

The Virtual Laboratory

CPFG Reference Manual

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Contents

1	Intr	oduction	3
	1.1	Installation	3
	1.2	Running $cpfg$	3
		1.2.1 Command line options	3
		1.2.2 Optional files	4
			5
	1.3	User Interface	5
			5
		•	5
		1.3.3 Animation menu	7
_	m.		_
2	2.1	L-system file Axiom statement	8
		Variables	
	2.2	2.2.1 Local vs. global variables	
		2.2.2 Arrays	
		2.2.2 Allays	0
3	Pro	ductions 10	
	3.1	The predecessor	0
		3.1.1 Ring L-systems	0
	3.2	Programming statements	0
4	Con	trol statements 1:	ำ
4	4.1	Start and End blocks	
	4.1	Ignore and Consider statements	
	4.3	Homomorphism	
	4.5	4.3.1 Recursive homomorphism	
		4.3.2 Context in homomorphism productions	
		4.3.3 Random numbers in homomorphism	
	4.4	Decomposition	
	4.5	Stochastic L-systems	
	4.0	Stochastic L-systems	-1
5		defined Functions 15	
	5.1	Mathematical functions	
	5.2	Rounding functions	
	5.3	Random number functions	
	5.4	Input and output functions	
	5.5	User-defined contours and functions	6
	5.6	Other functions	6
6	Pre	defined modules 1'	7
•	6.1	Position and drawing	
	6.2	Turtle rotations	
	6.3	Changing turtle parameters	
	6.4	Branching structures	
	6.5	Polygons	
	6.6	Circles and spheres	
	6.7	Surfaces and generalized cylinders	_
	0.7	6.7.1 Surface files	
		6.7.2 Laystom defined surfaces	

	6.8 6.9	6.7.3 Generalized cylinders 2 6.7.4 Textures 2 Tropisms 2 Query and communication 2 Labels 2	22 22 22
7		anced topics 2	24
	7.1 7.2	Mouse interaction 2 Sub-L-systems 2	
8	<i>cpfg</i> 8.1	View file 2 8.1.1 Turtle commands 2 8.1.2 Setting the view 2 8.1.3 Lights 2 8.1.4 Rendering 2 8.1.5 Lines, contours, and surfaces 2 8.1.6 User-defined functions 3 8.1.7 Textures 3 8.1.8 Tropisms and torque 3 8.1.9 Fonts 3 8.1.10 Deprecated view commands 3	26 27 28 29 30 31 32 32
	8.2 8.3	Background file 3 8.3.1 Primitives 3 8.3.2 Materials 3 8.3.3 Transformations 3 8.3.4 Lighting and projection 3 8.3.5 Example of a background file 3	33 34 35 35 36 36
9	App 9.1 9.2 9.3 9.4 9.5	Command line arguments	38 38 38 38 39
10	\mathbf{Cre}	its 4	10
11	Doc	ment revision history	ın

1 Introduction

cpfg is a program for modeling plants and visualizing their development using the formalism of L-systems, as well as other applications such as the generation of fractals. It is assumed that the user (and reader of this documentation) is familiar with the concepts of L-systems and turtle interpretation presented in *The Algorithmic Beauty of Plants* [1], as well as elements of the C programming language.

1.1 Installation

cpfq is distributed with vlab. Refer to the vlab documentation for installation instructions.

1.2 Running cpfg

The cpfg command line is defined as:

Note that the options can be listed in any order, but the L-system, view, and animation files must be specified in order at the end of the command line. The L-system and view files are mandatory. For example, the following command line sets the size of the drawing window and its title, and specifies a colormap file:

cpfg -w 600 400 -wt Daisy -m daisy.map daisy.l daisy.v

1.2.1 Command line options

Parameter	Description
-a	Start <i>cpfg</i> in animation mode with the Animation menu (Section 1.3.3), rather than with the main menu. If <i>animationfile</i> is specified, it will be used to control the animation. Otherwise default values will be used (Section 8.2).
-d	Set program output to debug mode. Information is sent to <i>stdout</i> . This mode is intended only for code development. See -v and -V for warning and verbose modes.
-g	Perform off-screen rendering. A colormap or material file must be specified (using -m or -M). cpfg will generate the string up to the last derivation step as defined in Lsystemfile. The results can be stored in a specified output file (Section 1.2.2).
-homo	Output the string after applying homomorphisms (Section 4.3), using a specified output file (Section 1.2.2).
-rmode $mode$	Set the method for re-reading input files. The values of <i>mode</i> are: expl = explicit cont = continuous trig = triggered Refresh mode may also be set with the Refresh mode menu item (Section 1.3.2), and within a <i>vlab</i> object's specification file (see the <i>Vlab Framework</i> manual). If not set, the default is explicit.
-v	Set program output to warning mode. Warning and error messages (significantly less than $-V$ mode) are sent to $stdout$.
-V	Set program output to verbose mode. Detailed warning and error messages are sent to <i>stdout</i> .

Parameter	Description	
-w xsize ysize	Set the size of the drawing window, in pixels. For example, -w 1024 683 will open	
	a window suitable for saving image files with an aspect ratio of 3:2, appropriate for	
	video recordings.	
-wnb Open the drawing window without borders or title bar.		
-wp xpos ypos	Specify the initial position of the top left corner of the window.	
-wpr $x y$	Specify the window position of the top left corner of the drawing window relative	
	to the top left corner of the screen. The numbers x and y may be between 0 and 1	
	denoting a fraction of the screen size, or between 1 and 100 representing a percentage.	
$-\mathtt{wr}\ w\ h$	Set the relative width and height of the drawing window with respect to the screen.	
	The numbers w and h may be between 0 and 1 denoting a fraction of the screen size,	
	or between 1 and 100 representing a percentage.	
-wt wintitle	Change the title of the window to wintitle.	

1.2.2 Optional files

The following input files are optional:

Parameter	Description		
-e filename	Input parameters for environment communication. Also sets environment		
	mode for communicating with an external program. See the <i>vlab</i> Environ-		
	mental Programs manual for more information on environmental processes.		
-m filename.map	Input a colormap from a .map file. See the colormap editor (palette) in the		
$-mn\ filename.map$	vlab Tools manual to interactively create a colormap file. Use $-mn$ to specify		
	more than one colormap file. The first file (-m1) will contain color indices		
	0-255, the second file (-m2) color indices 256-511, etc.		
extstyle ext	Input material records from a .mat file. Used instead of a colormap to im-		
	prove the results of shading calculations. See the Materials editor (medit) in		
	the <i>vlab</i> Tools manual to interactively create a materials file.		

One of the following file specifications should be used in batch mode (-g) and for output from animate mode (-a):

Parameter	Description
-gls filename.gls	In batch mode (-g), output the final result to the specified file.
-ps $filename.$ ps	In animate mode (-a), or Animate on the pop-up menu, output each
-ray filename.ray	frame as it is generated with the Step and/or Run menu items (Section
-str filename.str	1.3.3). The <i>filename</i> will be appended with the frame number, beginning
-strb filename.strb	with 000.
-vv filename.vv	Results can also be output interactively using the Save as and String >
	Output menu items (Section 1.3.2), as well as the Start recording menu
	item in animate mode (Section 1.3.3).

For rayshade output (-ray), the projection type must be set to perspective using the view file command projection (Section 8.1.2).

1.2.3 Main files

The following files are identified by their position at the end of the command line. The standard convention for each file extension is used here. They must be in this order:

Parameter	Description
$Lsystemfile. \mathtt{l}$	The file containing a <i>cpfg</i> model. This file is mandatory.
$view file$. $ extsf{v}$	The view parameters (Section 8.1). This file is mandatory, although there are default values for many of the parameters.
animationfile.a	The animation parameters (Section 8.2). This file is optional; default values will be used.

1.3 User Interface

1.3.1 View manipulation

The view in the drawing window is manipulated using the left and middle mouse buttons and the SHIFT key.

Action	Description
Rotate	Hold the left mouse button down. Rotate around the Y axis by moving the mouse
	horizontally, and around the X axis by moving the mouse vertically.
Pan	Hold the SHIFT key and left mouse button down. Move the mouse to pan in that
	direction.
Zoom	Hold the middle mouse button down. Zoom in by moving the mouse up, and zoom out
	by moving down.
Roll	Hold the SHIFT key and middle mouse button down. Roll clockwise around the Z axis
	by moving the mouse to the right, and roll counter-clockwise by moving the mouse to
	the left.

1.3.2 Main menu

A pop-up menu is displayed by clicking the right mouse button.

Menu item	Description		
New model	Reread the L-system and view files, generate a new string, and interpret it to create a new image. The model is automatically centered in the window, or placed according to the commands in the view file (Section 8.1).		
New L-system	Reread the L-system file, generate a new string and interpret it to create a new image without modifying the view.		
New view	Reread the view file and re-interpret the existing string to create a new image. The model is automatically centered in the window, or placed according to the commands in the file.		
New rendering	Reread the view file and update the image using the rendering commands in the file, but without changing the view (i.e. do not change the scale, camera, rotation, etc.).		
Save	Save to the default file name and type. The initial file name is the same as the original L-system file, with a PNG extension. Use Save as to change the name and/or file type. The file used in the Save as window will then become the default file for this Save command.		
Save as	Open a dialog window to save the current view with a different name and/or in a different format. (See below for a description of the dialog window).		

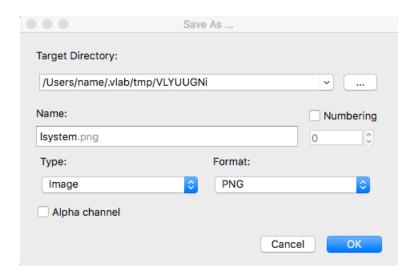


Figure 1: An example of the Save as... dialog window.

Menu item	Description	
String	Input or Output the L-system string to either a Text file or a Binary file. This can	
	be used to externally manipulate the string, and then re-read it.	
Animate Set cpfg to animate mode. The menu is updated with new items (Section		
Refresh mode	Set the mode for re-reading files and updating the object in the drawing window.	
	The default is Explicit - the files are re-read by invoking one of the New menu	
	items above. Alternatively, Triggered/Continuous mode uses cpfg's ability to re-	
	ceive messages from external programs (e.g. panels) to re-read a file as changes	
	are made.	
Exit	Exit cpfg.	

The Save as menu item opens a dialog window such as the one in Figure 1. The fields in the window are:

Menu item	Description
Target Directory	The directory in which to save the file. The default is the <i>lab table</i> directory.
Name	The name of the file. The default is the same as the Save command. If this name
	is changed, it will become the default for subsequent Save and String commands.
	Note that the file extension cannot be edited; it is set based on the Type (and
	possibly the Format) field.
Numbering	Check this box to add a number to the file name. The number will be incremented
	automatically each time the file is saved. For example, if the file name in this dialog
	box is set to lsystem0000.png, subsequent Save commands will automatically save
	lsystem0001.png, lsystem0002.png, and so on. This can be used to save the frames
	of an animation.
Type	The file type. This will set the extension in the Name field for all types except
	Image.
Format	Set the extension when Type is Image. This field is ignored for other types.
Alpha channel	Check this box to make the background transparent in the saved file.

1.3.3 Animation menu

When Animate is selected from the menu, or the -a option is included on the command line (Section 1.2.1), the following items are added to the menu. The menu items use parameters from the animation file, or their default values (Section 8.2).

Menu item	Description	Shortcut
Step	Display the frame resulting from the next step derivation steps. If	Cmd+F
	beyond the last frame, the first frame is displayed.	
Run	Display consecutive animation frames after each step derivation steps	Cmd+R
	until last frame is reached or passed.	
Forever	Display consecutive animation frames after each step derivation steps.	$\operatorname{Cmd}+V$
	When last frame is reached, return to first frame and continue.	
Stop	Pause the animation at the current frame.	Cmd+S
Rewind	Redisplay the first frame of the animation.	Cmd+W
Clear	Remove the current image from the window.	
New animate	Reread the animation file.	
Start recording	Initiate recording of animation frames. Use the Save as option before	
	beginning the recording to set the file name and type and, most im-	
	portantly, to set Numbering on. This menu item will change to Stop	
	recording once it begins.	
Don't animate	(Replaces the Animate item on the main menu.).	
	Quit animation mode and return to the main menu.	

2 The L-system file

An L-system can be defined over an arbitrary alphabet that does not contain the asterisk (*) or any separators (space, tab, etc.). Section 6 lists symbols that have a graphical interpretation.

A typical *cpfg* L-system file has the following format:

```
#define statements
lsystem: label
  declarations
derivation length: integer
axiom: list
  control statements
  productions
endlsystem
```

The parameter *label* is optional. It is ignored except when using sub-L-systems (Section 7.2).

2.1 Axiom statement

The axiom defines the starting string and cannot be blank. It is composed of symbols with and without parameters. If present, parameters must have specific numerical values. For example:

```
axiom: I(DELAY)FA(1)
```

is an axiom with three symbols, I, F and A, two of which have a parameter.

2.2 Variables

Variable names are defined as in C, and are assumed to be of type float.

2.2.1 Local vs. global variables

Both local and global variables can be defined. Local variables are used within a production's programming statements (see Section 3.2). Global variables are defined in start and end blocks before the productions (see Section 4.1).

2.2.2 Arrays

Arrays in cpfg are defined in a single statement in the declarations section. The statement has the format:

```
define: { array arrayname1[\ dimensions\ ]; array arrayname2[\ dimensions\ ]; ...}
```

Each array is specified by its name, *arrayname*, and the size of each dimension, *dimensions*, separated by commas. All arrays are defined in a single **define**: statement, separated and ending with a semicolon. The specification may extend over several lines.

The arrays may also be initialized at the same time using the syntax:

```
define: { array arrayname[ dimensions ] = { values }; }
```

where *values* are also separated by commas. For example, the following statement defines three arrays, two of which are initialized:

In a plant model, the value of a parameter frequently depends on the order, age, or vigor of the apex and each branch. It is possible to have separate productions for each branching order with different values in the successor. But in some cases it is more effective to define an array of values and use only one production.



See object: Lilac

3 Productions

A production in *cpfg* consists of three parts: the *predecessor* defines the string to be matched and the context in which it must be found; programming *statements* are evaluated once the predecessor is matched, and may include a condition that, if present, must evaluate to true; and the *successor* defines how the predecessor will change in the next derivation step.

The predecessor must be nonempty. The statements section is optional. An empty successor must be represented by an asterisk (*). The basic formats of a production are:

```
predecessor --> *
predecessor --> successor
predecessor : statements --> successor
```

3.1 The predecessor

The predecessor consists of three components: the *strict predecessor*, its *left context*, and its *right context*. It has the form:

```
lcontext < strict-predecessor > rcontext
```

Both the left and right context are optional (along with the corresponding separator), but the strict predecessor must be nonempty. Each component consists of symbols with or without parameters. The parameters are "formal": they are variables that represent actual parameter values. For example:

```
S(a,b) < A(i) > T
```

will match a symbol A that has a single parameter (of any value) and is preceded by a symbol S with any two parameters, and followed by a symbol T with no parameters.

For examples of context sensitive L-systems, see [1].

3.1.1 Ring L-systems

A ring L-system performs matching as if the last module in the string and the first module in the string are adjacent, so that the string forms a ring.

For example:

```
Axiom: A B C;
C < A --> ...
```

would match the A module in the axiom, because its left context is the C module at the end of the string.

To specify a ring L-system, include a statement before the Axiom:

See object: Ring

ring lsystem

3.2 Programming statements

A production may optionally include statements, which use C-like syntax. The statements are divided into three components formatted as:

```
{ before-stmts } condition { after-stmts }
```

3 PRODUCTIONS 11

where *condition* is a Boolean conditional expression. The production will only be used if *condition* evaluates to True.

Before-stmts are performed each time the predecessor (including the left and right context) match, before the *condition* is evaluated. Thus, these statements can be used to precompute expressions required in *condition*.

After-stmts are performed only after condition is evaluated as True, before the predecessor is replaced by the successor.

All components are optional. An empty *condition*, which is always True, is represented by an asterisk (*). Therefore, the general format of the statements can be:

```
 \left\{ \begin{array}{ll} \{before\text{-}stmts \ \} & condition \ \{after\text{-}stmts \ \} \\ \{before\text{-}stmts \ \} & condition \\ \{before\text{-}stmts \ \} & condition \\ \{before\text{-}stmts \ \} & condition \ \{after\text{-}stmts \ \} \\ & * & \{after\text{-}stmts \ \} \\ \end{array}
```

Three types of C statements may be used as part of the before-stmts and after-stmts:

• Assignment statements of the form:

```
varname = expression;
```

where *expression* is an arithmetic expression. The expression may include local variables assigned a value in previous assignment statements within the same production. For example:

```
A(y) : { x=y/2; s=x*x; } s<10 --> B(x)
```

• Conditional statements have two forms:

```
if ( condition ) { statement; \dots } else { statement; \dots }
```

where *condition* is a logical expression. Note that {} brackets are required even when there is only one *statement*. For example:

```
A(y) : * { if ( y>10 ) { y=10; } } --> B(y)
```

• Loop statements also have two forms:

```
while ( condition ) { statement; ... } do { statement; ... } while ( condition )
```

As in conditional statements, {} brackets are required in loop statements even when there is only one *statement*.

However, compared to C syntax, the syntax of L-system programming statements must follow specific rules:

- Each assignment statement must terminate with a semicolon, even if it is a last statement in a block of statements (just before the '}').
- Statements following if, else, while and do must always be enclosed in curly brackets, even if there is only one statement.
- All parameters are assumed to have real (floating point) values.
- Operators such as ++, -, +=, -=, *=, and /= are not supported.

4 Control Statements

4.1 START AND END BLOCKS

There are four blocks of statements that define procedures to be executed at specific points in an L-system simulation:

- Start called before the output string is initialized from the axiom
- StartEach called before each derivation step
- EndEach called after each derivation step
- End called after the final derivation step

Each block has the syntax:

```
block name: { statements };
```

where *statements* have the same syntax as programming statements within a production (Section 3.2). The four blocks are added before the productions in the L-system file.

For example, to set a counter i that is incremented after each derivation step:

```
Start: { i=0; }
EndEach: { i=i+1; }
```

Variables used on the left side of an assignment statement in these blocks are considered global, and can be accessed within other blocks and within productions.

4.2 Ignore and Consider Statements

Symbols can be ignored when context matching using the statement:

```
ignore: symbols
```

Alternatively, to consider only specific symbols when context matching, use the statement:

```
consider: symbols
```

In both cases, *symbols* are listed without parameters, separated by a space. For example:

```
ignore: / + - G
```

4.3 Homomorphism

An L-system homomorphism is defined as a set of productions applied only for interpretation purposes (i.e. when drawing the object from the string). This allows the modeler to change the details of the appearance without modifying the underlying logic of the model captured by the main L-system productions.

In *cpfg*, the homomorphism is specified by productions that are placed at the end of the L-system, beginning with the keyword homomorphism and ending with the endlsystem statement.

Once the string has been derived using the main L-system productions and is ready for interpretation, each module in the string is matched to the homomorphism productions creating the string to be interpreted. If a match is found, the successor in the homomorphism production is used in the string. If no match is found, the original module is retained as the successor. Note that the resulting string is used for interpretation purposes only. The next derivation step will use the string produced by the main L-system productions, excluding the changes made by the homomorphism productions.

For example, a simple plant can be described in terms of apices (A) and internodes (I):



See object: DragonCurve

```
Axiom: A
A --> I[+A][-A]IA
I --> II
```

The turtle commands to draw the apices and internodes can then be described in a homomorphism, and changed as needed:

```
homomorphism
A --> ;F
I --> F
endlsystem
```

Homomorphism productions with parameters or programming statements operate similarly to L-system productions: the expressions are evaluated and replace the formal parameters.

4.3.1 Recursive homomorphism

It is possible to repeatedly apply homomorphism productions to the string to be interpreted. To enable this, the following statement can be added after homomorphism and before the productions:

```
{\tt maximum} depth: d
```

where d is an integer representing the number of times the homomorphism productions are applied (to avoid infinite recursion). If maximum depth is omitted, the default is 1 - i.e. no recursion.

A warning may be issued if the maximum depth is reached and it is possible to further apply the homomorphism productions. To enable this, add warnings to the homomorphism statement:

```
homomorphism: warnings
```

No warnings are issued for the simple homomorphism statement. For backward compatibility, it is also possible to state:

```
homomorphism: no warnings
```

4.3.2 Context in homomorphism productions

The context for a homomorphism production is the context in the original L-system string; homomorphism successors do not affect the context search.

For example, the following homomorphism is used to draw only branches whose endpoint P has a y coordinate less than 3:

```
homomorphism F > P(x,y) : y > 3 \longrightarrow f
```

If the homomorphism in the previous example was defined as:

```
homomorphism
maximum depth: 2
F --> G P(0,0)
G > P(x,y) : y > 3 --> f
```

The context for the second homomorphism production would be a module P in the original L-system string (with its parameters), and not the module P introduced by the first homomorphism production.

4.3.3 Random numbers in homomorphism

The use of random values in a homomorphism is not recommended during an animation, since the values used in one simulation step would be different from values used in next step and visible discontinuities may result. The resulting structure may change after each redraw.

To prevent this, it is possible to define a separate random number generator used only with the homomorphism productions by including a **seed**: statement after the **homomorphism** statement and before the productions.

4.4 Decomposition

Decomposition productions make it possible to decompose a module in the string into several components. Thus the L-system productions can focus only on the development of main building blocks of a plant, such as an apex, meristem, or leaf.

After each simulation step, before the string is interpreted (and a possible homomorphism is applied), modules representing these organs can be replaced by several other modules, representing parts of the organs. Unlike homomorphism productions, the results of decomposition stay in the string.

Decomposition productions must be specified after L-system productions and before homomorphism productions (or at the end of an L-system if no homomorphism productions are included).

The syntax of a decomposition block is similar to a homomorphism block, beginning with a decomposition statement, with or without a warning. There can also be a maximum depth statement. However, decomposition productions use the same random number generator as the L-system productions. Therefore, the seed statement cannot be used.



See object: ContinuousDecomp

4.5 STOCHASTIC L-SYSTEMS

Stochastic L-systems require a seed for the random number generator. This is specified with the statement:

```
seed: svalue
```

where *svalue* is an integer number. This should be the first statement in the L-system directly after the lsystem: statement.

Productions have an added element as well:

```
predecessor : statements --> successor : probability
```

where *probability* is a percentage (1-99) representing the probability factor for that production. For example:

```
F --> F[+F]F : 40
F --> F[-F]F : 60
```

will create a branch to the left with 40% probability, and a branch to the right with 60% probability. The seed is re-initialized to *svalue* when the New model menu item is selected, but not with the New L-system menu item. This means that a random new image is displayed with each call to New L-system.



See object: RandomMoss

5 Predefined Functions

The following predefined functions can be included in L-system expressions (e.g. to define a parameter value, or in a predecessor statement).

5.1 MATHEMATICAL FUNCTIONS

Function	Description
$sin(\alpha)$	Return the sine, cosine, or tangent of angle α , where α is in degrees
$cos(\alpha)$	
$tan(\alpha)$	
asin(x)	Return an arcsine or arctangent value between -90° and $+90^{\circ}$
atan(x)	
acos(x)	Return an arccosine value between 0° and 90°
atan(x,y)	Return the arctangent of y/x in the range -90° to +90°
exp(x)	Return e^x .
log(x)	Return the log of x
sqrt(x)	Return the square root of x
fabs(x)	Return the absolute value of x
$\hat{x}y$	Return x^y

5.2 Rounding functions

Function	Description
floor(x)	Returns the largest integer $\leq x$
ceil(x)	Return the smallest integer $>= x$
trunc(x)	Truncate x to an integer
sign(x)	Return 0 if $x = 0$
	Return 1 if x is positive
	Return -1 if x is negative

5.3 Random number functions

Function	Description
srand(seed)	Initialize the random number generator used in the following functions.
ran(x)	Generate a random, floating point number uniformly distributed in the interval $[0, x]$.
$\operatorname{nran}(m, \delta)$	Generate a random number over a normal distribution with mean m and standard deviation δ .
$\mathtt{bran}(lpha,eta)$	Generate a random number with β distribution.
biran(n,p)	Generate a random number with a binomial distribution - i.e. with n numbers below p .



See object: WeepingBirch

5.4 Input and output functions

Function	Description
printf("format-string", var1, var2,)	Print variables to standard output using the specified format.
fopen("filename", "type")	Open the file <i>filename</i> for input $(type = r)$ or output $(type = w)$. Returns an identifier for the file, which is used in the functions below.
$ extsf{fclose}(extit{file-id})$	Close the file with identifier file-id.
fscan(file-id, "format-string", &var1, &var2,)	Input data from the file with identifier <i>file-id</i> , using the specified format.
fprintf(file-id, "format-string", var1, var2,)	Output the specified variables to the file with identifier <i>file-id</i> , using the specified format.
${\tt fflush}(\mathit{file-id})$	Flush the buffers of the file with identifier <i>file-id</i> .

Note that all variables are of type float. Therefore, the format strings should contain %f and %g only.

5.5 User-defined contours and functions

User-defined contours and functions are described in files (see the cuspy and funcedit tools in the vlab Tools manual for the format of the files). The files are specified in the view file (Sections 8.1.5 and 8.1.6, respectively) and assigned an id that is used in the following functions.

Function	Description
$\mathtt{curveX}(\mathit{id},t)$	Return the x , y , or z coordinate, respectively, at coordinate t of the contour
<pre>curveY(id,t)</pre>	identified by id. The value of t should be in the range [0,1]. If $t < 0$, return
$\mathtt{curveZ}(\mathit{id},t)$	the position of the start of the contour. If $t > 1$, return the position of the
	endpoint of the contour.
curveGAL(id)	Return the length of the contour identified by id.
func(id, x)	Return the value at x of the user-defined function with identifier id . The
	value of x should be in the range $[0,1]$. If $x < 0$, return the value of the
	function at 0. If $x > 1$, return the value of the function at 1.



See object: Canalization



See object: Ridley



See object: JumpingLamp

5.6 OTHER FUNCTIONS

Function	Description
<pre>vvXmin()</pre>	Return the minimum and maximum extents of the rendered volume, in x , y , and z
vvXmax()	coordinates.
<pre>vvYmin()</pre>	
vvymax()	
vvZmin()	
vvZmax()	
stop(n)	Stop the animation. If $n=1$, and Run or Forever is selected from the menu, draw the current string and continue. Otherwise, stop the simulation.

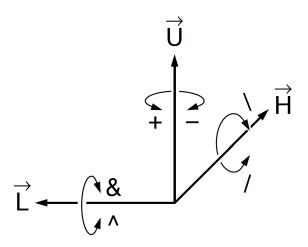


Figure 2: Controlling the turtle in three dimensions

6 Predefined modules

During visualization, the string of symbols is parsed from left to right. When a predefined symbol controlling the turtle is encountered, the function associated with the symbol is performed. Symbols with predefined interpretations are listed below. If a symbol has more parameters than those specified below, the additional parameters are ignored.

6.1 Position and drawing

In the following modules, the parameter l is optional. If not specified, the default is used.

Module	Description	Default
F(l)	Move forward a step of length l and draw a line segment from the original	1
	position to the new position of the turtle. If the polygon flag (Section 6.5) is	
	on, the final position is recorded as a vertex of the current polygon.	
f(l)	Move forward a step of length l without drawing a line. If the polygon flag	1
	(Section 6.5) is on, the final position is recorded as a vertex of the current	
	polygon.	
G(l)	Move forward a step of length l and draw a line.	1
g(<i>l</i>)	Move forward a step of length l without drawing a line.	1
$\mathtt{QM}(x,y,z)$	Set the turtle position to (x,y,z) .	

The view file command line style (Section 8.1.5) specifies whether the line is drawn as a line, polygon, or cylinder.

6.2 Turtle rotations

The turtle can be rotated around its heading, left, or up vector only (Figure 2).

Module	Description
+(\theta)	Turn left by angle θ° around the \vec{U} axis.
$-(\theta)$	Turn right by angle θ° around the \vec{U} axis.
&(θ)	Pitch down by angle θ° around the \vec{L} axis.

Module	Description
^ (θ)	Pitch up by angle θ° around the \vec{L} axis.
\ (\theta)	Roll left by angle θ° around the \vec{H} axis.
$/(\theta)$	Roll right by angle θ° around the \vec{H} axis.
1	Turn 180° around the \vec{U} axis. This is equivalent to +(180) or -(180).
	It does not roll or pitch the turtle.
@v	Roll the turtle around the \vec{H} axis such that \vec{H} and \vec{U} lie in a common
	vertical plane with \vec{U} closest to up.
$\mathtt{QR}(hx,hy,hz)$	Set the turtle heading to (hx,hy,hz). If the vector is not normalized, it
	will be done automatically. If (ux, uy, uz) are not specified, the turtle up
$\mathtt{QR}(hx,hy,hz,ux,uy,uz)$	and left vectors are adjusted to minimize their rotation with respect to
	their previous orientation. Otherwise, (ux,uy,uz) specify the turtle up
	vector (which will also be normalized automatically), the left vector will
	be computed directly from the heading and up vectors.

If the parameter θ is not specified, the value of the view file command angle increment, or its default, will be used (Section 8.1.1).

Modules @v and @R adjust the turtle orientation with respect to absolute coordinates (as compared to other rotations, which are performed with respect to the current turtle orientation).

6.3 Changing turtle parameters

The parameter is optional in all the following modules except **@D(s)**. When no parameter is given, the value of the indicated command in the view file or its default (Section 8.1.1) is used to increase or decrease the current value. When a parameter is given, it sets a new value.

Module	Description
; (n)	Increase the value of the current color index or material index by color increment,
	or set it to n .
, (n)	Decrease the value of the current color index or material index by color increment,
	or set it to n .
@;(n)	Increase the value of the current color index or material index of the back side of a
	surface by the second parameter of color increment, or set it to n .
@,(n)	Decrease the value of the current color index or material index of the back side of a
	surface by the second parameter of color increment, or set it to n.
#(n)	Increase the value of the current line width by line width increment, or set it to n .
! (n)	Decrease the value of the current line width by line width increment, or set it to n .
@D(s)	Set the current turtle scale to s. All subsequent geometry will be scaled by this value.
	The default scaling factor is initial scale.
@Di(s)	Multiply the current turtle scale by scale multiplier, or set it to s.
@Dd(s)	Divide the current turtle scale by scale multiplier, or set it to s.

Note that surfaces can have different colors or materials specified for each side only if the view file command initial color has two parameters.

6.4 Branching structures

A branch is created by pushing the current state of the turtle (all its parameters) onto a stack, and then popping them off the stack to return to the start of the branch when complete.

Module	Description
[Begin a new branch by pushing the current state of the turtle onto the stack.
]	Complete a branch by popping the last turtle state from the stack and setting the turtle
	to this state (i.e. the beginning of the branch).
%	Cut the remainder of the branch: ignore this symbol and all following modules up to the closest unmatched right bracket], therefore eliminating them from the gener-
	ated string. If no unmatched right bracket is found, all modules to the end of the string are eliminated. See example below. This symbol is ignored if introduced by a homomorphism production.

For example, if a new branch is defined in the string as

where the parameter of D is the age of the branch, it can be removed from the string when it reaches the age of 20 using the cut symbol %:

```
D(a) : a<20 --> D(a+1)
D(a) : a>=20 --> %
```



See object: Shedding

6.5 Polygons

The following modules are used in conjunction with F and f to create a polygon (Section 6.1).

Module	Description
{	Start a new polygon by pushing the current turtle position onto the polygon stack and setting the polygon flag on.
	0 1 00 0
}	Pop a polygon from the stack and render it, filling it with the current color. If there
	are no more polygons on the stack, turn the polygon flag off.
•	Create a polygon vertex at the current position, if the polygon flag is on, by placing
	the current state of the turtle on the polygon stack.

See also the generalized cylinder modules using the { and } symbols with a parameter (Section 6.7.3).

6.6 CIRCLES AND SPHERES

Module	Description	Default
@o(d)	Draw a circle of diameter d in the plane of the screen.	current line width
@c(d)	Draw a circle of diameter d in the HL plane.	current line width
@bo(d)	Draw the boundary of a circle with diameter d in the plane of the screen. The width of the boundary is set to the current line width.	
@bc(d)	Draw the boundary of a circle with diameter d in the HL plane. The width of the boundary is set to the current line width.	
@O(d)	Draw a sphere of diameter d .	current line width

Note that objects drawn on the plane of the screen keep their orientation in relationship to other elements of the scene when the scene is rotated.

6.7 Surfaces and generalized cylinders

6.7.1 Surface files

Surfaces may be defined in a file that contains all the control points, geometry and neighbourhood information. See the *bezieredit* and *stedit* tools in the *vlab* Tools manual for interactively creating surface files.

Surface files are specified in the view file (Section 8.1.5) and read at the beginning of the simulation. Each surface is identified by an id, and a single module within the L-system is used to draw it:

1	

See object: TexturedSurfaces

Module	Description	Default
$\sim id$	Draw the surface identified by id at the turtle's cur-	no scaling
\sim id(scale)	rent location and orientation. If the module has one	
$\sim id(sx, sy, sz)$	parameter, the surface is uniformly scaled by <i>scale</i> .	
	If there are three parameters, they specify the scal-	
	ing amount in the x , y , and z directions.	

6.7.2 L-system defined surfaces

Surfaces can also be defined within the L-system using an internal 4x4 array of control points, identified by an *id.* To define and draw the surface, the following modules are used:

Module	Description	Default
@PS(id,type)	Initialize the 4x4 set of control points for surface id to $(0,0,0)$. The $type$ can be one of: $1 = \text{B\'ezier}$, $2 = \text{B-spline}$, $3 = \text{Cardinal spline}$.	type = 1
@PC(<i>id</i> , <i>r</i> , <i>c</i>)	Set the current position of the turtle to the control point at row r and column c of surface id .	
@PD(<i>id</i> , <i>s</i> , <i>t</i>)	Draw the surface defined by the control points for surface id , forming a mesh with s lines along the rows and t lines along the columns.	

6.7.3 Generalized cylinders

A sequence of turtle positions can be interpreted as a control polygon of a bicubic curve. Moreover, a line or curve can be drawn as a generalized cylinder with a user-defined cross-section. These operations are controlled by the following modules:

Module	Description	Default
{ (type)	Start a generalized cylinder. The parameter <i>type</i> can be one of:	
	1 = an open curve of Hermite spline segments	
	2 = a closed curve of Hermite spline segments 3 = an open curve of B-spline segments	
	4 = a closed curve of B-spline segments	
	This module does not define the first control point. If type is not specified, a polygon is defined (Section 6.5).	
}(type)	Finish a generalized cylinder started by module { (type). The parameter type must match in both modules.	
@Gs	Start a generalized cylinder at the current turtle position. This is equivalent to {(1).	
@Ge(strips)	Finish a generalized cylinder. The parameter <i>strips</i> defines the number of mesh strips drawn between this final control point and the previous one. This is equivalent to	
	}(1).	



See object: Generalized-Cylinder

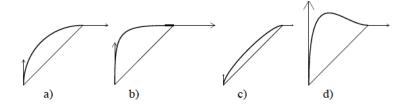


Figure 3: Hermite curves defined as: QGs-(45)f-(45)QGt(start,end)QGe(20), where start and end are (a) the default: 1.2, 1.2; (b) 2, 2; (c) 0.5, 0.5; (d) 4, 1. Visualized tangent vectors are scaled by 1/4 to fit the figure.

Module	Description	Default
@Gc(strips)	Specify a control point on the central line of the cylinder. The parameter <i>strips</i> defines the number of mesh strips drawn between this control point and the previous one.	strips = 1
. (strips)	Equivalent to QGc(strips). If strips is not specified, a polygon vertex is defined (Section 6.5).	
@! (npolygons)	Set the number of polygons around a generalized cylinder, or a cylinder represented by F or G, to <i>npolygons</i> .	
@#(contour-id)	Set the contour specified by $contour$ - id as the current contour for generalized cylinders. Contours are specified in the view file (Section 8.1.5). When $contour$ - $id = 0$, the default circle is used.	a circle
@Gt(start,end)	Modify the tangent coefficients at the start and end points of a Hermite curve specifying the generalized cylinder axis. The tangent lengths are equal to the distance between the two control points multiplied by the tangent coefficients. This module must be inserted before the module defining the second control point of the Hermite curve segment. (See Figure 3 and [2]).	start = end = 1.2
<pre>@Gr(angle1, length1,angle2, length2)</pre>	Specify the slope and length of two tangents of a Hermite curve which describe the change of radius of the generalized cylinder axis. (See [2]).	
@Gr(flag)	Switch on or off an automatic adjustment of radius tangents for segments of non-unit length. When on $(flag = 1)$, the tangents are defined for a segment of unit length and then stretched onto a segment of non-unit length, thus the specified tangent angles do not correspond to the real angles of the tangents. When off $(flag = 0)$, tangents are not adjusted after the stretching.	

Only one generalized cylinder can be defined at a time unless it is defined within a branch delimited by square brackets. For example:

If the generalized cylinder is started using the { module, control points are also defined after each f and F (Section 6.1), similar to polygons (Section 6.5). Since the number of strips cannot be specified, it defaults to 4.

6.7.4 Textures

Textures are images that can be mapped on surfaces, cylinders, cones, and generalized cylinders (not on disks or spheres). They are only used in material mode (with the -M command line option), and are defined in the view file (Section 8.1.7) and referenced by *id* number starting with 1.

Module	Description
@Tx(<i>id</i>)	Set the current texture to id . If $id = 0$, texturing is switched off.

If a predefined bicubic surface has an associated texture in the view file, its texture is fixed and cannot be changed by this module.

6.8 Tropisms

Tropisms are specified in the view file (Section 8.1.8) and referenced by id number starting with 1.

Module	Description
@Ts(id,value)	Set the elasticity parameter of tropism to value. This overrides the E: parameter of
	the tropism command in the view file.
QT(id,value)	Increase the elasticity parameter. If value is not specified, the S: parameter of the
	tropism command in the view file is used.
@Td(id,value)	Decrease the elasticity parameter. If value is not specified, the S: parameter of the
	tropism command in the view file is used.
@Tp	Adjust the turtle's up and left vector to minimize twist. The command operates
	locally, i.e. it adjust the turtle's vectors only at the current point.
@Tf	Force the twist. If the orientation of a segment following symbols / or \ is adjusted
	due to a tropism (which as a default adjusts the segment's up vector to prevent
	twist), the effect of symbols / or \ is nullified and it is necessary to add this module
	to force the twist. It operates locally, i.e. it prevents twist only for symbols / or \
	to the left of CTf.

See object: Tropisms

6.9 Query and communication

Module	Description
?P(x,y) ?P(x,y,z)	Query the turtle position.
? $H(x,y)$? $H(x,y,z)$	Query the current turtle heading vector.
?L(<i>x,y</i>) ?L(<i>x,y,z</i>)	Query the current turtle left vector.
PU(x,y) PU(x,y,z)	Query the current turtle up vector.
?E(p1,p2,)	Communicate with an external process. Used to both send and receive environmental information. The parameters can be set by the model and transferred to the environment process, or set by the environment process and transferred to the model. See the <i>Vlab Environment Programs</i> manual for more information on environmental processes, as well as [3] and [4].



See object: QueryPosition



See object: Horneophyton



See object: Canalization

23

If a query module is present in any L-system production, an interpretation step is performed after each derivation step, even if cpfg does not draw to the window. The parameters to the module can then be accessed in the following derivation step and affect the selection of productions.

6.10 Labels

Module	Description
@L("label")	Print <i>label</i> , or specify a printf -like <i>format</i> and print the values of
@L("format",p1,p2,)	parameters $p1, p2,$ The content is printed in the drawing window
	at the current turtle location using the font specified in the view
	file (Section 8.1.9).

7 ADVANCED TOPICS

7.1 Mouse interaction

It is possible to interact with the generated image using the mouse, by holding down the Shift and Command keys and clicking with the left mouse button. When the mouse is over an element of the model, an X module is inserted into the string immediately before the selected module.

Note that if there are several F modules in a row, X will be inserted before the first F. For more granularity, the F modules can be separated by a null module, such as f(0) or []. To avoid complicating the main L-system, this can be done in a homomorphism:

```
_^_
```

See object: Snowflake

```
homomorphism:
F --> Gf(0)
```

Replacing F with G ensure that the production is not applied recursively.

7.2 Sub-L-systems

Several L-systems can be combined to create a single model, by defining each with a separate label (Section 2). To call a sub-L-system, the following statement is added to the string:

```
?(label,s) mod $
```

where label is the number assigned in the lsystem: statement, s is the scaling factor, mod represents the module that will be processed by the sub-L-system, and \$ returns control to the calling L-system. The module mod may have parameters.

For example, the main L-system (lsystem:1) can have a production that replaces module A(t) with a call to a sub-L-system (lsystem:2), along with the module B(t-1). The sub-L-system then has a production to match module B:



See object: Sedge

```
lsystem: 1
...
A(t) --> ?(2,1)B(t-1)$
...
endlsystem

lsystem: 2
...
B(x) --> ....
...
endlsystem
```

Note that each L-system requires an axiom statement, but the axiom is ignored when it is called as a sub-L-system. However, if the L-system is run independently, it will use the axiom, which should include the module defined in the sub-L-system call. For example, the sub-L-system above could have the following statement:

```
axiom: !(3);(48)B(5)
```

to provide a starting point for the L-system that includes module B(x) with the defined parameter 5.

8 cpfg-specific input files

8.1 View file

The view file contains drawing, viewing, and rendering commands, as well as the names of external files such as surfaces and functions.

Unless otherwise stated, the values have the following formats:

- \bullet x,y,z floating point numbers
- \bullet *i* integer
- \bullet *id* a single character
- \bullet flag on or off

Comments may be included in the file using the standard C notation:

Note that the commands are processed in the order they are specified in the file. Thus if there are multiple instances of the same command, the last one takes precedence. Exceptions are noted for individual commands that allow for multiples.

8.1.1 Turtle commands

Command	Description	Default
angle increment: x angle factor: y	Set the angle associated with the +, -, &, $^{\circ}$, /, and modules. The angle is set to x° , or to $360^{\circ}/y$. These are alternative methods of setting the same parameter; therefore, the last one specified will be applied.	45°
initial color: $i1\ i2$	Set the initial index into the colormap or material file. The value should be a number between 0 and 255. The second value is optional. If present, $i2$ specified the index to be used for the back side of the surface.	128
color increment: i	Set the color increment associated with the current colormap or material file.	1
initial line width: $x\ style$	Set the initial line width to x . The $style$ parameter is optional; if included, the values are: pixels or p - flat shaded lines with width in pixels shaded or s - shaded cylinders in world units Alternatively, the line style command (Section 8.1.5) can be used.	width = 1 $style = p$
line width increment: x	Set the line width increment associated with the $\#$ and $!$ modules to x , using the same units as initial line width.	0
initial scale: x	Set the initial scale factor associated with the turtle to x . All geometry will be scaled by this factor. This value can be modified by modules \mathtt{QD} , \mathtt{QDi} , and \mathtt{QDd} (Section 6.3).	1

Command	Description	Default
scale multiplier: x	Set the multiplicative factor by which the tur-	1
	tle scale is multiplied or divided when module	
	QDi or QDd (Section 6.3) is interpreted.	
interpretation past %: flag	Interpret past the cut symbol $\%$ if $flag = on$.	on
	When $flag = off$, the symbols after % are not	
	interpreted.	

8.1.2 Setting the view

Command	Description	Default
$\verb viewpoint : x,y,z $	Set the x,y , and z coordinates of the viewpoint in world space.	0,0,1
view reference point: x,y,z	Set the x, y , and z coordinates of the view reference point in world space.	0,0,0
twist: i	Rotate the image on the screen by i tenths of a degree.	0
projection: type	Set the projection to <i>type</i> , which can be either parallel or perspective. Autocentering and auto-scaling work only in parallel mode.	parallel
viewing angle: x	Set the viewing angle of perspective projection. This command is ignored in parallel projection.	45°
front distance: x	Set the distance from the viewer to the front clipping plane in perspective project, or the position of the clipping plane with respect to the viewpoint in parallel projection (thus a negative value must be used).	-100000
back distance: x	Set the distance from the viewer to the back clipping plane in perspective project, or the position of the clipping plane with respect to the viewpoint in parallel projection.	100000
scale factor: x	Set the size of the final image on the screen. When $x = 1$, the image is full size.	1
box: x: xmin, xmax y: ymin, ymax z: zmin, zmax	Set the bounding box for the model. The view is adjusted so that the whole bounding box is visible. Effective only in parallel projection.	x: 0,1 y: 0,1 z: 0,1
min zoom: zmin max zoom: zmax	Set how much the user can zoom in or out on the view.	zmin = 0.05 $zmax = 50$
generate on view change: flag	Regenerate the L-system string (the simulator rewinds to the axiom and performs the derivations again) every time the view changes through rotation, zoom, or pan $(flag = on)$, or after the user releases the mouse button $(flag = triggered)$.	off

Note that modifying scale factor in perspective projection moves the viewer closer or farther from the viewpoint and therefore the front distance and back distance will need adjusting.

8.1.3 Lights

Colormap mode. The following commands are used in colormap mode only.

Command	Description	Default
light direction: x,y,z	Define the direction of light as the x , y , and z coordinates of a vector.	(1,0,0)
diffuse reflection: i	Define the coefficient used to determine the range of colors for lighting a shaded surface. See below for the formulas that use this coefficient.	10
$\operatorname{surface}$ ambient: a	Define the amount of ambient and diffuse light	a = 0.15
surface diffuse: d	present for shading bicubic surfaces and tsurfaces, where a and d are numbers between 0 and 1. See below for the formula used.	d = 0.75

The diffuse reflection, surface ambient and surface diffuse commands are used to vary the color based on the orientation of polygons representing the surface or cylinder with respect to the direction of the light source, where \vec{N} is the normal of the polygon, and \vec{L} is the direction towards the light source. Only the first light source is used, if more than one is specified in the view file.

The diffuse reflection coefficient i is used as follows:

- For a surface color col, the range of colors is varied within the interval [col-i, col+i].
- For a polygon representing a cylinder or generalized cylinder, the original color index col is used to calculate the final color using the formula: $col + i \cdot \vec{N} \cdot \vec{L}$

The surface coefficients, a and d, are used to calculate the final color of a surface with the formula:

$$64 \cdot int \cdot (a + d \cdot abs(\vec{N} \cdot \vec{L}))$$

where the color intensity int is calculated using the color index col associated with the surface:

$$int = col/64 - floor(col/64)$$

Material mode. In material mode the light command is used. There may be multiple light commands, each with a set of subcommands. Therefore, the syntax is:

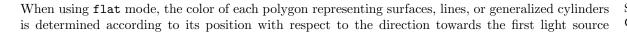
```
light: subcmd1 subcmd2 subcmd3 ... light: subcmd1 subcmd2 subcmd3 ...
```

The subcommands of light are:

Subcommand	Description	Default
0: x y z	Define the origin (x, y, z) of a point light source.	0 0 1
V: x y z	Define the vector (x, y, z) for a directional light source.	
A: r g b	Define the ambient light color in RGB components.	1 1 1
D: r g b	Define the diffuse light color in RGB components.	111
S: r g b	Define the specular light color in RGB components.	1 1 1
P: x y z e c	Define a spotlight with direction (x,y,z) , exponent e , and cutoff angle c .	0 0 -1 0 180
T: c l q	Define attenuation factors: constant c , linear l , and quadratic q .	100

8.1.4 Rendering

Command	Description	Default
render mode: mode	Render the object using one of the following modes: filled - All polygons have the same color. If materials are specified the diffuse color is used. fast - Same as filled except spheres and disks are drawn in wireframe. wireframe - All objects are drawn in wireframe. interpolated - Interpolate between colors at the beginning and end of a line or cylinder, or at different vertices of a poly- gon. flat - The color of each polygon is determined by its position with respect to the light. (See explanation below.) shaded - In colormap mode, the color is computed for each vertex of the polygon, similar to flat mode. In material mode, the normal for each polygon can be different at each vertex, resulting in smooth shading. shadows - Same as shaded but includes shadows. Additional shadow parameters are defined using the shadow map com- mand below. This mode forces the z-buffer on, and sets the texture mode to modulate, regardless of the z buffer com- mand below or the texture mode (E:) defined in Section 8.1.7. Define parameters for shadow mapping when using render	filled $n = 1024$
snadow map: size: n color: r g b offset: factor units	beine parameters for shadow mapping when using render mode: shadows. The shadow map will be generated using the first directional or spot light source specified with the light command. The following parameters are optional: size: the width and height of the shadow map $(n \times n)$, where n must be an even number. Values that are too small $(n < 100)$ or too large (dependent on graphics card) may cause shadows not to display. color: shadow color in rgb components. offset: polygon offset for generating depth map used to reduce shadow acne (erroneous self-shadowing). To reduce shadow acne, try increasing these values.	n = 1024 r = 0.2 g = 0.2 b = 0.4 factor = 5 units = 10
z buffer: flag	Define whether hidden surface elimination using the z buffer should be on or off. When off, the last object drawn will be visible.	on
antialiasing: flag	Draw with antialiasing ($flag = on$). Currently, this only works with line primitives.	off
concave polygons: flag	Enable the OpenGL tesselator ($flag = on$), which divides polygons into triangles. This allows for more complex concave polygon shapes, but will cause $cpfg$ to run slower.	off
background scene: filename1, filename2,	Specify additional objects to be drawn after the L-system generated string is interpreted. Each object is in a file containing a set of graphics commands (Section 8.3).	





See object: ConcavePolygons

specified in the view file (Section 8.1.3); other sources are ignored. In material mode, a single normal is used for the whole polygon. For colormap mode, see the notes on the diffuse reflection, surface ambient and surface diffuse commands in the view file.

8.1.5 Lines, contours, and surfaces

Command	Description	Default
line style: style	Specify how lines (represented by modules F and G) are drawn, where <i>style</i> is one of the following: pixel - flat shaded lines with width in pixels polygon - flat shaded polygons with width in world units cylinder - cylinders with width in world units	pixel
tapered lines: flag	Control whether lines and cylinders are drawn tapered (flag = on).	on
line: id filename.s s	Specify a line using a surface file $filename.s$ and assign it an id . The scaling factor s is mandatory.	
contour: id filename	Specify a contour in <i>filename</i> and assign it an <i>id</i> (Section 5.5). Contours are defined as planar B-spline curves, and are considered cross-sections of generalized cylinders. See the <i>cuspy</i> tool in the <i>vlab</i> Tools manual for interactively creating a contour file.	
contour sides: n	Define the level of detail used in generating the polygons for spheres and cylinders. For cylinders, n is the number of polygons around the circumference $(n > 3)$. For spheres, the closest upper power of two is used. For smooth connections between cylinders and spheres when using small values of n , use a power of 2. This initial value can be modified by module \mathfrak{Q} ! (Section 6.7.3).	3
twist of cylinders: flag	Do not minimize the twist when drawing generalized cylinders ($flag = on$).	off
surface: id filename.s s i j texfile	Specify a surface file $filename.s$ and assign it an id . The scaling factor s is mandatory. The values i and j are optional, but if present, define the level of detail used when drawing patches: i polygons along the rows, and j polygons along the columns. The final argument, $texfile$, is also optional, and specifies a texture file associated with the surface. This value takes precedence over the texture id assigned with the CTx module (Section 6.7.4). All instances of this surface will have the same texture. See the $bezieredit$ and $stedit$ tools in the $vlab$ Tools manual for interactively creating surface files.	i = j = 0
$\begin{array}{c} \texttt{tsurface:} \ id \\ filename. \texttt{ray} \ s \end{array}$	Specify a surface file <i>filename</i> .ray in rayshade format (Section 8.4), and assign it an id . The scaling factor s is mandatory.	

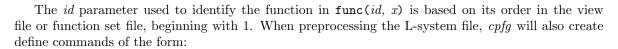
There may be several line, contour and surface commands in the view file. Each should have a unique id.

8.1.6 User-defined functions

The following commands specify files containing user-defined functions called with func (Section 5.5). The files contain function(s) of one variable defined as B-spline curves constrained to assign exactly one y value for every x in the normalized function domain [0,1]. See the function in the vlab Tools manual to interactively create a single function, and the gallery tool to create a set of functions.

The files are specified using the following commands:

Command	Description
function: filename n	Specify the <i>filename</i> containing a function. If the optional parameter n is present, $cpfg$ will precompute n values of the function, evenly spaced in $[0,1]$ and the value returned when the function is called will be a linear interpolation of the two closest precomputed values. If the parameter is omitted, the return value will be computed exactly each time the function is called.
function set: filename	Specify the <i>filename</i> containing a set of user-defined functions, rather than a single function. The number of precalculated samples (parameter n above) is specified in the function set file.





See object: JumpingLamp for an example of a function set

-D FUNCNAME = id

where *FUNCNAME* is an all-capitals version of the function's name as specified in the file, and *id* is its order number. This makes it possible to call a function by name rather than its position, using the format:

func(FUNCNAME,x)

where x is the parameter to the function. This applies to functions specified by both the function and function set commands.

8.1.7 Textures

Textures can be mapped on surfaces, cylinders, cones, and generalized cylinders (not disks or spheres). The command has the same format as the light command (Section 8.1.3):

```
\begin{tabular}{lll} texture: & subcmd1 & subcmd2 & subcmd3 & \dots \\ texture: & subcmd1 & subcmd2 & subcmd3 & \dots \\ \end{tabular}
```

The subcommands are:

Subcommand	Description	Default
F: filename	Specify the image file containing the texture, in PNG or RGB format.	
	This subcommand is mandatory. The image width and height are	
	clamped in such a way that the image size is $2^m \times 2^n$.	
E: mode	Control the way the texture is combined with the surface colors,	modulate
	where <i>mode</i> is one of the following:	
	modulate or m - multiply the surface color with the texel color	
	decal or d - use the texel color; the surface is not shaded	



See object: TexturedSurfaces



See object: Generalized-Cylinder

Subcommand	Description	Default
S:	Map the surface texture per surface, not per patch. The surface boundaries are found and then the texture is mapped into the $z=0$ plane with respect to the computed boundaries.	
R: ratio	Define the aspect ratio of a texture mapped on a cylinder or generalized cylinder. A value greater than 1 causes the texture to be more stretched along the cylinder.	1
H: filter	Define the display mode for textures with texels larger than image pixels, where <i>filter</i> can be: linear or 1 - texture image is smoothed near or n - texture pixels are visible	near
L: filter	Define the display mode for textures with texels smaller than image pixels, where filter can be: linear or 1 - more texture pixels are used to compute the given pixel near or n - only one texture pixel is used to compute the given pixel (may result in aliasing). mnn - use the nearest mipmap image and the nearest pixel in this mipmap. Produces some artefacts but is the fastest. mln - use the nearest mipmap image and linearly interpolate between neighbouring pixels. Still produces some artefacts. mnl - use the nearest pixels in the two best mipmaps and interpolate between values. mll or m - linearly interpolate between neighbouring pixels in the two best mipmaps and interpolate between the values. Produces the best result, but may be slower.	near

For mipmaps, the OpenGL library creates a smaller version of the texture (down to a size of 1×1), and for smaller objects uses the smaller texture, resulting in faster displaying. These are the four filters for L: beginning with m.

8.1.8 Tropisms and torque

There are two commands that have the same set of subcommands: tropism sets the tropism parameters, and torque sets the parameters of movement that adjust segments around their heading without modifying the heading orientation. The A: subcommand is ignored in the torque command. There may be multiple tropisms defined, each assigned a sequential *id* starting with 1.

The commands consists of a series of subcommands:

tropism: subcmd1 subcmd2 subcmd3 ...

. . .

 $\verb"torque: subcmd1 subcmd2 subcmd3 ...$

. .

The subcommands are:

Subcommand	Description	Default
T: x y z	Define the tropism vector. This subcommand is mandatory.	
A: angle	Define the <i>angle</i> , in degrees, with respect to the tropism vector that segments are trying to reach. For example, a 90° angle corresponds to diatropism.	0°
I: intensity	Define the global <i>intensity</i> of the tropism.	1

Subcommand	Description	Default
E: elasticity	Set the initial <i>elasticity</i> .	0
S: step	Set the elasticity increment/decrement step.	0

See Section 6.8 for modules using these tropisms. The elasticity modules \mathtt{QTs} , \mathtt{QT} and \mathtt{QTd} may override the \mathtt{E} and \mathtt{S} values defined here.

8.1.9 Fonts

Comm	and	Description	Default
font: j	font	Define the font type to be used when interpreting the @L mod-	-*-courier-bold-
		ules (Section 6.10), using the X font specification.	r-*-*-12-*-*-*-
			--*

8.1.10 Deprecated view commands

The following commands exist only for backwards compatibility. For all new view files, use the command in the 'Use instead' column.

Command	Description	Use instead
shade mode: i	Render using one of the following modes: 1 - Simple fill (default) 2 - Interpolated fill 3 - Gouraud shading 4 - B-spline 5 - Closed B-spline 6 - Two sided 7 - Wireframe	render mode
polygonization level: n	Define the level of detail used in generating the polygons for spheres and cylinders. A high value, such as 4, will generate very smooth surfaces, but take longer to display. The lowest value is 1 and produces very rough approximations of the surfaces. The default is 3.	contour sides
$\begin{array}{c} \texttt{tropism} \\ \texttt{direction:} \ x,y,z \end{array}$	Define the direction toward which branches tend to bend using the vector with coordinates x , y , and z . The default is $(0,1,0)$.	tropism
initial elasticity: x	Specify the susceptibility of a branch to bending. The default is 0.	tropism
elasticity increment: x	Increment or decrement the elasticity by x . The default is 0.	tropism

The following commands are ignored in the current version, but may exist in old models.

Command	Description	Use instead
ambient light: red, green, blue	Define the <i>red</i> , <i>green</i> , and <i>blue</i> components of ambient light.	In colormap mode: surface ambient
	<u> </u>	In material mode: light
background color: red, green, blue	Define the red, green, and blue components of the background color.	In colormap mode: color index 0 In material mode: emission color

Command	Description	Use instead
cue range: x	Specify the range of color indices used for depth cueing. A default of 0 indicates no depth cueing. Usual values are between 10 and 100.	
interpretation step: i	Set the number of interpreted symbols before the next X event is checked.	

8.2 Animation file

This file is input when cpfg enters Animation mode, either from the main menu (Section 1.3.2) or with the -a option on the command line (Section 1.2.1). If this file is not specified on the command line, default values are set for the animation commands.

Command	Description	Default
first frame: i	Set the first frame to be interpreted.	1
last frame: i	Set the last frame to be interpreted.	derivation step
step: i	Set the number of derivation steps between drawing (and recording) of frames.	1
clear between frames: flag	Specify whether the screen should be cleared between frames ($flag = on$). When off, successive images are superimposed.	on
new view between frames: flag	Specify whether to reset the view between frames ($flag = on$), or not ($flag = off$).	off
scale between frames: $flag$	Specify whether the view should be adjusted to fit the entire object in the window ($flag = on$), or not ($flag = off$). If on, this adjustment is made before applying the scale factor command (Section 8.1.2). This command works only in parallel projection.	off
double buffer: flag	Specify whether double buffering is on or off during animation.	on
frame intervals: f1, f2, f3,, fa-fb,, fc-fd step s, fe-ff rotate rx ry rz, fg-fh scale sx sy xz	Define specific frames and/or ranges of frames to be interpreted. A range may also include: step, to override the step command with a specified step s; rotate, to rotate after each frame by a specified angle (in degrees) around each axis; or scale, to scale after each frame. See examples below. This command takes precedence over the first frame, last frame, and step command regardless of the order in the file.	

When clear between frames is turned off, double buffer should also be turned off. Otherwise only every second frame will be displayed.

The frame interval command can simply select specific frames to be drawn. For example, to select frames 1, 3, 4, 5, 10, 12, 14, 16, 19, 21, the command would be:

frame intervals: 1, 3-5, 10-16 step 2, 19, 21

It can also specify a rotation after each frame. For example, to rotate the object 1.5° around the x axis after each frame is drawn, beginning with frame 11:

frame intervals: 1-10, 11-100 rotate 1.5 0 0

Or it can specify a scaling factor for each frame. For example, to scale the object to 90% of its size for each of the first 100 frames:

frame intervals: 1-100 scale 0.9 0.9 0.9

Deprecated commands The following animation commands are ignored in the current version, but may exist in old models.

Command	Description
swap interval: i	Set the minimum time i (in tenths of a second) between swapping of buffers in
	double buffer mode. The time is measured between the moment $cpfg$ begins
	drawing one frame until the moment it begins drawing the next frame. If it
	takes longer to draw a frame, the delay between frames will be longer.

8.3 Background file

A background scene can be effectively used to define additional objects around a simulated plant. It can also be used during simulation of plant-environment interactions, for visualizing the environmental field together with the plant (see the *vlab* Environmental Programs manual).

The name of the background file is specified by the background scene command in the view file (Section 8.1.4). The file consists of commands similar to statements in the OpenGL graphics library.



See object: Background-Scene

8.3.1 Primitives

The following commands define basic geometric primitives, where the coordinates of the vertices and/or the size of the primitives are defined with respect to the local coordinate system. It is possible to translate or scale the objects by translating and/or scaling the coordinate system using the transformation commands (Section 8.3.3).

Command	Description
$\texttt{polygon} \ x_1 \ y_1 \ z_1 \ \ x_n \ y_n \ z_n$	A polygon with n vertices, where $n \geq 3$.
$\verb"polygon" u x_1 y_1 z_1 nx_1 ny_1 nz_1$	A polygon with m vertices, where $m \geq 3$. Each vertex also
$\dots x_m y_m z_m nx_m ny_m nz_m$	has an associated normal (nx, ny, nz) .
${ t rectangle} a b$	A rectangle with one vertex at $(0,0,0)$ and edges of length a
	and b along the positive x and y axes respectively.
$\texttt{mesh}\ x_1\ y_1\ z_1\\ x_n\ y_n\ z_n$	A rectangular mesh, where $n = 4 + 2k$ and $k \ge 0$. Vertices
	2k, 2k + 1, 2k + 2, and $2k + 3$ define a single rectangle of the
	mesh.
box $a b c$	A box with one vertex at $(0,0,0)$ and edges of length a, b , and
	c along the positive x , y and z axes, respectively.
$\verb"cone"r_1r_2h$	A cone with its axis along the y axis, a radius of r_1 at the
	base and r_2 at the top, and a height of h .
$\verb cylinder r h$	A cylinder with its axis along the y axis, a radius of r , and
	height h .
sphere r	A sphere with center at $(0,0,0)$ and radius r .

8.3.2 Materials

Command	Description
$\texttt{material} \ n_1 \ n_2 \ \ n_{17}$	This material is applied to all subsequently defined primitives.
	n_1 - n_4 : ambient light
	n_5 - n_8 : diffuse color
	n_9 - n_{12} : specular color
	n_{13} - n_{16} : emissive color
	n_{17} : the specular exponent

The four values for each color are the R, G, and B components of the color (in the range of 0 to 1), and the alpha value controlling the opacity (1 = opaque, 0 = transparent). The specular exponent is a number in the range 0 to 128.

8.3.3 Transformations

The primitives above are defined with respect to a local coordinate system. The world coordinate system is expressed by a single matrix, specifying the transformation necessary to map the world coordinate system into the local coordinate system. Thus every rotation, translation, or scaling modifies only the transformation matrix. This approach is equivalent to the use of the *modelview matrix* in OpenGL.

The transformation matrix is set up using the commands:

Command	Description	
loadidentity	Set the transformation matrix to identity (i.e. equal to the local coor-	
	dinate system).	
loadmatrix $a_1 \ a_2 \ \ a_{16}$	Set the transformation matrix to a 4×4 matrix where a_1 - a_4 are the	
	values of the first column, a_5 - a_8 the second column, and so on.	
pushmatrix	Store the current transformation matrix on a matrix stack.	
popmatrix	Retrieve a matrix from the stack and set the transformation matrix to	
	these values.	

Transformations are then performed by modifying the current transformation matrix with the commands:

Command	Description
translate $tx \ ty \ tz$	Translate the local coordinate system by vector (tx, ty, tz) .
rotate $angle \ vx \ vy \ vz$	Rotate the coordinate system around vector (vx, vy, vz) by $angle$ degrees.
scale it sx sy sz	Scale the local coordinate system by factors sx , sy , and sz along the x ,
	y, and z axes respectively.
$\texttt{mulmatrix}\ a_1\ a_2\\ a_{16}$	Multiply the current transformation matrix by the specified matrix.

8.3.4 Lighting and projection

The -gls command line option outputs the geometry of the L-system string in the format described above. Thus, the geometry produced from one simulation can be included as a background scene in another simulation.

The output file may also include commands for lighting and projection, not required in a background file:

Command	Description
clear red green blue	The RGB components of the background color.
$\texttt{light}\ x\ y\ z\ w$	The light source, specified as four homogeneous coordi-
	nates of light position. If $w = 1$, the light is directional.
	The color of the light is always white.
ortho minx maxx miny maxy front back	An orthographic projection, where front and back are
	distances.
perspective $angle\ front\ back$	A perspective projection, where <i>angle</i> is the viewing an-
	gle, and $front$ and $back$ are distances.
${\tt lookat}\ posx\ posy\ posz$	The view: the camera position (pos), the view reference
refx refy refz upx upy upz	point (ref) and, optionally, the up vector (up) .
$\verb maxtrixmode mode $	The current matrix mode:
	0 = modelview matrix
	1 = projection matrix

8.3.5 Example of a background file

A background scene composed of a sphere, cone and box, all in grey, can be defined as follows:

```
material 0.1 0.1 0.1 1
                         /* subsequent surfaces are grey */
         0.16 0.21 0.27 1 /* with no specular reflections */
         0 0 0 1
                         /* and no emissive color */
         0 0 0 1
pushmatrix
translate 3 -20 -3
scale 1 0.7 0.7
sphere 15 /* ellipsoid */
popmatrix
pushmatrix
translate -14 -55.0 8
cone 15 2 14 /* cone */
popmatrix
translate -10 -65 0
box 30 5 30 /* box */
```

The file is preprocessed by cpfg , and therefore macros and comments are allowed.

8.4 TSURFACE SPECIFICATION FILE

An alternative to using a surface editor to create a surface as a bicubic patch (see the *vlab* Tools manual), is to define a set of triangles in a text file, using the same syntax as a *rayshade* output file. Each triangle is define by its three vertices (one per row), the normal to the vertice, and (optionally) the coordinates of a texture at the vertex:

```
\begin{array}{l} \texttt{triangle} \\ x_1 \ y_1 \ z_1 \ nx_1 \ ny_1 \ nz_1 \ u_1 \ v_1 \\ x_2 \ y_2 \ z_2 \ nx_2 \ ny_2 \ nz_2 \ u_2 \ v_2 \end{array}
```

```
x_3\ y_3\ z_3\ nx_3\ ny_3\ nz_3\ u_3\ v_3
```

where x_n , y_n and z_n are the coordinates of the vertex, nx_n , ny_n and nz_n specify the normal to the vertex, and u_n and v_n are the coordinates of the texture at the vertex. For example, two triangles without texture coordinates could be specified as:

```
triangle
-0.5 1 0 0 0 1
0.0 2 0 0 0 1
0.5 1 0 0 0 1
triangle
0.5 1 0 0 0 1
0.0 0 0 0 0 1
-0.5 1 0 0 0 1
```

and with added texture coordinates:

```
triangle
-0.5 1 0 0 0 1 0.5 0.0
0.0 2 0 0 0 1 1.0 0.5
0.5 1 0 0 0 1 0.5 1.0
triangle
0.5 1 0 0 0 1 0.5 1.0
0.0 0 0 0 0 1 0.5 0.5
-0.5 1 0 0 0 1 0.5 0.0
```

9 APPENDIX: DEPRECATED / UNDOCUMENTED FEATURES

The following features are no longer tested or supported, but may exist in older models.

9.1 Command line arguments

The following command line arguments are no longer in use:

Feature	Description	Use instead
-c <i>mapnr</i>	Define the 256-entry portion of the color or material table to be used.	-m and -M (Section 1.2.2)
-C commstr	Specify connections to other processes in a distributed simulation. Not available for Mac iOS.	
-mb	Create a menu bar, as well as the pop-up menu.	
-pipestrb	Convert a binary L-system string from <i>stdin</i> into a format specified by one of the output file options.	
-pm	Use X pixmap as back buffer.	
-sstrsize	Define the initial space allotment for a string generated by an L-system.	
-S socketno	Define the socket number to be used to receive menu commands from external programs.	File monitoring using Refresh mode (Sections 1.2.1 and 1.3.2)
-sb	Set to single buffering during animation.	double buffer command in the Animation file (Section 8.2)

9.2 Derivation Length

The functions GetDerivationLength(dummy) and SetDerivationLength(s) are no longer supported. If the derivation length is required within the L-system, it can be defined. For example:

```
#define DERIV 50
...
derivation length: DERIV
...
A(x): x < DERIV - 10 --> A(x+1)
A(x): x >= DERIV - 10 --> A(x+1)B
```

There is no functionality to change the derivation length during execution of *cpfg*, but it is possible to end before the final derivation step using the **stop** function (Section 5.6), and to end an animation earlier using the **last frame** command in the animation file (Section 8.2).

9.3 Substring Changes

The modules %(par) and %(par, turtle-index) to move a substring but save its position (the turtle parameters) are no longer supported. The %(par) functionality enabled a substring between % and %(par) to be moved to the end of the string, preceded by %(par, turtle-index), where turtle-index was a position in a special turtle array that stored the turtle parameters as they were when the module %(par) was encountered. After the substring was moved to the end of the L-system string, each time a module %(par, turtle-index) was encountered in the following interpretation steps, the turtle parameters were set to the values stored in the turtle array under turtle-index. This functionality is similar to the branching modules [and] (Section 6.4) without moving the substring.

The module % alone is still available to cut a branch from the string (Section 6.4). However, the module @mc(flag) to conditionally cut the remainder of a branch depending on the value of flag is no longer supported.

9.4 Rayshade functionality

It is possible to output a file in *rayshade* format using the Save As menu item (Section 1.3.2). However, specific *rayshade* functionality within L-system productions is no longer supported. This includes:

- The homomorphism production delimiter -o> to instantiate objects, as well as the rayshade objects command in the view file to set parameters for these objects.
- The rayshade scale command in the view file to scale objects.
- The module QJ(s1,s2,s3) to close the current grid for objects being output to rayshade, and start a new grid with the given size.
- The module QI("rayshade-object",s) to include a rayshade object at the current turtle location.

To match the scaling of *rayshade* objects generated by different L-systems use the view file command initial scale (Section 8.1.1).

9.5 System calls

The module QS("system-call") is not available for macOS systems.

10 Credits

Cpfg evolved from an earlier program, pfg (plant and fractal generator), developed by Przemyslaw Prusinkiewicz [5], extended from 2D to 3D by F. David Fracchia, and enhanced by Jim Hanan [6; 7] with input and guidance from Professor Aristid Lindenmayer [8]. The interface to rayshade [9] was developed under the guidance of Craig Kolb.

The extension to *cpfg* (*pfg* with **c**ontinuous parameters) was developed by Jim Hanan [10], based on ideas described in [1; 11]. Interactions with the environment were initiated with Mark James and Radomír Měch [4], and fully developed by Radomír Měch [3; 12]. Numerous further enhancements and improvements are due to Mark James, Mark Hammel, Radomír Měch [2], Brendan Lane, Jason Kraft and, most recently, by Pascal Ferraro and Mikolaj Cieslak.

11 DOCUMENT REVISION HISTORY

Date	Description	$\mathbf{B}\mathbf{y}$
1992	Original documentation	Jim Hanan
1994	Based on Version 2.0 of cpfg	Mark James
		Jim Hanan
		Przemyslaw Prusinkiewicz
1997	Based on Version 2.7 of cpfg	Mark James
		Mark Hammel
		Jim Hanan
		Radomír Měch
		Przemyslaw Prusinkiewicz
2016	Based on Version 4.0 of cpfg	Radomír Měch
		Radoslaw Karwowski
		Brendan Lane
2022	Updated to current version	Lynn Mercer
		Przemyslaw Prusinkiewicz
		Mikolaj Cieslak
		Pascal Ferraro

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- [2] Radomír Měch, Przemyslaw Prusinkiewicz, and James Hanan. Extensions to the graphical interpretation of L-systems based on turtle geometry. Technical Report 97/599/01, University of Calgary, Dept of Computer Science, 1997.
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