

## **HW** 3

This assignment covers several aspects of Linear Regresstion. **DO NOT ERASE**MARKDOWN CELLS AND INSTRUCTIONS IN YOUR HW submission

- Q QUESTION
- A Where to input your answer

### Instructions

Keep the following in mind for all notebooks you develop:

- Structure your notebook.
- Use headings with meaningful levels in Markdown cells, and explain the questions each piece of code is to answer or the reason it is there.
- Make sure your notebook can always be rerun from top to bottom (Kernel Tab -> Restart and Run All)
- Start working on this assignment as soon as possible. If you are a beginner in Python this might take a long time. One of the objectives of this assignment is to help you learn python and scikit-learn package.
- Follow README.md for homework submission instructions
- In this notebook we assume '../data/' location of all data files to be read and written

## Related sklearn material and online tutorials

sklearn User Guide

### sklearn data pre-processing

- train\_test\_split
- common\_pittfalls
- train test split tutorial

## sklearn multiple linear regression

- tutorial
- API documentation
- Linear Regression
- multiple linear regression tutorial

## sklearn polynomial regression

generate polynomial features

polinomial regression tutorial

#### correlation

correlation

# **Linear Regression**

In jupyter notebook environment, commands starting with the symbol % are magic commands or magic functions. %%timeit is one of such function. It basically gives you the speed of execution of certain statement or blocks of codes.

```
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
```

**Q1** Read the car\_data.csv data (we assume ../data/ location of all data files to be read and written) from **data** folder using pandas. Replace the ??? in the code cell below to accomplish this taks.

A1 Replace ??? with code in the code cell below

```
In [2]: # Replace ??? with code in the code cell below

df = pd.read_csv("C:\\Users\\alsae\\Desktop\\fake\\2024Spring\\data\\Car_data.c

In [3]: # View head of the data to confirm the correctness of your answer
    df.head()
```

	car_ID	symboling	CarName	fueltype	aspiration	doornumber	carbody	drive
0	1	3	alfa-romero giulia	gas	std	two	convertible	
1	2	3	alfa-romero stelvio	gas	std	two	convertible	
2	3	1	alfa-romero Quadrifoglio	gas	std	two	hatchback	
3	4	2	audi 100 ls	gas	std	four	sedan	
4	5	2	audi 100ls	gas	std	four	sedan	
	1 2 3	<ul><li>0 1</li><li>1 2</li><li>2 3</li><li>3 4</li></ul>	1 2 3 2 3 1 3 4 2	<ul> <li>1 3 alfa-romero giulia</li> <li>1 2 3 alfa-romero stelvio</li> <li>2 3 1 alfa-romero Quadrifoglio</li> <li>3 4 2 audi 100 ls</li> </ul>	<ul> <li>0 1 3 alfa-romero giulia gas</li> <li>1 2 3 alfa-romero stelvio gas</li> <li>2 3 1 alfa-romero Quadrifoglio gas</li> <li>3 4 2 audi 100 ls gas</li> </ul>	0       1       3       alfa-romero giulia       gas       std         1       2       3       alfa-romero stelvio       gas       std         2       3       1       alfa-romero Quadrifoglio       gas       std         3       4       2       audi 100 ls       gas       std	0       1       3       alfa-romero giulia       gas       std       two         1       2       3       alfa-romero stelvio       gas       std       two         2       3       1       alfa-romero Quadrifoglio       gas       std       two         3       4       2       audi 100 ls       gas       std       four	0       1       3       alfa-romero giulia       gas       std       two convertible         1       2       3       alfa-romero stelvio       gas       std       two convertible         2       3       1       alfa-romero Quadrifoglio       gas       std       two hatchback         3       4       2       audi 100 ls       gas       std       four       sedan

5 rows × 26 columns

## Data cleaning and manipulation

**Q2** Here, you will practice the usage of common data cleaning and manipulation functions in 3 steps.

- 1. Use isnull() to figure out the number of NaN values per column
- 2. Remove the column with majority NaN values (if any)
- 3. Check if there are still NaN values in the dataframe using isna() method

A2 Replace ??? with code in the code cell below

```
In [4]:
         # There is no missing data here on this dataset :
         print(df.isnull().sum())
         df.dropna()
         df.isna()
       car_ID
                           0
       symboling
                           0
       CarName
                           0
       fueltype
                           0
       aspiration
       doornumber
                           0
       carbody
       drivewheel
       enginelocation
                           0
      wheelbase
       carlength
       carwidth
       carheight
       curbweight
                           0
       enginetype
       cylindernumber
                           0
       enginesize
                           0
       fuelsystem
      boreratio
                           0
       stroke
       compressionratio
      horsepower
       peakrpm
                           0
       citympg
      highwaympg
                           0
       price
      dtype: int64
```

Out[4]:		car_ID	symboling	CarName	fueltype	aspiration	doornumber	carbody	drivewh
	0	False	False	False	False	False	False	False	Fa
	1	False	False	False	False	False	False	False	Fŧ
	2	False	False	False	False	False	False	False	Fa
	3	False	False	False	False	False	False	False	Fi
	4	False	False	False	False	False	False	False	Fi
	•••	•••			•••				

| 200 | False | Fŧ |
|-----|-------|-------|-------|-------|-------|-------|-------|----|
| 201 | False | Fŧ |
| 202 | False | Fŧ |
| 203 | False | Fŧ |
| 204 | False | Fã |

205 rows × 26 columns

```
In [5]: # lets get some statistical information :
    df.describe()
```

Out[5]:		car_ID	symboling	wheelbase	carlength	carwidth	carheight	curbwe
	count	205.000000	205.000000	205.000000	205.000000	205.000000	205.000000	205.000
	mean	103.000000	0.834146	98.756585	174.049268	65.907805	53.724878	2555.565
	std	59.322565	1.245307	6.021776	12.337289	2.145204	2.443522	520.680
	min	1.000000	-2.000000	86.600000	141.100000	60.300000	47.800000	1488.000
	25%	52.000000	0.000000	94.500000	166.300000	64.100000	52.000000	2145.000
	50%	103.000000	1.000000	97.000000	173.200000	65.500000	54.100000	2414.000
	75%	154.000000	2.000000	102.400000	183.100000	66.900000	55.500000	2935.000
	max	205.000000	3.000000	120.900000	208.100000	72.300000	59.800000	4066.000

**Q3:** In this task, out of all categorical columns, we focus only on the fueltype column processing in 2 steps.

- 1. Use label encoder from sklearn and convert the fueltype categorical values to numerical values.
- 2. Create a new dataframe that contains only the numerical columns.

**A3** Replace ??? with code in the code cell below.

```
In [6]: # Label Encoding for 2-class columns:
    from sklearn.preprocessing import LabelEncoder
    le = LabelEncoder()
    df['fueltype'] = le.fit_transform(df['fueltype'])

In [7]: # Create new dataframe with selected columns
    df_numeric = df.select_dtypes(include=['number'])
In [8]: df numeric.head()
```

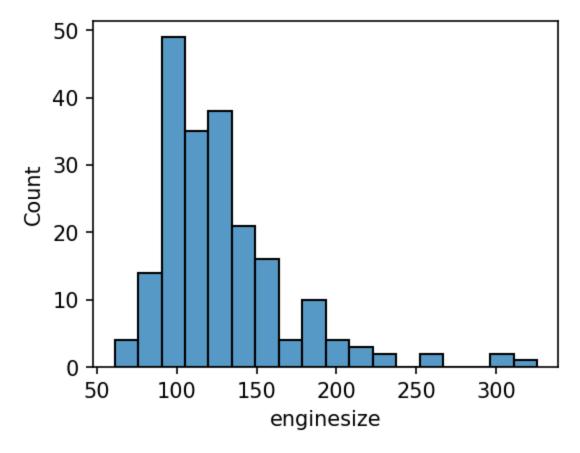
Out[8]:		car_ID	symboling	fueltype	wheelbase	carlength	carwidth	carheight	curbweight
	0	1	3	1	88.6	168.8	64.1	48.8	2548
	1	2	3	1	88.6	168.8	64.1	48.8	2548
	2	3	1	1	94.5	171.2	65.5	52.4	2823
	3	4	2	1	99.8	176.6	66.2	54.3	2337
	4	5	2	1	99.4	176.6	66.4	54.3	2824
	4								<b>•</b>

**Q4:** Use seaborn histplot to plot a distribution graph for the engine sizes

A4 Replace ??? with code in the code cell below

```
In [9]: plt.figure(figsize=(4,3),dpi=150)
    sns.histplot(df['enginesize'])
```

Out[9]: <Axes: xlabel='enginesize', ylabel='Count'>



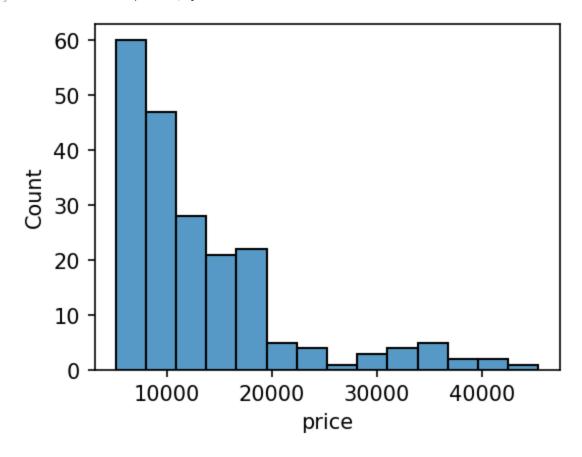
**Q5:** Use seaborn histplot to plot a distribution graph for the car prices

A5 Replace ??? with code in the code cell below

```
In [10]: plt.figure(figsize=(4,3),dpi=150)
```

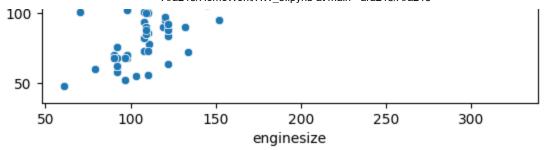
```
sns.histplot(df['price'])
```

Out[10]: <Axes: xlabel='price', ylabel='Count'>



**Q6:** Use seaborn scatterplot to present the relation between enginesize and the horsepower of a car

**A6** Replace ??? with code in the code cell below



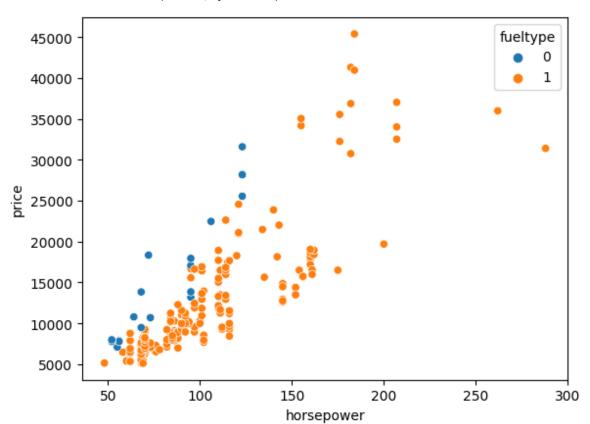
**Q7:** There is a correlation between the car price and the horsepower of a car. If horsepower of a car increase, the price of the car also increases most of the time, and in this question you will use the seaborn scatterplot to present the relation between price and horsepower.

Next, use hue parameter of scatterplot function to illustrate datapoints that relate to specific fueltype category.

A7 Replace ??? with code in the code cell below

```
In [12]: sns.scatterplot(x='horsepower', y='price', hue='fueltype', data=df_numeric)
```

Out[12]: <Axes: xlabel='horsepower', ylabel='price'>



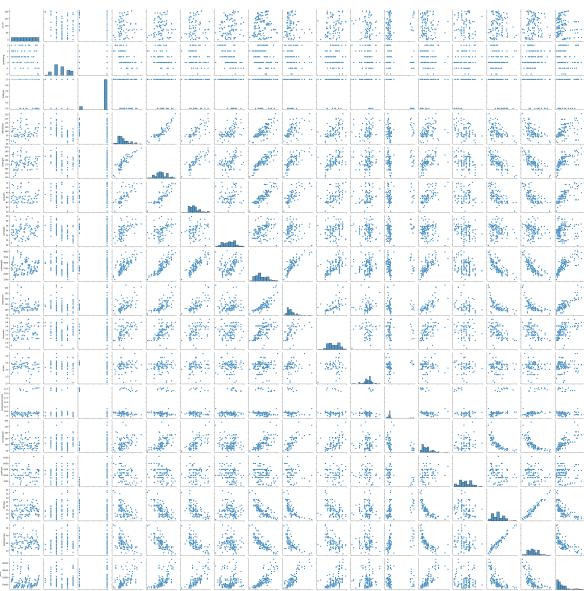
**Q8:** Use pairplot from sns to plot the data frame df and justify your feature selection.

**A8:** replace ??? with code in the code cell below.

```
In [13]: # 2. Use pairplot from sns to plot our data frame df
```

sns.pairplot(df\_numeric)

#### Out[13]: <seaborn.axisgrid.PairGrid at 0x1d3ce71ffa0>



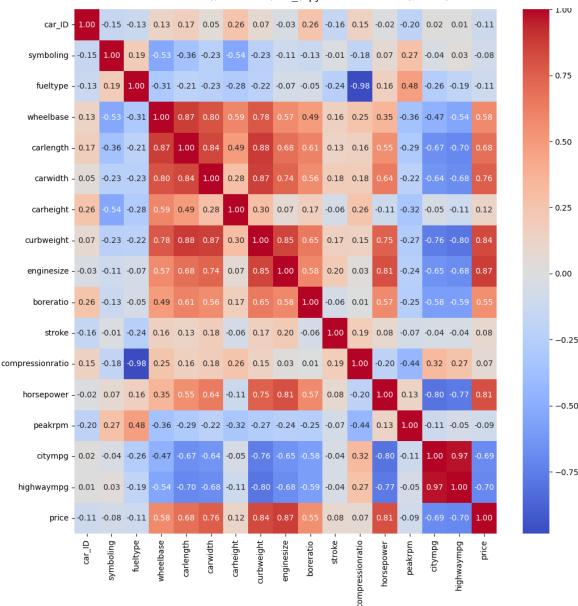
#### **Q9** Data Visualization:

- 1. Use heatmap chart from seaborn library to findout the correlation between the columns in our dataset.
- 2. Update data frame 'df' to contain 5 columns from existing 'df' with the highest correlation to column "price". Also include price column in the updated data frame.

#### A9 Replace ??? with code in the code cell below

```
In [14]:
    corr_matrix = df_numeric.corr()
    plt.figure(figsize=(12,12))
    sns.heatmap(corr_matrix, annot=True, cmap='coolwarm', fmt='.2f')
    plt.title('Correlation Heatmap')
    plt.show()
```

**Correlation Heatmap** 



```
In [15]: # Task 2: Update data frame 'df' to contain 5 columns from existing 'df' with t
    top_corr_features = corr_matrix['price'].sort_values(ascending=False).index[1:6
    top_corr_features = list(top_corr_features) + ['price'] # Include 'price' colu
    df = df[top_corr_features] # Update dataframe with selected columns
    print("Updated dataframe with selected columns:")
    print(df.head())
```

Updated dataframe with selected columns:

	enginesize	curbweight	horsepower	carwidth	carlength	price
0	130	2548	111	64.1	168.8	13495.0
1	130	2548	111	64.1	168.8	16500.0
2	152	2823	154	65.5	171.2	16500.0
3	109	2337	102	66.2	176.6	13950.0
4	136	2824	115	66.4	176.6	17450.0

## **Data Preparation**

**Q10** Pre-processing

1. Assign 'price' column value to y and rest of the columns to x

A10 Replace ??? with code in the code cell below

```
In [16]:
    y = df['price']
    X = df.drop(columns=['price'])
    X
```

Out[16]:		enginesize	curbweight	horsepower	carwidth	carlength
	0	130	2548	111	64.1	168.8
	1	130	2548	111	64.1	168.8
	2	152	2823	154	65.5	171.2
	3	109	2337	102	66.2	176.6
	4	136	2824	115	66.4	176.6
	•••					
	200	141	2952	114	68.9	188.8
	201	141	3049	160	68.8	188.8
	202	173	3012	134	68.9	188.8
	203	145	3217	106	68.9	188.8
	204	141	3062	114	68.9	188.8

205 rows × 5 columns

**Q11** Use train\_test\_split to split the data set as train:test=(80%:20%) ratio.

A11 Replace ??? with code in the code cell below

```
In [17]: from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=.2, random_
# View the shape of your data set
X_train.shape, X_test.shape, y_train.shape, y_test.shape
Out[17]: ((164, 5), (41, 5), (164,), (41,))
```

## **Regression Task**

## **Multiple Linear Regression**

**Q12** Fit multiple linear regression model on training data using all predictors, see (i) Linear Regression Example; (ii) scikit-learn linear model

$$Y = \beta_0 + \beta_1 * x_1 + \beta_2 * x_2 + \dots + \beta_p * x_p$$

A12: Replace ??? with code in the code cell below

```
In [18]:
    from sklearn.linear_model import LinearRegression

# Instantiate linear regression model
linear_model = LinearRegression()

# Fit the model to the training data using all predictors
linear_model.fit(X_train, y_train)

# Print the coefficients
print('Intercept (beta0):', linear_model.intercept_)
print('Coefficients (beta1, beta2, ..., betaP):', linear_model.coef_)
```

Intercept (beta0): -48350.72344500307
Coefficients (beta1, beta2, ..., betaP): [ 77.45307394 2.40643802 52.53065981
652.66827621 -16.62325241]

**Q13:** Model Scoring

- 1. Calculate the test MSE
- 2. Print the score from the model using test data

A13 Replace ??? with code in the code cell below

```
In [19]:
# Calculate the score on train and test sets
# Your code goes below
from sklearn.metrics import mean_squared_error
import matplotlib.pyplot as plt
y_pred= linear_model.predict(X_test)
mse = mean_squared_error(y_test, y_pred) # Calculate the test MSE
print("Test mean squared error (MSE): {:.2f}".format(mse))

print("Model score on test data:", linear_model.score(X_test, y_test))
```

Test mean squared error (MSE): 14134655.79 Model score on test data: 0.8209534347179518

## **Polinomial Regression**

**Q14:** Polynomial extension of the feature set captures the non-linear dependencies in the data

- Create a polinomial feature transformer with degree **TWO** using sklearn library PolynomialFeatures
- 2. Transform the training dataset using the polinomial feature transformer

**A14** Replace ??? with code in the code cell below

```
from sklearn.preprocessing import PolynomialFeatures
```

```
poiy = rolynomialreatures(degree=2)
poly_features = poly.fit_transform(X_train)
```

#### Q15: Train the new model

- 1. Create a LinearRegression model using sklearn
- 2. Train the model using the transformed Train data(X\_train)/ or Polinomial train data
- 3. Print the score for the Polinomial Regression for the Train data.

See (i) Linear Regression Example; (ii) Use the transformed X\_train features inside the score() function for the correct model scores.

**A15** Replace ??? with code in the code cell below

0.8911586225711094