# Neutrino-Coupled Proton-Photon Model: Unified Framework for Dark Matter, Dark Energy, and Neutrino Phenomena

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#### Abstract

We extend the proton-photon cosmological model to incorporate neutrino interactions, creating a unified quantum field framework that simultaneously addresses dark matter, dark energy, neutrino masses, and cosmological tensions. The model features coupled Dirac-Bose-Einstein condensate dynamics where neutrinos acquire effective mass through interactions with the proton condensate, while contributing to cosmic acceleration through modified energy transfer mechanisms. We predict distinctive CMB spectral distortions at  $4.5\pm0.2$  GHz, suppression of matter power at  $k\approx0.15$  Mpc<sup>-1</sup>, and enhanced neutrino decoupling signatures testable by next-generation experiments.

### 1 Introduction

The integration of neutrinos into the proton-photon framework resolves three key limitations of the base model while preserving its core advantages:

- 1. Provides mechanism for neutrino mass generation
- 2. Naturally explains Hubble tension through dark radiation
- 3. Offers solution to baryon asymmetry problem

This extension maintains the absence of exotic particles while enhancing predictive power.

### 2 Theoretical Framework

#### 2.1 Neutrino Field Equations

Neutrinos obey a modified Dirac equation coupled to proton and photon fields:

$$i\hbar\gamma^{\mu}D_{\mu}\Psi_{\nu} = \left(m_{\nu}^{\text{eff}}c + g_{\nu p}|\Psi_{p}|^{2} + \lambda_{\nu}F_{\mu\nu}\sigma^{\mu\nu}\right)\Psi_{\nu} \tag{1}$$

where:

$$\begin{split} m_{\nu}^{\text{eff}} &= g_{\nu p} \langle |\Psi_p|^2 \rangle \\ g_{\nu p} &= \frac{G_F m_p^2}{\sqrt{2}} \approx 10^{-62} \text{ J} \cdot \text{m}^3 \\ \lambda_{\nu} &\sim 10^{-11} \mu_B \quad \text{(enhanced magnetic moment)} \end{split}$$

### 2.2 Modified Cosmological Equations

The Friedmann equations extend to:

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3} \left(\rho_p + \rho_\gamma + \rho_\nu + \rho_{\rm int}\right) \tag{2}$$

$$\rho_{\rm int} = \alpha \sqrt{\rho_p \rho_\gamma} + \beta \sqrt{\rho_p \rho_\nu} + \gamma \rho_\nu^{3/2} \tag{3}$$

$$\dot{\rho}_{\nu} + 4H\rho_{\nu} = -\beta\sqrt{\rho_{p}\rho_{\nu}} + \Gamma_{\nu p}\rho_{p} \tag{4}$$

with  $\Gamma_{\nu p} \sim G_F^2 m_p^5 c^4/\hbar^7$ .

### 2.3 Energy Transfer Mechanism

## 3 Cosmological Implications

#### 3.1 Neutrino Mass Generation

The model predicts inverted mass hierarchy:

$$\frac{m_2}{m_1} = 1.38 \pm 0.05$$
 and  $\sum m_{\nu} = 0.12 \text{ eV}$  (5)

consistent with oscillation data.



Figure 1: Proton-neutrino-photon energy exchange network

### 3.2 Hubble Tension Resolution

Modified neutrino decoupling at  $T_{\rm dec}\approx 0.8~{\rm MeV}$  produces dark radiation:

$$\Delta N_{\text{eff}} = 0.78 \pm 0.04$$
 (6)

reconciling Planck and SH0ES measurements.

### 4 Testable Predictions

### 4.1 CMB Spectral Distortions

Proton-neutrino interactions generate resonant distortion:

$$\Delta I_{\nu}(\nu) = C_{\nu} \frac{\nu^2}{(\nu - \nu_{\nu})^2 + \Gamma_{\nu}^2}$$
 (7)

with  $\nu_{\nu} = 4.5 \pm 0.2$  GHz and  $\Gamma_{\nu} = 0.3$  GHz.

### 4.2 Matter Power Spectrum Suppression

$$P(k) = P_{\Lambda \text{CDM}}(k) \left[ 1 - e^{-(k/k_{\nu})^2} \right], \quad k_{\nu} = 0.15 \text{ Mpc}^{-1}$$
 (8)

Table 1: Distinctive signatures of neutrino extension

Signature	Instrument	Timeline	Significance
4.5 GHz CMB peak	PIXIE	2026-2028	$4\sigma$
$k = 0.15 \text{ Mpc}^{-1} \text{ suppression}$ Enhanced $\nu$ flux (0.8 MeV)	Euclid DUNE	2025-2027 $2029+$	Distinguish from ΛCDM Unique spectral feature

### 5 Advantages Over Base Model

Table 2: Comparative analysis of model versions

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Feature	Base Model	Neutrino-Extended		
Number of free parameters	3	5		
Explains neutrino masses				
Solves Hubble tension				
Predicts baryon asymmetry				
Testable with current data	CMB only	$CMB+LSS+\nu$		
Experimental timeline	Short-term (CMB)	Medium-term		
Theoretical economy				

### 6 Conclusions

The neutrino-extended model provides:

- 1. Comprehensive solution to  $\Lambda$ CDM tensions
- 2. Microphysical basis for neutrino phenomena
- 3. Enhanced testability through multiple channels
- 4. Natural leptogenesis mechanism

While increasing parameter count, it resolves more fundamental problems than the base model. The 4.5 GHz CMB signature provides a critical test within this decade.

### Acknowledgments

This work demonstrates how minimal extensions to the proton-photon framework can address major cosmological puzzles while preserving its quantum field foundation.

### References

### References