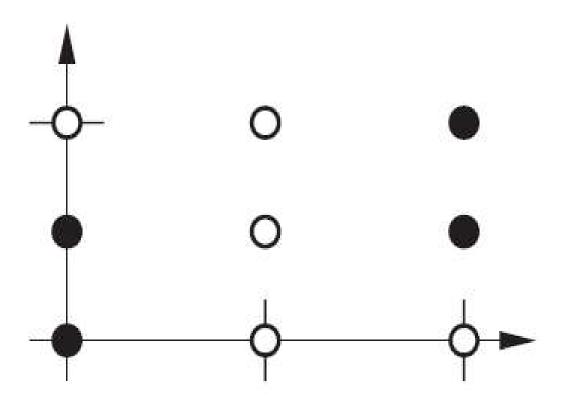
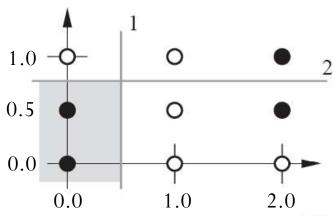
Example



Elementary Decision Boundaries



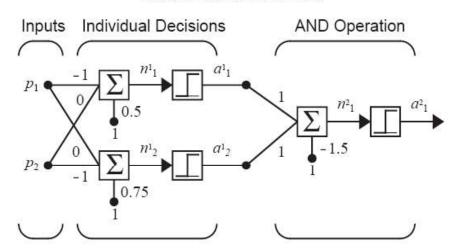
First Boundary:

$$a_1^1 = hardlim(\begin{bmatrix} -1 & 0 \end{bmatrix} \mathbf{p} + 0.5)$$

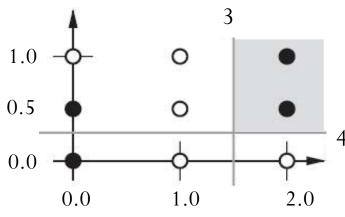
Second Boundary:

$$a_2^1 = hardlim(\begin{bmatrix} 0 \\ -1 \end{bmatrix} \mathbf{p} + 0.75)$$

First Subnetwork



Elementary Decision Boundaries



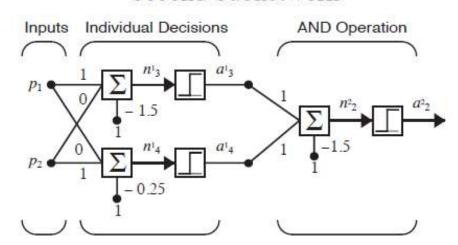
Third Boundary:

$$a_3^1 = hardlim(\begin{bmatrix} 1 & 0 \end{bmatrix} \mathbf{p} - 1.5)$$

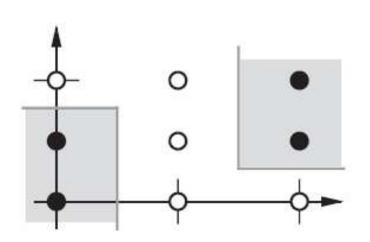
Fourth Boundary:

$$a_4^1 = hardlim(\begin{bmatrix} 0 & 1 \end{bmatrix} \mathbf{p} - 0.25)$$

Second Subnetwork



Total Network



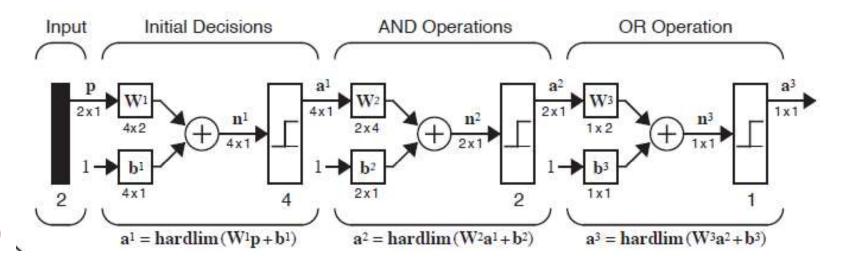
$$\mathbf{W}^{1} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} \qquad \mathbf{b}^{1} =$$

$$\mathbf{W}^2 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \qquad \mathbf{b}^2 = \begin{bmatrix} -1.5 \\ -1.5 \end{bmatrix}$$

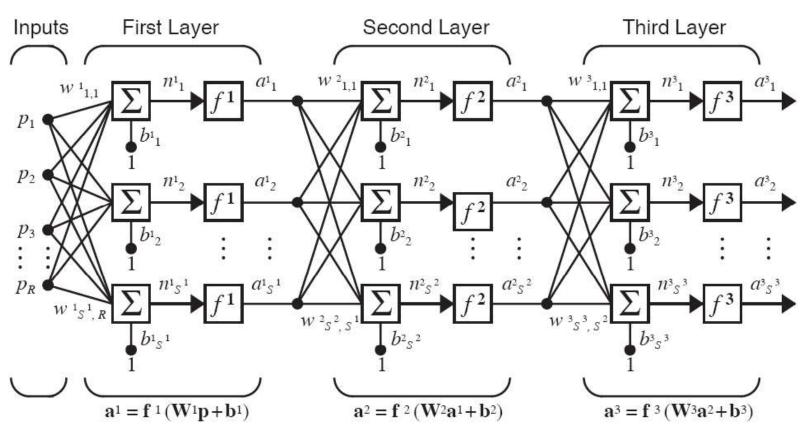
$$\mathbf{b}^2 = \begin{bmatrix} 1.5 \\ -1.5 \end{bmatrix}$$

$$\mathbf{W}^3 = \begin{bmatrix} 1 & 1 \end{bmatrix} \qquad \mathbf{b}^3 = \begin{bmatrix} -0.5 \end{bmatrix}$$

$$b^3 = \begin{bmatrix} -0.5 \end{bmatrix}$$



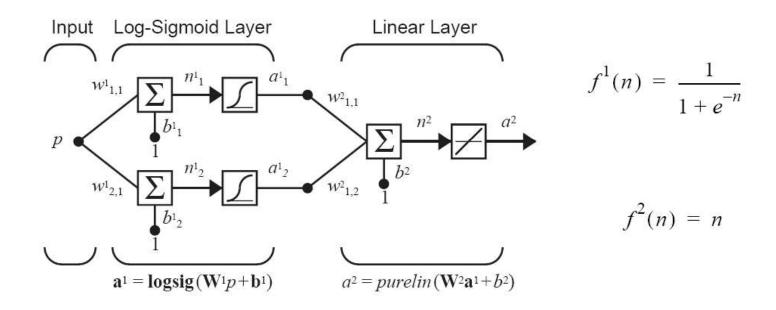
Multilayer Perceptron



$$\mathbf{a}^3 = \mathbf{f}^3 (\mathbf{W}^3 \mathbf{f}^2 (\mathbf{W}^2 \mathbf{f}^1 (\mathbf{W}^1 \mathbf{p} + \mathbf{b}^1) + \mathbf{b}^2) + \mathbf{b}^3)$$

$$R - S^1 - S^2 - S^3$$
 Network

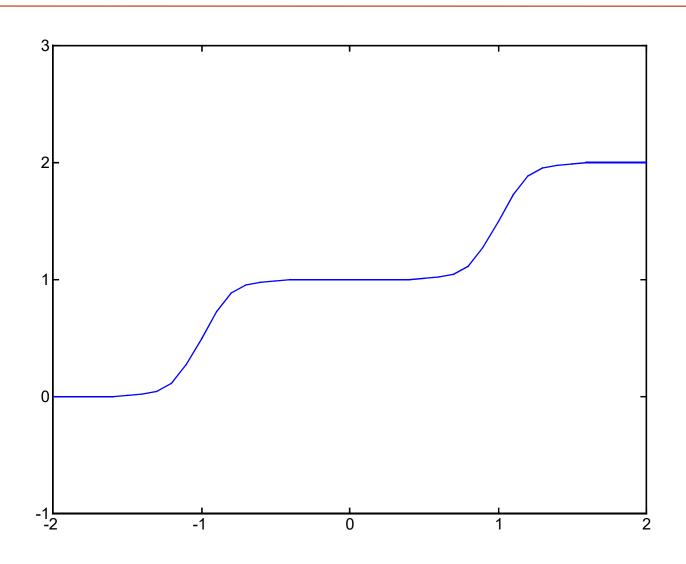
Function Approximation Example



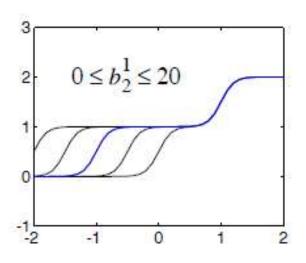
Nominal Parameter Values

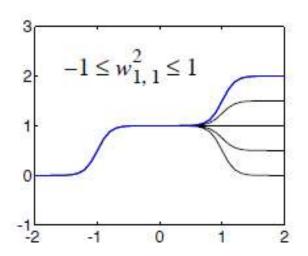
$$w_{1,1}^{1} = 10$$
 $w_{2,1}^{1} = 10$ $b_{1}^{1} = -10$ $b_{2}^{1} = 10$ $w_{1,1}^{2} = 1$ $b^{2} = 0$

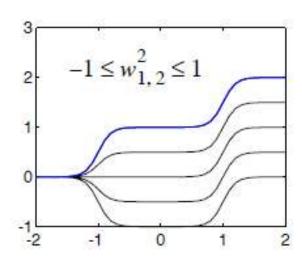
Nominal Response

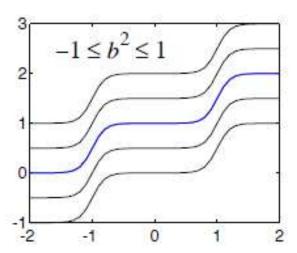


Parameter Variations

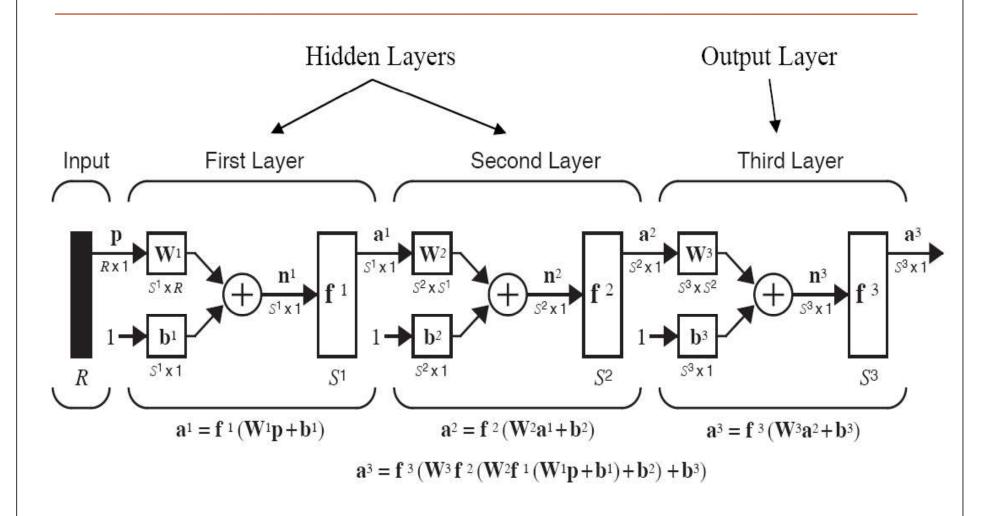






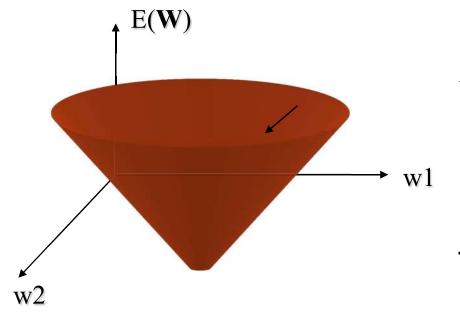


Multilayer Network



الگوریتم Gradient descent

با توجه به نحوه تعریف E، سطح خطا به صورت یک سهمی خواهد بود. ما به دنبال وزنهایی هستیم که حداقل خطا را داشته باشند . الگوریتم Gradient descent در فضای وزنها به دنبال برداری می گردد که خطا را حداقل کند.



این الگوریتم از یک مقدار دلخواه برای بردار وزن شروع کرده و در هر مرحله وزنها را طوری تغییر میدهد که در جهت شیب کاهشی منحنی فوق خطا کاهش داده شود.

Perceptron Vs. LMS

Derivative

• Linear activation function has derivative

but

• Sign (bipolar, unipolar) has not derivative

Chain Rule

$$\frac{df(n(w))}{dw} = \frac{df(n)}{dn} \times \frac{dn(w)}{dw}$$

Example

$$f(n) = \cos(n)$$
 $n = e^{2w}$ $f(n(w)) = \cos(e^{2w})$

$$\frac{df(n(w))}{dw} = \frac{df(n)}{dn} \times \frac{dn(w)}{dw} = (-\sin(n))(2e^{2w}) = (-\sin(e^{2w}))(2e^{2w})$$

Performance Index

Training Set

$$\{\mathbf{p}_1, \mathbf{t}_1\}, \{\mathbf{p}_2, \mathbf{t}_2\}, \dots, \{\mathbf{p}_{\mathcal{Q}}, \mathbf{t}_{\mathcal{Q}}\}$$

Mean Square Errors

$$F(\mathbf{x}) = E[e^2] = E[(t-a)^2]$$

Vector Case

$$F(\mathbf{x}) = E[\mathbf{e}^T \mathbf{e}] = E[(\mathbf{t} - \mathbf{a})^T (\mathbf{t} - \mathbf{a})]$$

Approximate Mean Square Error (Single Sample)

$$\hat{F}(\mathbf{x}) = (\mathbf{t}(k) - \mathbf{a}(k))^{T} (\mathbf{t}(k) - \mathbf{a}(k)) = \mathbf{e}^{T}(k)\mathbf{e}(k)$$

A Simple Example

$$n^3 = (W^3a^2 + b^3)$$

$$a^3 = f^3 (W^3 a^2 + b^3)$$

$$\mathbf{w}^{m}(k+1) = \mathbf{w}^{m}(k) - \alpha \frac{\partial \hat{F}}{\partial \mathbf{w}^{m}}$$

$$\frac{\partial \hat{F}}{\partial W^3} = \frac{\partial \hat{F}}{\partial e} \cdot \frac{\partial e}{\partial a^3} \cdot \frac{\partial a^3}{\partial n^3} \cdot \frac{\partial n^3}{\partial W^3}$$

$$\frac{\partial \Gamma}{\partial W^3} = \frac{\partial \Gamma}{\partial e} \cdot \frac{\partial e}{\partial a^3} \cdot \frac{\partial a}{\partial n^3} \cdot \frac{\partial n}{\partial W^3}$$

$$\frac{\partial \hat{F}}{\partial e} = 2e$$

$$\frac{\partial e}{\partial a^3} = -1$$

$$\frac{\partial e}{\partial a^3} = -1 \qquad \frac{\partial a^3}{\partial n^3} = \dot{f}^3(n^3) \qquad \frac{\partial n^3}{\partial W^3} = a^2$$

$$\frac{\partial n^3}{\partial W^3} = a^2$$

A Simple Example

$$n^3 = (W^3a^2 + b^3)$$

$$a^3 = f^3 (W^3 a^2 + b^3)$$

$$b^{m}(k+1) = b^{m}(k) - \alpha \frac{\partial \hat{F}}{\partial b^{m}}$$

$$\frac{\partial \hat{F}}{\partial b^{3}} = \frac{\partial \hat{F}}{\partial e} \cdot \frac{\partial e}{\partial a^{3}} \cdot \frac{\partial a^{3}}{\partial n^{3}} \cdot \frac{\partial n^{3}}{\partial b^{3}}$$

$$\frac{\partial \hat{F}}{\partial e} = 2e$$

$$\frac{\partial e}{\partial a^3} = -1$$

$$\begin{array}{c|c}
 & \mathbf{a}^2 \\
\hline
S^2 \times 1 \\
\hline
 & \mathbf{b}^3 \\
\hline
S^3 \times 1 \\
\hline
 & \mathbf{b}^3 \\
\hline
 & \mathbf{b}^3
\end{array}$$

$$\begin{array}{c|c}
 & \mathbf{a}^3 \\
\hline
S^3 \times 1 \\
\hline
 & \mathbf{b}^3
\end{array}$$

$$\frac{\partial e}{\partial a^3} = -1 \qquad \frac{\partial a^3}{\partial n^3} = \dot{f}^3(n^3) \qquad \frac{\partial n^3}{\partial b^3} = 1$$

Chain Rule

Approximate Steepest Descent

$$w_{i,j}^m(k+1) = w_{i,j}^m(k) - \alpha \frac{\partial \hat{F}}{\partial w_{i,j}^m} \qquad b_i^m(k+1) = b_i^m(k) - \alpha \frac{\partial \hat{F}}{\partial b_i^m}$$

Application to Gradient Calculation

$$\frac{\partial \hat{F}}{\partial w_{i,j}^{m}} = \frac{\partial \hat{F}}{\partial n_{i}^{m}} \times \frac{\partial n_{i}^{m}}{\partial w_{i,j}^{m}} \qquad \frac{\partial \hat{F}}{\partial b_{i}^{m}} = \frac{\partial \hat{F}}{\partial n_{i}^{m}} \times \frac{\partial n_{i}^{m}}{\partial b_{i}^{m}}$$

Gradient Calculation

$$n_i^m = \sum_{j=1}^{S^{m-1}} w_{i,j}^m a_j^{m-1} + b_i^m$$

$$\frac{\partial n_i^m}{\partial w_{i,j}^m} = a_j^{m-1} \qquad \frac{\partial n_i^m}{\partial b_i^m} = 1$$

Sensitivity

$$s_i^m \equiv \frac{\partial \hat{F}}{\partial n_i^m}$$

Gradient

$$\frac{\partial \hat{F}}{\partial w_{i,j}^{m}} = s_{i}^{m} a_{j}^{m-1} \qquad \frac{\partial \hat{F}}{\partial b_{i}^{m}} = s_{i}^{m}$$

Steepest Descent

$$w_{i,j}^{m}(k+1) = w_{i,j}^{m}(k) - \alpha s_{i}^{m} a_{j}^{m-1}$$
 $b_{i}^{m}(k+1) = b_{i}^{m}(k) - \alpha s_{i}^{m}$

$$\mathbf{W}^{m}(k+1) = \mathbf{W}^{m}(k) - \alpha \mathbf{s}^{m}(\mathbf{a}^{m-1})^{T} \qquad \mathbf{b}^{m}(k+1) = \mathbf{b}^{m}(k) - \alpha \mathbf{s}^{m}$$

$$\mathbf{s}^{m} = \frac{\partial \hat{F}}{\partial \mathbf{n}^{m}} = \begin{bmatrix} \frac{\partial \hat{F}}{\partial n_{1}^{m}} \\ \frac{\partial \hat{F}}{\partial n_{2}^{m}} \\ \vdots \\ \frac{\partial \hat{F}}{\partial n_{S^{m}}^{m}} \end{bmatrix}$$

Next Step: Compute the Sensitivities (Backpropagation)

Jacobian Matrix

$$\frac{\partial \mathbf{n}_{1}^{m+1}}{\partial n_{1}^{m}} = \frac{\partial n_{1}^{m+1}}{\partial n_{1}^{m}} \frac{\partial n_{1}^{m+1}}{\partial n_{2}^{m}} \cdots \frac{\partial n_{1}^{m+1}}{\partial n_{S}^{m}} \\ \frac{\partial \mathbf{n}_{1}^{m+1}}{\partial \mathbf{n}_{1}^{m}} = \frac{\partial n_{2}^{m+1}}{\partial n_{1}^{m}} \frac{\partial n_{2}^{m+1}}{\partial n_{2}^{m}} \cdots \frac{\partial n_{2}^{m+1}}{\partial n_{S}^{m}} \\ \vdots & \vdots & \vdots \\ \frac{\partial n_{S}^{m+1}}{\partial n_{1}^{m}} \frac{\partial n_{2}^{m+1}}{\partial n_{2}^{m}} \cdots \frac{\partial n_{S}^{m+1}}{\partial n_{S}^{m}} \cdots \frac{\partial n_{S}^{m+1}}{\partial n_{S}^{m}} \end{bmatrix}$$

$$\frac{\partial \mathbf{n}^{m+1}}{\partial \mathbf{n}^{m}} = \begin{bmatrix} \frac{\partial n_{1}^{m+1}}{\partial n_{1}^{m}} & \frac{\partial n_{1}^{m+1}}{\partial n_{2}^{m}} & \cdots & \frac{\partial n_{1}^{m+1}}{\partial n_{S}^{m}} \\ \frac{\partial \mathbf{n}_{1}^{m+1}}{\partial \mathbf{n}_{1}^{m}} & \frac{\partial n_{2}^{m+1}}{\partial n_{2}^{m}} & \cdots & \frac{\partial n_{2}^{m+1}}{\partial n_{S}^{m}} \\ \vdots & \vdots & & \vdots \\ \frac{\partial n_{S}^{m+1}}{\partial n_{1}^{m}} & \frac{\partial n_{2}^{m+1}}{\partial n_{2}^{m}} & \cdots & \frac{\partial n_{S}^{m+1}}{\partial n_{S}^{m+1}} \\ \frac{\partial n_{S}^{m+1}}{\partial n_{1}^{m}} & \frac{\partial n_{2}^{m+1}}{\partial n_{2}^{m}} & \cdots & \frac{\partial n_{S}^{m+1}}{\partial n_{S}^{m}} \end{bmatrix} \quad \frac{\partial n_{i}^{m+1}}{\partial n_{j}^{m}} = \frac{\partial \left(\sum_{l=1}^{S^{m}} w_{i,l}^{m+1} a_{l}^{l} + b_{i}^{m+1}\right)}{\partial n_{j}^{m}} = w_{i,j}^{m+1} \frac{\partial a_{j}^{m}}{\partial n_{j}^{m}} \\ \frac{\partial n_{i}^{m+1}}{\partial n_{j}^{m}} = w_{i,j}^{m+1} \frac{\partial a_{j}^{m}}{\partial n_{j}^{m}} = w_{i,j}^{m+1} f^{m}(n_{j}^{m}) \\ f^{m}(n_{j}^{m}) = \frac{\partial f^{m}(n_{j}^{m})}{\partial n_{j}^{m}} \end{cases}$$

$$\frac{\partial \mathbf{n}^{m+1}}{\partial \mathbf{n}^m} = \mathbf{W}^{m+1} \dot{\mathbf{F}}^m (\mathbf{n}^m)$$

$$\frac{\partial \mathbf{n}^{m+1}}{\partial \mathbf{n}^m} = \mathbf{W}^{m+1} \dot{\mathbf{F}}^m(\mathbf{n}^m) \qquad \qquad \dot{\mathbf{F}}^m(\mathbf{n}^m) = \begin{bmatrix} \dot{f}^m(n_1^m) & 0 & \dots & 0 \\ 0 & \dot{f}^m(n_2^m) & \dots & 0 \\ \vdots & \vdots & & \vdots \\ 0 & 0 & \dots & \dot{f}^m(n_S^m) \end{bmatrix}$$

Backpropagation (Sensitivities)

$$\mathbf{s}^{m} = \frac{\partial \hat{F}}{\partial \mathbf{n}^{m}} = \left(\frac{\partial \mathbf{n}^{m+1}}{\partial \mathbf{n}^{m}}\right)^{T} \frac{\partial \hat{F}}{\partial \mathbf{n}^{m+1}} = \dot{\mathbf{F}}^{m} (\mathbf{n}^{m}) (\mathbf{W}^{m+1})^{T} \frac{\partial \hat{F}}{\partial \mathbf{n}^{m+1}}$$

$$\left[\mathbf{s}^{m} = \dot{\mathbf{F}}^{m}(\mathbf{n}^{m})(\mathbf{W}^{m+1})^{T}\mathbf{s}^{m+1}\right]$$

The sensitivities are computed by starting at the last layer, and then propagating backwards through the network to the first layer.

$$\mathbf{s}^M \to \mathbf{s}^{M-1} \to \dots \to \mathbf{s}^2 \to \mathbf{s}^1$$

Initialization (Last Layer)

$$s_i^M = \frac{\partial \hat{F}}{\partial n_i^M} = \frac{\partial (\mathbf{t} - \mathbf{a})^T (\mathbf{t} - \mathbf{a})}{\partial n_i^M} = \frac{\partial \sum_{j=1}^{S^M} (t_j - a_j)^2}{\partial n_i^M} = -2(t_i - a_i) \frac{\partial a_i}{\partial n_i^M}$$

$$\frac{\partial a_i}{\partial n_i^M} = \frac{\partial a_i^M}{\partial n_i^M} = \frac{\partial f^M(n_i^M)}{\partial n_i^M} = f^M(n_i^M)$$

$$s_i^M = -2(t_i - a_i) f^M(n_i^M)$$

$$\mathbf{s}^{M} = -2\mathbf{\dot{F}}^{M}(\mathbf{n}^{M})(\mathbf{t} - \mathbf{a})$$

Summary

Forward Propagation

$$\mathbf{a}^{0} = \mathbf{p}$$

$$\mathbf{a}^{m+1} = \mathbf{f}^{m+1} (\mathbf{W}^{m+1} \mathbf{a}^{m} + \mathbf{b}^{m+1}) \qquad m = 0, 2, \dots, M-1$$

$$\mathbf{a} = \mathbf{a}^{M}$$

Backpropagation

$$\mathbf{s}^{M} = -2\mathbf{\dot{F}}^{M}(\mathbf{n}^{M})(\mathbf{t} - \mathbf{a})$$

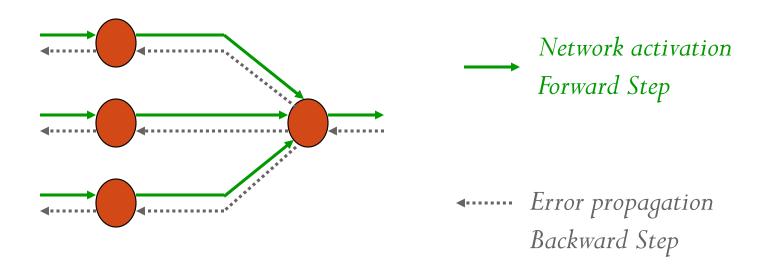
$$\mathbf{s}^{m} = \mathbf{\dot{F}}^{m}(\mathbf{n}^{m})(\mathbf{W}^{m+1})^{T}\mathbf{s}^{m+1} \qquad m = M-1, \dots, 2, 1$$

Weight Update

$$\mathbf{W}^{m}(k+1) = \mathbf{W}^{m}(k) - \alpha \mathbf{s}^{m}(\mathbf{a}^{m-1})^{T}$$
 $\mathbf{b}^{m}(k+1) = \mathbf{b}^{m}(k) - \alpha \mathbf{s}^{m}$

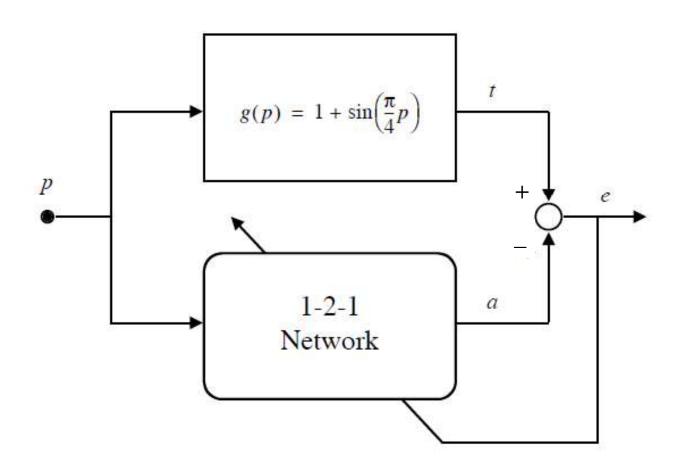
Summary

• Back-propagation training algorithm

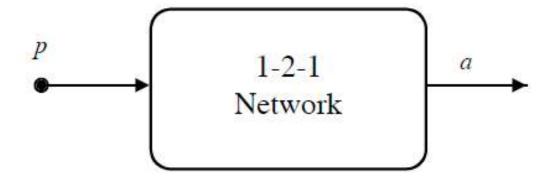


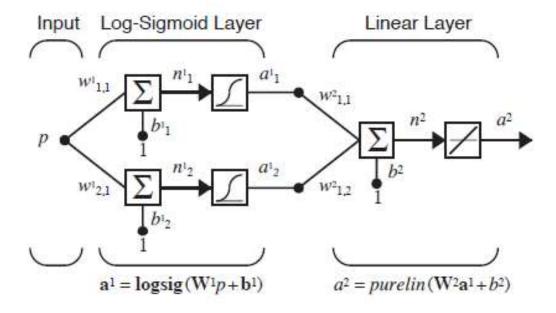
• Backpropagation adjusts the weights of the NN in order to minimize the network total mean squared error.

Example: Function Approximation



Network





Initial Conditions

$$\mathbf{W}^{1}(0) = \begin{bmatrix} -0.27 \\ -0.41 \end{bmatrix} \quad \mathbf{b}^{1}(0) = \begin{bmatrix} -0.48 \\ -0.13 \end{bmatrix} \quad \mathbf{W}^{2}(0) = \begin{bmatrix} 0.09 & -0.17 \end{bmatrix} \quad \mathbf{b}^{2}(0) = \begin{bmatrix} 0.48 \end{bmatrix}$$

$$\begin{array}{c} -\text{Network Response} \\ -\text{Sine Wave} \end{array}$$

Forward Propagation

$$a^0 = p = 1$$

$$\mathbf{a}^{1} = \mathbf{f}^{1}(\mathbf{W}^{1}\mathbf{a}^{0} + \mathbf{b}^{1}) = \mathbf{logsig} \begin{bmatrix} -0.27 \\ -0.41 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} + \begin{bmatrix} -0.48 \\ -0.13 \end{bmatrix} = \mathbf{logsig} \begin{bmatrix} -0.75 \\ -0.54 \end{bmatrix}$$

$$\mathbf{a}^{1} = \begin{bmatrix} \frac{1}{1 + e^{0.75}} \\ \frac{1}{1 + e^{0.54}} \end{bmatrix} = \begin{bmatrix} 0.321 \\ 0.368 \end{bmatrix}$$

$$a^2 = f^2(\mathbf{W}^2 \mathbf{a}^1 + \mathbf{b}^2) = purelin([0.09 -0.17] \begin{bmatrix} 0.321 \\ 0.368 \end{bmatrix} + [0.48]) = [0.446]$$

$$e = t - a = \left\{1 + \sin\left(\frac{\pi}{4}p\right)\right\} - a^2 = \left\{1 + \sin\left(\frac{\pi}{4}1\right)\right\} - 0.446 = 1.261$$

Transfer Function Derivatives

$$\dot{f}^{1}(n) = \frac{d}{dn} \left(\frac{1}{1 + e^{-n}} \right) = \frac{e^{-n}}{(1 + e^{-n})^{2}} = \left(1 - \frac{1}{1 + e^{-n}} \right) \left(\frac{1}{1 + e^{-n}} \right) = (1 - a^{1})a^{1}$$

$$\dot{f}^2(n) = \frac{d}{dn}(n) = 1$$

Backpropagation

$$\mathbf{s}^{2} = -2\dot{\mathbf{F}}^{2}(\mathbf{n}^{2})(\mathbf{t} - \mathbf{a}) = -2\left[\dot{f}^{2}(n^{2})\right](1.261) = -2\left[1\right](1.261) = -2.522$$

$$\mathbf{s}^{1} = \dot{\mathbf{F}}^{1}(\mathbf{n}^{1})(\mathbf{W}^{2})^{T}\mathbf{s}^{2} = \begin{bmatrix} (1 - a_{1}^{1})(a_{1}^{1}) & 0\\ 0 & (1 - a_{2}^{1})(a_{2}^{1}) \end{bmatrix} \begin{bmatrix} 0.09\\ -0.17 \end{bmatrix} \begin{bmatrix} -2.522 \end{bmatrix}$$

$$\mathbf{s}^{1} = \begin{bmatrix} (1 - 0.321)(0.321) & 0 \\ 0 & (1 - 0.368)(0.368) \end{bmatrix} \begin{bmatrix} 0.09 \\ -0.17 \end{bmatrix} \begin{bmatrix} -2.522 \end{bmatrix}$$

$$\mathbf{s}^1 = \begin{bmatrix} 0.218 & 0 \\ 0 & 0.233 \end{bmatrix} \begin{bmatrix} -0.227 \\ 0.429 \end{bmatrix} = \begin{bmatrix} -0.0495 \\ 0.0997 \end{bmatrix}$$

Weight Update

$$\alpha = 0.1$$

$$\mathbf{W}^{2}(1) = \mathbf{W}^{2}(0) - \alpha \mathbf{s}^{2}(\mathbf{a}^{1})^{T} = \begin{bmatrix} 0.09 & -0.17 \end{bmatrix} - 0.1 \begin{bmatrix} -2.522 \end{bmatrix} \begin{bmatrix} 0.321 & 0.368 \end{bmatrix}$$
$$\mathbf{W}^{2}(1) = \begin{bmatrix} 0.171 & -0.0772 \end{bmatrix}$$

$$\mathbf{b}^{2}(1) = \mathbf{b}^{2}(0) - \alpha \mathbf{s}^{2} = \begin{bmatrix} 0.48 \end{bmatrix} - 0.1 \begin{bmatrix} -2.522 \end{bmatrix} = \begin{bmatrix} 0.732 \end{bmatrix}$$

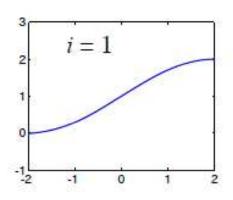
$$\mathbf{W}^{1}(1) = \mathbf{W}^{1}(0) - \alpha \mathbf{s}^{1}(\mathbf{a}^{0})^{T} = \begin{bmatrix} -0.27 \\ -0.41 \end{bmatrix} - 0.1 \begin{bmatrix} -0.0495 \\ 0.0997 \end{bmatrix} \boxed{1} = \begin{bmatrix} -0.265 \\ -0.420 \end{bmatrix}$$

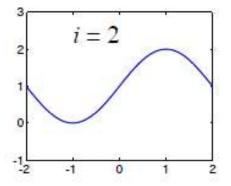
$$\mathbf{b}^{1}(1) = \mathbf{b}^{1}(0) - \alpha \mathbf{s}^{1} = \begin{bmatrix} -0.48 \\ -0.13 \end{bmatrix} - 0.1 \begin{bmatrix} -0.0495 \\ 0.0997 \end{bmatrix} = \begin{bmatrix} -0.475 \\ -0.140 \end{bmatrix}$$

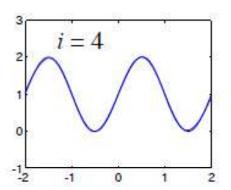
Choice of Network Architecture

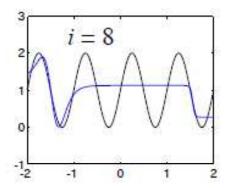
$$g(p) = 1 + \sin\left(\frac{i\pi}{4}p\right) \text{ for } -2 \le p \le 2$$

1-3-1 Network



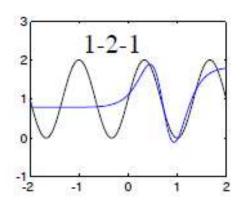


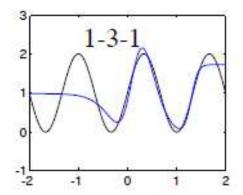


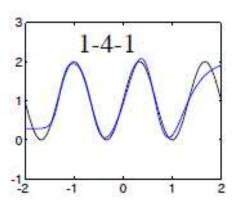


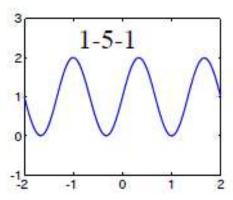
Choice of Network Architecture

$$g(p) = 1 + \sin\left(\frac{6\pi}{4}p\right)$$
 for $-2 \le p \le 2$









Disadvantage of BP algorithm

- Slow convergence speed
- Sensitivity to initial conditions
- Trapped in local minima
- Instability if learning rate is too large
- Note: despite above disadvantages, it is popularly used in control community. There are numerous extensions to improve BP algorithm.

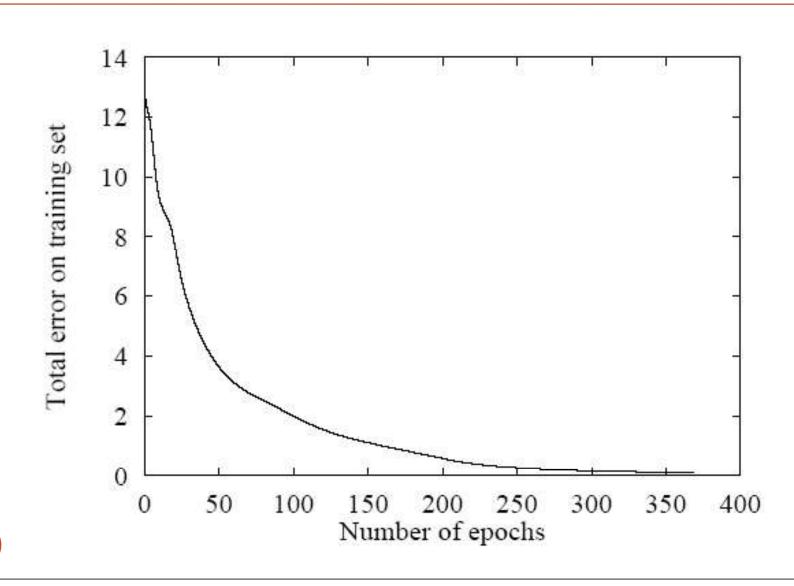
شرط خاتمه

معمولا الگوریتم BP پیش از خاتمه هزاران بار با استفاده از همان دادههای آموزشی تکرار میشود. در این حالت شروط مختلفی را میتوان برای خاتمه الگوریتم به کار برد:

- توقف بعد از تکرار به دفعات معین،
- توقف وقتی که خطا از یک مقدار تعیین شده کمتر شود،
- توقف وقتی که خطا در مثالهای مجموعه اعتبار سنجی از قاعده خاصی پیروی کند.

اگر دفعات تکرار کم باشد خطا خواهیم داشت و اگر زیاد باشد مساله Overfitting رخ خواهد داد.

منحني يادگيري



قدرت تعمیم و Overfitting

- شرط پایان الگوریتم BP چیست؟
- یک انتخاب این است که الگوریتم را آنقدر ادامه دهیم تا خطا از مقدار معینی کمتر شود. این امر می تواند منجر به Overfitting شود.

