# **Deep Learning and Temporal Data Processing**

0 - Gradient Descent

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July 10th, 2017

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# Agenda



**Gradient Descent** 

**Credits** 

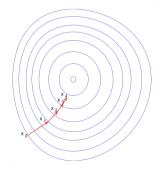
References

# **Gradient Descent**

### **Gradient Descent**



**Gradient descent** is an iterative optimization algorithm for finding the minimum of a function. How? Take step proportional to the negative of the gradient of the function at the current point.



Gradient descent on a series of level sets

# **Gradient Descent Update**



If we consider a function  $f(\theta)$ , the gradient descent update can be expressed as:

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} f(\boldsymbol{\theta}) \tag{1}$$

for each parameter  $\theta_i$ .

The size of the step is controlled by **learning rate**  $\alpha$ .

# Visualizing Gradient Descent

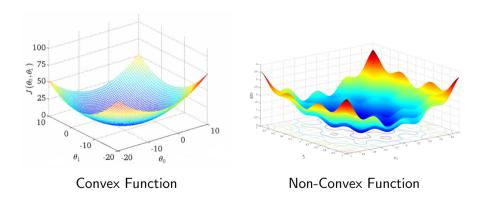


Gradient Descent for 1-d function  $f(\theta)$ .

# Convexity



Turns out that if the function is **convex** gradient descent will converge to the **global minimum**. For **non-convex** functions, it may converge to **local minima**.



### **Gradient Descent**



Gradient descent is often used in machine learning to **minimize a cost function**, usually also called *objective* or *loss* function and denoted  $L(\cdot)$  or  $J(\cdot)$ .

The cost function depends on the model's parameters and is a proxy to evaluate model's performance. Generally speaking, in this framework minimizing the cost equals to maximizing the effectiveness of the model.

## Stochastic Gradient Descent



In principle, to perform a single update step you should run through all your training examples. This is known as **batch gradient descent**.

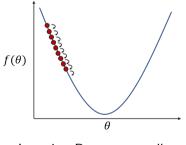
A different strategy is the one of **minibatch stochastic gradient descent**. In this case, only a small subset of the training dataset is considered at each update step.

In the extreme case in which only a random example of the training set is considered to perform the update step, we talk of **stochastic gradient descent**.

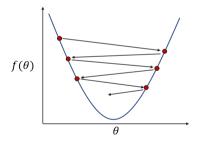
## **Learning Rate**



Choosing the the right **learning rate**  $\alpha$  is essential to correctly proceed towards the minimum. A step *too small* could lead to an extremely *slow* convergence. If the step is *too big* the optimizer could *overshoot* the minimum or even *diverge*.



Learning Rate too small



Learning Rate too big

## **Advanced Optimizers**



In practice, it's quite rare to see the procedure described above (so called **vanilla SGD**) used for optimization in the real-world.

Conversely, a number of cutting-edge optimizers [2, 1, 3] are commonly used. However, these advanced optimization techniques are out of the scope of this short overview.

# **Credits**

### Credits i



These slides heavily borrow from a number of awesome sources. I'm really grateful to all the people who take the time to share their knowledge on this subject with others.

### In particular:

- Stanford CS231n Convolutional Neural Networks for Visual Recognition http://cs231n.stanford.edu/
- Stanford CS20SI TensorFlow for Deep Learning Research http://web.stanford.edu/class/cs20si/syllabus.html
- Deep Learning Book (GoodFellow, Bengio, Courville)
   http://www.deeplearningbook.org/

## Credits ii



- Marc'Aurelio Ranzato, "Large-Scale Visual Recognition with Deep Learning"
   www.cs.toronto.edu/~ranzato/publications/ranzato\_cvpr13.pdf
- Convolution arithmetic animations
   https://github.com/vdumoulin/conv\_arithmetic
- Andrej Karphathy personal blog http://karpathy.github.io/
- WildML blog on AI, DL and NLP http://www.wildml.com/
- Michael Nielsen Deep Learning online book http://neuralnetworksanddeeplearning.com/

References

## References i



[1] J. Duchi, E. Hazan, and Y. Singer.

Adaptive subgradient methods for online learning and stochastic optimization.

Journal of Machine Learning Research, 12(Jul):2121-2159, 2011.

[2] D. Kingma and J. Ba.

Adam: A method for stochastic optimization.

arXiv preprint arXiv:1412.6980, 2014.

[3] M. D. Zeiler.

Adadelta: an adaptive learning rate method.

arXiv preprint arXiv:1212.5701, 2012.