

# Unit 8 – TF-IDF

CS 201 - Data Structures II

Spring 2022

Habib University

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# Bag of words

1. The sun is shining
2. The weather is sweet
3. The sun is shining and the weather is sweet

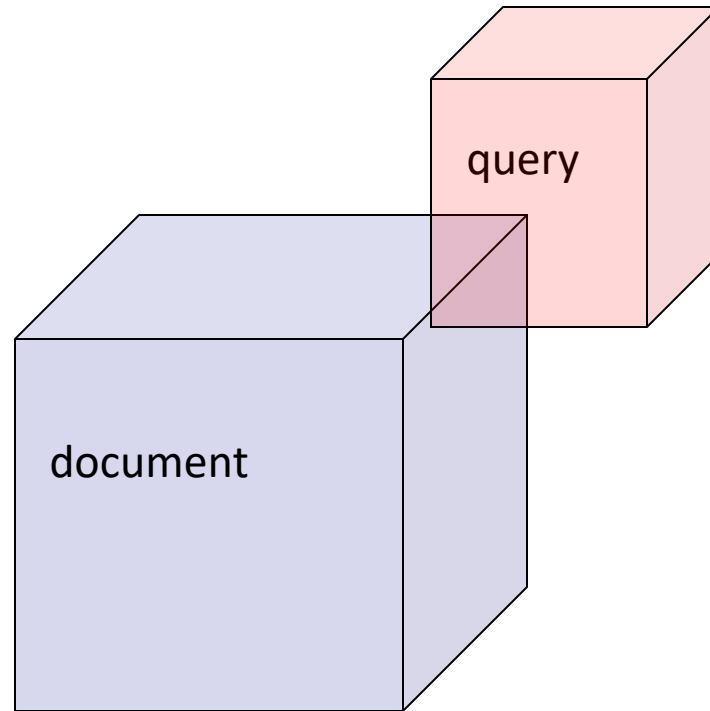
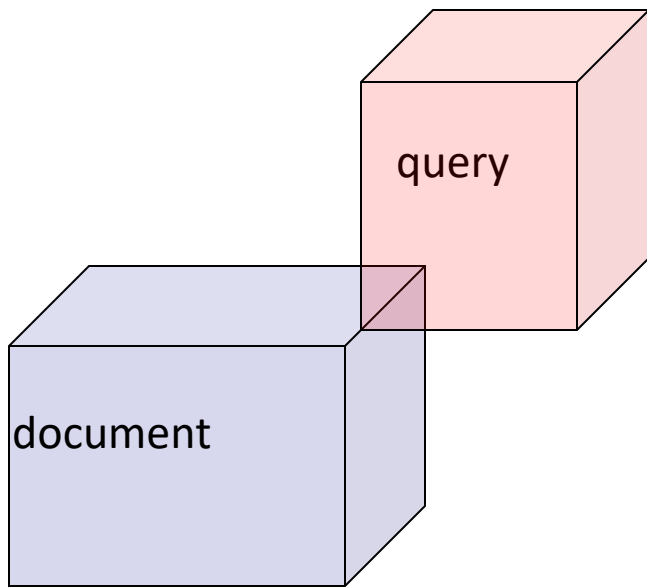
{'the': 5, 'shining': 2, 'weather': 6, 'sun': 3, 'is': 1, 'sweet': 4, 'and': 0}

[ [0 1 1 1 0 1 0]

[0 1 0 0 1 1 1]

[1 2 1 1 1 2 1] ]

# Some things to be careful of...



What is the issue?

Need some notion of the length of a document

# Term Frequency

- In document  $d$ , the frequency represents the number of instances of a given word  $t$ .

$$tf_{i,j} = \frac{n_{i,j}}{\sum_k n_{k,j}}$$

# Pitfall with term frequency

← Tweet



The most popular word in each state

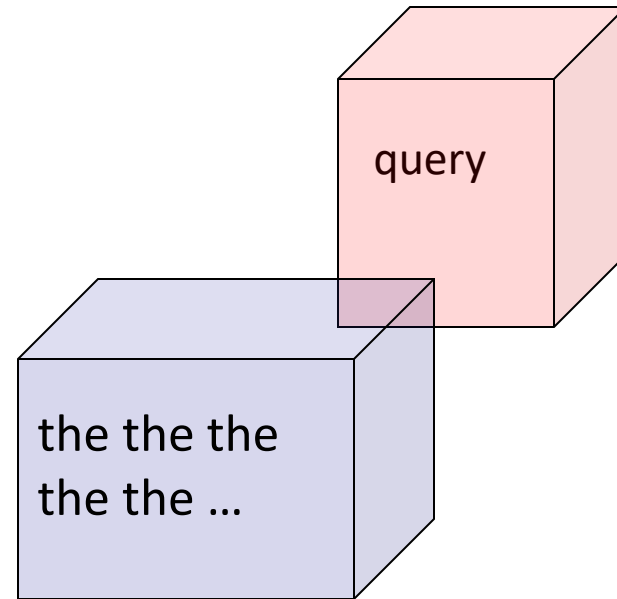
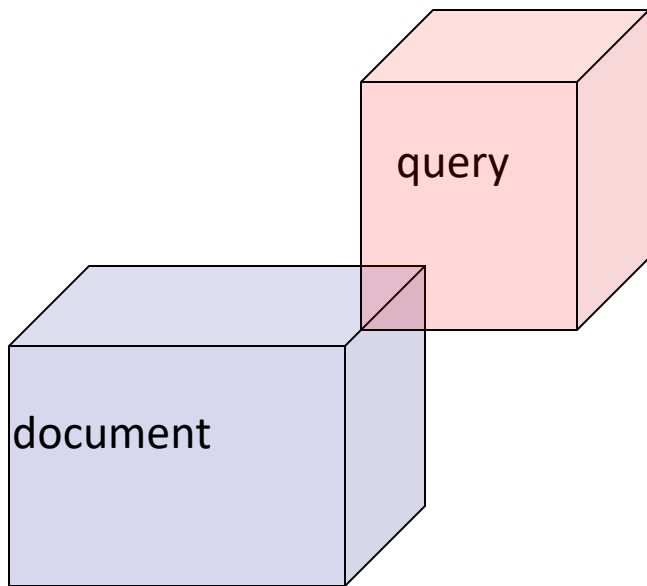


Most frequent word on twitter in each state in the United States .

[Terrible Maps on Twitter: "The most popular word in each state](https://t.co/LY7LewNohn)

[https://t.co/LY7LewNohn" / Twitter](https://t.co/LY7LewNohn)

# Some things to be careful of...



Need some notion of the importance of words

# Term importance

- Rare terms are more informative than frequent terms
  - Recall stop words
- Consider a term in the query that is rare in the collection
- How to quantify rareness of a term?

# Document frequency

- Terms that occur in many documents are weighted less, since overlapping with these terms is very likely
  - In the extreme case, take a word like **the** that occurs in EVERY document
- Terms that occur in only a few documents are weighted more



# Inverse Document Frequency (IDF)

- Inverse Document Frequency (IDF)

$$idf_i = \log \frac{|D|}{|d : t_i \in d|}$$

- Calculates how common a word is across documents. Most common terms are less significant.

# TF-IDF

- **TF-IDF (term frequency-inverse document frequency)** is a statistical measure that evaluates how relevant a word is to a document in a collection of documents.

$$\text{tf-idf}_{i,j} = \text{tf}_{i,j} \times \text{idf}_i$$

# Bag of Words

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{'the': 5, 'shining': 2, 'weather': 6, 'sun': 3, 'is': 1, 'sweet': 4, 'and': 0}

```
[ [0 1 1 1 0 1 0]
  [0 1 0 0 1 1 1]
  [1 2 1 1 1 2 1] ]
```

# TF-IDF

1. The sun is shining
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{'the': 5, 'shining': 2, 'weather': 6, 'sun': 3, 'is': 1, 'sweet': 4, 'and': 0}
```

```
[ [ 0.      0.43  0.56  0.56  0.      0.43  0.    ]  
  [ 0.      0.43  0.      0.      0.56  0.43  0.56]  
  [ 0.4     0.48  0.31  0.31  0.31  0.48  0.31] ]
```

# Interpreting TF-IDF

In other words,  $\text{tf-idf}_{t,d}$  assigns to  $t$  a weight in document  $d$  that is:

- highest when  $t$  occurs many times within a small number of documents (thus lending high discriminating power to those documents);
- lower when the term occurs fewer times in a document, or occurs in many documents (thus offering a less pronounced relevance signal);
- lowest when the term occurs in virtually all documents.

# Exercise

	Doc1	Doc2	Doc3
car	27	4	24
auto	3	33	0
insurance	0	33	29
best	14	0	17

- Compute TF-IDF score of each term in this corpus.

# Cosine Similarity

$$\cos(\mathbf{a}, \mathbf{b}) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|} = \frac{\sum_{i=1}^n \mathbf{a}_i \mathbf{b}_i}{\sqrt{\sum_{i=1}^n (\mathbf{a}_i)^2} \sqrt{\sum_{i=1}^n (\mathbf{b}_i)^2}}$$

# Example

An example is measuring the similarity between documents based on word counts:

Document	Advertising	Auto	Car	Detroit	Engine	Germany	Sales
<i>a</i>	5	88	123	43	35	0	36
<i>b</i>	71	125	42	76	0	27	88

$$a \cdot b = (5 \times 71) + (88 \times 125) + \cdots + (36 \times 88) = 22957$$

$$\|a\| = \sqrt{5^2 + 88^2 + 123^2 + 43^2 + 35^2 + 0^2 + 36^2} = 165.13$$

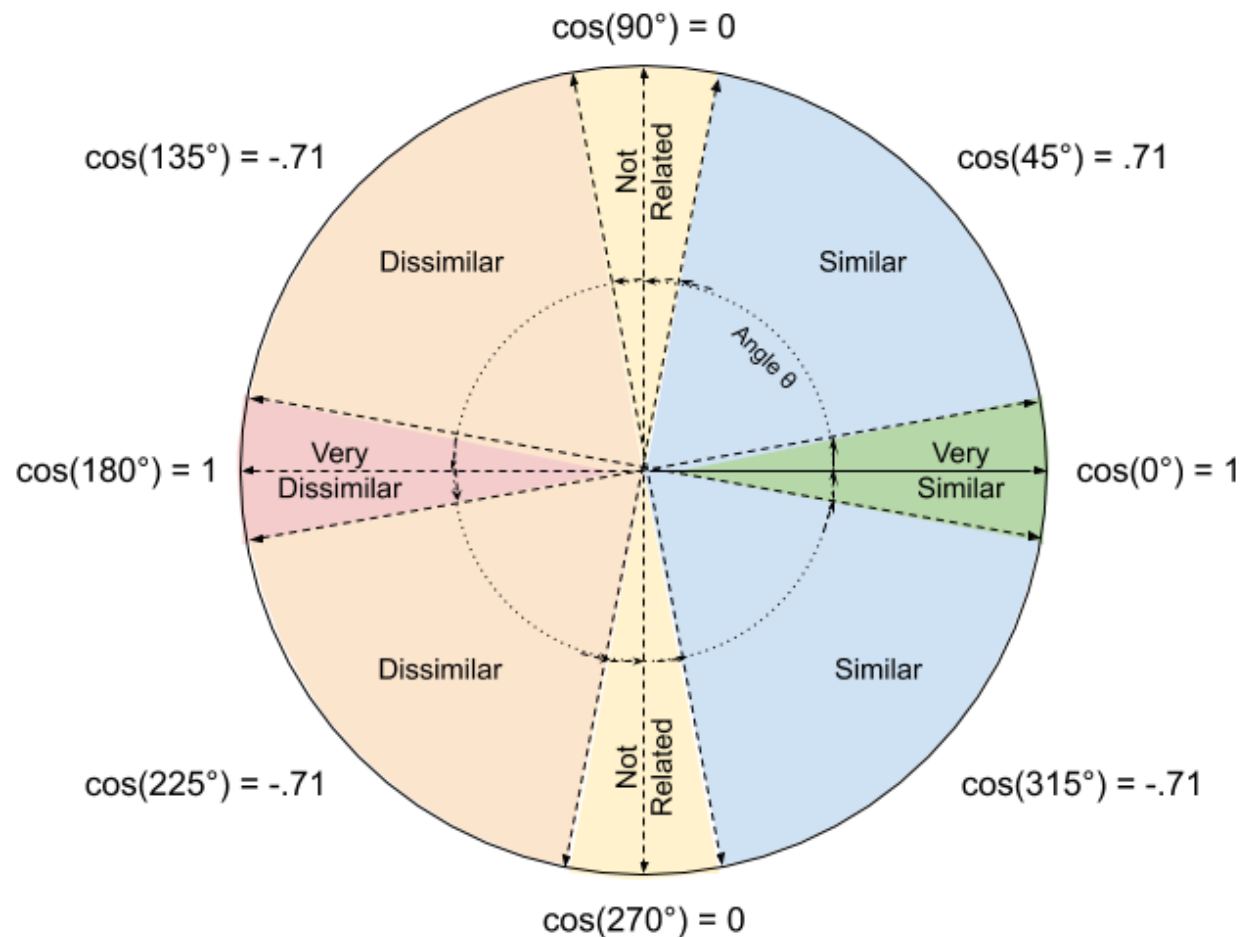
$$\|b\| = \sqrt{71^2 + 125^2 + 42^2 + 76^2 + 0^2 + 27^2 + 88^2} = 191.52$$

$$\|a\| \|b\| = 165.13 \times 191.52 = 31626$$

$$\text{cosine similarity} = \cos \theta = \frac{a \cdot b}{\|a\| \|b\|} = \frac{22957}{31626} = .73$$



# Interpreting Results



# The Three Documents and Similarity Metrics



Considering only the 3 words from the above documents: 'sachin', 'dhoni', 'cricket'

## Doc Sachin: Wiki page on Sachin Tendulkar

Dhoni - 10  
Cricket - 50  
Sachin - 200

## Doc Dhoni: Wiki page on Dhoni

Dhoni - 400  
Cricket - 100  
Sachin - 20

## Doc Dhoni\_Small: Subsection of wiki on Dhoni

Dhoni - 10  
Cricket - 5  
Sachin - 1

## Document - Term Matrix (Word Counts)

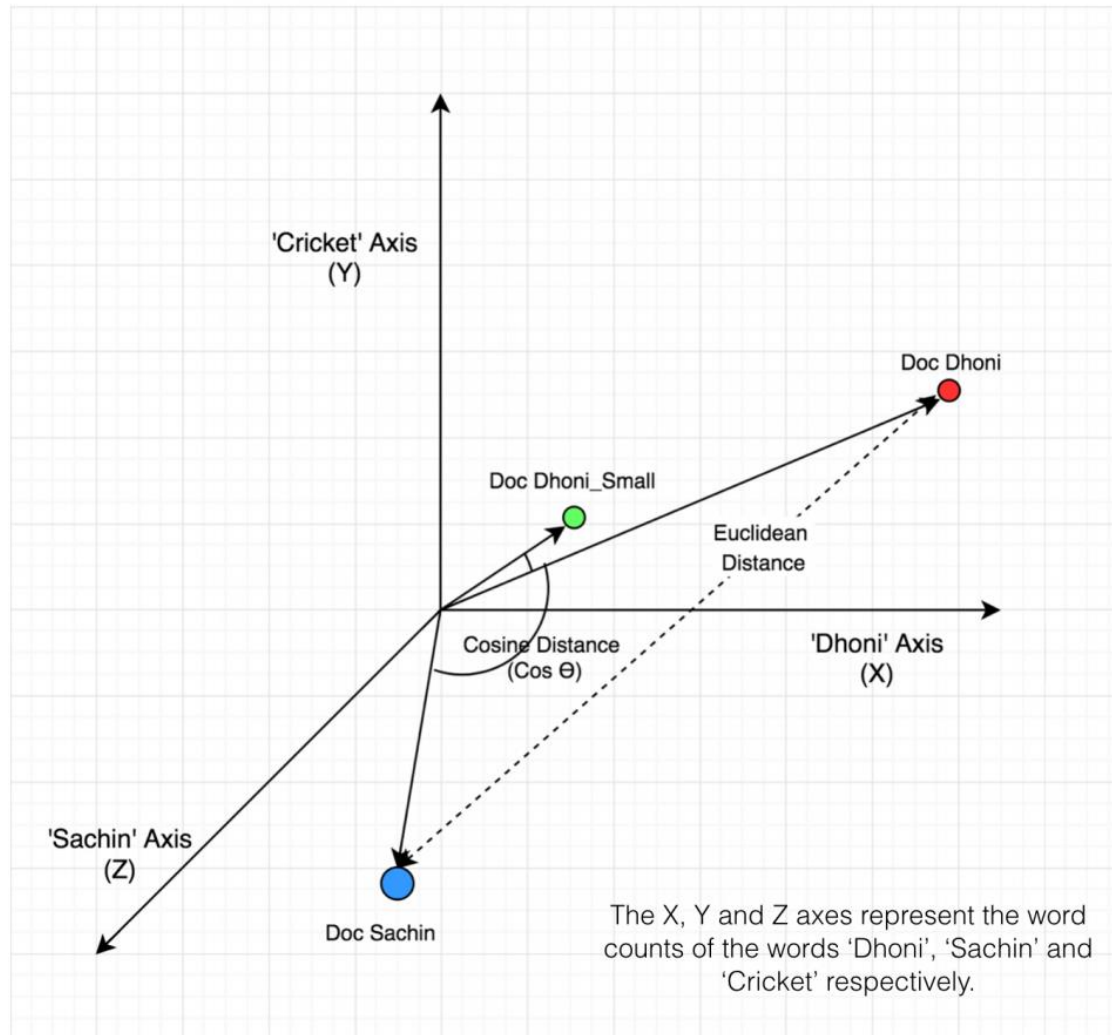
Word Counts	"Dhoni"	"Cricket"	"Sachin"
<i>Doc Sachin</i>	10	50	200
<i>Doc Dhoni</i>	400	100	20
<i>Doc Dhoni_Small</i>	10	5	1



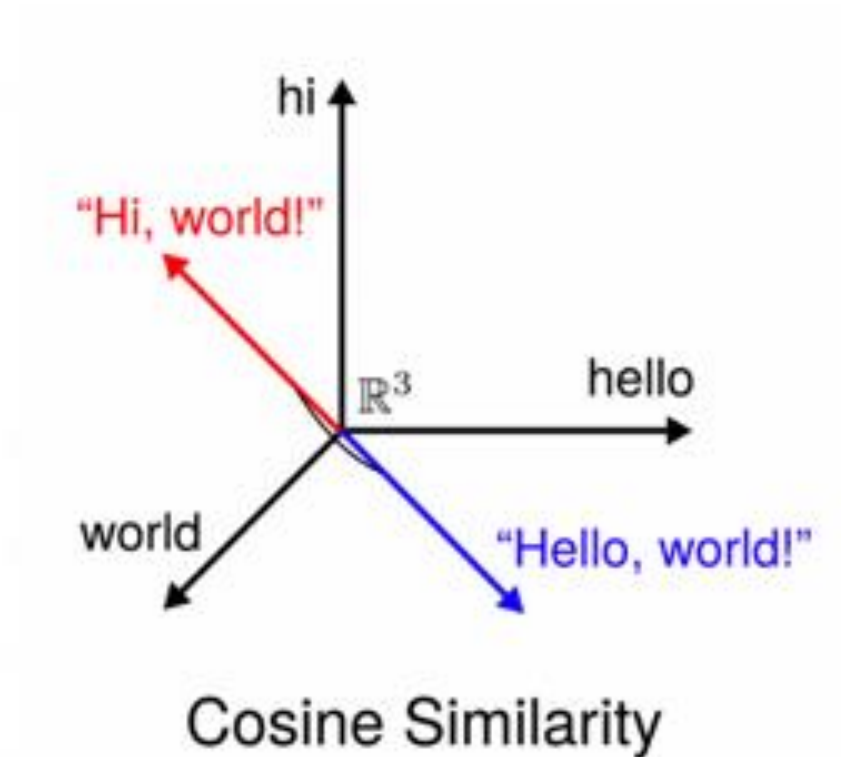
## Similarity Metrics

Similarity or Distance Metrics	Total Common Words	Euclidean distance	Cosine Similarity
<i>Doc Sachin</i> & <i>Doc Dhoni</i>	$10 + 50 + 10 = 70$	432.4	0.15
<i>Doc Dhoni</i> & <i>Doc Dhoni_Small</i>	$20 + 10 + 7 = 37$	204.0	0.23
<i>Doc Sachin</i> & <i>Doc Dhoni_Small</i>	$10 + 10 + 7 = 27$	401.85	0.77

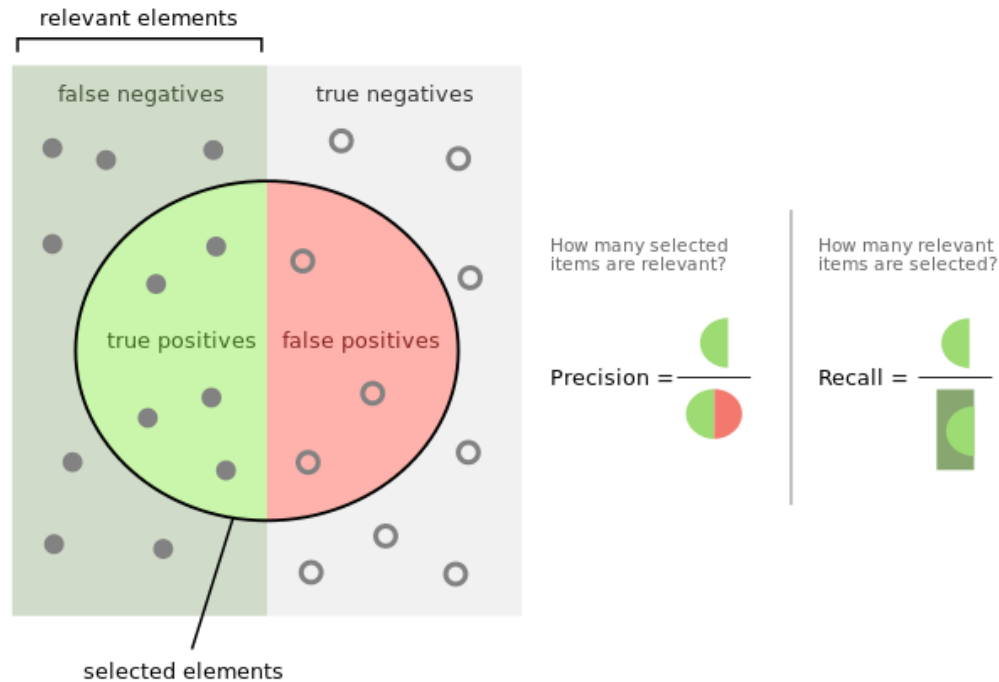
# Projection of Documents in 3D Space



# Projection of documents in 3D space



# Precision vs Recall



[https://en.wikipedia.org/wiki/Precision\\_and\\_recall](https://en.wikipedia.org/wiki/Precision_and_recall)

Thanks