

**Computing and Data Science**

***Simulations***

**Assignment no. 5 (Continuous Distributions)**

**3<sup>rd</sup> Year**

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1. Let  $x$  be the random variable described by the **uniform probability** distribution with its lower bound at  $a = 120$ , upper bound at  $b = 140$ . Find the following:

- a. PDF
- b. Average
- c. SD
- d. Variance
- e.  $p(x = 130)$
- f.  $p(125 \leq x \leq 135)$

Answer:

$$\text{a. pdf} = \left\{ \frac{1}{b-a} \quad a \leq x \leq b \right.$$

$$\text{pdf} = \frac{1}{140-120} = 0.05 \quad 120 \leq x \leq 140$$

$$\text{b. } E(x) = \frac{140+120}{2} = 130$$

$$\text{c. SD} = \frac{(b-a)}{\sqrt{12}} = \frac{140-120}{\sqrt{12}} = 5.77305$$

$$\text{d. Variance} = \frac{(b-a)^2}{12} = 33.333333$$

$$\text{e. } p(x = 130) = \frac{1}{b-a} = 0.05$$

$$\begin{aligned} \text{f. } p(125 \leq x \leq 135) &= F(135) - F(125) \\ &= \frac{135-125}{140-120} = 0.5 \end{aligned}$$

2. According to British weather forecasters, the average monthly rainfall in London during the month of June is  $\mu = 2.09$  inches. Assume the monthly precipitation is a normally-distributed random variable with a standard deviation of  $\sigma = 0.48$  inches.
- What is the probability that London will have between 1.5 and 2.5 inches of precipitation next June?
  - What is the probability that London will have 1 inch or less of precipitation?
  - If London authorities prepare for flood conditions when the monthly precipitation falls in the upper 5% of the normal June amounts, how much rain would have to fall to cause local authorities to begin flood preparations?

Answer:

a.  $p(1.5 \leq x \leq 2.5) =$

$$= p\left(\frac{1.5-2.09}{0.48} \leq z \leq \frac{2.5-2.09}{0.48}\right)$$

$$= p(-1.229 \leq z \leq 0.854)$$

$$= \Phi(0.854) - \Phi(-1.229)$$

$$= \Phi(0.854) - (1 - \Phi(1.229))$$

$$= 0.693$$

b.  $p(x \leq 1) = p\left(z \leq \frac{1-2.09}{0.48}\right) = p(z \leq -2.2708) = 0.0116$

c.  $P(Z > z) = 0.05 = P(Z \leq z) = 0.95$

$$\frac{x-2.09}{0.48} = z_{0.95} = \Phi^{-1}(0.95) = 1.64$$

$$x = 1.64 \cdot 0.48 + 2.09 = 2.8772$$

3. The number of visits to the Book4Less.com discount travel website is a Poisson- distributed random variable with a mean arrival rate of 10 visits per minute.

a. What is the CDF?

b. What is the standard deviation of the distribution?

Answer:

$$\text{a. CDF} = \sum_{i=0}^{k=10} \frac{e^{-\lambda} * \lambda^i}{i!} = \sum_{i=0}^{k=10} \frac{e^{-10} * 10^i}{i!}$$

$$\text{b. standard deviation} = \sqrt{10}$$

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4. Solve same Erlang question with three lambs in the device.

Answer:

$$k = 3$$

$$E = 1/k\theta$$

$$\theta = 0.0003$$

$$F(2160) = 1 - \sum_{i=0}^{k-1} \frac{e^{-k\theta x} k\theta x^i}{i!} = 1 - \sum_{i=0}^2 \frac{e^{-1.944} 1.944^i}{i!} = 0.308$$

the required probability is  $1 - 0.308 = 0.6918$