

# Petri Nets I



# Definition of Petri Net

## ■ $C = (P, T, I, O)$

- Places

$$P = \{p_1, p_2, p_3, \dots, p_n\}$$

- Transitions

$$T = \{t_1, t_2, t_3, \dots, t_n\}$$

- Input

$$I : T \rightarrow P^r \text{ (r = number of places)}$$

- Output

$$O : T \rightarrow P^q \text{ (q = number of places)}$$

■ marking  $\mu$  : assignment of tokens to the places of Petri net  $\mu = \mu_1, \mu_2, \mu_3, \dots, \mu_n$

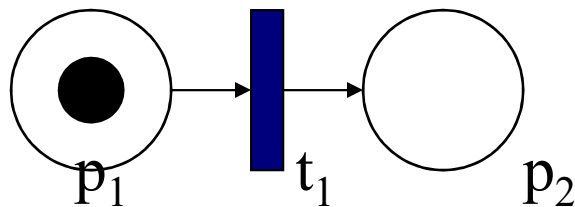


# Applications of Petri Net

- Petri net is primarily used for studying the dynamic concurrent behavior of network-based systems where there is a discrete flow.
- Petri Nets are applied in practice by industry, academia, and other places. [-reference](#)

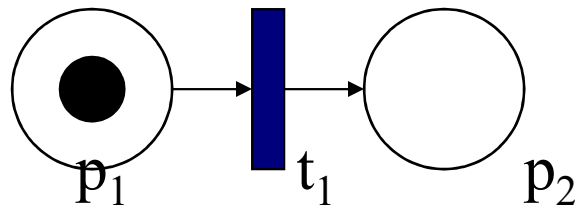
## Basics of Petri Nets

- Petri net consist two types of nodes: *places* and *transitions*. And arc exists only from a place to a transition or from a transition to a place.
- A place may have zero or more *tokens*.
- Graphically, places, transitions, arcs, and tokens are represented respectively by: circles, bars, arrows, and dots.



## Basics of Petri Nets -continued

- Below is an example Petri net with two places and one transaction.
- Transition node is ready to **fire** if and only if there is at least one token at each of its input places



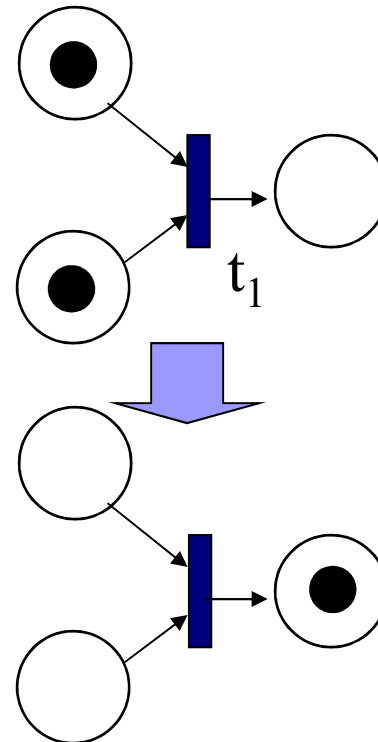
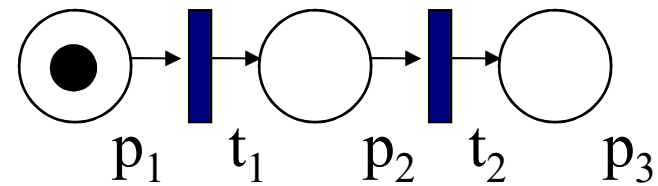
state transition of form  $(1, 0) \rightarrow (0, 1)$

$p_1$  : input place

$p_2$ : output place

## Properties of Petri Nets

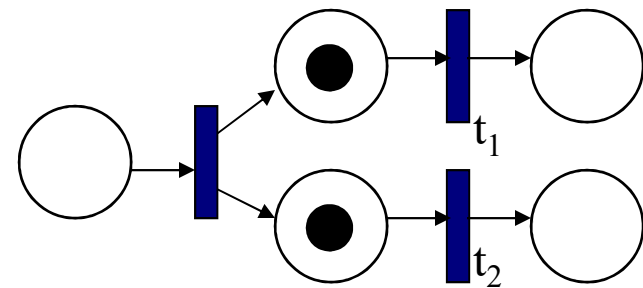
- **Sequential Execution**  
Transition  $t_2$  can fire only after the firing of  $t_1$ . This imposes the precedence of constraints " $t_2$  after  $t_1$ ."
- **Synchronization**  
Transition  $t_1$  will be enabled only when a token is present at each of its input places.
- **Merging**  
Happens when tokens from several places arrive for service at the same transition.



## Properties of Petri Nets -continued

### ■ Concurrency

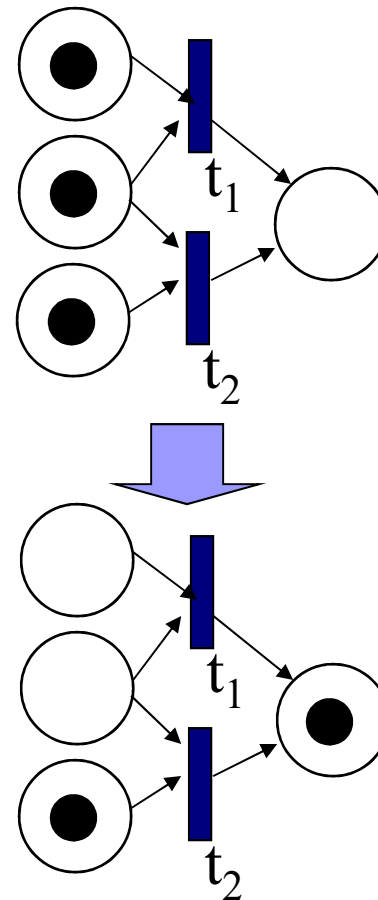
$t_1$  and  $t_2$  are concurrent.  
- with this property, Petri net is able to model systems of distributed control with multiple processes executing concurrently in time.



## Properties of Petri Nets -continued

### ■ Conflict

$t_1$  and  $t_2$  are both ready to fire but the firing of any leads to the disabling of the other transitions.



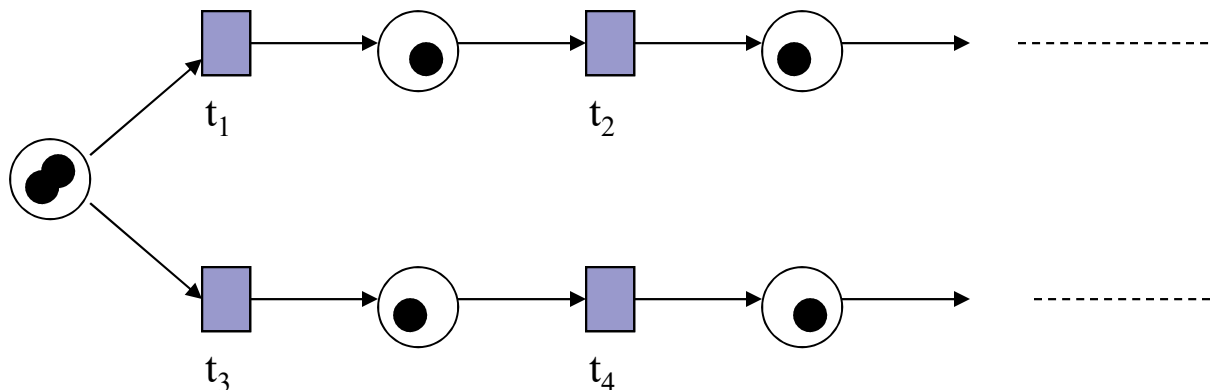


## Properties of Petri Nets -continued

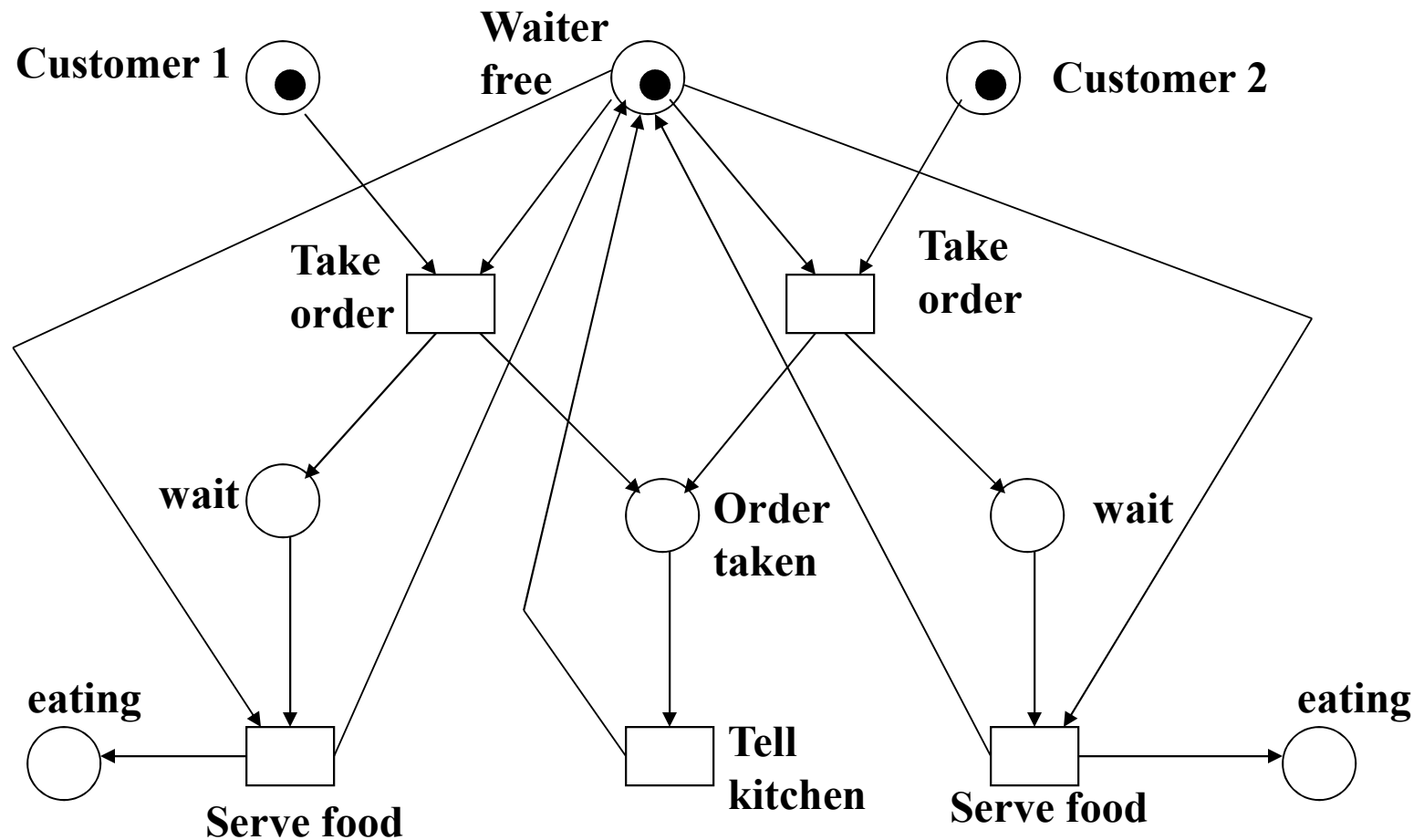
### ■ Conflict - continued

- the resulting conflict may be resolved in a purely non-deterministic way or in a probabilistic way, by assigning appropriate probabilities to the conflicting transitions.

there is a choice of either  $t_1$  and  $t_2$ , or  $t_3$  and  $t_4$



# Example: In a Restaurant (A Petri Net)





## Example: In a Restaurant (Two Scenarios)

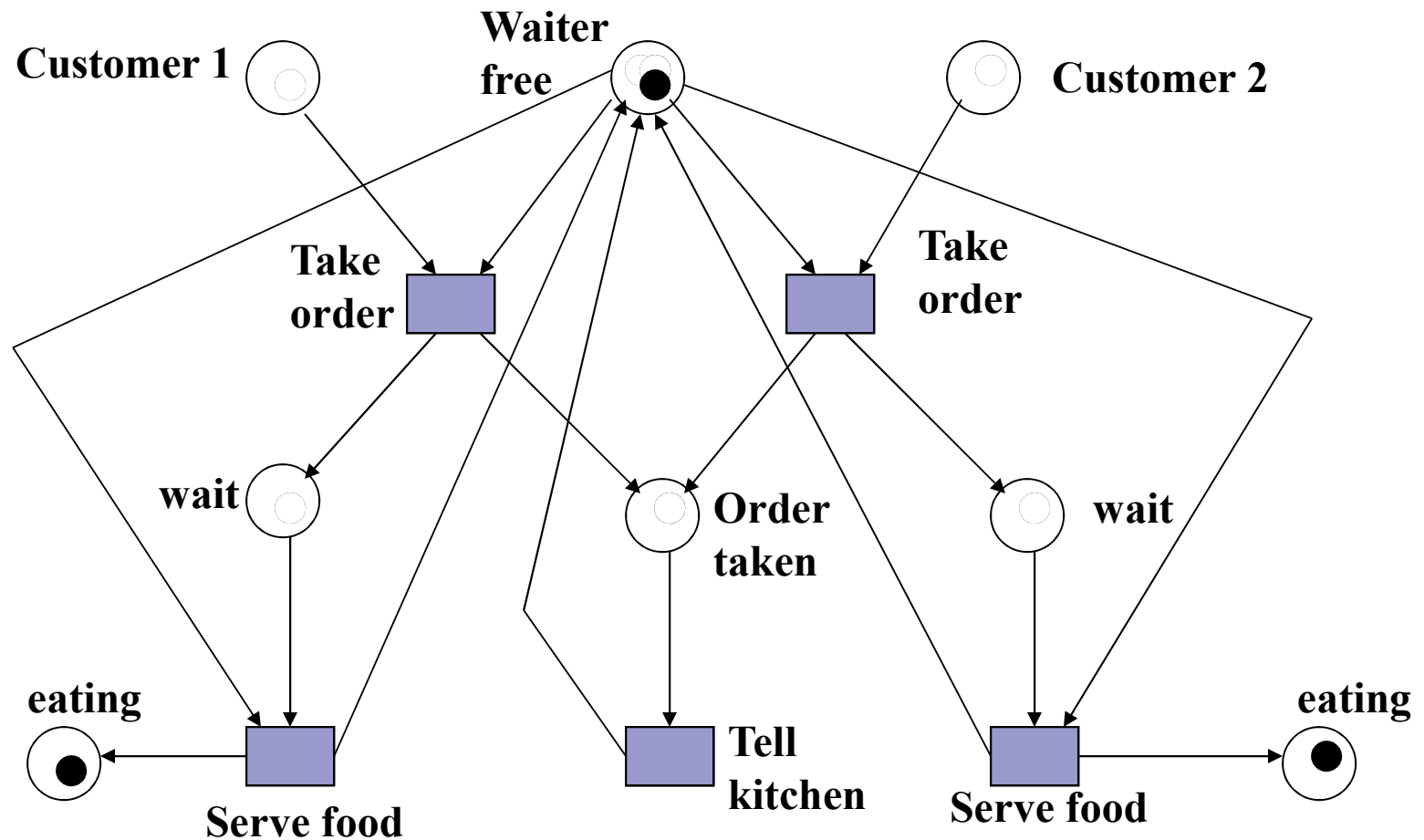
- Scenario 1:

- Waiter takes order from customer 1; serves customer 1; takes order from customer 2; serves customer 2.

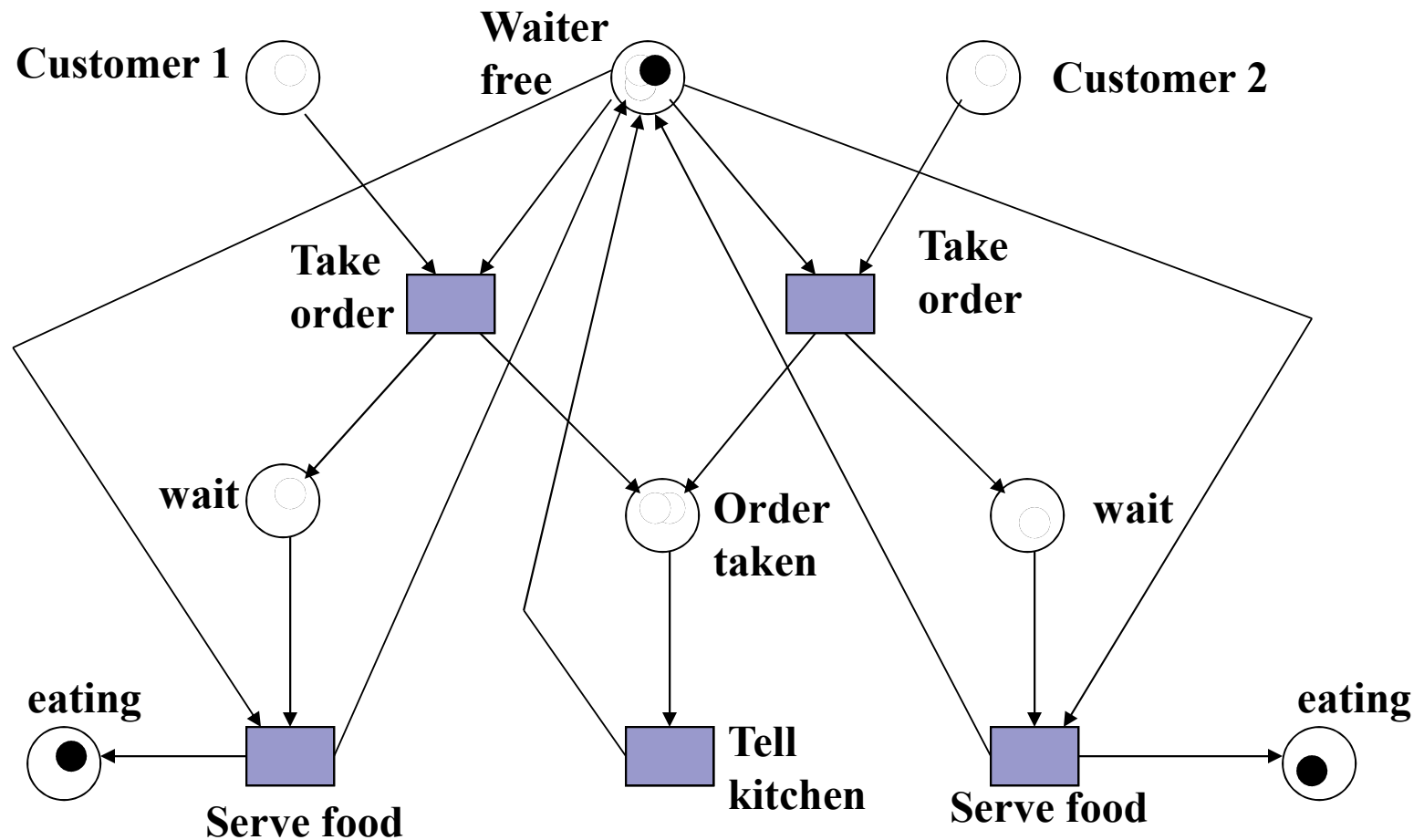
- Scenario 2:

- Waiter takes order from customer 1; takes order from customer 2; serves customer 2; serves customer 1.

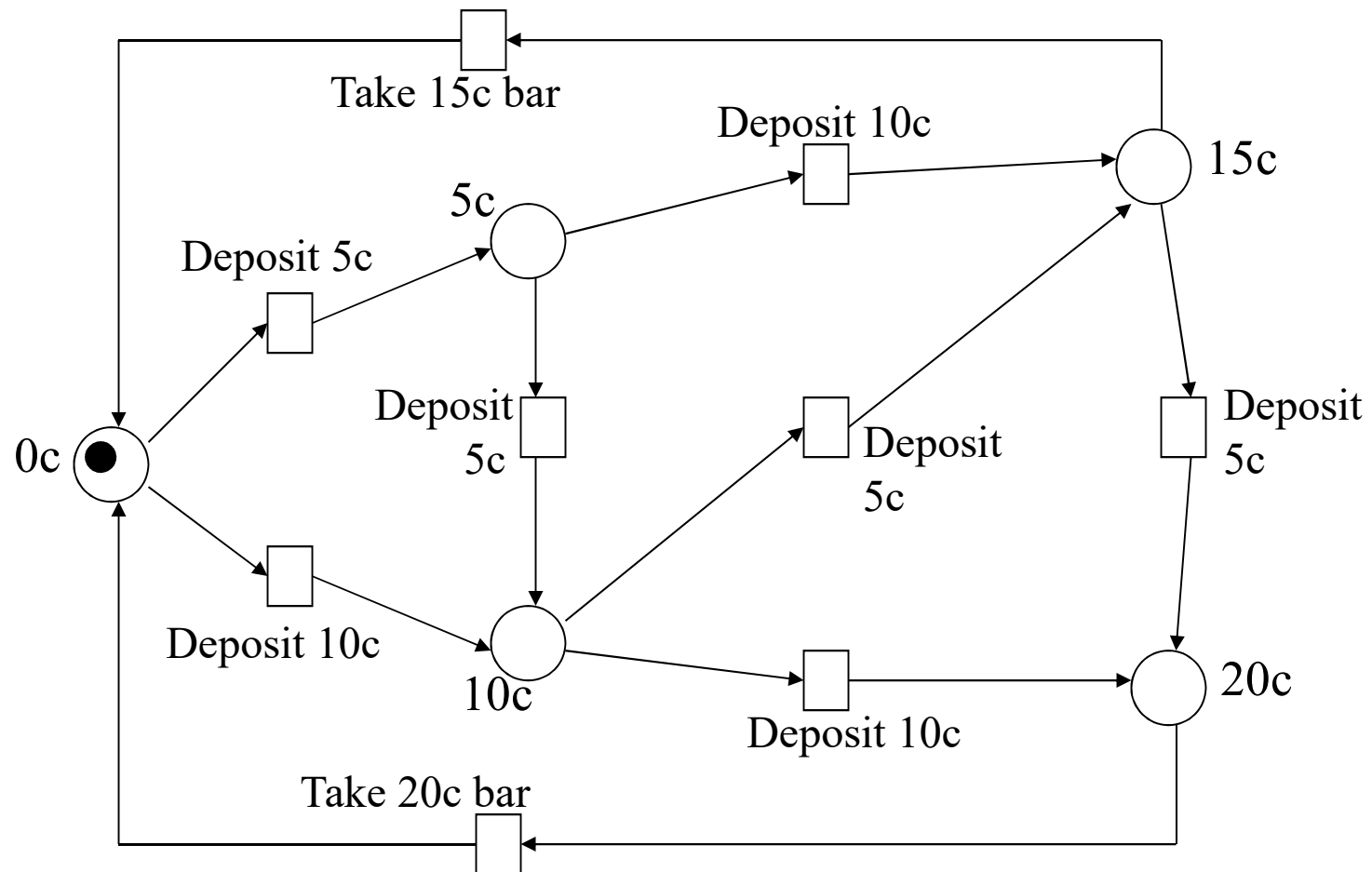
## Example: In a Restaurant (Scenario 1)



## Example: In a Restaurant (Scenario 2)



## Example: Vending Machine (A Petri net)





## Example: Vending Machine (3 Scenarios)

### ■ Scenario 1:

- Deposit 5c, deposit 5c, deposit 5c, deposit 5c, take 20c snack bar.

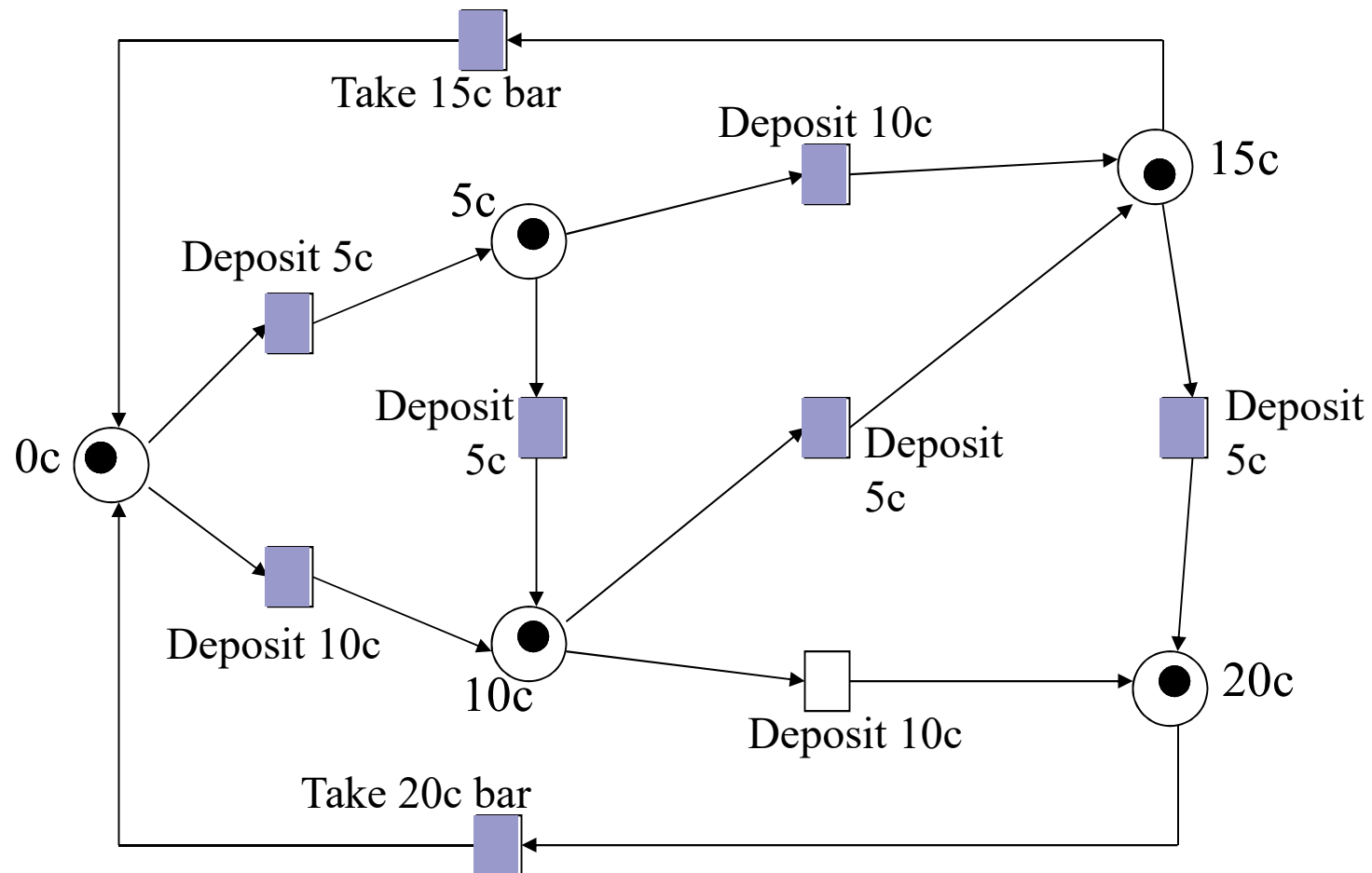
### ■ Scenario 2:

- Deposit 10c, deposit 5c, take 15c snack bar.

### ■ Scenario 3:

- Deposit 5c, deposit 10c, deposit 5c, take 20c snack bar.

## Example: Vending Machine (Token Games)





# Petri Net examples

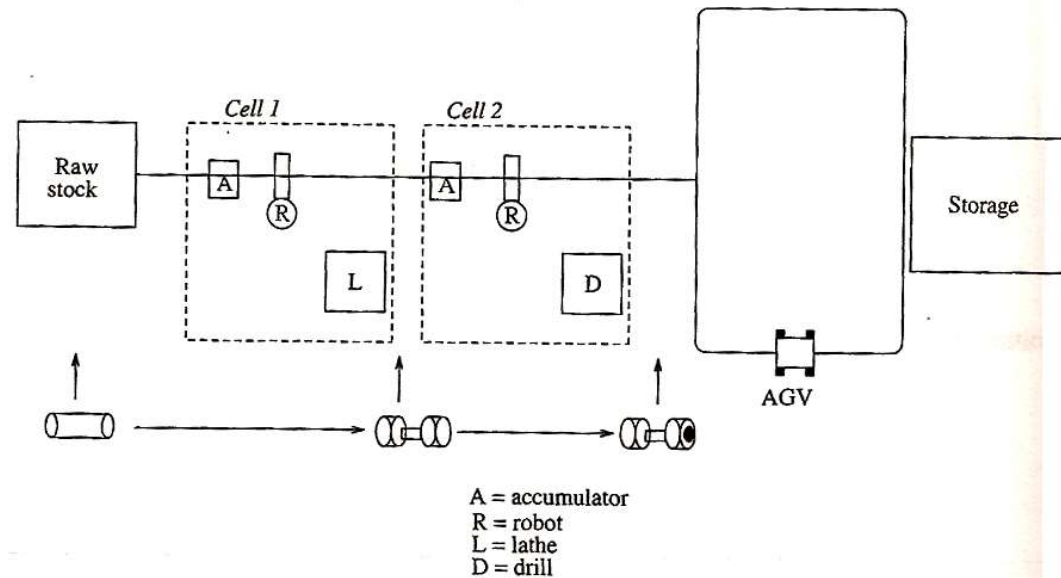


Figure 4.40 Manufacturing line with two robots and two machines.

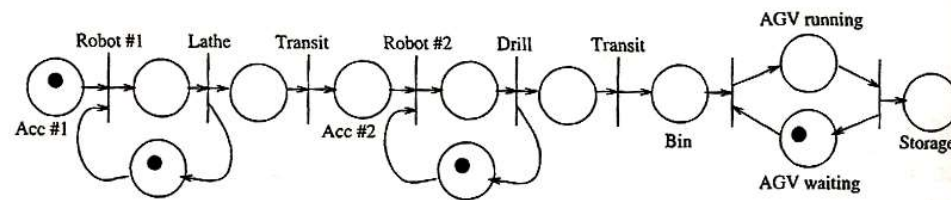


Figure 4.41 Petri net for manufacturing line.

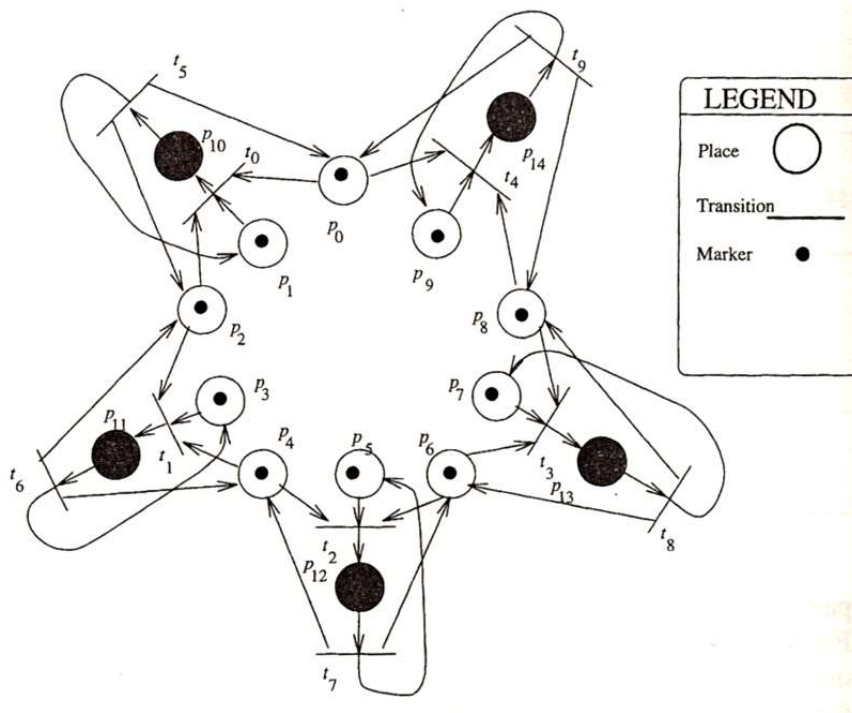


Dining Philosophers Problem States that there are 5 Philosophers who are engaged in two activities Thinking and Eating. Meals are taken communally in a table with five plates and five forks in a cyclic manner as shown in the figure.

**Constraints and Condition for the problem :**

1. Every Philosopher needs two forks in order to eat.
2. Every Philosopher may pick up the forks on the left or right but only one fork at once.
3. Philosophers only eat when they had two forks. We have to design such a protocol i.e. pre and post protocol which ensures that a philosopher only eats if he or she had two forks.
4. Each fork is either clean or dirty.

# Petri Net examples (Dining Philosophers)



- Five philosophers alternatively think and eating
- Chopsticks:  
 $p_0, p_2, p_4, p_6, p_8$
- Philosophers eating:  
 $p_{10}, p_{11}, p_{12}, p_{13}, p_{14}$
- Philosophers thinking/meditating:  
 $p_1, p_3, p_5, p_7, p_9$



# Petri Net with Time

- 1962 - Carl Adam Petri originally proposed Petri without any notion of time. Concept of time was intentionally avoided because addition of time restricts the behavior of the net.
- 1970s ~ - Addition of time has been discussed in order to analyze the performance of the modeled system.
- Many properties are still undecided for Petri nets extended with data and time.



# References

- Fishwick, Paul(1995) – Simulation Model Design and Execution
- [Petri Nets World](#)
- Ling,Chris(2001) – Lecture on Petri Nets Method
- Chapman, Nick(1997) – Surprise97 journal on Petri Nets Models