

# BACKTRACKING

## Types of Backtracking

- Decision
- Optimization
- Enumeration

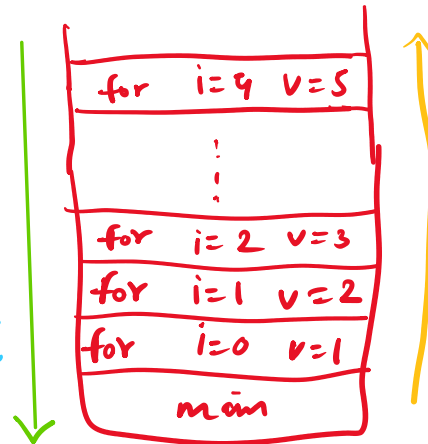
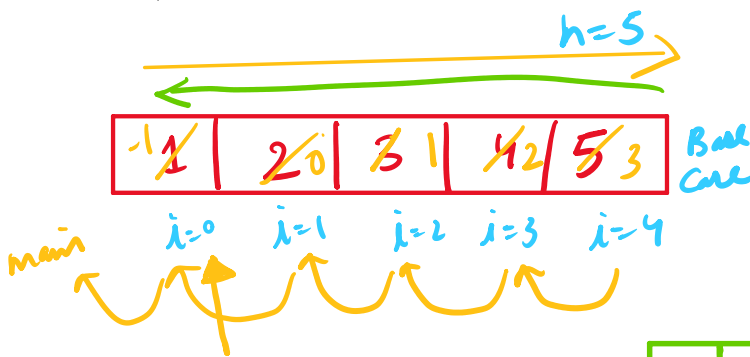
Shortest Path  
or  
Decision making

Yes/No Backtracking

From starting to ending  
how many paths are there.

1 | 2 | 3 | 4 | 5

## Backtracking - Arrays



- 

-1	0	1	2	3
----	---	---	---	---

```
public static void changeArr(int arr[], int i, int val) {
    //base case
    if(i == arr.length) {
        printArr(arr);
        return;
    }
    //recursion
    arr[i] = val;
    changeArr(arr, i+1, val+1);
    arr[i] = arr[i] - 2;
}
```

```

public static void changeArr(int arr[], int i, int val) {
    //base case
    if(i == arr.length) {
        printArr(arr);
        return;
    }
    //recursion
    arr[i] = val;
    changeArr(arr, i+1, val+1);
    arr[i] = arr[i] - 2;
}

```

```

public static void printArr(int arr[]){
    for(int i=0; i<arr.length; i++) {
        System.out.print(arr[i]+" ");
    }
    System.out.println();
}

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Run | Debug
public static void main(String args[]) {
    int arr[] = new int[5];
    changeArr(arr, 0, 1);
    printArr(arr);
}

```

APNA COLLEGE

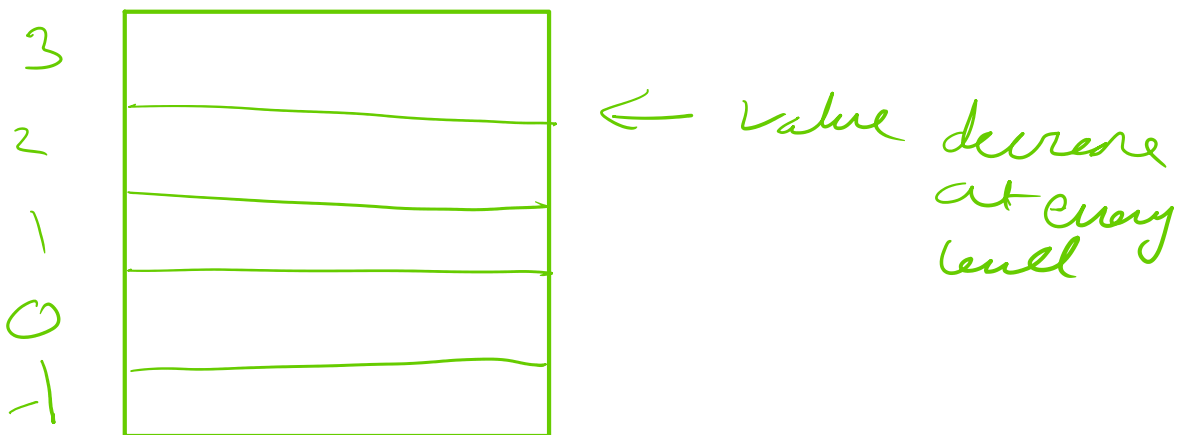
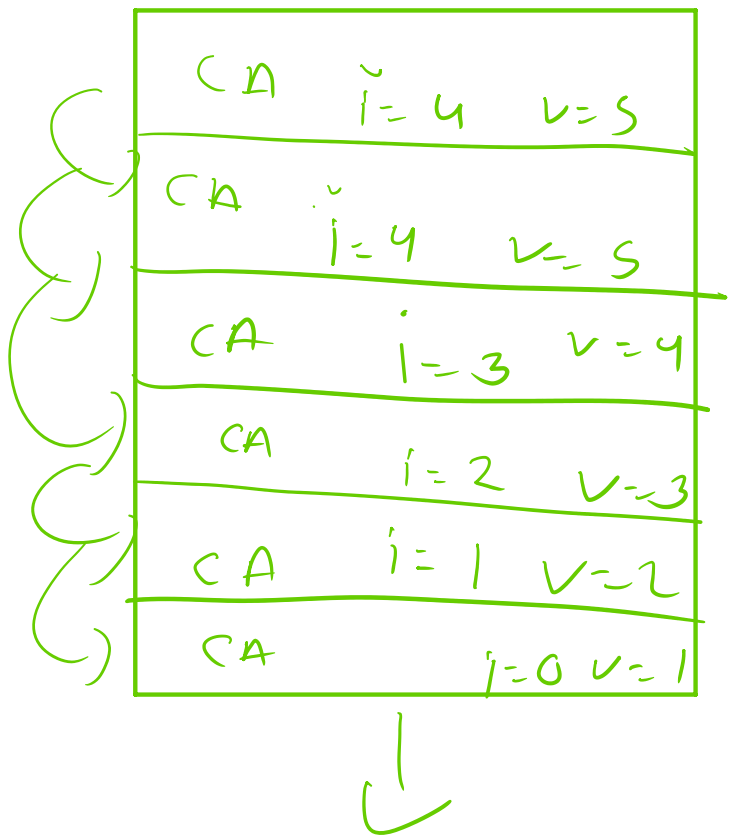
```

public static void changeArr(int arr[], int i, int val) {
    //base case
    if(i == arr.length) {
        printArr(arr);
        return;
    }

    //recursion
    → arr[i] = val; ✓
    → changeArr(arr, i+1, val+1); //fnx call step
    arr[i] = arr[i]-2; //backtracking step
}

```

Base case print arr



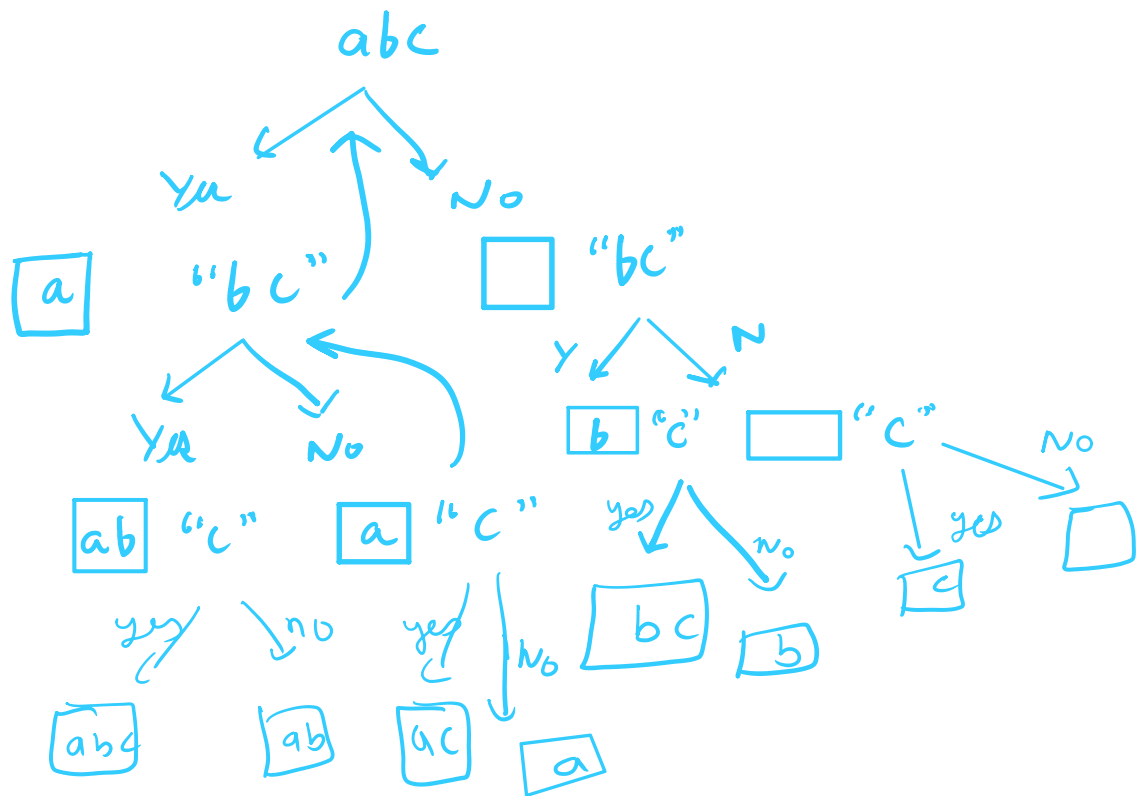
## \* Find Subsets

find & print all subsets of a given string

"abc"

"", "b", "c", "ab", "bc", "ac", "abc", ""

$a, b, c, ab, bc, ac, abc,$   
 $\downarrow$   
 $\emptyset$  (null set)



find subsets(str, ans)

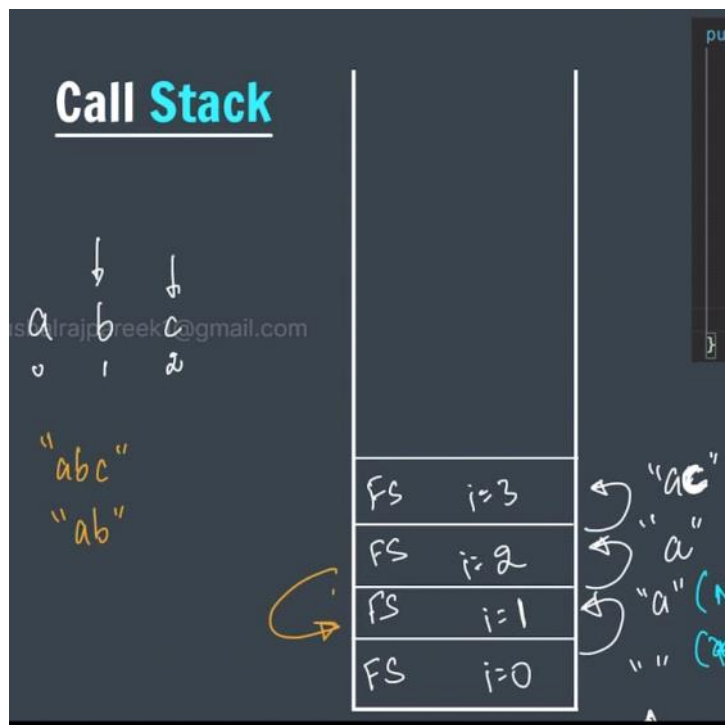
Select one Time  $\rightarrow$  ans + str.charAt(i) } recursive calls  
 don't select  $\rightarrow$  ans

```

public static void findSubsets(String str, String ans, int i) {
    //base case
    if(i == str.length()) {
        System.out.println(ans);
        return;
    }

    //Yes choice
    findSubsets(str, ans+str.charAt(i), i+1);
    //No choice
    findSubsets(str, ans, i+1);
}

```



You can draw stack just follow recursion tree.

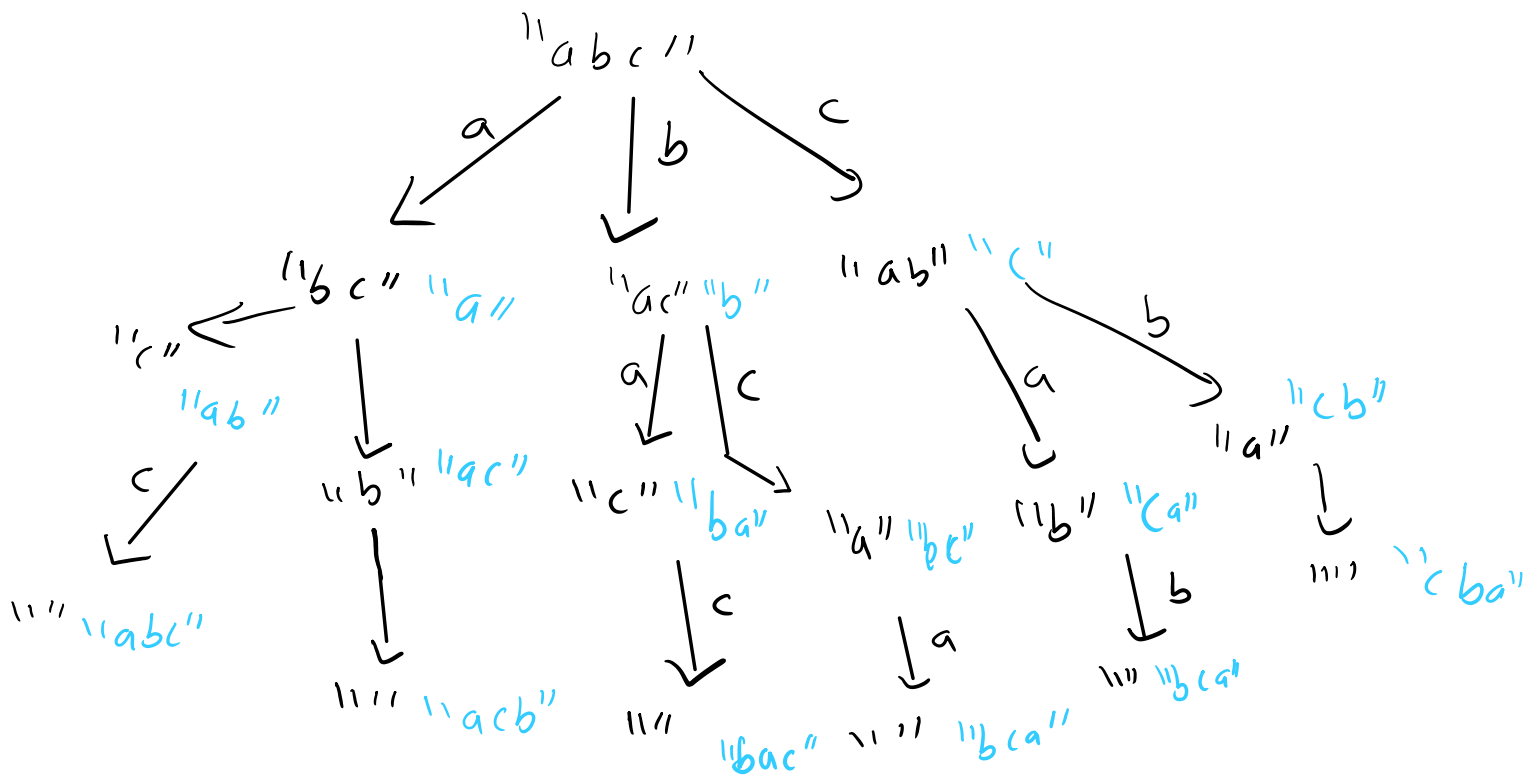
X ————— X

Find Permutations

Find & print all permutations of a String.

"abc"

abc, acb, bac, bca, cab, cba



```
public static void findPermutation(String str, String ans) {
    //base case
    if(str.length() == 0) {
        System.out.println(ans);
        return;
    }
    //recursion
    for(int i=0; i<str.length(); i++){
        char curr = str.charAt(i);
        // "abcde" => "ab" + "de" = "abde"
        String NewStr = str.substring(0, i) + str.substring(i+1);
        findPermutation(NewStr, ans+curr);
    }
}
```



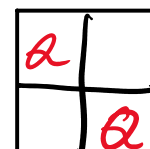
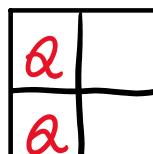
## N-Queens

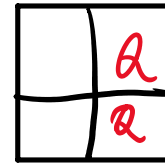
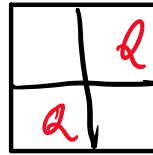
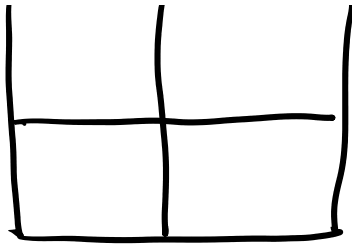
Place  $N$  queens on an  $N \times N$  chessboard such that no 2 queens can attack each other

$N=4$

	0	1	2	3
0			Q	
1	Q			
2				Q
3		Q		

$N=2$





```
public static void nQueens(char board[][], int row) {
    //base
    if(row == board.length) {
        printBoard(board);
        return;
    }
    //column loop
    for(int j=0; j<board.length; j++) {
        if(isSafe(board, row, j)) {
            board[row][j] = 'Q';
            nQueens(board, row+1); //function call
            board[row][j] = 'x'; //backtracking step
        }
    }
}
```

```
public static void printBoard(char board[][]) {
    System.out.println("----- chess board -----");
    for(int i=0; i<board.length; i++) {
        for(int j=0; j<board.length; j++) {
            System.out.print(board[i][j] + " ");
        }
        System.out.println();
    }
}
```

```
//diag right up
for(int i=row-1, j=col+1; i>=0 && j<board.length; i--,j++) {
    if(board[i][j] == 'Q') {
        return false;
    }
}
```



```

public static boolean isSafe(char board[][], int row, int col) {
    //vertical up
    for(int i=row-1; i>=0; i--) {
        if(board[i][col] == 'Q') {
            return false;
        }
    }
}

```

```

public static void main(String args[]) {
    int n = 4;
    char board[][] = new char[n][n];
    //initialize
    for(int i=0; i<n; i++) {
        for(int j=0; j<n; j++) {
            board[i][j] = 'x';
        }
    }
}

```

```

//diag left up
for(int i=row-1, j=col-1; i>=0 && j>=0; i--,j--) {
    if(board[i][j] == 'Q') {
        return false;
    }
}

```

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$$T(n) = 1 \text{ queen place} \times T(n-1) + \text{isSafe}()$$

↓  
O(n)

$$T(n) = n \times T(n-1) + \text{isSafe}()$$

Time Complexity ( $O(n!)$ )

\* N Queens - Time Complexity

N - Queens Total ways count:-

```
public static void nQueens(char board[][], int row) {  
    //base  
    if(row == board.length) {  
        // printBoard(board);  
        count++;  
        return;  
    }  
}
```

Print Exactly one Pair:-

```

public static boolean nQueens(char board[][], int row) {
    //base
    if(row == board.length) {
        //printBoard(board);
        count++;
        return true;
    }

    //column loop
    for(int j=0; j<board.length; j++) {
        if(isSafe(board, row, j)) {
            board[row][j] = 'Q';
            if(nQueens(board, row+1)){
                return true;
            }
            board[row][j] = 'x'; //backtracking step
        }
    }

    return false;
}

```

```

if(nQueens(board, 0)) {
    System.out.println("solution is possible");
    printBoard(board);
} else {
    System.out.println("solution is not possible");
}

// System.out.println("total ways to solve n queens =

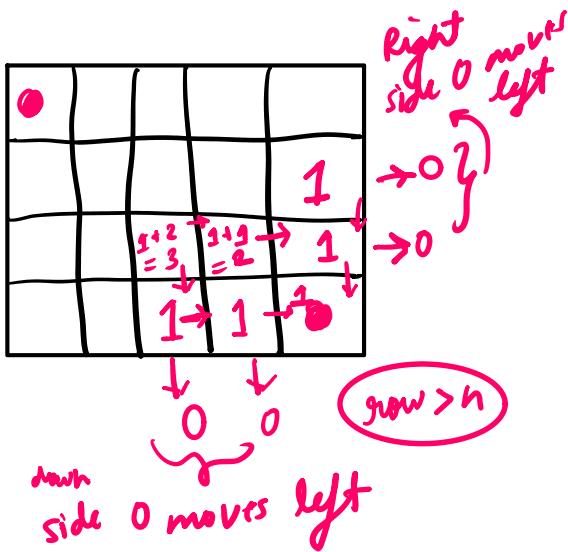
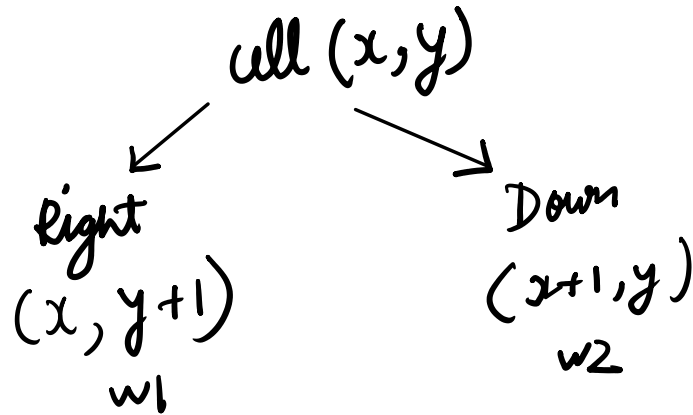
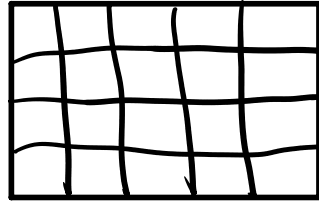
```

Grid ways :-→

Find number of ways to reach from (0,0)  
to (N-1, M-1) in a N x M Grid.

Allowed moves - right or down

Allowed move - right & down



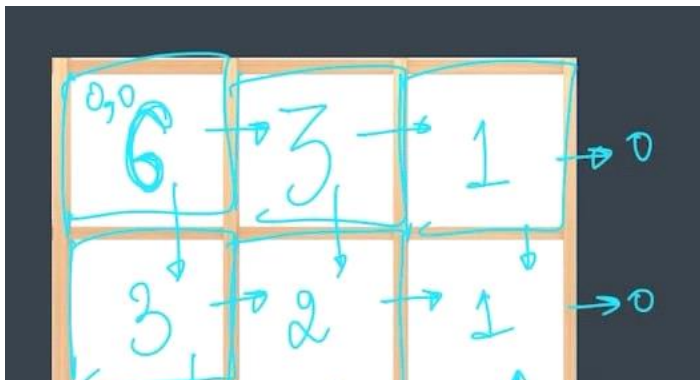
$w_1 + w_2 = \text{total ways}$

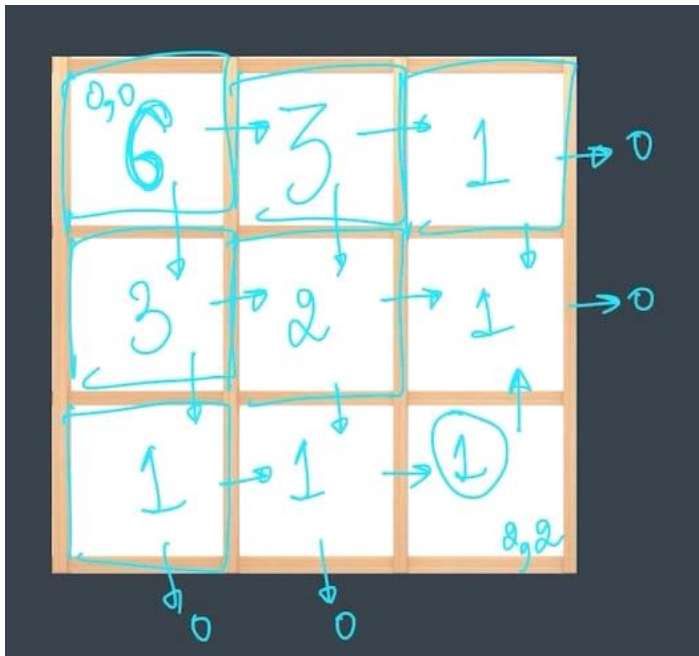
$$f(x, y) = f(x+1, y) + f(x, y+1)$$

(Down)  $f(x, y)$       (Right)  $f(x, y+1)$

Time complexity Grid ways =

$2^{n+m}$





```

public class Classroom {
    public static int gridWays(int i, int j, int n, int m) {
        //base case
        if(i == n-1 && j == m-1) { //condn for last cell
            return 1;
        } else if(i == n || j == m) {
            return 0;
        }

        int w1 = gridWays(i+1, j, n, m);
        int w2 = gridWays(i, j+1, n, m);
        return w1 + w2;
    }

    Run | Debug
    public static void main(String args[]) {
        int n = 3, m = 3;
        System.out.println(gridWays(0, 0, n, m));
    }
}

```

Sudoku :->

		8						
4	9		1	5	7			2
		3			4	1	9	
1	8	5		6			2	
				2			6	
9	6		4		5	3		
	3			7	2			4

		8						
4	9		1	5	7			2
		3			4	1	9	
1	8	5		6			2	
				2			6	
9	6		4		5	3		
	3			7	2			4
	4	9		3			5	7
8	2	7			9		1	3

Sudoku

Calculating Grid

column

for (int i = 0 to 8)

s[i][col] == digit → false

Row

for (int j = 0 to 8)

s[row][j] == digit → false

0 1 2

grid(3x3)

		8						
4	9		1	5	7			2
		3			4	1	9	
1	8	5		6			2	
				2			6	
9	6		4		5	3		
	3			7	2			4
	4	9		3			5	7
8	2	7			9		1	3

row

column

(3,3)

row = 4

col = 5

sr = (4/3) \* 3

sr = 3

sc = (5/3) \* 3

sc = 3

Calculating Grid (row, col) → 3x3 grid (sr, sc)

sr = (row/3) \* 3

sc = (col/3) \* 3





SC = 0, 1, 2

0 1 2 0 1 2

```
public class Classroom {
    public static boolean isSafe(int sudoku[][], int row, int col, int digit) {
        //column
        for(int i=0; i<=8; i++) {
            if(sudoku[i][col] == digit) {
                return false;
            }
        }

        //row
        for(int j=0; j<=8; j++) {
            if(sudoku[row][j] == digit) {
                return false;
            }
        }
    }
}
```

```
//grid
int sr = (row/3) * 3;
int sc = (col/3) * 3;
//3x3 grid
for(int i=sr; i<sr+3; i++) {
    for(int j=sc; j<sc+3; j++) {
        if(sudoku[i][j] == digit) {
            return false;
        }
    }
}

return true;
}
```

```
public static boolean sudokuSolver(int sudoku[][], int row, int col) {
    //base case
    if(row == 9 && col == 0) {
        return true;
    }

    //recursion
    int nextRow = row, nextCol = col+1;
    if(col+1 == 9) {
        nextRow = row+1;
        nextCol = 0;
    }

    if(sudoku[row][col] != 0) {
        return sudokuSolver(sudoku, nextRow, nextCol);
    }

    for(int digit=1; digit<=9; digit++) {
        if(isSafe(sudoku, row, col, digit)) {
            sudoku[row][col] = digit;
        }
    }
}
```

```

    if(sudoku[row][col] != 0) {
        return sudokuSolver(sudoku, nextRow, nextCol);
    }

    for(int digit=1; digit<=9; digit++) {
        if(isSafe(sudoku, row, col, digit)) {
            sudoku[row][col] = digit;
            if(sudokuSolver(sudoku, nextRow, nextCol)) { //soln exists
                return true;
            }
            sudoku[row][col] = 0;
        }
    }

    return false;
}

```

```

public static void printSudoku(int sudoku[][]) {
    for(int i=0; i<9; i++) {
        for(int j=0; j<9; j++) {
            System.out.print(sudoku[i][j]+" ");
        }
        System.out.println();
    }
}

```

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