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function [V, X, t] = myBlackScholes(r, sigma, X_0, X_T, K, T, M, N)
% This function computes the solution to the Black-Scholes PDE using
% the Crank-Nicolson finite difference method.
%
% INPUTS:
% r:      risk-free interest rate
% sigma:  volatility of the underlying asset
% X_0:    initial underlying asset price
% X_T:    initial underlying asset price
% K:      strike price
% T:      time to maturity
% M:      number of underlying asset price grid points
% N:      number of time grid points
%
% OUTPUTS:
% V:      option prices (M+1 x N+1 matrix)
% X:      stock prices (M+1 x 1 vector)
% t:      time points (N+1 x 1 vector)

% Compute parameters
dx = (X_T - X_0) / M;
dt = T / N;
u = @(p) 0.25 * dt * ((sigma^2 * p.^2) - (r * p));
v = @(p) 0.5 * dt * ((sigma^2 * p.^2) + r);
w = @(p) 0.25 * dt * ((sigma^2 * p.^2) + (r * p));

% Initialize matrices
V = zeros(M+1, N+1);
X = (0:M)' * dx;
t = (0:N)' * dt;

% Set boundary conditions
V(:, end) = max(X - K, 0);
V(1, :) = 0;
V(end, :) = max(X - K * exp(-r * (T - t)));

% Set up tridiagonal matrix
A = diag(1 + v(1:M-1)) - diag(u(2:M-1), -1) - diag(w(1:M-2), 1);
B = diag(1 - v(1:M-1)) + diag(u(2:M-1), -1) + diag(w(1:M-2), 1);

% Iterate through time steps backwards and compute call
% option prices implicitly
for n = N:-1:1
    % boundary set for previous time
    b = zeros(M-1, 1);
    b(1) = -u(1) * V(1, n);
    b(end) = -w(M-1) * V(end, n);

    % boundary set for current time

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c = zeros(M-1,1);  
c(1) = u(1) * V(1, n);  
c(end) = w(M-1) * V(end, n);  
  
% solve for previous time  
V(2:M, n) = A \ ((B * V(2:M, n+1)) + c - b);
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end
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end
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