

**Predictive Modelling** 

Week 05-BEM2031 Term2: 2023/24



# **Today:**

- What is random?
- What is predictive modelling?
- Making a ML model work: a step-by-step approach
- Supervised learning
  - Regression
  - Classification

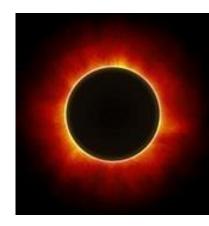
# Types of Analytics:

- Descriptive Analytics: WHAT happened (or is happening)?
- Diagnostic Analytics: WHY did it happen?
- Predictive Analytics: WHAT is likely to happen in the future?
- Prescriptive Analytics: WHAT can we do about it?









List of solar eclipses in the 21st century -Wikipedia

Date	Time	Saros	Туре	Magnitude	Duration	Location	Path	width	Geography
									Total: Mexico,
									central and
									northeastern
									United States,
April 8, 2024	18:18:29	139	Total	1.057	4:28	25.3°N 104.1°W	198	123	East Canada
									Partial: North
									America,
									Central

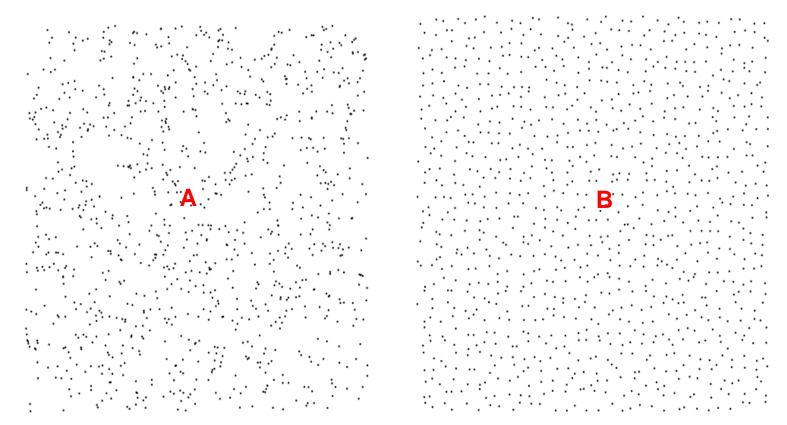


Random in the context of prediction models means that some aspect of the model is determined by chance rather than by design.



Randomness is also a source of uncertainty and error. Random phenomena are difficult to measure, predict, and control.





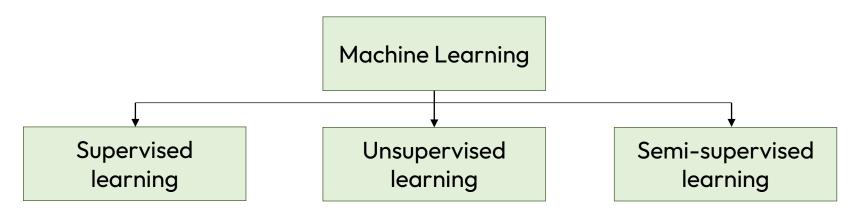
Which of these could be modelled and which is completely random?



- set.seed(42)
- Create these random fields of points
- Random coin throw, random dice

week_05_age_balance	<b>②</b>	16/11/2023 17:45	Microsoft Exc
® week_05_what_is_random	<b>⊘</b>	07/02/2024 13:21	RMD File
week_05_yummy_mushrooms_prep	$\odot$	16/11/2023 17:45	RMD File
Week5_yummy_mushrooms_prep	$\odot$	21/11/2023 18:57	Microsoft Edg
Week5_yummy_mushrooms_prep.knit	$\odot$	21/11/2023 18:56	MD File
Week5_yummy_mushrooms_prep	$\odot$	16/11/2023 18:17	RMD File

# Supervised vs Unsupervised methods

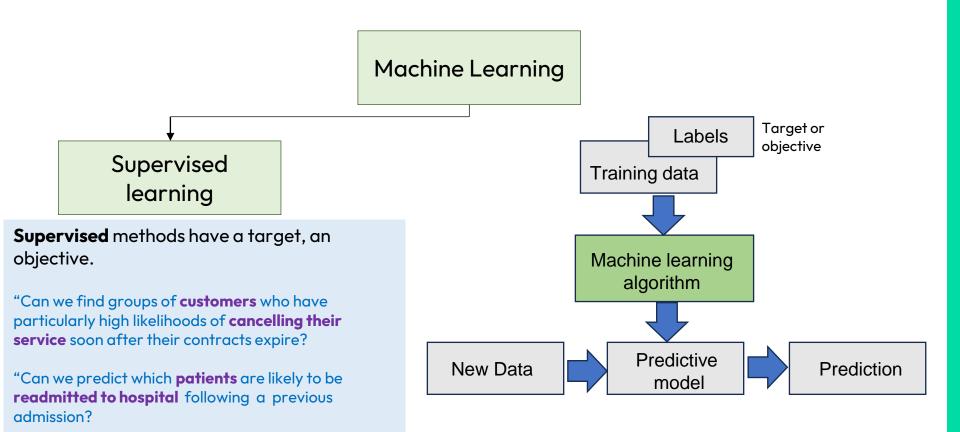


**Supervised** methods have a target, an objective.

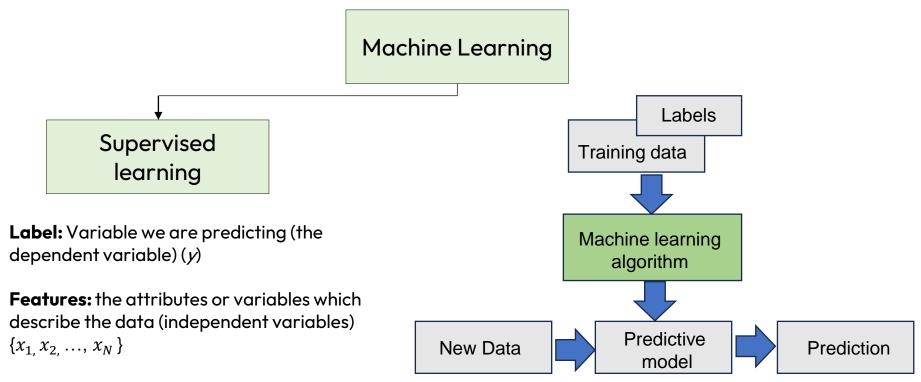
"Can we find groups of customers who have particularly high likelihoods of cancelling their service soon after their contracts expire?" **Unsupervised** methods have no specific target.

"Do our customers naturally fall into different groups

# Supervised vs Unsupervised methods

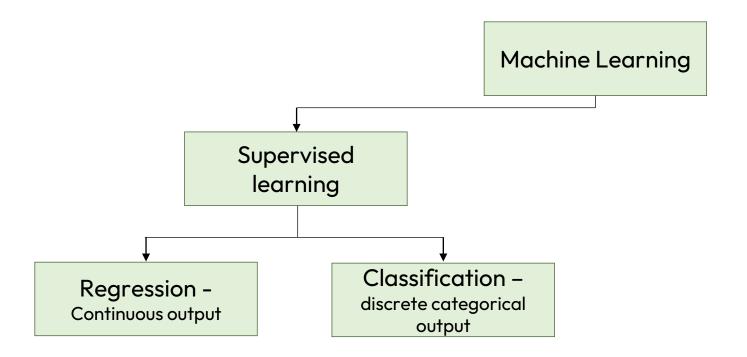


# Supervised vs Unsupervised methods



**Unseen (new) data:** test the performance of the model y=f(x) on unlabelled data

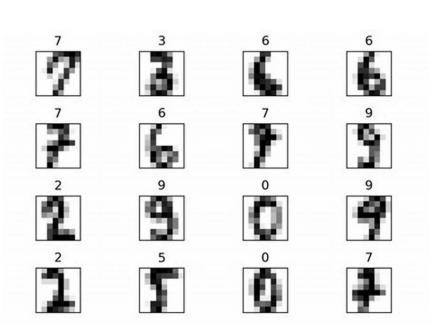
# Types of supervised learning



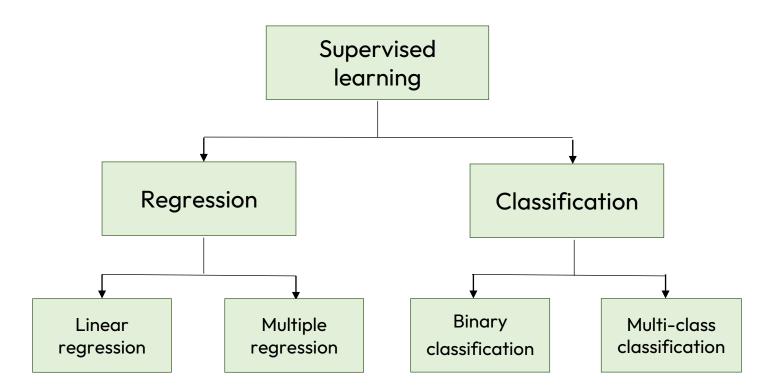
# Regression or classification?



- Weather prediction
- Identification of cancer cells
- Identification of handwritten digits
- Oil price prediction
- Identification of fraudulent credit card transactions
- Monthly income prediction



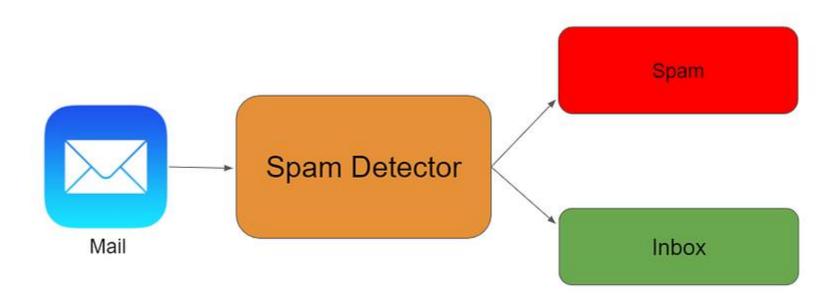
# Machine Learning





# Example: Email spam prediction

Trained on a large number of spam and non-spam emails, the algorithm's goal is to predict whether or not an email is spam





## Regression: House Price Prediction

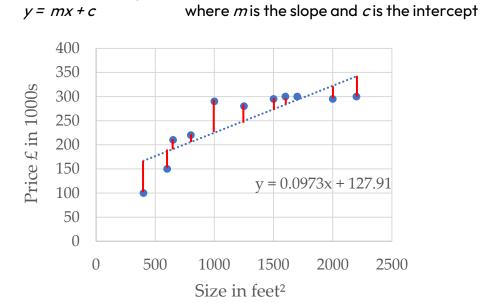
Given a set of input features (which may influence the price of a house), the goal of the algorithm is to predict the price of a new house going to market

#### House Price Prediction

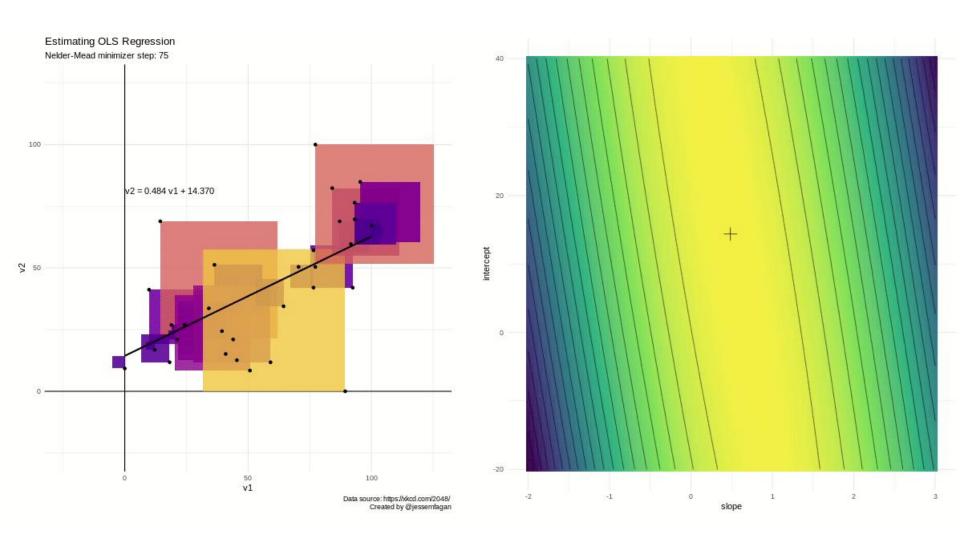
	Price (\$) in 1000's	Num of floors	Parking Facility?	Garden?	Num of Rooms	Square footage
	460	2		Yes	3	
Labeled Examp	320	1	No	No		1700
					5	
	•					
(y)	arget/Dependent Variable	, <b>x</b> <sub>n</sub> ) Ta	dent Variables (x <sub>1</sub> , x <sub>2</sub> ,	ures/Independ	Attributes/Feat	



- Feature Selection input variables that can used to predict house prices
  let's consider one input variable (size in sq.ft) → univariate/simple regression
- Simple linear regression finds a linear function (straight line) that predicts the target variable (y) as a function of the features or independent variables (x)



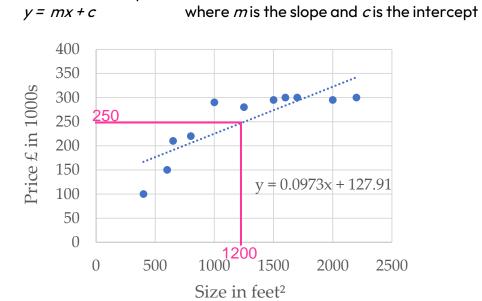
Features/independent variables (x)	Target/dependent variable (y)
Size in feet <sup>2</sup>	Price £ in 1000s
400	100
600	150
650	210
800	220
1000	290
1250	280
1500	295
1600	300
1700	300
2000	295
2200	300





Consider the problem of **predicting house prices (y)** 

- Feature Selection input variables that can used to predict house prices
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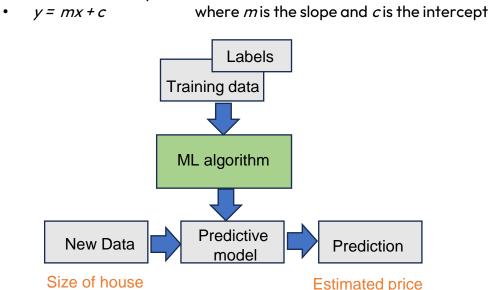


variables (x)	Target/dependent variable (y)
Size in feet <sup>2</sup>	Price £ in 1000s
400	100
600	150
650	210
800	220
1000	290
1250	280
1500	295
1600	300
1700	300
2000	295
2200	300

Footures/independent



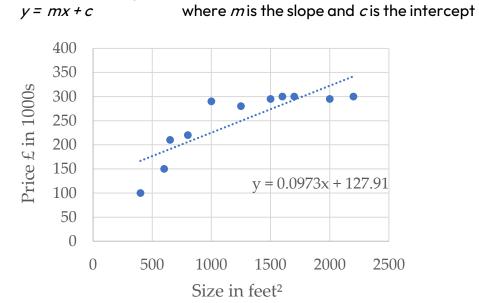
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Features/independent variables (x)	Target/dependent variable (y)
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1000	290
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1500	295
1600	300
1700	300
2000	295
2200	300

## Multiple Linear Regression



- Feature Selection input variables that can used to predict house prices
  let's consider multiple input variable → multiple linear regression
- Multiple linear regression models a linear function that predicts a target variable as a function of the independent variables:  $y = a_0 + a_1x_1 + a_2x_2 + a_3x_3 + ...$

Square footage	Num of Rooms	Garden?	Parking Facility?	Num of floors	Price (\$) in 1000's	
	3	Yes		2	460	
1700		No	No	1	320	
	5					<i>m</i> training
						examples
						·
					<b></b>	
	Attributes/Featu	ures/Indepen	dent Variables (X1. X2	<b>x</b> <sub>n</sub> ) Ta	arget/Dependent Variable	(v)



# Problems faced: Underfitting

## Should we use linear regression?

	Year	Value	1.0						•
0	1960	5.918412e+10							•
1	1961	4.955705e+10	0.8	-					•
2	1962	4.668518e+10							•
3	1963	5.009730e+10	0.6						•
4	1964	5.906225e+10	8						•
5	1965	6.970915e+10	0.4	1					•
6	1966	7.587943e+10	0.2						
7	1967	7.205703e+10						********	
8	1968	6.999350e+10	0.0	196	*******	00000000	***************************************		
9	1969	7.871882e+10		1960	1970	1980	1990 Year	2000	2010
							rear		

These data points correspond to China's gross domestic product (GDP) from 1960–2014.

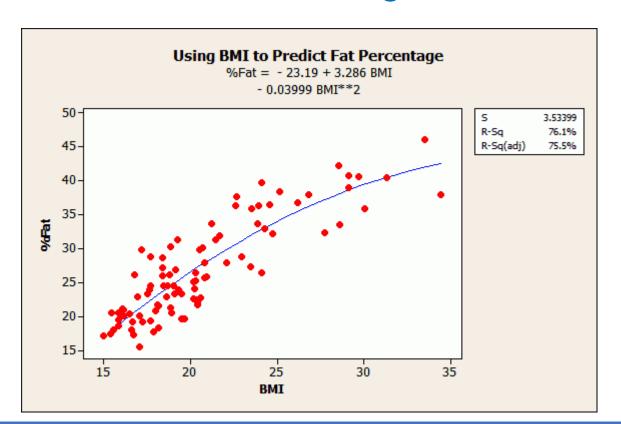
Model is not complex enough to capture the underlying patterns in the data.

#### Leads to bias:

The amount of error introduced by approximating real-world phenomena in a simplified model

# Non-linear regression





If a regression equation doesn't follow the rules for a linear model, then it must be a nonlinear model.

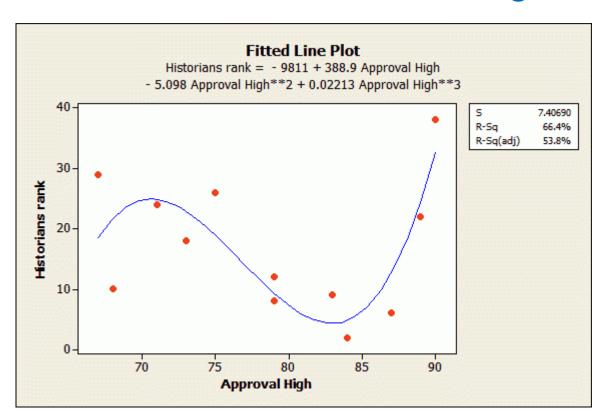
The regression example models the relationship between body mass index (BMI) and body fat percent.

It is a linear model that uses a quadratic (squared) term to model the curved relationship.

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_1^2$$

# Problems faced: Overfitting





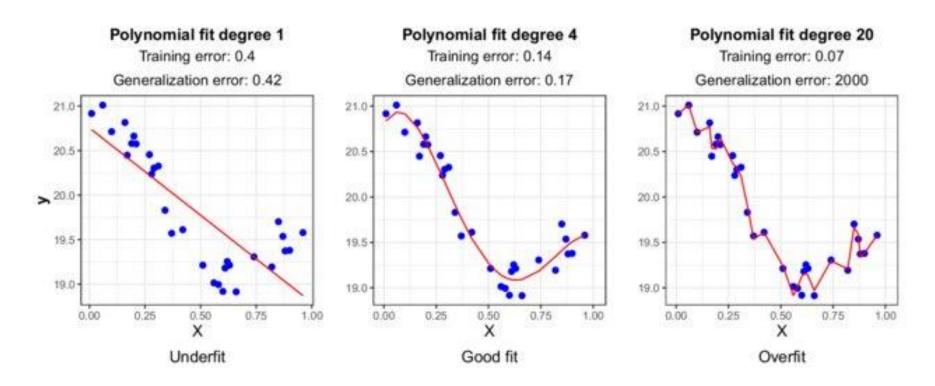
If you try to estimate too many parameters, you will overfit!

The size of your dataset restricts the number of terms you can safely add to your model

If your study calls for a complex model, you must collect a relatively large sample size.

# Problems faced: Overfitting

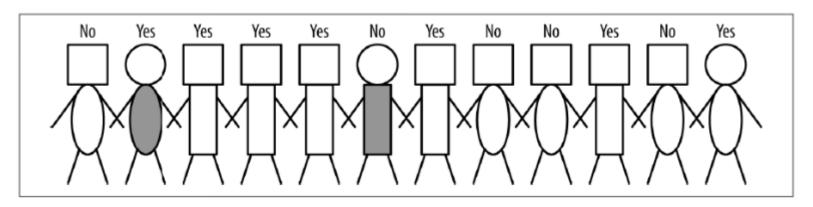




Badillo, S., Banfai, B., Birzele, F., Davydov, I.I., Hutchinson, L., Kam-Thong, T., Siebourg-Polster, J., Steiert, B. and Zhang, J.D. (2020), An Introduction to Machine Learning. Clin. Pharmacol. Ther., 107: 871-885 <a href="https://doi.org/10.1002/cpt.1796">https://doi.org/10.1002/cpt.1796</a>

### Classification





#### Attributes:

Head shape: square, circle Body shape: rectangle, oval Body colour: grey, white

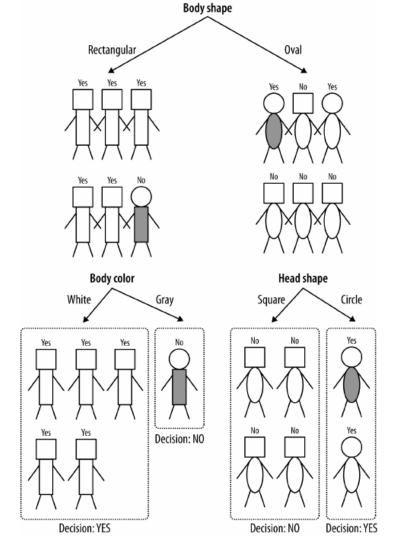
### Target:

Write-off: yes, no

Attributes rarely split a group perfectly

Not all attributes are binary

How do we segment for numeric values?





### Classification: Decision trees

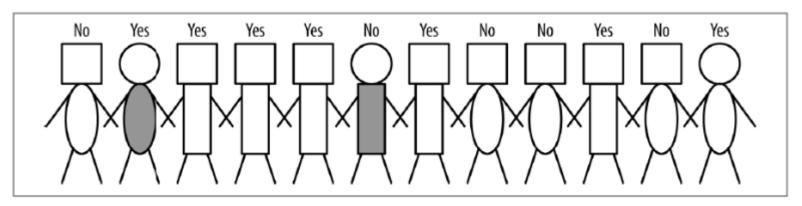
A decision tree is a model with a number of branching options that lead to a decision at the end.

Each point on the tree is called a **node**. The **depth** of the of the tree is maximum number of steps to reach a decision.

A **leaf** of the tree is where the decision is made (when there's no more splitting).

### Classification – decision trees





### Entropy:

The amount of uncertainty or randomness in a system

### Information gain:

Measures the amount of reduction in entropy or uncertainty about a random variable after observing another random variable

→ How *impure* a node (how mixed the training data assigned to that node is)

→ To decide which attribute to split on at each step in a decision tree by selecting the attribute which results in most significant reduction in entropy Features that result in a higher information gain are considered more important – as they provide more information

# Classification - entropy

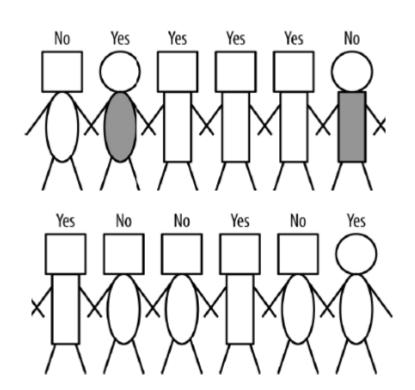


An information gain is how much an attribute improves (or decreases) **entropy** (uncertainty) of the model prediction.

$$entropy = -p_1 \log(p_1) - p_2 \log(p_2) - \dots$$

$$p_yes = 7/12$$
  
 $p_no = 5/12$ 

$$entropy(S) = -\left[\left(\frac{7}{12}\right) \times \log_2\left(\frac{7}{12}\right) + \left(\frac{5}{12}\right) \times \log_2\left(\frac{5}{12}\right)\right]$$
$$= 0.98$$



# Classification - entropy

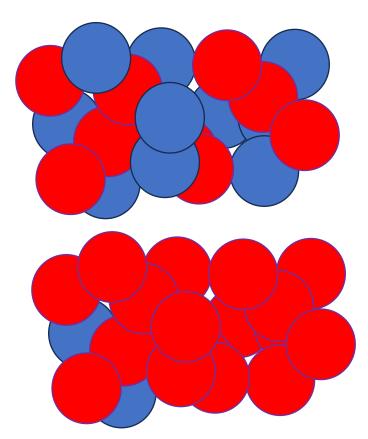


Pick a ball at random and guess the colour! The chances of being right or wrong depends on the mix of colours.

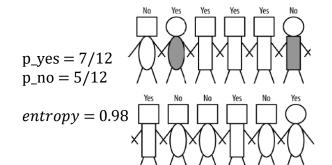
If your bag has an equal number of red and blue balls, your uncertainty is highest – this is a state of high entropy.

If the bag has mostly red balls, and not many blue balls, you'd probably guess red, and you would be right most of the time. This is a state of low entropy.

Entropy quantifies the uncertainty.



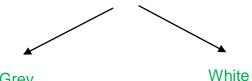




IG(parent, children) = entropy(parent)  $p(c_1) \times entropy(c_1) + p(c_2) \times entropy(c_2) +$ ...

$$IG = 0.98 - (0.17 \times 1.0 + 0.83 \times 0.97)$$
$$= 0.005$$

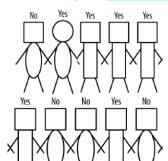
### Body colour



Grey

 $p_{yes} = 1/2$  $p_{no} = 1/2$ entropy = 1.0

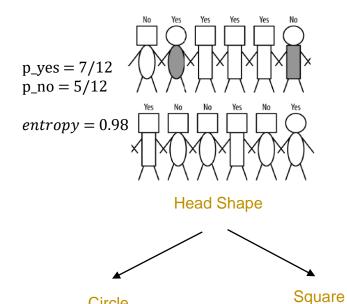




$$p_yes = 6/10$$
  
 $p_no = 4/10$ 

entropy = 0.97





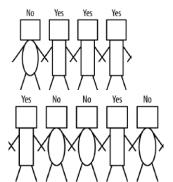
$$IG = entropy(base) - p(c_1) \times entropy(c_1) + p(c_2) \times entropy(c_2) + \dots$$

$$IG = 0.98 - (0.25 \times 0.92 + 0.75 \times 0.99)$$
$$= 0.0075$$

$$p_yes = 2/3$$
  
 $p_no = 1/3$ 

entropy = 0.92

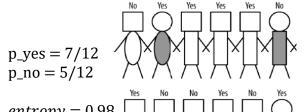


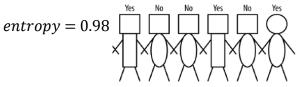


$$p_yes = 5/9$$
  
 $p_no = 4/9$ 

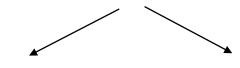
entropy = 0.99



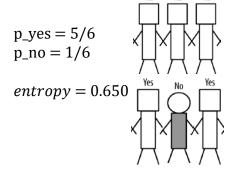




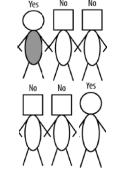
### **Body Shape**



#### Rectangle



#### Oval



$$IG = entropy(base) - p(c_1) \times entropy(c_1) + p(c_2) \times entropy(c_2) + \dots$$

$$IG = 0.98 - (0.5 \times 0.650 + 0.5 \times 0.918)$$
$$= 0.196$$

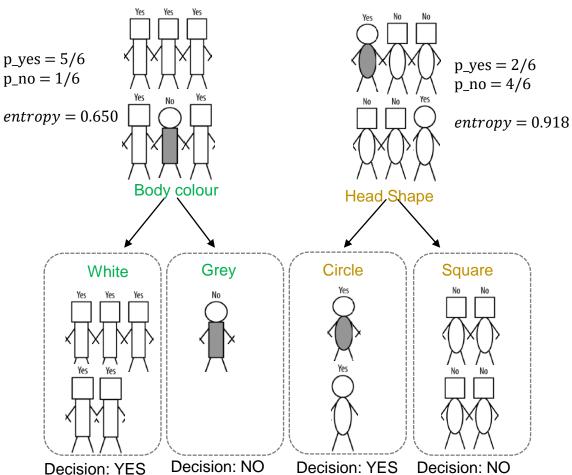
$$p_yes = 2/6$$
  
 $p_no = 4/6$ 

$$entropy = 0.918$$

### Body Shape(rectangle)

### Body Shape(oval)



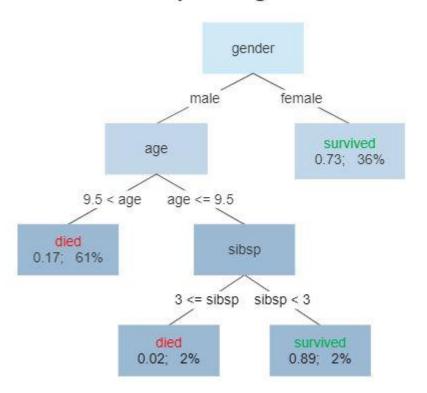


 $IG = entropy(base) - p(c_1) \times entropy(c_1) + p(c_2) \times entropy(c_2) + ...$   $IG = 0.650 - (0.17 \times 0 + 0.83 \times 0) = 0.650$   $IG = 0.919 - (0.33 \times 0 + 0.67 \times 0) = 0.918$ 

### **Decision trees**



### Survival of passengers on the Titanic



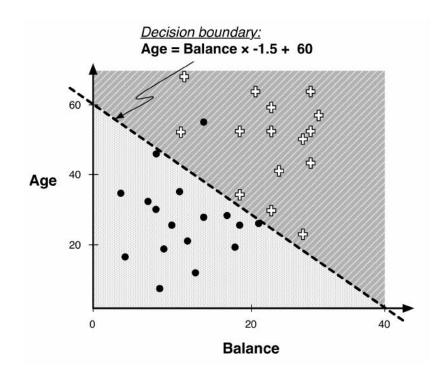
- Widely used for regression and classification problems
- Root at top, leaves at bottom

- Titanic survival model predicts survival for:
  - females
  - males younger than 9.5 years with less than 2.5 siblings
- The figures under the leaves show the probability of survival and the percentage of observations in the leaf.

# Fitting models

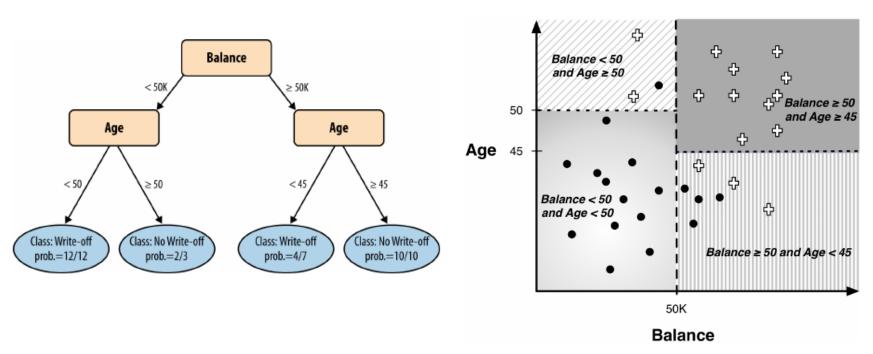


- Decision boundaries
- How do we know how best to draw the boundary?



# Decision trees: hyperplanes



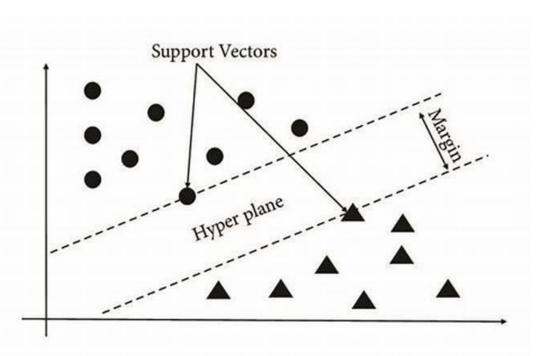


A decision tree can be plotted with each decision segmenting a space into boxes.

The decision boundary is called a hyperplane.

## **Support Vector Machines**



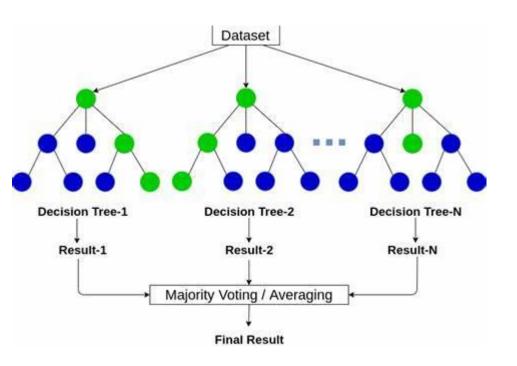


For SVM, part of the objective function (the goal) uses not only the accuracy of the prediction, but also maximises the width of the margin between categories.

Used for both regression and classification.

### Random Forests





- Widely used for regression and classification problems
- Consists of a 'forest' of decision trees, all fit on random bootstrap samples of the data.
- The results are averaged for regression
- Majority vote for classification



# Next Week: Reading Week – For week 7:

- Read Data Science for Business, chapters 5, 7, 8
- Read <u>AUC-ROC</u>: a really good article
- Watch StatQuest: <u>ROC and AUC, Clearly Explained! YouTube</u>
- Watch StatQuest: <u>Bias and Variance</u>
- Watch StatQuest: <u>Cross validation</u>
- Watch StatQuest: <u>Sensitivity and Specificity</u>





Any questions?

