Deep Learning and Temporal Data Processing

0 - Gradient Descent

Andrea Palazzi

July 10th, 2017

University of Modena and Reggio Emilia

Agenda



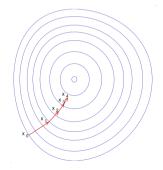
Gradient Descent

Credits

References



Gradient descent is an iterative optimization algorithm for finding the minimum of a function. How? Take step proportional to the negative of the gradient of the function at the current point.



Gradient Descent Update



If we consider a function $f(\theta)$, the gradient descent update can be expressed as:

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} f(\boldsymbol{\theta}) \tag{1}$$

for each parameter θ_i .

The size of the step is controlled by **learning rate** α .

Visualizing Gradient Descent

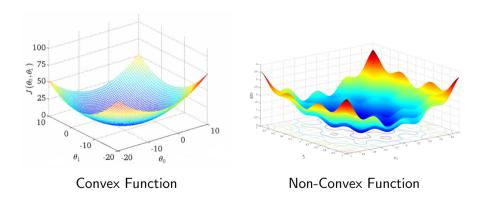


Gradient Descent for 1-d function $f(\theta)$.

Convexity



Turns out that if the function is **convex** gradient descent will converge to the **global minimum**. For **non-convex** functions, it may converge to **local minima**.





Gradient descent is often used in machine learning to **minimize a cost function**, usually also called *objective* or *loss* function and denoted $L(\cdot)$ or $J(\cdot)$.

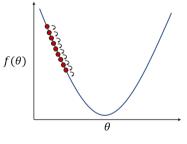
The cost function depends on the model's parameters and is a proxy to evaluate model's performance. Generally speaking, in this framework minimizing the cost equals to maximizing the effectiveness of the model.



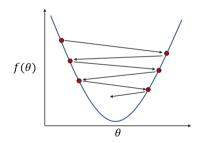
In practice, SGD



Choosing the the right **learning rate** α is essential to correctly proceed towards the minimum. A step *too small* could lead to an extremely *slow* convergence. If the step is *too big* the optimizer could *overshoot* the minimum or even *diverge*.



Learning Rate too small



Learning Rate too big

Advanced Optimizers



A number of different optimizer [2, 1, 3] are commonly used , but these are out of the scope of this short introduction.

Credits

Credits i



These slides heavily borrow from a number of awesome sources. I'm really grateful to all the people who take the time to share their knowledge on this subject with others.

In particular:

- Stanford CS231n Convolutional Neural Networks for Visual Recognition http://cs231n.stanford.edu/
- Deep Learning Book (GoodFellow, Bengio, Courville)
 http://www.deeplearningbook.org/
- Convolution arithmetic animations
 https://github.com/vdumoulin/conv_arithmetic

Credits ii



- Andrej Karphathy personal blog http://karpathy.github.io/
- WildML blog on AI, DL and NLP http://www.wildml.com/
- Michael Nielsen Deep Learning online book http://neuralnetworksanddeeplearning.com/

References

References i



[1] J. Duchi, E. Hazan, and Y. Singer.

Adaptive subgradient methods for online learning and stochastic optimization.

Journal of Machine Learning Research, 12(Jul):2121-2159, 2011.

[2] D. Kingma and J. Ba.

Adam: A method for stochastic optimization.

arXiv preprint arXiv:1412.6980, 2014.

[3] M. D. Zeiler.

Adadelta: an adaptive learning rate method.

arXiv preprint arXiv:1212.5701, 2012.