

[Midterm Exam] Name:

ID:

Fall 2022: CS 212: Nature of Computation (L3)

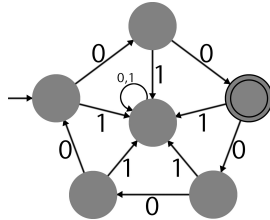
Due: 9:55 am, Wednesday, October 5, 2022. Total Marks: 25

Question 1

[5 points]

Write **T** if the statement is true and **F** otherwise.

1. Every Subset of a Regular language is Regular. \_\_\_\_\_
2. Let  $P$  and  $Q$  be regular expressions, then  $(P + Q)^* = P^* + Q^*$ . \_\_\_\_\_
3. The NFA accepts the language  $00(00000)^*$ . \_\_\_\_\_



4. Every nonempty language contains a nonempty Regular language. \_\_\_\_\_
5. The set of all first names given to children born in 2021 is Regular. \_\_\_\_\_

Question 2

[10 points]

For each language below, either prove that it is Regular or Context-Free. Assume the binary alphabet for each.

- (a) (5 points) The set of all strings that do not contain 1101.
- (b) (5 points) The set of all strings that are palindromes. A palindrome is a string that reads the same backwards as forwards, i.e.  $s$  is a palindrome if  $s = u_1u_2...u_n = u_n...u_2u_1$ .

Question 3

[10 points]

- (a) (5 points) Prove that  $\{0^n1^m \mid n < m\}$  is not regular.
- (b) (5 points) Prove that its complement (w.r.t.  $\{0,1\}^*$ ) is not regular either.