Índice

1. algorithm

#include <algorithm> #include <numeric>

Algo	Funcion
sort, stable_sort	ordena el intervalo
nth_element	*void* ordena el n-esimo, y particiona el resto
fill, fill_n	*void* llena [f, l) o [f, f+n) con elem
lower_bound, upper_bound	*it* al primer / ultimo donde se puede insertar elem para que quede ordenada
binary_search	*bool* esta elem en [f, l)
copy	hace resul+i=f+i $\forall i$
find, find_if, find_first_of	*it* encuentra i $\in$[f,l) tq. i=elem, pred(i), i$\in$[f2,l2)
count, count_if	cuenta elem, pred(i)
search	busca [f2,l2) $\in$ [f,l)
replace, replace_if	cambia old / pred(i) por new / pred, new
reverse	da vuelta
partition, stable_partition	pred(i) ad, !pred(i) atras
min_element, max_element	*it* min, max de [f,l]
lexicographical_compare	*bool* con [f1,l1]¡[f2,l2]
next/prev_permutation	deja en [f,l) la perm sig, ant
set_intersection, set_difference, set_union, set_symmetric_difference,	[res, ...) la op. de conj
push_heap, pop_heap, make_heap	mete/saca e en heap [f,l), hace un heap de [f,l)
is_heap	*bool* es [f,l) un heap
accumulate	T = $\sum$/oper de [f,l)
inner_product	T = i + [f1, l1) . [f2, ...)
partial_sum	r+i = $\sum$/oper de [f,f+i] $\forall i \in$[f,l)
__builtin_ffs	Pos. del primer 1 desde la derecha
__builtin_clz	Cant. de ceros desde la izquierda.
__builtin_ctz	Cant. de ceros desde la derecha.
__builtin_popcount	Cant. de 1's en x.
__builtin_parity	1 si x es par, 0 si es impar.
__builtin_XXXXXXll	= pero para long long's.

2. Estructuras

2.1. Easy segment

```
const int N = 1e5;  // limit for array size
int n;  // array size
int t[2 * N];

void build() {  // build the tree
  for (int i = n - 1; i > 0; --i) t[i] = t[i<<1]
      + t[i<<1|1];
}

void modify(int p, int value) {  // set value at
    position p
  for (t[p += n] = value; p > 1; p >>= 1) t[p>>1]
       = t[p] + t[p^1];
}

int query(int l, int r) {  // sum on interval [l,
     r)
  int res = 0;
  for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
    if (l&1) res += t[l++];
    if (r&1) res += t[--r];
  }
  return res;
}

int main() {
  scanf("%d", &n);
  for (int i = 0; i < n; ++i) scanf("%d", t + n +
       i);
  build();
  modify(0, 1);
  printf("%d\n", query(3, 11));
  return 0;
}
```

2.2. RMQ (static)

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: LVL $\geq$ ceil(logn); Usar [ ] para llenar arreglo y luego build().

```
struct RMQ{
  #define LVL 10
  tipo vec[LVL][1<<(LVL+1)];
  tipo &operator[](int p){return vec[0][p];}
  tipo get(int i, int j) {//intervalo [i,j)
    int p = 31-__builtin_clz(j-i);
    return min(vec[p][i],vec[p][j-(1<<p)]);
  }
  void build(int n) {//O(nlogn)
    int mp = 31-__builtin_clz(n);
    forn(p, mp) forn(x, n-(1<<p))
      vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p
          )]);
  }};
```

2.3. RMQ (dynamic)

```
//Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre el rango [i, j).
#define MAXN 100000
#define operacion(x, y) max(x, y)
const int neutro=0;
struct RMQ{
  int sz;
  tipo t[4*MAXN];
  tipo &operator[](int p){return t[sz+p];}
  void init(int n){//O(nlgn)
    sz = 1 << (32-__builtin_clz(n));
    forn(i, 2*sz) t[i]=neutro;
  }
  void updall(){//O(n)
    dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);}
  tipo get(int i, int j){return get(i,j,1,0,sz);}
  tipo get(int i, int j, int n, int a, int b){//O(lgn)
    if(j<=a || i>=b) return neutro;
    if(i<=a && b<=j) return t[n];
    int c=(a+b)/2;
    return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
  }
  void set(int p, tipo val){//O(lgn)
    for(p+=sz; p>0 && t[p]!=val;){
      t[p]=val;
      p/=2;
      val=operacion(t[p*2], t[p*2+1]);
    }
  }
}rmq;
//Usage:
cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i];
rmq.updall();
```

2.4. RMQ (lazy)

```
//Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre el rango [i, j).
typedef int Elem;//Elem de los elementos del arreglo
typedef int Alt;//Elem de la alteracion
#define operacion(x,y) x+y
const Elem neutro=0; const Alt neutro2=0;
#define MAXN 100000
struct RMQ{
  int sz;
  Elem t[4*MAXN];
  Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem
  Elem &operator[](int p){return t[sz+p];}
  void init(int n){//O(nlgn)
    sz = 1 << (32-__builtin_clz(n));
    forn(i, 2*sz) t[i]=neutro;
    forn(i, 2*sz) dirty[i]=neutro2;
  }
  void push(int n, int a, int b){//propaga el dirty a sus hijos
    if(dirty[n]!=0){
      t[n]+=dirty[n]*(b-a);//altera el nodo
      if(n<sz){
        dirty[2*n]+=dirty[n];
        dirty[2*n+1]+=dirty[n];
      }
      dirty[n]=0;
    }
  }
  Elem get(int i, int j, int n, int a, int b){//O(lgn)
    if(j<=a || i>=b) return neutro;
    push(n, a, b);//corrige el valor antes de usarlo
    if(i<=a && b<=j) return t[n];
    int c=(a+b)/2;
    return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
  }
  Elem get(int i, int j){return get(i,j,1,0,sz);}
  //altera los valores en [i, j) con una alteracion de val
  void alterar(Alt val, int i, int j, int n, int a, int b){//O(lgn)
    push(n, a, b);
    if(j<=a || i>=b) return;
    if(i<=a && b<=j){
      dirty[n]+=val;
      push(n, a, b);
      return;
    }
    int c=(a+b)/2;
    alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
    t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
  }
  void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
}rmq;
```

2.5. RMQ (persistente)

```
typedef int tipo;
tipo oper(const tipo &a, const tipo &b){
    return a+b;
}
struct node{
  tipo v; node *l,*r;
  node(tipo v):v(v), l(NULL), r(NULL) {}
    node(node *l, node *r) : l(l), r(r){
        if(!l) v=r->v;
        else if(!r) v=l->v;
        else v=oper(l->v, r->v);
    }
};
```

```
node *build (tipo *a, int tl, int tr) {//
    modificar para que tome tipo a
  if (tl+1==tr) return new node(a[tl]);
  int tm=(tl + tr)>>1;
  return new node(build(a, tl, tm), build(a, tm,
      tr));
}
node *update(int pos, int new_val, node *t, int
    tl, int tr){
  if (tl+1==tr) return new node(new_val);
  int tm=(tl+tr)>>1;
  if(pos < tm) return new node(update(pos,
      new_val, t->l, tl, tm), t->r);
  else return new node(t->l, update(pos, new_val,
       t->r, tm, tr));
}
tipo get(int l, int r, node *t, int tl, int tr){
    if(l==tl && tr==r) return t->v;
  int tm=(tl + tr)>>1;
    if(r<=tm) return get(l, r, t->l, tl, tm);
    else if(l>=tm) return get(l, r, t->r, tm, tr)
        ;
  return oper(get(l, tm, t->l, tl, tm), get(tm, r
      , t->r, tm, tr));
}
```

2.6. Union Find

```
class UnionFind {
private:
  vi p, rank, setSize;
  int numSets;
public:
  UnionFind(int N) {
    setSize.assign(N, 1); numSets = N; rank.
        assign(N, 0);
    p.assign(N, 0); for (int i = 0; i < N; i++) p
        [i] = i; }
  int findSet(int i) { return (p[i] == i) ? i : (
      p[i] = findSet(p[i])); }
  bool isSameSet(int i, int j) { return findSet(i
      ) == findSet(j); }
  void unionSet(int i, int j) {
    if (!isSameSet(i, j)) { numSets--;
    int x = findSet(i), y = findSet(j);
    // rank is used to keep the tree short
    if (rank[x] > rank[y]) { p[y] = x; setSize[x]
        += setSize[y]; }
    else                   { p[x] = y; setSize[y]
        += setSize[x];
                             if (rank[x] == rank[
                                 y]) rank[y]++; }
                              } }
  int numDisjointSets() { return numSets; }
  int sizeOfSet(int i) { return setSize[findSet(i
      )]; }
};
```

2.7. Disjoint Intervals

```
bool operator< (const ii &a, const ii &b) {return
     a.fst<b.fst;}
//Stores intervals as [first, second]
//in case of a collision it joins them in a
    single interval
struct disjoint_intervals {
  set<ii> segs;
  void insert(ii v) {//O(lgn)
    if(v.snd-v.fst==0.) return;//OJO
    set<ii>::iterator it,at;
    at = it = segs.lower_bound(v);
    if (at!=segs.begin() && (--at)->snd >= v.fst)
      v.fst = at->fst, --it;
    for(; it!=segs.end() && it->fst <= v.snd;
        segs.erase(it++))
      v.snd=max(v.snd, it->snd);
    segs.insert(v);
  }
};
```

2.8. RMQ (2D)

```
struct RMQ2D{//n filas x m columnas
  int sz;
  RMQ t[4*MAXN];
  RMQ &operator[](int p){return t[sz/2+p];}//t[i
      ][j]=i fila, j col
  void init(int n, int m){//O(n*m)
    sz = 1 << (32-__builtin_clz(n));
    forn(i, 2*sz) t[i].init(m); }
  void set(int i, int j, tipo val){//O(lgm.lgn)
    for(i+=sz; i>0;){
      t[i].set(j, val);
      i/=2;
      val=operacion(t[i*2][j], t[i*2+1][j]);
    } }
  tipo get(int i1, int j1, int i2, int j2){return
       get(i1,j1,i2,j2,1,0,sz);}
  //O(lgm.lgn), rangos cerrado abierto
  int get(int i1, int j1, int i2, int j2, int n,
      int a, int b){
    if(i2<=a || i1>=b) return 0;
    if(i1<=a && b<=i2) return t[n].get(j1, j2);
    int c=(a+b)/2;
    return operacion(get(i1, j1, i2, j2, 2*n, a,
        c),
         get(i1, j1, i2, j2, 2*n+1, c, b));
  }
} rmq;
//Example to initialize a grid of M rows and N
    columns:
RMQ2D rmq; rmq.init(n,m);
forn(i, n) forn(j, m){
  int v; cin >> v; rmq.set(i, j, v);}
```

2.9. Treap para set

Treap para set tiene un Key unico por nodo. En el split if (key <= t->key). En at, if(key == t->key) return t; en lugar de pos.

```
void erase(pnode &t, Key key) {
```

```
    if (!t) return; push(t);
    if (key == t->key) t=merge(t->l, t->r);
    else if (key < t->key) erase(t->l, key);
    else erase(t->r, key);
    if(t) pull(t);}
```

2.10. Treap para arreglo

```
typedef struct node *pnode;
struct node{
    Value val, mini;
    int dirty;
    int prior, size;
    pnode l,r,parent;
    node(Value val): val(val), mini(val), dirty
        (0), prior(rand()), size(1), l(0), r(0),
        parent(0) {}
};
static int size(pnode p) { return p ? p->size :
    0; }
void push(pnode p) {//propagar dirty a los hijos(
    aca para lazy)
  p->val.fst+=p->dirty;
  p->mini.fst+=p->dirty;
  if(p->l) p->l->dirty+=p->dirty;
  if(p->r) p->r->dirty+=p->dirty;
  p->dirty=0;
}
static Value mini(pnode p) { return p ? push(p),
    p->mini : ii(1e9, -1); }
// Update function and size from children's Value
void pull(pnode p) {//recalcular valor del nodo
    aca (para rmq)
  p->size = 1 + size(p->l) + size(p->r);
  p->mini = min(min(p->val, mini(p->l)), mini(p->
      r));//operacion del rmq!
  p->parent=0;
  if(p->l) p->l->parent=p;
  if(p->r) p->r->parent=p;
}
//junta dos arreglos
pnode merge(pnode l, pnode r) {
  if (!l || !r) return l ? l : r;
  push(l), push(r);
  pnode t;
  if (l->prior < r->prior) l->r=merge(l->r, r), t
       = l;
  else r->l=merge(l, r->l), t = r;
  pull(t);
  return t;
}
//parte el arreglo en dos, sz(l)==tam
void split(pnode t, int tam, pnode &l, pnode &r)
    {
  if (!t) return void(l = r = 0);
  push(t);
  if (tam <= size(t->l)) split(t->l, tam, l, t->l
      ), r = t;
  else split(t->r, tam - 1 - size(t->l), t->r, r)
      , l = t;
  pull(t);
}
pnode at(pnode t, int pos) {
  if(!t) exit(1);
  push(t);
  if(pos == size(t->l)) return t;
  if(pos < size(t->l)) return at(t->l, pos);
  return at(t->r, pos - 1 - size(t->l));
}
int getpos(pnode t){//inversa de at
  if(!t->parent) return size(t->l);
  if(t==t->parent->l) return getpos(t->parent)-
      size(t->r)-1;
  return getpos(t->parent)+size(t->l)+1;
}
void split(pnode t, int i, int j, pnode &l, pnode
     &m, pnode &r) {
  split(t, i, l, t), split(t, j-i, m, r);}
Value get(pnode &p, int i, int j){//like rmq
  pnode l,m,r;
    split(p, i, j, l, m, r);
    Value ret=mini(m);
    p=merge(l, merge(m, r));
    return ret;
}

//Sample program: C. LCA Online from Petrozavodsk
     Summer-2012. Petrozavodsk SU Contest
//Available at http://opentrains.snarknews.info/~
    ejudge
const int MAXN=300100;
int n;
pnode beg[MAXN], fin[MAXN];
pnode lista;
```

2.11. Set con busq binaria

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace  __gnu_pbds;
typedef tree<int,null_type,less<int>,//key,mapped
     type, comparator
    rb_tree_tag,tree_order_statistics_node_update
        > set_t;
//find_by_order(i) devuelve iterador al i-esimo
    elemento
//order_of_key(k): devuelve la pos del lower
    bound de k
```

3. Algos

3.1. Longest Increasing Subsequence

```

typedef vector<int> VI;
typedef pair<int,int> PII;
typedef vector<PII> VPII;

#define STRICTLY_INCREASNG
```

```

VI LongestIncreasingSubsequence(VI v) {
  VPII best;
  VI dad(v.size(), -1);

  for (int i = 0; i < v.size(); i++) {
#ifdef STRICTLY_INCREASNG
    PII item = make_pair(v[i], 0);
    VPII::iterator it = lower_bound(best.begin(),
        best.end(), item);
    item.second = i;
#else
    PII item = make_pair(v[i], i);
    VPII::iterator it = upper_bound(best.begin(),
        best.end(), item);
#endif
    if (it == best.end()) {
      dad[i] = (best.size() == 0 ? -1 : best.back
          ().second);
      best.push_back(item);
    } else {
      dad[i] = it == best.begin() ? -1 : prev(it)
          ->second;
      *it = item;
    }
  }
```

3.2. Alpha-Beta prunning

```
ll alphabeta(State &s, bool player = true, int
    depth = 1e9, ll alpha = -INF, ll beta = INF)
    { //player = true -> Maximiza
    if(s.isFinal()) return s.score;
  //~ if (!depth) return s.heuristic();
    vector<State> children;
    s.expand(player, children);
    int n = children.size();
    forn(i, n) {
        ll v = alphabeta(children[i], !player,
            depth-1, alpha, beta);
        if(!player) alpha = max(alpha, v);
        else beta = min(beta, v);
        if(beta <= alpha) break;
    }
    return !player ? alpha : beta;}
```

3.3. Mo's algorithm

```
int n,sq;
struct Qu{//queries [l, r]
    //intervalos cerrado abiertos !!! importante
        !!
    int l, r, id;
}qs[MAXN];
int ans[MAXN], curans;//ans[i]=ans to ith query
bool bymos(const Qu &a, const Qu &b){
    if(a.l/sq!=b.l/sq) return a.l<b.l;
    return (a.l/sq)&1? a.r<b.r : a.r>b.r;
}
void mos(){
    forn(i, t) qs[i].id=i;
    sort(qs, qs+t, bymos);
    int cl=0, cr=0;
    sq=sqrt(n);
    curans=0;
    forn(i, t){ //intervalos cerrado abiertos !!!
        importante!!
        Qu &q=qs[i];
        while(cl>q.l) add(--cl);
        while(cr<q.r) add(cr++);
        while(cl<q.l) remove(cl++);
        while(cr>q.r) remove(--cr);
        ans[q.id]=curans;
    }
}
```

3.4. Ternary search

```
#include <functional>
//Retorna argmax de una funcion unimodal 'f' en
    el rango [left,right]
double ternarySearch(double l, double r, function
    <double(double)> f){
  for(int i = 0; i < 300; i++){
    double m1 = l+(r-l)/3, m2 = r-(r-l)/3;
    if (f(m1) < f(m2))  l = m1; else r = m2;
  }
  return (left + right)/2;
}
```

4. Strings

4.1. Manacher

```
int d1[MAXN];//d1[i]=long del maximo palindromo
    impar con centro en i
int d2[MAXN];//d2[i]=analogo pero para longitud
    par
//0 1 2 3 4
//a a b c c <--d1[2]=3
//a a b b <--d2[2]=2 (estan uno antes)
void manacher(){
  int l=0, r=-1, n=sz(s);
  forn(i, n){
    int k=(i>r? 1 : min(d1[l+r-i], r-i));
    while(i+k<n && i-k>=0 && s[i+k]==s[i-k]) ++k;
    d1[i] = k--;
    if(i+k > r) l=i-k, r=i+k;
  }
  l=0, r=-1;
  forn(i, n){
    int k=(i>r? 0 : min(d2[l+r-i+1], r-i+1))+1;
    while(i+k-1<n && i-k>=0 && s[i+k-1]==s[i-k])
        k++;
    d2[i] = --k;
    if(i+k-1 > r) l=i-k, r=i+k-1;
  }
```

4.2. KMP

```
string T;//cadena donde buscar(where)
string P;//cadena a buscar(what)
```

```
int b[MAXLEN];//back table b[i] maximo borde de [0..i)
void kmppre(){//by gabina with love
    int i =0, j=-1; b[0]=-1;
    while(i<sz(P)){
        while(j>=0 && P[i] != P[j]) j=b[j];
        i++, j++, b[i] = j;
    }
}
void kmp(){
    int i=0, j=0;
    while(i<sz(T)){
        while(j>=0 && T[i]!=P[j]) j=b[j];
        i++, j++;
        if(j==sz(P)) printf("P is found at index %d in T\n", i-j), j=b[j];
    }
}

int main(){
    cout << "T=";
    cin >> T;
    cout << "P=";
```

4.3. Trie

```
struct trie{ map<char, trie> m;
  void add(const string &s, int p=0){ if(s[p]) m[s[p]].add(s, p+1);}
  void dfs(){/*Do stuff*/ forall(it, m) it->second.dfs();}};
```

4.4. Suffix Array (largo, nlogn)

```
#define MAX_N 1000
#define rBOUND(x) (x<n? r[x] : 0)
//sa will hold the suffixes in order.
int sa[MAX_N], r[MAX_N], n;
string s; //input string, n=sz(s)

int f[MAX_N], tmpsa[MAX_N];
void countingSort(int k){
  zero(f);
  forn(i, n) f[rBOUND(i+k)]++;
  int sum=0;
  forn(i, max(255, n)){
    int t=f[i]; f[i]=sum; sum+=t;}
  forn(i, n)
    tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
  memcpy(sa, tmpsa, sizeof(sa));
}
void constructsa(){//O(n log n)
  n=sz(s);
  forn(i, n) sa[i]=i, r[i]=s[i];
  for(int k=1; k<n; k<<=1){
    countingSort(k), countingSort(0);
    int rank, tmpr[MAX_N];
    tmpr[sa[0]]=rank=0;
    forr(i, 1, n)
      tmpr[sa[i]]=(r[sa[i]]==r[sa[i-1]] && r[sa[i]+k]==r[sa[i-1]+k] )? rank : ++rank;
    memcpy(r, tmpr, sizeof(r));
    if(r[sa[n-1]]==n-1) break;
  }
}
//returns (lowerbound, upperbound) of the search
ii stringMatching(string P){ //O(sz(P)lgn)
  int lo=0, hi=n-1, mid=lo;
  while(lo<hi){
```

4.5. String Matching With Suffix Array

```
//returns (lowerbound, upperbound) of the search
ii stringMatching(string P){ //O(sz(P)lgn)
  int lo=0, hi=n-1, mid=lo;
  while(lo<hi){
    mid=(lo+hi)/2;
    int res=s.compare(sa[mid], sz(P), P);
    if(res>=0) hi=mid;
    else lo=mid+1;
  }
  if(s.compare(sa[lo], sz(P), P)!=0) return ii(-1, -1);
  ii ans; ans.fst=lo;
  lo=0, hi=n-1, mid;
  while(lo<hi){
    mid=(lo+hi)/2;
    int res=s.compare(sa[mid], sz(P), P);
    if(res>0) hi=mid;
    else lo=mid+1;
  }
  if(s.compare(sa[hi], sz(P), P)!=0) hi--;
  ans.snd=hi;
  return ans;
}
```

4.6. LCP (Longest Common Prefix)

```
//Calculates the LCP between consecutives suffixes in the Suffix Array.
//LCP[i] is the length of the LCP between sa[i] and sa[i-1]
int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
void computeLCP(){//O(n)
  phi[sa[0]]=-1;
  forr(i, 1, n) phi[sa[i]]=sa[i-1];
  int L=0;
  forn(i, n){
    if(phi[i]==-1) {PLCP[i]=0; continue;}
    while(s[i+L]==s[phi[i]+L]) L++;
    PLCP[i]=L;
    L=max(L-1, 0);
  }
  forn(i, n) LCP[i]=PLCP[sa[i]];
}
```

4.7. Corasick

```

struct trie{
  map<char, trie> next;
  trie* tran[256];//transiciones del automata
```

```
  int idhoja, szhoja;//id de la hoja o 0 si no lo es
  //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que es hoja
  trie *padre, *link, *nxthoja;
  char pch;//caracter que conecta con padre
  trie(): tran(),  idhoja(), padre(), link() {}
  void insert(const string &s, int id=1, int p=0){//id>0!!!
    if(p<sz(s)){
      trie &ch=next[s[p]];
      tran[(int)s[p]]=&ch;
      ch.padre=this, ch.pch=s[p];
      ch.insert(s, id, p+1);
    }
    else idhoja=id, szhoja=sz(s);
  }
  trie* get_link() {
    if(!link){
      if(!padre) link=this;//es la raiz
      else if(!padre->padre) link=padre;//hijo de la raiz
      else link=padre->get_link()->get_tran(pch);
    }
    return link; }
  trie* get_tran(int c) {
    if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
    return tran[c]; }
  trie *get_nxthoja(){
    if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
    return nxthoja; }
  void print(int p){
    if(idhoja) cout << "found " << idhoja << "  at position " << p-szhoja << endl;
    if(get_nxthoja()) get_nxthoja()->print(p); }
  void matching(const string &s, int p=0){
    print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
}tri;


int main(){
  tri=trie();//clear
  tri.insert("ho", 1);
  tri.insert("hoho", 2);
```

4.8. Suffix Automaton

```
struct state {
  int len, link;
  map<char,int> next;
  state() { }
};
const int MAXLEN = 10010;
state st[MAXLEN*2];
int sz, last;
void sa_init() {
  forn(i,sz) st[i].next.clear();
  sz = last = 0;
  st[0].len = 0;
  st[0].link = -1;
  ++sz;
}
// Es un DAG de una sola fuente y una sola hoja
// cantidad de endpos = cantidad de apariciones = cantidad de caminos de la clase al nodo terminal
// cantidad de miembros de la clase = st[v].len-st[st[v].link].len (v>0) = caminos del inicio a la clase
// El arbol de los suffix links es el suffix tree de la cadena invertida. La string de la arista link(v)->v son los caracteres que difieren
void sa_extend (char c) {
  int cur = sz++;
  st[cur].len = st[last].len + 1;
  // en cur agregamos la posicion que estamos extendiendo
  //podria agregar tambien un identificador de las cadenas a las cuales pertenece (si hay varias)
  int p;
  for (p=last; p!=-1 && !st[p].next.count(c); p=st[p].link) // modificar esta linea para hacer separadores unicos entre varias cadenas (c=='$')
    st[p].next[c] = cur;
  if (p == -1)
    st[cur].link = 0;
  else {
    int q = st[p].next[c];
    if (st[p].len + 1 == st[q].len)
      st[cur].link = q;
    else {
      int clone = sz++;
      // no le ponemos la posicion actual a clone sino indirectamente por el link de cur
      st[clone].len = st[p].len + 1;
      st[clone].next = st[q].next;
      st[clone].link = st[q].link;
      for (; p!=-1 && st[p].next.count(c) && st[p].next[c]==q; p=st[p].link)
        st[p].next[c] = clone;
      st[q].link = st[cur].link = clone;
    }
  }
  last = cur;
}
```

4.9. Z Function

```
char s[MAXN];
int z[MAXN]; // z[i] = i==0 ? 0 : max k tq s[0,k) match with s[i,i+k)
void z_function(char s[],int z[]) {
    int n = strlen(s);
    forn(i, n) z[i]=0;
```

```
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
        if (i <= r) z[i] = min (r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])  ++z[i];
        if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
    }
}

int main() {
    ios::sync_with_stdio(0);
```

4.10. Palindromic tree

```
const int maxn = 10100100;

int len[maxn];
int suffLink[maxn];
int to[maxn][2];
int cnt[maxn];
int numV;
char str[maxn];

int v;

void addLetter(int n) {
        while (str[n - len[v] - 1] != str[n] )
                v = suffLink[v];
        int u = suffLink[v];
        while (str[n - len[u] - 1] != str[n] )
                u = suffLink[u];
        int u_ = to[u][str[n] - 'a'];
        int v_ = to[v][str[n] - 'a'];
        if (v_ == -1)
        {
                v_ = to[v][str[n] - 'a'] = numV;
                len[numV++] = len[v] + 2;
                suffLink[v_] = u_;
        }
        v = v_;
        cnt[v]++;
}

void init() {
        memset(to, -1, sizeof to);
        str[0] = '#';
        len[0] = -1;
        len[1] = 0;
        len[2] = len[3] = 1;
        suffLink[1] = 0;
        suffLink[0] = 0;
        suffLink[2] = 1;
        suffLink[3] = 1;
        to[0][0] = 2;
        to[0][1] = 3;
        numV = 4;
}

int main() {
        init();
        scanf("%s", str + 1);
        int n = strlen(str);
        for (int i = 1; i < n; i++)
                addLetter(i);
        long long ans = 0;
        for (int i = numV - 1; i > 0; i--)
                {
                cnt[suffLink[i] ] += cnt[i];
                ans = max(ans, cnt[i] * 1LL * len[i] );
//              fprintf(stderr, "i = %d, cnt = %d, len = %d\n", i, cnt[i], len[i] );
        }
        printf("%lld\n", ans);
        return 0;
}
```

4.11. Rabin Karp - Distinct Substrings

```
int count_unique_substrings(string const& s) {
    int n = s.size();

    const int p = 31;
    const int m = 1e9 + 9;
    vector<long long> p_pow(n);
    p_pow[0] = 1;
    for (int i = 1; i < n; i++)
        p_pow[i] = (p_pow[i-1] * p) % m;

    vector<long long> h(n + 1, 0);
    for (int i = 0; i < n; i++)
        h[i+1] = (h[i] + (s[i] - 'a' + 1) * p_pow[i]) % m;

    int cnt = 0;
    for (int l = 1; l <= n; l++) {
        set<long long> hs;
        for (int i = 0; i <= n - l; i++) {
            long long cur_h = (h[i + l] + m - h[i]) % m;
            cur_h = (cur_h * p_pow[n-i-1]) % m;
            hs.insert(cur_h);
        }
        cnt += hs.size();
    }
    return cnt;
}
```

5. Geometria

5.1. Punto

```
struct pto{
  double x, y;
  pto(double x=0, double y=0):x(x),y(y){}
  pto operator+(pto a){return pto(x+a.x, y+a.y);}
  pto operator-(pto a){return pto(x-a.x, y-a.y);}
  pto operator+(double a){return pto(x+a, y+a);}
  pto operator*(double a){return pto(x*a, y*a);}
```

```
  pto operator/(double a){return pto(x/a, y/a);}
  //dot product, producto interno:
  double operator*(pto a){return x*a.x+y*a.y;}
  //module of the cross product or vectorial product:
  //if a is less than 180 clockwise from b, a^b>0
  double operator^(pto a){return x*a.y-y*a.x;}
  //returns true if this is at the left side of line qr
  bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
  bool operator<(const pto &a) const{return x<a.x-EPS || (abs(x-a.x)<EPS && y<a.y-EPS);}
bool operator==(pto a){return abs(x-a.x)<EPS && abs(y-a.y)<EPS;}
  double norm(){return sqrt(x*x+y*y);}
  double norm_sq(){return x*x+y*y;}
};
double dist(pto a, pto b){return (b-a).norm();}
typedef pto vec;

double angle(pto a, pto o, pto b){
  pto oa=a-o, ob=b-o;
  return atan2(oa^ob, oa*ob);}

//rotate p by theta rads CCW w.r.t. origin (0,0)
pto rotate(pto p, double theta){
  return pto(p.x*cos(theta)-p.y*sin(theta),
      p.x*sin(theta)+p.y*cos(theta));
}
```

5.2. Orden radial de puntos

```
struct Cmp{//orden total de puntos alrededor de un punto r
  pto r;
  Cmp(pto r):r(r) {}
  int cuad(const pto &a) const{
    if(a.x > 0 && a.y >= 0)return 0;
    if(a.x <= 0 && a.y > 0)return 1;
    if(a.x < 0 && a.y <= 0)return 2;
    if(a.x >= 0 && a.y < 0)return 3;
    assert(a.x ==0 && a.y==0);
    return -1;
  }
  bool cmp(const pto&p1, const pto&p2)const{
    int c1 = cuad(p1), c2 = cuad(p2);
    if(c1==c2) return p1.y*p2.x<p1.x*p2.y;
        else return c1 < c2;
  }
    bool operator()(const pto&p1, const pto&p2) const{
    return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
    }
};
```

5.3. Line

```
int sgn(ll x){return x<0? -1 : !!x;}
struct line{
  line() {}
  double a,b,c;//Ax+By=C
//pto MUST store float coordinates!
  line(double a, double b, double c):a(a),b(b),c(c){}
  line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
  int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
};
bool parallels(line l1, line l2){return abs(l1.a*l2.b-l2.a*l1.b)<EPS;}
pto inter(line l1, line l2){//intersection
  double det=l1.a*l2.b-l2.a*l1.b;
  if(abs(det)<EPS) return pto(INF, INF);//parallels
  return pto(l2.b*l1.c-l1.b*l2.c, l1.a*l2.c-l2.a*l1.c)/det;
}
```

5.4. Segment

```
struct segm{
  pto s,f;
  segm(pto s, pto f):s(s), f(f) {}
  pto closest(pto p) {//use for dist to point
     double l2 = dist_sq(s, f);
     if(l2==0.) return s;
     double t =((p-s)*(f-s))/l2;
     if (t<0.) return s;//not write if is a line
     else if(t>1.)return f;//not write if is a line
     return s+((f-s)*t);
  }
    bool inside(pto p){return abs(dist(s, p)+dist(p, f)-dist(s, f))<EPS;}
};

pto inter(segm s1, segm s2){
  pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
    if(s1.inside(r) && s2.inside(r)) return r;
  return pto(INF, INF);
}
```

5.5. Polygon Area

```
double area(vector<pto> &p){//O(sz(p))
  double area=0;
  forn(i, sz(p)) area+=p[i]^p[(i+1)%sz(p)];
  //if points are in clockwise order then area is negative
  return abs(area)/2;
}
//Area ellipse = M_PI*a*b where a and b are the semi axis lengths
//Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
```

5.6. Circle

```
vec perp(vec v){return vec(-v.y, v.x);}
line bisector(pto x, pto y){
  line l=line(x, y); pto m=(x+y)/2;
  return line(-l.b, l.a, -l.b*m.x+l.a*m.y);
}
struct Circle{
  pto o;
  double r;
  Circle(pto x, pto y, pto z){
    o=inter(bisector(x, y), bisector(y, z));
    r=dist(o, x);
  }
  pair<pto, pto> ptosTang(pto p){
    pto m=(p+o)/2;
    tipo d=dist(o, m);
    tipo a=r*r/(2*d);
    tipo h=sqrt(r*r-a*a);
    pto m2=o+(m-o)*a/d;
    vec per=perp(m-o)/d;
    return make_pair(m2-per*h, m2+per*h);
  }
};
//finds the center of the circle containing p1 and p2 with radius r
//as there may be two solutions swap p1, p2 to get the other
bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
      double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
      if(det<0) return false;
      c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
      return true;
}
#define sqr(a) ((a)*(a))
#define feq(a,b) (fabs((a)-(b))<EPS)
pair<tipo, tipo> ecCuad(tipo a, tipo b, tipo c){
  //a*x*x+b*x+c=0
  tipo dx = sqrt(b*b-4.0*a*c);
  return make_pair((-b + dx)/(2.0*a),(-b - dx)/(2.0*a));
}
pair<pto, pto> interCL(Circle c, line l){
  bool sw=false;
  if((sw=feq(0,l.b))){
  swap(l.a, l.b);
  swap(c.o.x, c.o.y);
  }
  pair<tipo, tipo> rc = ecCuad(
  sqr(l.a)+sqr(l.b),
  2.0*l.a*l.b*c.o.y-2.0*(sqr(l.b)*c.o.x+l.c*l.a),
  sqr(l.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(l.c)-2.0*l.c*l.b*c.o.y
  );
  pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
        pto(rc.second, (l.c - l.a * rc.second) / l.b) );
  if(sw){
  swap(p.first.x, p.first.y);
  swap(p.second.x, p.second.y);
  }
  return p;
}
pair<pto, pto> interCC(Circle c1, Circle c2){
  line l;
  l.a = c1.o.x-c2.o.x;
  l.b = c1.o.y-c2.o.y;
  l.c = (sqr(c2.r)-sqr(c1.r)+sqr(c1.o.x)-sqr(c2.o.x)+sqr(c1.o.y)
  -sqr(c2.o.y))/2.0;
  return interCL(c1, l);
}
```

5.7. Point in Poly

```
//checks if v is inside of P, using ray casting
//works with convex and concave.
//excludes boundaries, handle it separately using segment.inside()
bool inPolygon(pto v, vector<pto>& P) {
  bool c = false;
  forn(i, sz(P)){
    int j=(i+1)%sz(P);
    if((P[j].y>v.y) != (P[i].y > v.y) &&
   (v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))
      c = !c;
  }
  return c;
}
```

5.8. Point in Convex Poly log(n)

```
void normalize(vector<pto> &pt){//delete collinear points first!
  //this makes it clockwise:
    if(pt[2].left(pt[0], pt[1])) reverse(pt.begin(), pt.end());
  int n=sz(pt), pi=0;
  forn(i, n)
    if(pt[i].x<pt[pi].x || (pt[i].x==pt[pi].x && pt[i].y<pt[pi].y))
      pi=i;
  vector<pto> shift(n);//puts pi as first point
    forn(i, n) shift[i]=pt[(pi+i)%n];
    pt.swap(shift);
}
bool inPolygon(pto p, const vector<pto> &pt){
  //call normalize first!
  if(p.left(pt[0], pt[1]) || p.left(pt[sz(pt)-1], pt[0])) return false;
  int a=1, b=sz(pt)-1;
  while(b-a>1){
    int c=(a+b)/2;
    if(!p.left(pt[0], pt[c])) a=c;
    else b=c;
  }
  return !p.left(pt[a], pt[a+1]);
}
```

5.9. Convex Check CHECK

```
bool isConvex(vector<int> &p){//O(N), delete collinear points!
  int N=sz(p);
  if(N<3) return false;
  bool isLeft=p[0].left(p[1], p[2]);
  forr(i, 1, N)
    if(p[i].left(p[(i+1)%N], p[(i+2)%N])!=isLeft)
      return false;
  return true; }
```

5.10. Convex Hull

```
//stores convex hull of P in S, CCW order
//left must return >=0 to delete collinear points!
void CH(vector<pto>& P, vector<pto> &S){
  S.clear();
  sort(P.begin(), P.end());//first x, then y
  forn(i, sz(P)){//lower hull
    while(sz(S)>= 2 && S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
    S.pb(P[i]);
  }
  S.pop_back();
  int k=sz(S);
  dforn(i, sz(P)){//upper hull
    while(sz(S) >= k+2 && S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
    S.pb(P[i]);
  }
  S.pop_back();
}
```

5.11. Cut Polygon

```
//cuts polygon Q along the line ab
//stores the left side (swap a, b for the right one) in P
void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
  P.clear();
  forn(i, sz(Q)){
    double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)%sz(Q)]-a);
    if(left1>=0) P.pb(Q[i]);
    if(left1*left2<0)
      P.pb(inter(line(Q[i], Q[(i+1)%sz(Q)]), line(a, b)));
  }
}
```

5.12. Bresenham

```
//plot a line approximation in a 2d map
void bresenham(pto a, pto b){
  pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
  pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
  int err=d.x-d.y;
  while(1){
    m[a.x][a.y]=1;//plot
    if(a==b) break;
    int e2=err;
    if(e2 >= 0) err-=2*d.y, a.x+=s.x;
    if(e2 <= 0) err+= 2*d.x, a.y+= s.y;
  }
}
```

5.13. Interseccion de Circulos en n3log(n)

```
struct event {
    double x; int t;
    event(double xx, int tt) : x(xx), t(tt) {}
    bool operator <(const event &o) const { return x < o.x; }
};
typedef vector<Circle> VC;
typedef vector<event> VE;
int n;
double cuenta(VE &v, double A,double B) {
    sort(v.begin(), v.end());
    double res = 0.0, lx = ((v.empty())?0.0:v[0].x);
    int contador = 0;
    forn(i,sz(v)) {
        //interseccion de todos (contador == n), union de todos (contador > 0)
        //conjunto de puntos cubierto por exacta k Circulos (contador == k)
        if (contador == n) res += v[i].x - lx;
        contador += v[i].t, lx = v[i].x;
    }
    return res;
}
// Primitiva de sqrt(r*r - x*x) como funcion double de una variable x.
inline double primitiva(double x,double r) {
    if (x >= r) return r*r*M_PI/4.0;
    if (x <= -r) return -r*r*M_PI/4.0;
    double raiz = sqrt(r*r-x*x);
    return 0.5 * (x * raiz + r*r*atan(x/raiz));
}
double interCircle(VC &v) {
    vector<double> p; p.reserve(v.size() * (v.size() + 2));
    forn(i,sz(v))  p.push_back(v[i].c.x + v[i].r), p.push_back(v[i].c.x - v[i].r);
    forn(i,sz(v)) forn(j,i) {
        Circle &a = v[i], b = v[j];
        double d = (a.c - b.c).norm();
        if (fabs(a.r - b.r) < d && d < a.r + b.r) {
            double alfa = acos((sqr(a.r) + sqr(d) - sqr(b.r)) / (2.0 * d * a.r));
            pto vec = (b.c - a.c) * (a.r / d);
            p.pb((a.c + rotate(vec, alfa)).x), p.pb((a.c + rotate(vec, -alfa)).x);
        }
    }
    sort(p.begin(), p.end());
```

```
    double res = 0.0;
    forn(i,sz(p)-1) {
        const double A = p[i], B = p[i+1];
        VE ve; ve.reserve(2 * v.size());
        forn(j,sz(v)) {
            const Circle &c = v[j];
            double arco = primitiva(B-c.c.x,c.r)
                - primitiva(A-c.c.x,c.r);
            double base = c.c.y * (B-A);
            ve.push_back(event(base + arco,-1));
            ve.push_back(event(base - arco, 1));
        }
        res += cuenta(ve,A,B);
    }
    return res;
}
```

6. Math

6.1. Identidades

$\sum_{i=0}^{n} i\binom{n}{i} = n * 2^{n-1}$
$\sum_{i=0}^{n} i(i-1) = \frac{8}{6}(\frac{n}{2})(\frac{n}{2}+1)(n+1)$ (doubles) → Sino ver caso impar y par
$\sum_{i=0}^{n} i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$
$\sum_{i=0}^{n} i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_k}{p-k+1}\binom{p}{k}(n+1)^{p-k+1}$
Caras + Vertices = Aristas + 2 (Poliedros convexos y Grafos planos)
Teorema de Pick: (Area, puntos interiores y puntos en el borde)
$A = I + \frac{B}{2} - 1$
$\left\{ {n+1 \atop k} \right\} = k\left\{ {n \atop k} \right\} + \left\{ {n \atop k-1} \right\}$ for $k > 0$ with initial conditions $\left\{ {0 \atop 0} \right\} = 1$ and $\left\{ {n \atop 0} \right\} = \left\{ {0 \atop n} \right\} = 0$ for $n > 0$. Same as $\frac{1}{k!}\sum_{j=0}^{k}(-1)^{k-j}\binom{k}{j}j^n$
$\left[{n+1 \atop k} \right] = n\left[{n \atop k} \right] + \left[{n \atop k-1} \right]$ for $k > 0$, with the initial conditions $\left[{0 \atop 0} \right] = 1$ and $\left[{n \atop 0} \right] = \left[{0 \atop n} \right] = 0$ for $n > 0$.

6.2. Ec. Caracteristica

$a_0T(n) + a_1T(n-1) + ... + a_kT(n-k) = 0$
$p(x) = a_0x^k + a_1x^{k-1} + ... + a_k$
Sean $r_1, r_2, ..., r_q$ las raíces distintas, de mult. $m_1, m_2, ..., m_q$
$T(n) = \sum_{i=1}^{q}\sum_{j=0}^{m_i-1} c_{ij}n^j r_i^n$
Las constantes c_{ij} se determinan por los casos base.

6.3. Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
  comb[i][0]=comb[i][i]=1;
  forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i
      -1][k-1])%MOD;
}
ll lucas (ll n, ll k, int p){ //Calcula (n,k)%p
    teniendo comb[p][p] precalculado.
  ll aux = 1;
  while (n + k) aux = (aux * comb[n%p][k%p]) %p,
      n/=p, k/=p;
  return aux;
}
```

6.4. Gauss Jordan, Determinante

```
// Gauss-Jordan elimination with full pivoting.
//
// Uses:
//   (1) solving systems of linear equations (AX=
    B)
//   (2) inverting matrices (AX=I)
//   (3) computing determinants of square
    matrices
//
// Running time: O(n^3)
//
// INPUT:    a[][] = an nxn matrix
//           b[][] = an nxm matrix
//
// OUTPUT:   X      = an nxm matrix (stored in b
    [][])
//           A^{-1} = an nxn matrix (stored in a
    [][])
//           returns determinant of a[][]

#include <iostream>
#include <vector>
#include <cmath>

using namespace std;

const double EPS = 1e-10;

typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;

T GaussJordan(VVT &a, VVT &b) {
  const int n = a.size();
  const int m = b[0].size();
  VI irow(n), icol(n), ipiv(n);
  T det = 1;

  for (int i = 0; i < n; i++) {
    int pj = -1, pk = -1;
    for (int j = 0; j < n; j++) if (!ipiv[j])
      for (int k = 0; k < n; k++) if (!ipiv[k])
  if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])
      ) { pj = j; pk = k; }
    if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix␣
        is␣singular." << endl; exit(0); }
    ipiv[pk]++;
    swap(a[pj], a[pk]);
    swap(b[pj], b[pk]);
    if (pj != pk) det *= -1;
    irow[i] = pj;
    icol[i] = pk;

    T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
```

```
    a[pk][pk] = 1.0;
    for (int p = 0; p < n; p++) a[pk][p] *= c;
    for (int p = 0; p < m; p++) b[pk][p] *= c;
    for (int p = 0; p < n; p++) if (p != pk) {
      c = a[p][pk];
      a[p][pk] = 0;
      for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
      for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
    }
  }

  for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
  }

  return det;
}

int main() {
  const int n = 4;
  const int m = 2;
  double A[n][n] = {{1,2,3,4},{1,0,1,0},{5,3,2,4},{6,1,4,6} };
  double B[n][m] = { {1,2},{4,3},{5,6},{8,7} };
  VVT a(n), b(n);
  for (int i = 0; i < n; i++) {
    a[i] = VT(A[i], A[i] + n);
    b[i] = VT(B[i], B[i] + m);
  }

  double det = GaussJordan(a, b);

  // expected: 60
  cout << "Determinant: " << det << endl;

  // expected: -0.233333 0.166667 0.133333 0.0666667
  //           0.166667 0.166667 0.333333 -0.333333
  //           0.233333 0.833333 -0.133333 -0.0666667
  //           0.05 -0.75 -0.1 0.2
  cout << "Inverse: " << endl;
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++)
      cout << a[i][j] << ' ';
    cout << endl;
  }

  // expected: 1.63333 1.3
  //           -0.166667 0.5
  //           2.36667 1.7
  //           -1.85 -1.35
  cout << "Solution: " << endl;
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++)
      cout << b[i][j] << ' ';
    cout << endl;
  }
}
```

6.5. Teorema Chino del Resto

```
// Chinese remainder theorem (special case): find z such that
// z % m1 = r1, z % m2 = r2.  Here, z is unique modulo M = lcm(m1, m2).
// Return (z, M).  On failure, M = -1.
PII chinese_remainder_theorem(int m1, int r1, int m2, int r2) {
  int s, t;
  int g = extended_euclid(m1, m2, s, t);
  if (r1%g != r2%g) return make_pair(0, -1);
  return make_pair(mod(s*r2*m1 + t*r1*m2, m1*m2) / g, m1*m2 / g);
}

// Chinese remainder theorem: find z such that
// z % m[i] = r[i] for all i.  Note that the solution is
// unique modulo M = lcm_i (m[i]).  Return (z, M).  On
// failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese_remainder_theorem(const VI &m, const VI &r) {
  PII ret = make_pair(r[0], m[0]);
  for (int i = 1; i < m.size(); i++) {
    ret = chinese_remainder_theorem(ret.second, ret.first, m[i], r[i]);
    if (ret.second == -1) break;
  }
  return ret;
}
```

6.6. Funciones de primos

Iterar mientras el $p^2 \leq N$. Revisar que N!=1, en este caso N es primo. **NumDiv**: Producto (exponentes+1). **SumDiv**: Product suma geom. factores. **EulerPhi** (coprimos): Inicia ans=N. Para cada primo divisor: ans-=ans/primo (una vez) y dividir luego N todo lo posible por p.

6.7. Phollard's Rho (rolando)

```
ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}

ll mulmod (ll a, ll b, ll c) { //returns (a*b)%c, and minimize overfloor
  ll x = 0, y = a%c;
  while (b > 0){
    if (b % 2 == 1) x = (x+y) % c;
    y = (y*2) % c;
    b /= 2;
  }
  return x % c;
```

```
}

ll expmod (ll b, ll e, ll m){//O(log b)
  if(!e) return 1;
  ll q= expmod(b,e/2,m); q=mulmod(q,q,m);
  return e%2? mulmod(b,q,m) : q;
}

bool es_primo_prob (ll n, int a)
{
  if (n == a) return true;
  ll s = 0,d = n-1;
  while (d % 2 == 0) s++,d/=2;

  ll x = expmod(a,d,n);
  if ((x == 1) || (x+1 == n)) return true;

  forn (i, s-1){
    x = mulmod(x, x, n);
    if (x == 1) return false;
    if (x+1 == n) return true;
  }
  return false;
}

bool rabin (ll n){ //devuelve true si n es primo
  if (n == 1) return false;
  const int ar[] = {2,3,5,7,11,13,17,19,23};
  forn (j,9)
    if (!es_primo_prob(n,ar[j]))
      return false;
  return true;
}

ll rho(ll n){
    if( (n & 1) == 0 ) return 2;
    ll x = 2 , y = 2 , d = 1;
    ll c = rand() % n + 1;
    while( d == 1 ){
        x = (mulmod( x , x , n ) + c)%n;
        y = (mulmod( y , y , n ) + c)%n;
        y = (mulmod( y , y , n ) + c)%n;
        if( x - y >= 0 ) d = gcd( x - y , n );
        else d = gcd( y - x , n );
    }
    return d==n? rho(n):d;
}

map<ll,ll> prim;
void factRho (ll n){ //O (lg n)^3. un solo numero
  if (n == 1) return;
  if (rabin(n)){
    prim[n]++;
    return;
  }
  ll factor = rho(n);
  factRho(factor);
  factRho(n/factor);
}
```

6.8. GCD

```
tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b
    ;}
```

6.9. Extended Euclid

```
void extendedEuclid (ll a, ll b){ //a * x + b * y
    = d
  if (!b) { x = 1; y = 0; d = a; return;}
  extendedEuclid (b, a%b);
  ll x1 = y;
  ll y1 = x - (a/b) * y;
  x = x1; y = y1;
}
```

6.10. Polinomio

```
        int m = sz(c), n = sz(o.c);
        vector<tipo> res(max(m,n));
        forn(i, m) res[i] += c[i];
        forn(i, n) res[i] += o.c[i];
        return poly(res);    }
    poly operator*(const tipo cons) const {
    vector<tipo> res(sz(c));
        forn(i, sz(c)) res[i]=c[i]*cons;
        return poly(res);    }
    poly operator*(const poly &o) const {
        int m = sz(c), n = sz(o.c);
        vector<tipo> res(m+n-1);
        forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[
            j];
        return poly(res);    }
  tipo eval(tipo v) {
    tipo sum = 0;
    dforn(i, sz(c)) sum=sum*v + c[i];
    return sum; }
    //poly contains only a vector<int> c (the
        coeficients)
  //the following function generates the roots of
      the polynomial
//it can be easily modified to return float roots
  set<tipo> roots(){
    set<tipo> roots;
    tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
    vector<tipo> ps,qs;
    forr(p,1,sqrt(a0)+1) if (a0%p==0) ps.pb(p),ps
        .pb(a0/p);
    forr(q,1,sqrt(an)+1) if (an%q==0) qs.pb(q),qs
        .pb(an/q);
    forall(pt,ps)
      forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
        tipo root = abs((*pt) / (*qt));
        if (eval(root)==0) roots.insert(root);
      }
    return roots; }
};
pair<poly,tipo> ruffini(const poly p, tipo r) {
  int n = sz(p.c) - 1 ;
  vector<tipo> b(n);
  b[n-1] = p.c[n];
```

```
  dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
  tipo resto = p.c[0] + r*b[0];
  poly result(b);
  return make_pair(result,resto);
}
poly interpolate(const vector<tipo>& x,const vector<tipo>& y) {
    poly A; A.c.pb(1);
    forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux; }
  poly S; S.c.pb(0);
  forn(i,sz(x)) { poly Li;
    Li = ruffini(A,x[i]).fst;
    Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the coefficients instead of 1.0 to avoid using double
    S = S + Li * y[i];  }
  return S;
}

int  main(){
  return 0;
}
```

6.11. FFT

```
//~ typedef complex<double> base; //menos codigo, pero mas lento
//elegir si usar complejos de c (lento) o estos
struct base{
    double r,i;
    base(double r=0, double i=0):r(r), i(i){}
    double real()const{return r;}
    void operator/=(const int c){r/=c, i/=c;}
};
base operator*(const base &a, const base &b){
    return base(a.r*b.r-a.i*b.i, a.r*b.i+a.i*b.r);}
base operator+(const base &a, const base &b){
    return base(a.r+b.r, a.i+b.i);}
base operator-(const base &a, const base &b){
    return base(a.r-b.r, a.i-b.i);}
vector<int> rev; vector<base> wlen_pw;
inline static void fft(base a[], int n, bool invert) {
    forn(i, n) if(i<rev[i]) swap(a[i], a[rev[i]]);
  for (int len=2; len<=n; len<<=1) {
    double ang = 2*M_PI/len * (invert?-1:+1);
    int len2 = len>>1;
    base wlen (cos(ang), sin(ang));
    wlen_pw[0] = base (1, 0);
        forr(i, 1, len2) wlen_pw[i] = wlen_pw[i-1] * wlen;
    for (int i=0; i<n; i+=len) {
      base t, *pu = a+i, *pv = a+i+len2,  *pu_end = a+i+len2, *pw = &wlen_pw[0];
      for (; pu!=pu_end; ++pu, ++pv, ++pw)
        t = *pv * *pw, *pv = *pu - t,*pu = *pu + t;
    }
  }
  if (invert) forn(i, n) a[i]/= n;}
inline static void calc_rev(int n){//precalculo: llamar antes de fft!!
    wlen_pw.resize(n), rev.resize(n);
    int lg=31-__builtin_clz(n);
    forn(i, n){
    rev[i] = 0;
        forn(k, lg) if(i&(1<<k)) rev[i]|=1<<(lg-1-k);
    }}
inline static void multiply(const vector<int> &a, const vector<int> &b, vector<int> &res) {
  vector<base> fa (a.begin(), a.end()),  fb (b.begin(), b.end());
    int n=1; while(n < max(sz(a), sz(b))) n <<= 1; n <<= 1;
    calc_rev(n);
  fa.resize (n),  fb.resize (n);
  fft (&fa[0], n, false),  fft (&fb[0], n, false);
  forn(i, n) fa[i] = fa[i] * fb[i];
  fft (&fa[0], n, true);
  res.resize(n);
    forn(i, n) res[i] = int (fa[i].real() + 0.5);
}
void toPoly(const string &s, vector<int> &P){// convierte un numero a polinomio
    P.clear();
    dforn(i, sz(s)) P.pb(s[i]-'0');}
```

7. Grafos

7.1. Bellman-Ford

```
vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
int dist[MAX_N];
void bford(int src){//O(VE)
  dist[src]=0;
  forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
    dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
}

bool hasNegCycle(){
  forn(j, N) if(dist[j]!=INF) forall(it, G[j])
    if(dist[it->snd]>dist[j]+it->fst) return true;
  //inside if: all points reachable from it->snd will have -INF distance(do bfs)
  return false;
}
```

7.2. 2-SAT + Tarjan SCC

```
//We have a vertex representing a var and other for his negation.
```

```
//Every edge stored in G represents an
    implication. To add an equation of the form a
    ||b, use addor(a, b)
//MAX=max cant var, n=cant var
#define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].
    pb(a))
vector<int> G[MAX*2];
//idx[i]=index assigned in the dfs
//lw[i]=lowest index(closer from the root)
    reachable from i
int lw[MAX*2], idx[MAX*2], qidx;
stack<int> q;
int qcmp, cmp[MAX*2];
//verdad[cmp[i]]=valor de la variable i
bool verdad[MAX*2+1];

int neg(int x) { return x>=n? x-n : x+n;}
void tjn(int v){
  lw[v]=idx[v]=++qidx;
  q.push(v), cmp[v]=-2;
  forall(it, G[v]){
    if(!idx[*it] || cmp[*it]==-2){
      if(!idx[*it]) tjn(*it);
      lw[v]=min(lw[v], lw[*it]);
    }
  }
  if(lw[v]==idx[v]){
    int x;
    do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=
        v);
    verdad[qcmp]=(cmp[neg(v)]<0);
    qcmp++;
  }
}
//remember to CLEAR G!!!
bool satisf(){//O(n)
  memset(idx, 0, sizeof(idx)), qidx=0;
  memset(cmp, -1, sizeof(cmp)), qcmp=0;
  forn(i, n){
    if(!idx[i]) tjn(i);
    if(!idx[neg(i)]) tjn(neg(i));
  }
  forn(i, n) if(cmp[i]==cmp[neg(i)]) return false
      ;
  return true;
}
```

7.3. Puentes y Articulation Points

```
int dfsNumberCounter, dfsRoot, rootChildren;
vi dfs_num, dfs_low, dfs_parent,
    articulation_vertex;

void articulationPointAndBridge(int u) {
  dfs_low[u] = dfs_num[u] = dfsNumberCounter++;
  for (int j = 0; j < (int)AdjList[u].size(); j
      ++) {
    ii v = AdjList[u][j];
    if (dfs_num[v.first] == -1) {
      dfs_parent[v.first] = u;
      if (u == dfsRoot) rootChildren++;
      articulationPointAndBridge(v.first);
      if (dfs_low[v.first] >= dfs_num[u])
        articulation_vertex[u] = true;
      if (dfs_low[v.first] > dfs_num[u])
        printf("␣Edge␣(%d,␣%d)␣is␣a␣bridge\n", u,
            v.first);
      dfs_low[u] = min(dfs_low[u], dfs_low[v.
          first]);
    }
    else if (v.first != dfs_parent[u])
      dfs_low[u] = min(dfs_low[u], dfs_num[v.
          first]);
} }
  // At main
  dfsNumberCounter = 0; dfs_num.assign(V, -1);
      dfs_low.assign(V, 0);
  dfs_parent.assign(V, -1); articulation_vertex.
      assign(V, 0);
  printf("Bridges:\n");
  for (int i = 0; i < V; i++)
    if (dfs_num[i] == -1) {
      dfsRoot = i; rootChildren = 0;
      articulationPointAndBridge(i);
      articulation_vertex[dfsRoot] = (
          rootChildren > 1); }
  printf("Articulation␣Points:\n");
  for (int i = 0; i < V; i++)
    if (articulation_vertex[i])
      printf("␣Vertex␣%d\n", i);
```

7.4. LCA + Climb

```
const int MAXN=100001;
const int LOGN=20;
//f[v][k] holds the 2^k father of v
//L[v] holds the level of v
int N, f[MAXN][LOGN], L[MAXN];
//call before build:
void dfs(int v, int fa=-1, int lvl=0){//generate
    required data
  f[v][0]=fa, L[v]=lvl;
  forall(it, G[v])if(*it!=fa) dfs(*it, v, lvl+1);
       }
void build(){//f[i][0] must be filled previously,
     O(nlgn)
  forn(k, LOGN-1) forn(i, N) f[i][k+1]=f[f[i][k
      ]][k];}
#define lg(x) (31-__builtin_clz(x))//=floor(log2(
    x))
int climb(int a, int d){//O(lgn)
  if(!d) return a;
  dforn(i, lg(L[a])+1) if(1<<i<=d) a=f[a][i], d
      -=1<<i;
    return a;}
int lca(int a, int b){//O(lgn)
  if(L[a]<L[b]) swap(a, b);
  a=climb(a, L[a]-L[b]);
  if(a==b) return a;
  dforn(i, lg(L[a])+1) if(f[a][i]!=f[b][i]) a=f[a
```

```
      ][i], b=f[b][i];
  return f[a][0]; }
int dist(int a, int b) {//returns distance between nodes
  return L[a]+L[b]-2*L[lca(a, b)];}
```

7.5. Heavy Light Decomposition

```
int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
int dad[MAXN];//dad[v]=padre del nodo v
void dfs1(int v, int p=-1){//pre-dfs
  dad[v]=p;
  treesz[v]=1;
  forall(it, G[v]) if(*it!=p){
    dfs1(*it, v);
    treesz[v]+=treesz[*it];
  }
}
//PONER Q EN 0  !!!!!
int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
//Las cadenas aparecen continuas en el recorrido!
int cantcad;
int homecad[MAXN];//dada una cadena devuelve su nodo inicial
int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
void heavylight(int v, int cur=-1){
  if(cur==-1) homecad[cur=cantcad++]=v;
  pos[v]=q++;
  cad[v]=cur;
  int mx=-1;
  forn(i, sz(G[v])) if(G[v][i]!=dad[v])
    if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;
  if(mx!=-1) heavylight(G[v][mx], cur);
  forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
    heavylight(G[v][i], -1);
}
//ejemplo de obtener el maximo numero en el camino entre dos nodos
//RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
//esta funcion va trepando por las cadenas
int query(int an, int v){//O(logn)
  //si estan en la misma cadena:
  if(cad[an]==cad[v]) return rmq.get(pos[an], pos[v]+1);
  return max(query(an, dad[homecad[cad[v]]]),
         rmq.get(pos[homecad[cad[v]]], pos[v]+1));
}
```

7.6. Centroid Decomposition

```
int n;
vector<int> G[MAXN];
bool taken[MAXN];//poner todos en FALSE al principio!!
int padre[MAXN];//padre de cada nodo en el centroid tree

int szt[MAXN];
void calcsz(int v, int p) {
  szt[v] = 1;
  forall(it,G[v]) if (*it!=p && !taken[*it])
    calcsz(*it,v), szt[v]+=szt[*it];
}
void centroid(int v=0, int f=-1, int lvl=0, int tam=-1) {//O(nlogn)
  if(tam==-1) calcsz(v, -1), tam=szt[v];
  forall(it, G[v]) if(!taken[*it] && szt[*it]>=tam/2)
    {szt[v]=0; centroid(*it, f, lvl, tam); return;}
  taken[v]=true;
  padre[v]=f;
  forall(it, G[v]) if(!taken[*it])
    centroid(*it, v, lvl+1, -1);
}
```

7.7. Euler Cycle

```
int n,m,ars[MAXE], eq;
vector<int> G[MAXN];//fill G,n,m,ars,eq
list<int> path;
int used[MAXN];
bool usede[MAXE];
queue<list<int>::iterator> q;
int get(int v){
  while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;
  return used[v];
}
void explore(int v, int r, list<int>::iterator it ){
  int ar=G[v][get(v)]; int u=v^ars[ar];
  usede[ar]=true;
  list<int>::iterator it2=path.insert(it, u);
  if(u!=r) explore(u, r, it2);
  if(get(v)<sz(G[v])) q.push(it);
}
void euler(){
  zero(used), zero(usede);
  path.clear();
  q=queue<list<int>::iterator>();
  path.push_back(0); q.push(path.begin());
  while(sz(q)){
    list<int>::iterator it=q.front(); q.pop();
    if(used[*it]<sz(G[*it])) explore(*it, *it, it);
  }
  reverse(path.begin(), path.end());
}
void addEdge(int u, int v){
  G[u].pb(eq), G[v].pb(eq);
  ars[eq++]=u^v;
}
```

7.8. Chu-liu

```
void visit(graph &h, int v, int s, int r,
  vector<int> &no, vector< vector<int> > &comp,
  vector<int> &prev, vector< vector<int> > &next,
       vector<weight> &mcost,
  vector<int> &mark, weight &cost, bool &found) {
  if (mark[v]) {
    vector<int> temp = no;
    found = true;
    do {
      cost += mcost[v];
      v = prev[v];
      if (v != s) {
        while (comp[v].size() > 0) {
          no[comp[v].back()] = s;
          comp[s].push_back(comp[v].back());
          comp[v].pop_back();
        }
      }
    } while (v != s);
    forall(j,comp[s]) if (*j != r) forall(e,h[*j
        ])
      if (no[e->src] != s) e->w -= mcost[ temp[*j
          ] ];
  }
  mark[v] = true;
  forall(i,next[v]) if (no[*i] != no[v] && prev[
      no[*i]] == v)
    if (!mark[no[*i]] || *i == s)
      visit(h, *i, s, r, no, comp, prev, next,
          mcost, mark, cost, found);
}
weight minimumSpanningArborescence(const graph &g
    , int r) {
    const int n=sz(g);
  graph h(n);
  forn(u,n) forall(e,g[u]) h[e->dst].pb(*e);
  vector<int> no(n);
  vector<vector<int> > comp(n);
  forn(u, n) comp[u].pb(no[u] = u);
  for (weight cost = 0; ;) {
    vector<int> prev(n, -1);
    vector<weight> mcost(n, INF);
    forn(j,n) if (j != r) forall(e,h[j])
      if (no[e->src] != no[j])
        if (e->w < mcost[ no[j] ])
          mcost[ no[j] ] = e->w, prev[ no[j] ] =
              no[e->src];
    vector< vector<int> > next(n);
    forn(u,n) if (prev[u] >= 0)
      next[ prev[u] ].push_back(u);
    bool stop = true;
    vector<int> mark(n);
    forn(u,n) if (u != r && !mark[u] && !comp[u].
        empty()) {
      bool found = false;
      visit(h, u, u, r, no, comp, prev, next,
          mcost, mark, cost, found);
      if (found) stop = false;
    }
    if (stop) {
      forn(u,n) if (prev[u] >= 0) cost += mcost[u
          ];
      return cost;
    }
  }
}
```

7.9. Hungarian

```
//Dado un grafo bipartito completo con costos no
    negativos, encuentra el matching perfecto de
    minimo costo.
tipo cost[N][N], lx[N], ly[N], slack[N]; //llenar
    : cost=matriz de adyacencia
int n, max_match, xy[N], yx[N], slackx[N],prev2[N
    ];//n=cantidad de nodos
bool S[N], T[N]; //sets S and T in algorithm
void add_to_tree(int x, int prevx) {
  S[x] = true, prev2[x] = prevx;
  forn(y, n) if (lx[x] + ly[y] - cost[x][y] <
      slack[y] - EPS)
    slack[y] = lx[x] + ly[y] - cost[x][y], slackx
        [y] = x;
}
void update_labels(){
  tipo delta = INF;
  forn (y, n) if (!T[y]) delta = min(delta, slack
      [y]);
  forn (x, n) if (S[x]) lx[x] -= delta;
  forn (y, n) if (T[y]) ly[y] += delta; else
      slack[y] -= delta;
}
void init_labels(){
  zero(lx), zero(ly);
  forn (x,n) forn(y,n) lx[x] = max(lx[x], cost[x
      ][y]);
}
void augment() {
  if (max_match == n) return;
  int x, y, root, q[N], wr = 0, rd = 0;
  memset(S, false, sizeof(S)), memset(T, false,
      sizeof(T));
  memset(prev2, -1, sizeof(prev2));
  forn (x, n) if (xy[x] == -1){
    q[wr++] = root = x, prev2[x] = -2;
    S[x] = true; break; }
  forn (y, n) slack[y] = lx[root] + ly[y] - cost[
      root][y], slackx[y] = root;
  while (true){
    while (rd < wr){
      x = q[rd++];
      for (y = 0; y < n; y++) if (cost[x][y] ==
          lx[x] + ly[y] && !T[y]){
        if (yx[y] == -1) break; T[y] = true;
        q[wr++] = yx[y], add_to_tree(yx[y], x); }
      if (y < n) break; }
    if (y < n) break;
    update_labels(), wr = rd = 0;
```

```
    for (y = 0; y < n; y++) if (!T[y] && slack[y]
         == 0){
      if (yx[y] == -1){x = slackx[y]; break;}
      else{
        T[y] = true;
        if (!S[yx[y]]) q[wr++] = yx[y],
            add_to_tree(yx[y], slackx[y]);
      }}
    if (y < n) break; }
  if (y < n){
    max_match++;
    for (int cx = x, cy = y, ty; cx != -2; cx =
        prev2[cx], cy = ty)
      ty = xy[cx], yx[cy] = cx, xy[cx] = cy;
    augment(); }
}
tipo hungarian(){
  tipo ret = 0; max_match = 0, memset(xy, -1,
      sizeof(xy));
  memset(yx, -1, sizeof(yx)), init_labels(),
      augment(); //steps 1-3
  forn (x,n) ret += cost[x][xy[x]]; return ret;
}
```

7.10. Dynamic Conectivity

```
struct UnionFind {
    int n, comp;
    vector<int> pre,si,c;
    UnionFind(int n=0):n(n), comp(n), pre(n), si(
        n, 1) {
        forn(i,n) pre[i] = i; }
    int find(int u){return u==pre[u]?u:find(pre[u
        ]);}
    bool merge(int u, int v) {
        if((u=find(u))==(v=find(v))) return false
            ;
        if(si[u]<si[v]) swap(u, v);
        si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
        return true;
    }
    int snap(){return sz(c);}
    void rollback(int snap){
        while(sz(c)>snap){
            int v = c.back(); c.pop_back();
            si[pre[v]] -= si[v], pre[v] = v, comp
                ++;
        }
    }
};
enum {ADD,DEL,QUERY};
struct Query {int type,u,v;};
struct DynCon {
    vector<Query> q;
    UnionFind dsu;
    vector<int> match,res;
    map<ii,int> last;//se puede no usar cuando
        hay identificador para cada arista (
        mejora poco)
    DynCon(int n=0):dsu(n){}
    void add(int u, int v) {
        if(u>v) swap(u,v);
        q.pb((Query){ADD, u, v}), match.pb(-1);
        last[ii(u,v)] = sz(q)-1;
    }
    void remove(int u, int v) {
        if(u>v) swap(u,v);
        q.pb((Query){DEL, u, v});
        int prev = last[ii(u,v)];
        match[prev] = sz(q)-1;
        match.pb(prev);
    }
    void query() {//podria pasarle un puntero
        donde guardar la respuesta
        q.pb((Query){QUERY, -1, -1}), match.pb
            (-1);}
    void process() {
        forn(i,sz(q)) if (q[i].type == ADD &&
            match[i] == -1) match[i] = sz(q);
        go(0,sz(q));
    }
    void go(int l, int r) {
        if(l+1==r){
            if (q[l].type == QUERY)//Aqui
                responder la query usando el dsu!
                res.pb(dsu.comp);//aqui query=
                    cantidad de componentes
                    conexas
            return;
        }
        int s=dsu.snap(), m = (l+r) / 2;
        forr(i,m,r) if(match[i]!=-1 && match[i]<l
            ) dsu.merge(q[i].u, q[i].v);
        go(l,m);
        dsu.rollback(s);
        s = dsu.snap();
        forr(i,l,m) if(match[i]!=-1 && match[i]>=
            r) dsu.merge(q[i].u, q[i].v);
        go(m,r);
        dsu.rollback(s);
    }
}dc;
```

8. Network Flow

8.1. Dinic

```

const int MAX = 300;
// Corte minimo: vertices con dist[v]>=0 (del
    lado de src) VS.  dist[v]==-1 (del lado del
    dst)
// Para el caso de la red de Bipartite Matching (
    Sean V1 y V2 los conjuntos mas proximos a src
     y dst respectivamente):
// Reconstruir matching: para todo v1 en V1 ver
    las aristas a vertices de V2 con it->f>0, es
    arista del Matching
// Min Vertex Cover: vertices de V1 con dist[v
    ]==-1 + vertices de V2 con dist[v]>0
```

```
// Max Independent Set: tomar los vertices NO tomados por el Min Vertex Cover
// Max Clique: construir la red de G complemento (debe ser bipartito!) y encontrar un Max Independet Set
// Min Edge Cover: tomar las aristas del matching + para todo vertices no cubierto hasta el momento, tomar cualquier arista de el
int nodes, src, dst;
int dist[MAX], q[MAX], work[MAX];
struct Edge {
    int to, rev;
    ll f, cap;
    Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap) {}
};
vector<Edge> G[MAX];
void addEdge(int s, int t, ll cap){
    G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0, 0));}
bool dinic_bfs(){
    fill(dist, dist+nodes, -1), dist[src]=0;
    int qt=0; q[qt++]=src;
    for(int qh=0; qh<qt; qh++){
        int u =q[qh];
        forall(e, G[u]){
            int v=e->to;
            if(dist[v]<0 && e->f < e->cap)
                dist[v]=dist[u]+1, q[qt++]=v;
        }
    }
    return dist[dst]>=0;
}
ll dinic_dfs(int u, ll f){
    if(u==dst) return f;
    for(int &i=work[u]; i<sz(G[u]); i++){
        Edge &e = G[u][i];
        if(e.cap<=e.f) continue;
        int v=e.to;
        if(dist[v]==dist[u]+1){
                ll df=dinic_dfs(v, min(f, e.cap-e.f));
                if(df>0){
                        e.f+=df, G[v][e.rev].f-=df;
                        return df;  }
        }
    }
    return 0;
}
ll maxFlow(int _src, int _dst){
    src=_src, dst=_dst;
    ll result=0;
    while(dinic_bfs()){
        fill(work, work+nodes, 0);
        while(ll delta=dinic_dfs(src,INF))
            result+=delta;
    }
    // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1 forman el min-cut
    return result; }
```

8.2. Edmonds Karp's

```
#define MAX_V 1000
#define INF 1e9
//special nodes
#define SRC 0
#define SNK 1
map<int, int> G[MAX_V];//limpiar esto
//To add an edge use
#define add(a, b, w) G[a][b]=w
int f, p[MAX_V];
void augment(int v, int minE){
  if(v==SRC) f=minE;
  else if(p[v]!=-1){
    augment(p[v], min(minE, G[p[v]][v]));
    G[p[v]][v]-=f, G[v][p[v]]+=f;
  }
}
ll maxflow(){//O(VE^2)
  ll Mf=0;
  do{
    f=0;
    char used[MAX_V]; queue<int> q; q.push(SRC);
    zero(used), memset(p, -1, sizeof(p));
    while(sz(q)){
      int u=q.front(); q.pop();
      if(u==SNK) break;
      forall(it, G[u])
        if(it->snd>0 && !used[it->fst])
          used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
    }
    augment(SNK, INF);
    Mf+=f;
  }while(f);
  return Mf;
}
```

8.3. Max Matching

```
int LEFT, r[MAXV]; bool seen[MAXV]; VI AdjList[MAXV];
bool can_match(int u) {
    for (auto & v : AdjList[u]) {
        if (!seen[v]) {
            seen[v] = true;
            if (r[v] < 0 || can_match(r[v])) {
                r[v] = u; return true;
            }
        }
    } return false;
}
int max_matching() {
    memset(r, -1, sizeof r);
    int ans = 0;
    for (int u=0 ; u<LEFT ; u++) {
        memset(seen, 0, sizeof seen);
        if (can_match(u)) ans++;
    } return ans;
```

```
}
```

8.4. Min-cost Max-flow

```
const int MAXN=10000;
typedef ll tf;
typedef ll tc;
const tf INFFLUJO = 1e14;
const tc INFCOSTO = 1e14;
struct edge {
  int u, v;
  tf cap, flow;
  tc cost;
  tf rem() { return cap - flow; }
};
int nodes; //numero de nodos
vector<int> G[MAXN]; // limpiar!
vector<edge> e;  // limpiar!
void addEdge(int u, int v, tf cap, tc cost) {
  G[u].pb(sz(e)); e.pb((edge){u,v,cap,0,cost});
  G[v].pb(sz(e)); e.pb((edge){v,u,0,0,-cost});
}
tc dist[MAXN], mnCost;
int pre[MAXN];
tf cap[MAXN], mxFlow;
bool in_queue[MAXN];
void flow(int s, int t) {
  zero(in_queue);
  mxFlow=mnCost=0;
  while(1){
    fill(dist, dist+nodes, INFCOSTO); dist[s] =
        0;
    memset(pre, -1, sizeof(pre)); pre[s]=0;
    zero(cap); cap[s] = INFFLUJO;
    queue<int> q; q.push(s); in_queue[s]=1;
    while(sz(q)){
      int u=q.front(); q.pop(); in_queue[u]=0;
      for(auto it:G[u]) {
        edge &E = e[it];
        if(E.rem() && dist[E.v] > dist[u] + E.
            cost + 1e-9){ // ojo EPS
          dist[E.v]=dist[u]+E.cost;
          pre[E.v] = it;
          cap[E.v] = min(cap[u], E.rem());
          if(!in_queue[E.v]) q.push(E.v),
              in_queue[E.v]=1;
        }
      }
    }
    if (pre[t] == -1) break;
    mxFlow +=cap[t];
    mnCost +=cap[t]*dist[t];
    for (int v = t; v != s; v = e[pre[v]].u) {
      e[pre[v]].flow += cap[t];
      e[pre[v]^1].flow -= cap[t];
    }
  }
}
```

9. Template y Otros

Template

```
//touch {a..m}.in; tee {a..m}.cpp < template.cpp
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i=(a); i<(b); i++)
#define forn(i,n) forr(i,0,n)
#define sz(c) ((int)c.size())
#define zero(v) memset(v, 0, sizeof(v))
#define forall(it,v) for(auto it=v.begin();it!=v.
    end();++it)
#define pb push_back
#define fst first
#define snd second
typedef long long ll;
typedef pair<int,int> ii;
#define dforn(i,n) for(int i=n-1; i>=0; i--)
#define dprint(v) cout << #v"=" << v << endl //;)

const int MAXN=100100;
int n;

int main() {
    freopen("input.in", "r", stdin);
    ios::sync_with_stdio(0);
    while(cin >> n){

    }
    return 0;
}
```

Rellenar con espacios(para justificar)

```
#include <iomanip>
cout << setfill('␣') << setw(3) << 2 << endl;
```

Aleatorios

```
#define RAND(a, b) (rand()%(b-a+1)+a)
srand(time(NULL));
```

Doubles Comp.

```
const double EPS = 1e-9;
x == y  <=> fabs(x-y) < EPS, x >  y <=> x > y +
    EPS
x >= y  <=> x > y - EPS
```

Expandir pila

```
#include <sys/resource.h>
rlimit rl;
getrlimit(RLIMIT_STACK, &rl);
rl.rlim_cur=1024L*1024L*256L;//256mb
setrlimit(RLIMIT_STACK, &rl);
```

Iterar subconjunto

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```

Split

```
vector<string> split(string str,string sep){
    char* cstr=const_cast<char*>(str.c_str());
    char* current;
    vector<string> arr;
    current=strtok(cstr,sep.c_str());
    while(current!=NULL){
        arr.push_back(current);
        current=strtok(NULL,sep.c_str());
    }
    return arr;
}
```