work[u]; i < (int) G[u].size(); i++) {
    Edge &e = G[u][i];
    if (e.cap <= e.f) continue;
    int v = e.to;
    if (dist[v] == dist[u] + 1) {
      ll df = dinic_dfs(v, min(f, e.cap - e.f));
      if (df > 0) {
        e.f += df;
        G[v][e.rev].f -= df;
        return df;
      }
    }
  }
  return 0;
}

ll maxFlow(int _src, int _dest) {//O(V^2 E)<
  src = _src;
  dest = _dest;
  ll result = 0;
  while (dinic_bfs()) {
    fill(work, work + nodes, 0);
    while(ll delta = dinic_dfs(src, INF))
      result += delta;
  }

  // todos los nodos  con dist[v]!=-1 vs los que tienen dist[v]==-1
     forman el min cut

  return result;
}
```

8.2. Konig

```
// asume que el dinic YA ESTA tirado
// asume que nodes-1 y nodes-2 son la fuente y destino
int match[maxnodes]; // match[v]=u si u-v esta en el matching, -1 si v
    no esta matcheado
int s[maxnodes]; // numero de la bfs del koning
queue<int> kq;
// s[e]%2==1  o si e esta en V1 y s[e]==-1-> lo agarras
void koning() {//O(n)
  forn(v,nodes-2) s[v] = match[v] = -1;
  forn(v,nodes-2) forall(it,g[v]) if (it->to < nodes-2 && it->f>0)
    { match[v]=it->to; match[it->to]=v;}
  forn(v,nodes-2) if (match[v]==-1) {s[v]=0;kq.push(v);}
  while(!kq.empty()) {
    int e = kq.front(); kq.pop();
    if (s[e]%2==1) {
      s[match[e]] = s[e]+1;
      kq.push(match[e]);
    } else {

      forall(it,g[e]) if (it->to < nodes-2 && s[it->to]==-1) {
        s[it->to] = s[e]+1;
        kq.push(it->to);
      }
    }
  }
}
```

8.3. Edmonds Karp's

```
#define MAX_V 1000
#define INF 1e9
//special nodes
#define SRC 0
#define SNK 1
map<int, int> G[MAX_V];//limpiar esto
//To add an edge use
#define add(a, b, w) G[a][b]=w
int f, p[MAX_V];
void augment(int v, int minE){
  if(v==SRC) f=minE;
  else if(p[v]!=-1){
```

```
    augment(p[v], min(minE, G[p[v]][v]));
    G[p[v]][v]-=f, G[v][p[v]]+=f;
  }
}
ll maxflow(){//O(VE^2)
  ll Mf=0;
  do{
    f=0;
    char used[MAX_V]; queue<int> q; q.push(SRC);
    zero(used), memset(p, -1, sizeof(p));
    while(sz(q)){
      int u=q.front(); q.pop();
      if(u==SNK) break;
      forall(it, G[u])
        if(it->snd>0 && !used[it->fst])
          used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
    }
    augment(SNK, INF);
    Mf+=f;
  }while(f);
  return Mf;
}
```

8.4. Push-Relabel

```
#define MAX_V 1000
int N;//valid nodes are [0...N-1]
#define INF 1e9
//special nodes
#define SRC 0
#define SNK 1
map<int, int> G[MAX_V];
//To add an edge use
#define add(a, b, w) G[a][b]=w
ll excess[MAX_V];
int height[MAX_V], active[MAX_V], count[2*MAX_V+1];
queue<int> Q;
void enqueue(int v) {
  if (!active[v] && excess[v] > 0) active[v]=true, Q.push(v); }
void push(int a, int b) {
  int amt = min(excess[a], ll(G[a][b]));
  if(height[a] <= height[b] || amt == 0) return;
  G[a][b]-=amt, G[b][a]+=amt;
  excess[b] += amt, excess[a] -= amt;
  enqueue(b);
}
void gap(int k) {
  forn(v, N){
    if (height[v] < k) continue;
    count[height[v]]--;
    height[v] = max(height[v], N+1);
    count[height[v]]++;
    enqueue(v);
  }
}
void relabel(int v) {
  count[height[v]]--;
  height[v] = 2*N;
  forall(it, G[v])
    if(it->snd)
      height[v] = min(height[v], height[it->fst] + 1);
  count[height[v]]++;
  enqueue(v);
}
ll maxflow() {//O(V^3)
  zero(height), zero(active), zero(count), zero(excess);
  count[0] = N-1;
  count[N] = 1;
  height[SRC] = N;
  active[SRC] = active[SNK] = true;
  forall(it, G[SRC]){
    excess[SRC] += it->snd;
    push(SRC, it->fst);
  }
  while(sz(Q)) {
    int v = Q.front(); Q.pop();
    active[v]=false;
  forall(it, G[v]) push(v, it->fst);
  if(excess[v] > 0)
    count[height[v]] == 1? gap(height[v]):relabel(v);
  }
  ll mf=0;
  forall(it, G[SRC]) mf+=G[it->fst][SRC];
  return mf;
}
```

8.5. Min-cost Max-flow

```
struct edge {
  int u, v;
  ll cap, cost, flow;
  ll rem() { return cap - flow; }
};
int n;//numero de nodos
vector<int> G[MAXN];
vector<edge> e;
void addEdge(int u, int v, ll cap, ll cost) {
  G[u].pb(si(e)); e.pb((edge){u,v,cap,cost,0});
  G[v].pb(si(e)); e.pb((edge){v,u,0,-cost,0});
}
ll pot[MAXN], dist[MAXN], pre[MAXN], cap[MAXN];
ll mxFlow, mnCost;
void flow(int s, int t) {
  fill(pot, pot+n, 0);
  mxFlow=mnCost=0;
  while(1){
    fill(dist, dist+n, INF); dist[s] = 0;
    fill(pre, pre+n, -1); pre[s]=0;
    fill(cap, cap+n, 0); cap[s] = INF;
    priority_queue<pair<ll,int> > q; q.push(mkp(0,s));
    while (!q.empty()) {
      pair<ll,int> top = q.top(); q.pop();
      int u = top.second, d = -top.first;
      if (u == t) break;
      if (d > dist[u]) continue;
      forn(i,si(G[u])) {
        edge E = e[G[u][i]];
        int c = E.cost + pot[u] - pot[E.v];
        if (E.rem() && dist[E.v] > dist[u] + c) {
          dist[E.v] = dist[u] + c;
          pre[E.v] = G[u][i];
          cap[E.v] = min(cap[u], E.rem());
          q.push(mkp(-dist[E.v], E.v));
        }
      }
    }
    if (pre[t] == -1) break;
    forn(u,n)
      if (dist[u] == INF) pot[u] = INF;
      else pot[u] += dist[u];
    mxFlow +=cap[t];
    mnCost +=cap[t]*pot[t];
    for (int v = t; v != s; v = e[pre[v]].u) {
      e[pre[v]].flow += cap[t];
      e[pre[v]^1].flow -= cap[t];
    }
  }
}
```

9. Ayudamemoria

Cant. decimales

```
#include <iomanip>
cout << setprecision(2) << fixed;
```

Rellenar con espacios(para justificar)

```
#include <iomanip>
cout << setfill('␣') << setw(3) << 2 << endl;
```

Leer hasta fin de linea

```
#include <sstream>
//hacer cin.ignore() antes de getline()
while(getline(cin, line)){
     istringstream is(line);
     while(is >> X)
       cout << X << "␣";
     cout << endl;
}
```

Aleatorios

```
#define RAND(a, b) (rand()%(b-a+1)+a)
srand(time(NULL));
```

Doubles Comp.

```
const double EPS = 1e-9;
x == y  <=> fabs(x-y) < EPS
x >  y  <=> x > y + EPS
x >= y  <=> x > y - EPS
```

Limites

```
#include <limits>
numeric_limits<T>
  ::max()
  ::min()
  ::epsilon()
```

Muahaha

```
#include <signal.h>
void divzero(int p){
  while(true);}
void segm(int p){
  exit(0);}
//in main
signal(SIGFPE, divzero);
signal(SIGSEGV, segm);
```

Mejorar velocidad

```
ios::sync_with_stdio(false);
```

Mejorar velocidad 2

```
//Solo para enteros positivos
inline void Scanf(int& a){
  char c = 0;
  while(c<33) c = getc(stdin);
  a = 0;
  while(c>33) a = a*10 + c - '0', c = getc(stdin);
}
```

Leer del teclado

```
freopen("/dev/tty", "a", stdin);
```

Iterar subconjunto

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```

File setup

```
//tambien se pueden usar comas: {a, x, m, l}
touch {a..l}.in; tee {a..l}.cpp < template.cpp
```