

Linear Search and Binary Search

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June 2025

Linear Search Example

- ▶ **Problem:** Find book ID 42 in shelf: [23, 15, 42, 19, 7].
- ▶ Check each book from left to right.
- ▶ **Step-by-Step:**
 1. Check 23: Not 42.
 2. Check 15: Not 42.
 3. Check 42: Found at position 3.

Linear Search

- ▶ Check each element until target is found or list ends.
- ▶ Simple but slow for large lists.
- ▶ **Time Complexity:** $O(n)$ (worst/average case).
- ▶ **Space Complexity:** $O(1)$.

Binary Search Example

- ▶ **Problem:** Find page 42 in sorted catalog: [10, 20, 30, 40, 42, 50, 60].
- ▶ Check middle, narrow to left or right half.
- ▶ **Step-by-Step:**
 1. Middle: 40. $42 \geq 40$, search [42, 50, 60].
 2. Middle: 42. Found at position 5.

Binary Search

- ▶ Requires sorted list. Divide search range in half each step.
- ▶ Compare middle element, recurse on appropriate half.
- ▶ **Time Complexity:** $O(\log n)$.
- ▶ **Space Complexity:** $O(1)$ (iterative version).