## Quiz 14A: The class P

## CS 212 Nature of Computation

## Habib University — Fall 2023

Total Marks: 10	Date: November 22, 2023
Duration: 15 minutes	Time: 830–845h
Student ID:	
Student Name:	У
1. (10 points) Show that the class P is closed under union.	
<b>Solution:</b> We prove the closure by constructing a polynomial time d languages in $P$ .	ecider for the union of two
<i>Proof.</i> Consider the languages $L_1, L_2 \in P$ and let $R$ and $S$ be their pol- Construct $T$ to decide $L_1 \cup L_2$ as follows. On input $w$ :	ynomial time deciders.
<ol> <li>Simulate R on w.</li> <li>If R accepts, accept.</li> </ol>	
3. If $R$ rejects,  (a) Simulate $S$ on $w$ .	
(b) If $S$ accepts, $accept$ ; if $S$ rejects, $reject$ .	
Step 1 runs in polynomial time, Step 2 in constant time, and Step 3 alt Thus the total time taken is polynomial.	ogether in polynomial time. $\Box$