

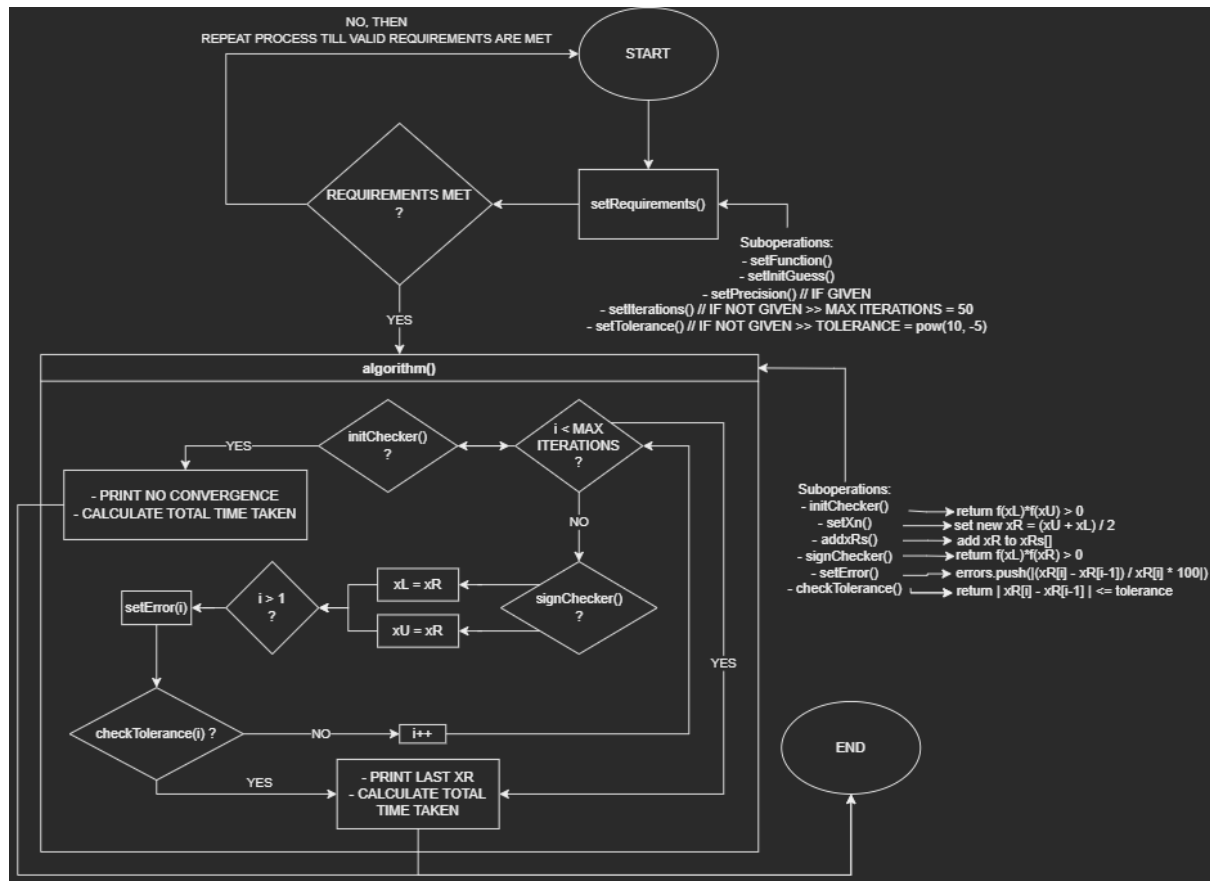
## PROJECT - PHASE 1

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# Bisection Method

## Flowchart



## Sample Runs

- Sample #1

### Bisection Method

\* Function

\* Initial Guess

Additional Specifications

...:

- Setting x root for iteration #2:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.0825$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.0825$
- Evaluating error at iteration #2
- Relative Error = 33.333%
- 
- Setting x root for iteration #3:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.06875$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.06875$
- Evaluating error at iteration #3
- Relative Error = 20%
- 
- Setting x root for iteration #4:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.061875$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned +. Setting x root to be the new x lower.  $x_{\text{lower}} = 0.061875$
- Evaluating error at iteration #4
- Relative Error = 11.111%
- 
- Setting x root for iteration #5:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.065312$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.065312$

And so on till iteration #10. Note that we have calculated time taken and plotted solutions.

- Setting x root for iteration #10:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.062412$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.062412$
- Evaluating error at iteration #10
- Relative Error = 0.17144%

Time taken: 6ms

- Sample #2

**Bisection Method**

\* Function

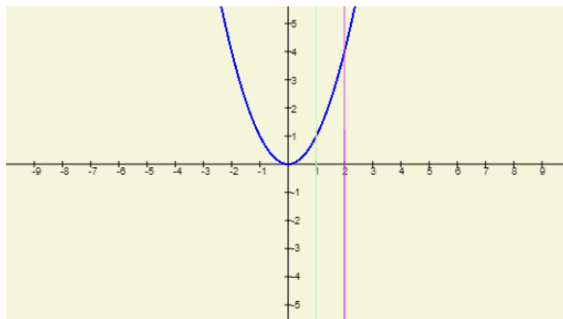
\* Initial Guess

Additional Specifications

**SOLVE**

$$x^2 \text{ root} = 0$$

$$\text{Init Guesses} = \{1, 2\}$$



The solution

**Bisection Method**

\* Function

\* Initial Guess

Additional Specifications

- Checking if the initial guesses would converge to a root or not by evaluating  $f(x_{\text{lower}}) * f(x_{\text{upper}})$ :
- Initial guesses would not converge to a root.

Time taken: 3ms

- Sample #3

**Bisection Method**

\* Function

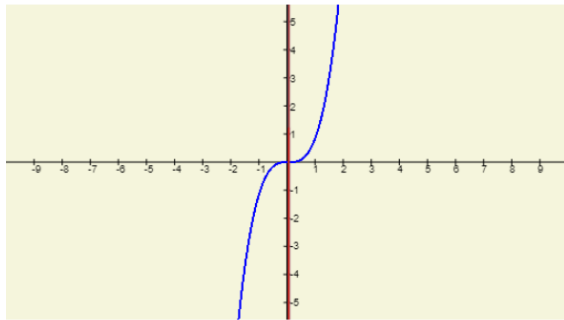
\* Initial Guess

Additional Specifications

**SOLVE**

When a user inputs

$$x_L > x_U$$



Program still functions  
properly &  
calculates  
 $x_r$

### Bisection Method

\* Function

$x^3 - 0.165x^2 + 3.993 \times 10^{-4}$

\* Initial Guess

0.11

0

Additional Specifications

Number of Iterations, Default = 50

Tolerance, Default = 10 to power -5

Precision, Default = Machine's Default

- 
- Checking if the initial guesses would converge to a root or not by evaluating  $f(x_{\text{lower}}) * f(x_{\text{upper}})$ :
- Initial guesses would converge to a root.
- 
- Setting x root for iteration #1:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.055$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.055$
- 
- 
- Setting x root for iteration #12:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.06238525390625001$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned +. Setting x root to be the new x lower.  $x_{\text{lower}} = 0.06238525390625001$
- Evaluating error at iteration #12
- Relative Error = 0.04304778303917882%
- 
- Setting x root for iteration #13:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.062371826171875006$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper.  $x_{\text{upper}} = 0.062371826171875006$
- Evaluating error at iteration #13
- Relative Error = 0.021528525296019892%
- 
- Setting x root for iteration #14:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.062378540039062506$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned +. Setting x root to be the new x lower.  $x_{\text{lower}} = 0.062378540039062506$
- Evaluating error at iteration #14
- Relative Error = 0.010763104079217779%
- Tolerance satisfied. ROOT FOUND!  $x_{\text{root}} = 0.062378540039062506$

Time taken: 7ms

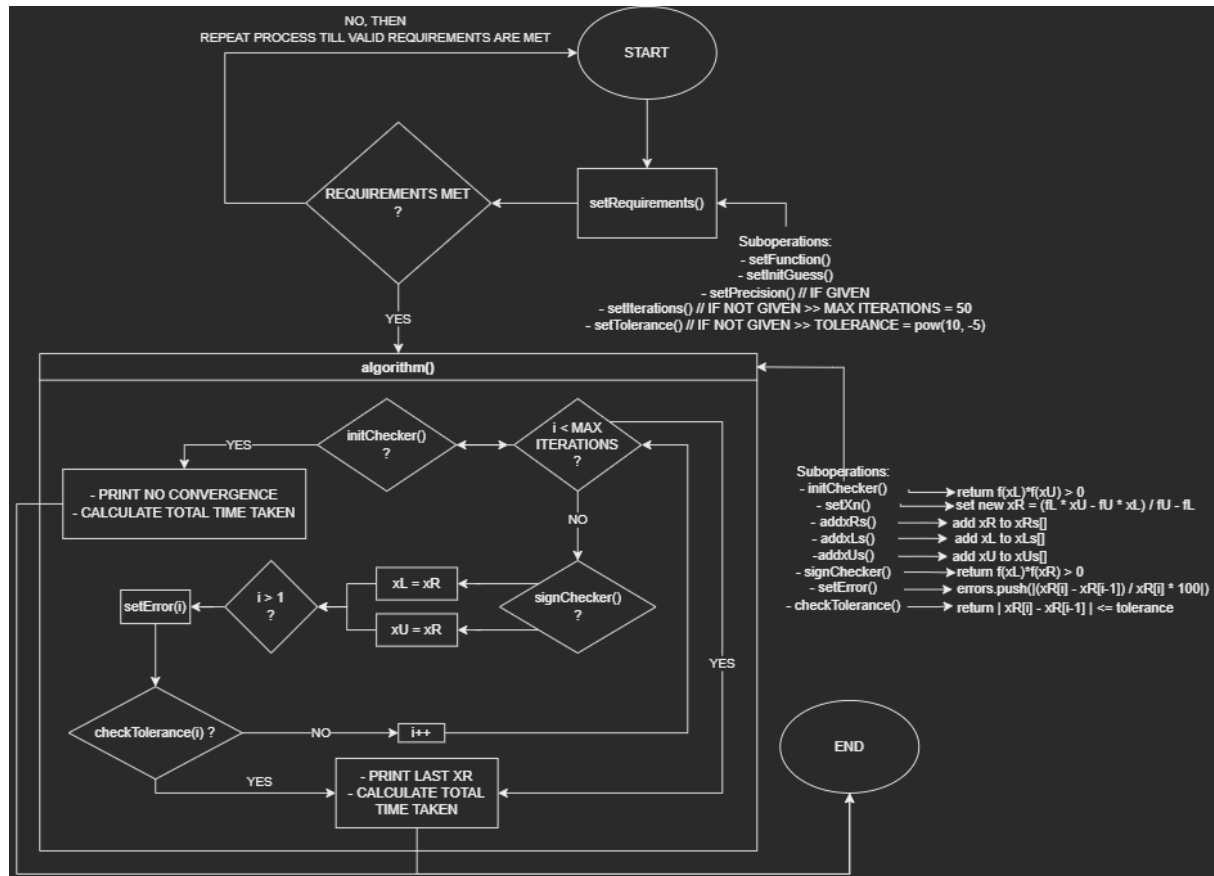
### Used Data Structure

- ArrayLists used as a good storage for variables at the runtime
- Maps was useful when evaluating the equation input

# False-Position Method

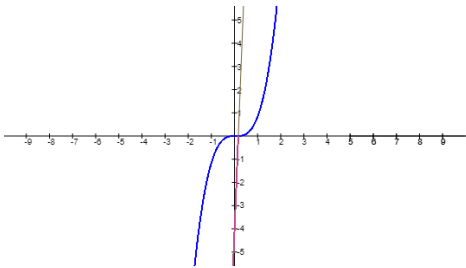
## Flowchart

We note that the flowchart of false-position is pretty much like bisection with slight changes.



Sample Runs

• Sample #1



Continue....:

False-Position Method

\* Function

x<sup>3</sup>-0.165\*x<sup>2</sup>+3.993\*10<sup>-4</sup>

\* Initial Guess

-5

5

Additional Specifications

Number of Iterations, Default = 50

Tolerance, Default = 10 to power -5

Precision, Default = Machine's Default

•

• Checking if the initial guesses would converge to a root or not by evaluating f(x lower) \* f(x upper):

• Initial guesses would converge to a root.

•

• Setting x root for iteration #1: x root = (xl + xu) / 2 = 0.1649840279999987

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.1649840279999987

•

• Setting x root for iteration #2: x root = (xl + xu) / 2 = 0.1649680734394242

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.1649680734394242

• Evaluating error at iteration #2

• Relative Error = 0.009671301993783899%

•

•

• Setting x root for iteration #3: x root = (xl + xu) / 2 = 0.16495213629240127

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.16495213629240127

• Evaluating error at iteration #3

• Relative Error = 0.009661679673364246%

•

• Setting x root for iteration #4: x root = (xl + xu) / 2 = 0.16493621653311102

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.16493621653311102

• Evaluating error at iteration #4

• Relative Error = 0.00965207013042464%

•

• Setting x root for iteration #5: x root = (xl + xu) / 2 = 0.164920314135785

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.164920314135785

• Evaluating error at iteration #5

• Relative Error = 0.009642473341958632%

•

• Setting x root for iteration #6: x root = (xl + xu) / 2 = 0.16490442907470615

• Checking whether f(x lower) \* f(x root) is positive, negative, or zero:

• Evaluation returned -. Setting x root to be the new x upper. x upper = 0.16490442907470615

• Evaluating error at iteration #6

• Relative Error = 0.009632889285017985%

•

And so on till all iterations are consumed. Note that we have calculated time taken and plotted solutions

```

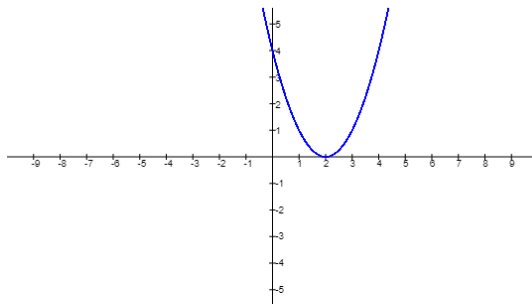
• Setting x root for iteration #48: x root = (xl + xu) / 2
= 0.1642525780225253
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = 0.1642525780225253
• Evaluating error at iteration #48
• Relative Error = 0.009241559555729632%
•
• Setting x root for iteration #49: x root = (xl + xu) / 2
= 0.16423741479992152
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = 0.16423741479992152
• Evaluating error at iteration #49
• Relative Error = 0.009232501998557073%
•
• Setting x root for iteration #50: x root = (xl + xu) / 2
= 0.16422226783095314
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = 0.16422226783095314
• Evaluating error at iteration #50
• Relative Error = 0.009223456214819408%
• Max iterations consumed. ROOT FOUND! x root =
0.16422226783095314

```

Time taken: 41ms

### • Sample #2

In this case, the user initial guess outputs positive values when entering the function. False Position would never converge in such a case.



### False-Position Method

\* Function

(x-2)\*2

\* Initial Guess

-5

5

Additional Specifications

Number of Iterations, Default = 50

Tolerance, Default = 10 to power -5

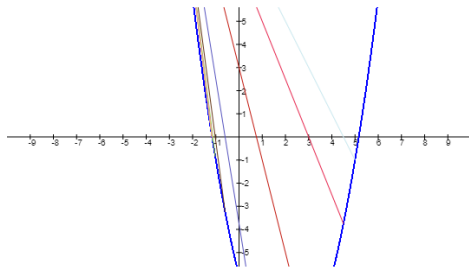
Precision, Default = Machine's Default

- 
- Checking if the initial guesses would converge to a root or not by evaluating  $f(x_{\text{lower}}) * f(x_{\text{upper}})$ :
- Initial guesses would not converge to a root.

Time taken: 2ms



- Sample #3



## False-Position Method

\* Function

 $(x-2)^2-10$ 

\* Initial Guess

-3

5

Additional Specifications

Number of Iterations, Default = 50

Tolerance, Default = 10 to power -5

Precision, Default = Machine's Default

- 
- Checking if the initial guesses would converge to a root or not by evaluating  $f(x_{\text{lower}}) * f(x_{\text{upper}})$ :
- Initial guesses would converge to a root.
- 
- Setting x root for iteration #1:  $x_{\text{root}} = (x_l + x_u) / 2 = 4.5$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = 4.5
- 
- Setting x root for iteration #2:  $x_{\text{root}} = (x_l + x_u) / 2 = 3$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = 3
- Evaluating error at iteration #2
- Relative Error = 50%
- 
- 
- Setting x root for iteration #3:  $x_{\text{root}} = (x_l + x_u) / 2 = 0.75$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = 0.75
- Evaluating error at iteration #3
- Relative Error = 300%
- 
- 
- Setting x root for iteration #4:  $x_{\text{root}} = (x_l + x_u) / 2 = -0.6$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = -0.6
- Evaluating error at iteration #4
- Relative Error = 225.00000000000006%
- 
- 
- Setting x root for iteration #5:  $x_{\text{root}} = (x_l + x_u) / 2 = -1.0263157894736843$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = -1.0263157894736843
- Evaluating error at iteration #5
- Relative Error = 41.53846153846155%
- 
- 
- Setting x root for iteration #6:  $x_{\text{root}} = (x_l + x_u) / 2 = -1.131147540983607$
- Checking whether  $f(x_{\text{lower}}) * f(x_{\text{root}})$  is positive, negative, or zero:
- Evaluation returned -. Setting x root to be the new x upper. x upper = -1.131147540983607
- Evaluating error at iteration #6
- Relative Error = 9.267734553775767%
-

And so on till convergence on iteration #13.

```
• Setting x root for iteration #11: x root = (xl + xu) / 2
= -1.1622595607293897
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = -1.1622595607293897
• Evaluating error at iteration #11
• Relative Error = 0.005359281473255834%
•
• Setting x root for iteration #12: x root = (xl + xu) / 2
= -1.162273585102753
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = -1.162273585102753
• Evaluating error at iteration #12
• Relative Error = 0.0012066327190982536%
•
• Setting x root for iteration #13: x root = (xl + xu) / 2
= -1.1622767426741225
• Checking whether f(x lower) * f(x root) is positive,
negative, or zero:
• Evaluation returned -. Setting x root to be the new x
upper. x upper = -1.1622767426741225
• Evaluating error at iteration #13
• Relative Error = 0.00027167121680662%
• Tolerance satisfied. ROOT FOUND! x root =
-1.1622767426741225
```

Time taken: 8ms

## Used Data Structure

- ArrayLists used as a good storage for variables at the runtime
- Maps was useful when evaluating the equation input

## Secant Method:

- **Data Structures used:** Array.
- **Pseudo code:**

Secant Function

beginTime = time of beginning

While(maxIteration > 0 && relativeError > tolerance && !diverge )

prevRelative = (x - prevX)/x

nextX = x - (( F(x) \* (prevX - x)) / (F(prevX)-F(x) ))

relativeError =(nextX - x) / nextX

If( relativeError > prevRelative)

divergeTimes--

End If

If( divergeTimes = 0)

diverge = true

End If

prevCoff.push(prevX);

prevCoffSub.push( F(prevX) )

coff.push(x);

coffSub.push( F(x) )

nextCoff.push( nextX )

nextCoffSub.push( F(nextX) )

relatives.push( relativeError \* 100

prevX = x

$x = \text{nextX}$

$\text{maxIteration} -$

$\text{runtime} = \text{beginTime} - \text{EndTime}$

End While

End Function

- **Sample run:**



## Secant Method (you can modify and solve again without refresh)

**Run Time = 516 milli second**

Iteration: 0

$X_0 = -9 \parallel X_1 = 15 \parallel X_2 = 3$

$F(X_0) = -36 \parallel F(X_1) = 36 \parallel F(X_2) = 0$

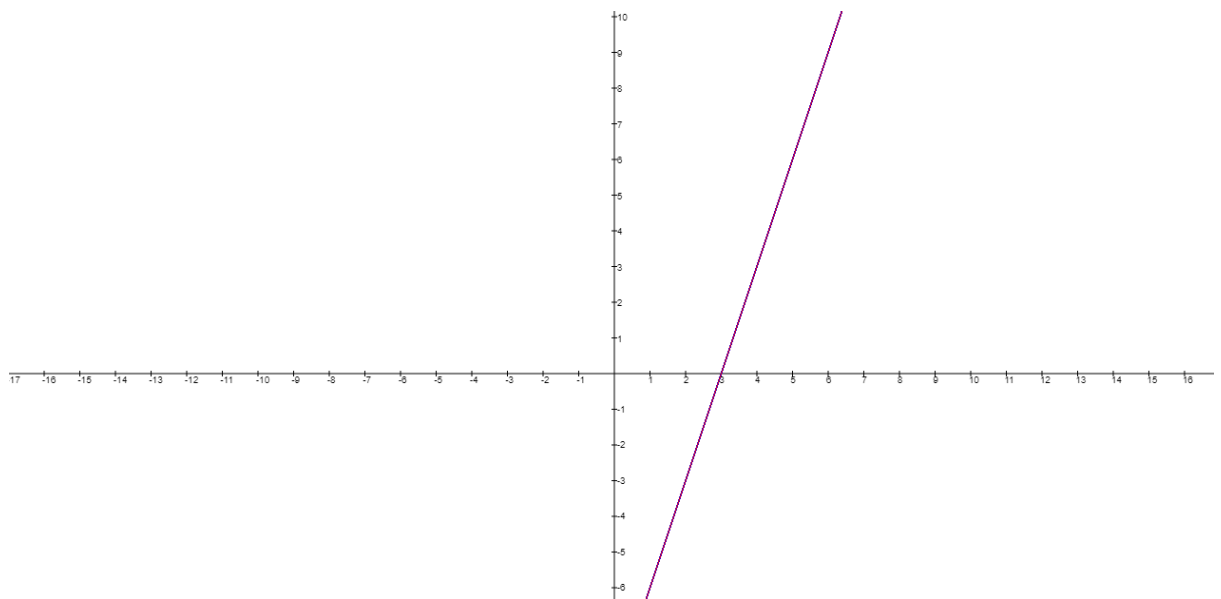
Relative Error = 400%

Iteration: 1

$X_1 = 15 \parallel X_2 = 3 \parallel X_3 = 3$

$F(X_1) = 36 \parallel F(X_2) = 0 \parallel F(X_3) = 0$

Relative Error = 0%



**Secant Method**  
**(you can modify and solve again without refresh)**

**Run Time = 638 milli second**

Iteration: 0

$X_0 = -18 \parallel X_1 = 20 \parallel X_2 = -70.2$

$F(X_0) = 261 \parallel F(X_1) = 451 \parallel F(X_2) = 4708.44$

Relative Error = 128%

Iteration: 1

$X_1 = 20 \parallel X_2 = -70.2 \parallel X_3 = 29.6$

$F(X_1) = 451 \parallel F(X_2) = 4708.44 \parallel F(X_3) = 955.96$

Relative Error = 337%

Iteration: 2

$X_2 = -70.2 \parallel X_3 = 29.6 \parallel X_4 = 55$

$F(X_2) = 4708.44 \parallel F(X_3) = 955.96 \parallel F(X_4) = 3181$

Relative Error = 46.2%

Iteration: 3

$X_3 = 29.6 \parallel X_4 = 55 \parallel X_5 = 18.7$

$F(X_3) = 955.96 \parallel F(X_4) = 3181 \parallel F(X_5) = 396.78999999999996$

Relative Error = 194%

Iteration: 4

$X_4 = 55 \parallel X_5 = 18.7 \parallel X_6 = 13.5$

$F(X_4) = 3181 \parallel F(X_5) = 396.78999999999996 \parallel F(X_6) = 213.75$

Relative Error = 38.5%

Iteration: 5

$X_5 = 18.7 \parallel X_6 = 13.5 \parallel X_7 = 7.43$

$F(X_5) = 396.78999999999996 \parallel F(X_6) = 213.75 \parallel F(X_7) = 68.4949$

Relative Error = 81.69999999999999%

Iteration: 6

$X_6 = 13.5 \parallel X_7 = 7.43 \parallel X_8 = 4.57$

$F(X_6) = 213.75 \parallel F(X_7) = 68.4949 \parallel F(X_8) = 25.594900000000003$

Relative Error = 62.6%



Iteration: 7

$X_7 = 7.43 \parallel X_8 = 4.57 \parallel X_9 = 2.86$

$F(X_7) = 68.4949 \parallel F(X_8) = 25.594900000000003 \parallel F(X_9) = 7.759599999999999$

Relative Error = 59.8%

Iteration: 8

$X_8 = 4.57 \parallel X_9 = 2.86 \parallel X_{10} = 2.12$

$F(X_8) = 25.594900000000003 \parallel F(X_9) = 7.759599999999999 \parallel F(X_{10}) = 1.8544000000000018$

Relative Error = 34.9%

Iteration: 9

$X_9 = 2.86 \parallel X_{10} = 2.12 \parallel X_{11} = 1.89$

$F(X_9) = 7.759599999999999 \parallel F(X_{10}) = 1.8544000000000018 \parallel F(X_{11}) = 0.24210000000000065$

Relative Error = 12.2%

Iteration: 10

$X_{10} = 2.12 \parallel X_{11} = 1.89 \parallel X_{12} = 1.86$

$F(X_{10}) = 1.8544000000000018 \parallel F(X_{11}) = 0.24210000000000065 \parallel F(X_{12}) = 0.03960000000000008$

Relative Error = 1.609999999999999%

Iteration: 11

$X_{11} = 1.89 \parallel X_{12} = 1.86 \parallel X_{13} = 1.85$

$F(X_{11}) = 0.24210000000000065 \parallel F(X_{12}) = 0.03960000000000008 \parallel F(X_{13}) = -0.02749999999999858$

Relative Error = 0.541%

Iteration: 12

$X_{12} = 1.86 \parallel X_{13} = 1.85 \parallel X_{14} = 1.85$

$F(X_{12}) = 0.03960000000000008 \parallel F(X_{13}) = -0.02749999999999858 \parallel F(X_{14}) = -0.02749999999999858$

Relative Error = 0%

