

Statistics & Inferencing Homework #03

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Chapter 8 → Ken Black

Q8.3) $n=81$ $\bar{x}=47$ $\sigma=5.89$ $CI=90\%$

$\alpha=0.1$ $\alpha/2=0.05$ $z_{\alpha/2}=1.645$

$$\bar{x} - z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$47 - 1.645 \left[\frac{5.89}{\sqrt{81}} \right] \leq \mu \leq 47 + 1.645 \left[\frac{5.89}{\sqrt{81}} \right]$$

$$45.923 \leq \mu \leq 48.077$$

P8.9) $n=36$ $\sigma=1.17$ $CI=98\%$ $\alpha=0.02$ $\alpha/2=0.01$

$z_{\alpha/2}=2.3263$ $\bar{x} = \sum x_i / n = 3.3056$

$$3.3056 - 2.3263 (1.17/\sqrt{36}) \leq \mu \leq 3.3056 + 2.3263 (1.17/\sqrt{36})$$

$$2.852 \leq \mu \leq 3.759$$

P8.13) $CI=95\%$ $n=13$ $\bar{x}=45.615$ $\sum x=593$

$\sum x^2=27439$ $s^2=5.47$

$\alpha=0.05$ $\alpha/2=0.025$

$t(\alpha/2, n-1)=2.1788$

$$45.615 - 2.1788 \left[\frac{5.47}{\sqrt{13}} \right] \leq \mu \leq 45.615 + 2.1788 \left[\frac{5.47}{\sqrt{13}} \right]$$

$$42.31 \leq \mu \leq 49.0$$

P8.17) $CI=99\%$ $n=25$ $\sum x=4022$ $\sum x^2=6486.6$

$\bar{x}=16.088$ $\sigma^2=0.800$ Point Estimate = 16.088

$\alpha=0.01$ $\alpha/2=0.005$

$t(\alpha/2, n-1)=2.7969$

$$16.088 - 2.7969 (0.8/\sqrt{25}) \leq \mu \leq 16.088 + 2.7969 (0.8/\sqrt{25})$$

$$15.6 \leq \mu \leq 16.54$$

P8.25) (a) $n=44$ $\hat{p}=0.51$ $CI=90\%$ $\alpha=0.1$ $z_{\alpha/2}=1.645$

$$0.51 - 1.645 \sqrt{(0.51)(0.49)/44} \leq p \leq 0.51 + 1.645 \sqrt{(0.51)(0.49)/44}$$

$$0.386 \leq p \leq 0.634$$

(b) $n=300$ $\hat{p}=0.82$ $CI=95\%$ $\alpha=0.05$ $z_{\alpha/2}=1.96$

$$\hat{p} - z_{\alpha/2} \sqrt{\hat{p}\hat{q}/n} \leq p \leq \hat{p} + z_{\alpha/2} \sqrt{\hat{p}\hat{q}/n}$$

$$0.777 \leq p \leq 0.863$$

(c) $n=1150$ $\hat{p}=0.48$ $CI=90\%$ $0.456 \leq p \leq 0.504$

(d) $n=95$ $\hat{p}=0.32$ $CI=88\%$ $0.246 \leq p \leq 0.394$

P8.27) $n=284$ 40 items contain characteristic of interest

① CI 290%

② CI 295%

③ CI 299%

$$\alpha/2 = 0.1 \quad z_{\alpha/2} = 1.645$$

$$z_{\alpha/2} = 1.96$$

$$z_{\alpha/2} = 2.5758$$

$$\hat{p} = 40/284 = 0.141$$

$$\hat{q} = 1 - \hat{p} = 0.859$$

~~ref~~

$$\hat{p} \pm z_{\alpha/2} \sqrt{\hat{p}\hat{q}/n}$$

① CI 290%

$$0.386 \leq p \leq 0.566$$

② CI 295%

$$0.369 \leq p \leq 0.583$$

③ CI 299%

$$0.336 \leq p \leq 0.616$$

As the level of confidence increases, the ~~margin of error~~ confidence interval increases as the value of p deviates more from the true value - margin of error increases.

P8.35) (a) $n=12$ $\bar{x}=28.4$ $s^2=44.9$ CI 299%

$$(n-1)s^2 / \chi^2_{\alpha/2} \leq \sigma^2 \leq (n-1)s^2 / \chi^2_{1-\alpha/2} \rightarrow \alpha/2 = 0.01 \quad \alpha/2 = 0.005$$

$$\chi^2_{\alpha/2, 11} = 26.7568 \quad \chi^2_{1-\alpha/2, 11} = 2.6032$$

$$11 \times 44.9 / 26.7568 \leq \sigma^2 \leq 11 \times 44.9 / 2.6032$$

$$18.46 \leq \sigma^2 \leq 189.73$$

(b) $n=7$, $\bar{x}=4.37$ $s^2=1.24$ CI 295% ~~$\alpha/2 = 0.05$~~ ~~$\alpha/2 = 0.025$~~

$$s^2 = 1.5376 \quad \chi^2_{\alpha/2, 6} = 14.4494 \quad \chi^2_{1-\alpha/2, 6} = 1.2376 \quad \alpha/2 = 0.025$$

$$0.064 \leq \sigma^2 \leq 7.46$$

(c) $n=20$, $\bar{x}=105$, $s^2=32$, 90% CI $\alpha/2 = 0.05$ $s^2 = 1024$

$$645.45 \leq \sigma^2 \leq 1923.10$$

(d) $n=17$, $s^2=18.56$, 80% CI $12.61 \leq \sigma^2 \leq 31.89$

P8.37) $n=20$ $sd=4.3$ 98% CI $\alpha/2 = 0.01$

$$\chi^2_{\alpha/2, 19} = 36.1909$$

$$\chi^2_{1-\alpha/2, 19} = 7.6327$$

$$s^2 = (4.3)^2$$

$$(19)(4.3)^2 / 36.1909 \leq \sigma^2 \leq (19)(4.3)^2 / 7.6327$$

$$9.707 \leq \sigma^2 \leq 46.03$$

Point Estimate $s^2 = 4.3^2 = 18.49$