

Maharashtra State Board

HSC 2017 - 2018 July

12th Board Exam

Mathematics and Statistics

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BOARD QUESTION PAPER : July 2018

Notes:

- All questions are compulsory.
- Figures to the right indicate full marks.
- Graph paper is necessary for L.P.P.
- Use of logarithmic table is allowed.
- Answers to the question in Section – I and Section – II should be written in two separate answer books.
- Question from Section – I attempted in the answer book of Section – II and vice-versa will not be assessed / not be given any credit.
- Answer to every question must be written on a new page.

Section – I

Q.1. Attempt any SIX of the following:

[12]

- p: It is a day time, q: It is warm
Give the verbal statements for the following symbolic statements :

 - $p \wedge \sim q$
 - $p \rightarrow q$

(2)
- Express the truth of each of the following statements using Venn diagrams:

 - No circles are polygons
 - Some quadratic equations have equal roots.

(2)
- Find the values of x and y if

$$2 \begin{bmatrix} x & 5 \\ 7 & y-3 \end{bmatrix} + \begin{bmatrix} 3 & -4 \\ 1 & 2 \end{bmatrix} = \begin{bmatrix} 7 & 6 \\ 15 & 14 \end{bmatrix}$$

(2)
- Find $\frac{dy}{dx}$; if $x = \sin^3 \theta$, $y = \cos^3 \theta$

(2)
- Find $\frac{dy}{dx}$; if $y = \cos^{-1}(2x\sqrt{1-x^2})$

(2)
- Evaluate: $\int x \cdot \log x \, dx$

(2)
- The cost C of producing x articles is given as $C = x^3 - 16x^2 + 47x$. For what values of x , the average cost is decreasing?

(2)
- Evaluate: $\int_0^{\frac{\pi}{4}} \frac{1}{1+x^2} \, dx$

(2)

Q.2. (A) Attempt any TWO of the following:

(6)[14]

- Solve the following equations by reduction method:

$$x + y + z = 6, 3x - y + 3z = 10, 5x + y - 4z = 3$$

(3)
- Evaluate: $\int \frac{2x+1}{(x+1)(x-2)} \, dx$

(3)
- Evaluate: $\int_0^1 x(1-x)^2 \, dx$

(3)

(B) Attempt any TWO of the following: (8)

i. Using the rules of negation, write the negation of the following :

a. $p \wedge (q \rightarrow r)$ (b) $\sim p \vee \sim q$ (4)

ii. If the function f is continuous at $x = 2$ and $x = 4$ then find the values of a and b .

Where $f(x) = x^2 + ax + b, x < 2$

$$= 3x + 2, \quad 2 \leq x \leq 4$$

$$= 2ax + 5b, \quad 4 \leq x$$
 (4)

iii. A manufacturing company produces x items at the total cost of ₹ $(180 + 4x)$. The demand function of this product is $P = (240 - x)$. Find x for which profit is increasing. (4)

Q.3. (A) Attempt any TWO of the following: (6)[14]

i. If $A = \begin{bmatrix} 1 & 2 \\ 3 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 7 & 1 \\ 2 & 5 \end{bmatrix}$, verify that $|AB| = |A| \cdot |B|$ (3)

ii. Evaluate : $\int \frac{1}{x[(\log x)^2 + 4]} dx$ (3)

iii. Find the volume of solid generated by rotating the area bounded by $x^2 + y^2 = 36$ and the lines $x = 0, x = 3$ about X -axis. (3)

(B) Attempt any TWO of the following: (8)

i. If f is continuous at $x = 0$, then find $f(0)$. Where $f(x) = \frac{(3^{\sin x} - 1)^2}{x \log(x+1)}, x \neq 0$ (4)

ii. If $x^7 \cdot y^9 = (x+y)^{16}$, then show that $\frac{dy}{dx} = \frac{y}{x}$ (4)

iii. In a firm the cost function for output x is given as $C = \frac{x^3}{3} - 20x^2 + 70x$. Find the output for which marginal cost (C_m) is minimum. (4)

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Section – II

Q.4. Attempt any SIX of the following:

[12]

- i. The price of a T.V. set is ₹ 17,000. An agent charges at 3% and earns ₹ 25,500. Find the number of T.V. sets sold by him
- ii. Find the Age-Specific death rate (Age –SDR) for the following data:

Age groups (in years)	Population (in '000)	Number of deaths
0 – 10	11	275
10 – 20	12	180
20 – 60	9	81
60 and above	2	32

- iii. The regression equation of y on x is given by $3x + 2y - 26 = 0$. Find b_{yx} .
- iv. Verify whether the following function can be regarded as p.m.f. of the random variable X :

$$P(x) = \begin{cases} \frac{x-1}{3}, & x=1, 2, 3 \\ 0, & \text{otherwise} \end{cases}$$
- v. If X has a binomial distribution with $n = 20$, $p = \frac{1}{10}$, find $E(X)$ and $V(X)$.
- vi. Bring out the inconsistency, if any: $b_{YX} + b_{XY} = 1.30$ and $r = 0.75$
- vii. A train travelled between two stations. The distance and time were recorded as below:

Distance (km)	80	120	160	200	240
Time (hr)	2	3	4	5	6

Draw scatter diagram and identify the type of correlation.

- viii. If $r = 0.5$, $\sigma_x = 1$ and $\sigma_y = 4$, then find $\text{Cov.}(X, Y)$.

Q.5. (A) Attempt any TWO of the following:

[6][14]

- i. Calculate e_0^* , e_1^* , e_2^* from the following.

Age x	0	1	2
I_x	1000	880	876
T_x	-	-	3323

(3)

- ii. Calculate the CDR for Districts A and B compare them :

Age group (in years)	District A		District B	
	No. of persons (in '000)	No. of deaths	No. of persons (in '000)	No. of deaths
0 – 15	1	20	2	50
15 -60	3	30	7	70
60 and above	2	40	1	25

- (3)
- iii. The equation of the line of regression of Y on X is $3x + 2y = 26$ and X on Y is $6x + y = 31$. Find Var. (X) if Var. (Y) = 36. (3)

(B) Attempt any TWO of the following: (8)

- i. Calculate Spearman's Rank Correlation Coefficient between the following marks given by 'two' judges (A and B) to 'eight' contestants in the elocution competition: (4)

Contestants	1	2	3	4	5	6	7	8
Marks by A	81	72	60	33	29	11	56	42
Marks by B	75	56	42	15	30	20	60	80

- ii. Solve the following assignment problem to minimize the cost:

Persons	Jobs		
	I	II	III
A	7	3	5
B	2	7	4
C	6	5	3
D	3	4	7

- (4)
- iii. Find the sequence of the following five jobs to be processed on three machines M_1 , M_2 , M_3 that will minimize the total elapsed time to complete the tasks. Each job is to be processed in the order $M_1 - M_2 - M_3$:

Jobs	1	2	3	4	5
Machine M_1	5	11	5	7	6
Machine M_2	1	4	2	5	3
Machine M_3	1	5	2	3	4

(4)

Q.6. (A) Attempt any TWO of the following: (6)[14]

- i. Minimize : $Z = 2x + y$
 Subject to : $x + y \leq 5$
 $x + 2y \leq 8$
 $4x + 3y \geq 12$
 $x \geq 0, y \geq 0$

Solve graphically.

- (3)
- ii. Find the graphical solution for the following system of linear equations:
 $3x + 4y \geq 12$, $4x + 7y \leq 28$, $y \geq 1$, $x \geq 0$, $y \geq 0$.

Hence find the co-ordinates of corner points of the common region.

- (3)
- iii. A wholesaler allows 25% trade discount and 5% cash discount. Find the list price of an article, if it was sold for the net amount of ₹ 1,140. (3)

(B) Attempt any TWO of the following: (8)

- i. Find the accumulated value after 3 years of an immediate annuity of ₹ 2,000 p.a. with interest compounded at 10% p.a. [Given $(1.1)^3 = 1.331$] (4)
- ii. If the difference between true discount and banker's discount on a sum due 4 months hence is ₹ 20, find true discount, banker's discount and amount of the bill, the rate of simple interest charged being 5% p.a. (4)
- iii. If a random variable X follows Poisson distribution such that $P(X = 1) = P(X = 2)$, then find $(X \geq 1)$. [Use $e^{-2} = 0.1353$] (4)