

# Parallel and Distributed Computing

## CS3006 (BDS-6A)

### Lecture 06

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# Previous Lecture

- Network Topologies:
  - Linear array (with or without wraparound links)
  - K-d meshes
  - Hypercubes
  - Tree-based networks (fat-trees or otherwise, static or dynamic)
- Evaluating static interconnections
  - Cost, diameter, bisection width, arc connectivity

# Evaluating Static Interconnections

Network	Diameter	Bisection Width	Arc Connectivity	Cost (No. of links)
Completely-connected	1	$p^2/4$	$p - 1$	$p(p - 1)/2$
Star	2	1	1	$p - 1$
Complete binary tree	$2 \log((p + 1)/2)$	1	1	$p - 1$
Linear array	$p - 1$	1	1	$p - 1$
2-D mesh, no wraparound	$2(\sqrt{p} - 1)$	$\sqrt{p}$	2	$2(p - \sqrt{p})$
2-D wraparound mesh	$2\lfloor\sqrt{p}/2\rfloor$	$2\sqrt{p}$	4	$2p$
Hypercube	$\log p$	$p/2$	$\log p$	$(p \log p)/2$

# *Parallel Algorithm Design Life Cycle*

# *Principles of Parallel Algorithm Design*

# Principles of Parallel Algorithm Design

## Steps in Parallel Algorithm Design

- 1. Identification:** Identifying portions of the work that can be performed concurrently.
  - Work-units are also known as tasks
  - E.g., Initializing two mega-arrays are two tasks and can be performed in parallel
- 2. Mapping:** The process of mapping concurrent pieces of the work or tasks onto multiple processes running in parallel.
  - Multiple processes can be physically mapped on a single processor.

# Principles of Parallel Algorithm Design

## Steps in Parallel Algorithm Design

3. **Data Partitioning**: Distributing the input, output, and intermediate data associated with the program.
  - One way is to copy whole data at each processing node
    - Memory challenges for huge-size problems
  - Other way is to give fragments of data to each processing node
    - Communication overheads
4. **Defining Access Protocol**: Managing accesses to data shared by multiple processors (i.e., managing communication & synchronization).

# Parallel computing Examples - Chess Player

- A parallel program to play chess might look at all the possible first moves it could make
- Each different first move could be explored by a different processor, to see how the game would continue from that point
- Results have to be combined to figure out which is the best first move
- The famous IBM Deep Blue machine that beat Kasparov
- Brute force computing power, massively parallel with 30 nodes, with each node containing a 120 MHz P2SC microprocessor



# Load Balance

- Inefficient if many processors are idle while one processor has lots of work to do and this slows down the whole application
- Best utilizations of parallel processors
- Require load balancing (parallel processors are typically symmetric)
- For example
  - Web Servers
  - Matrix Multiplication

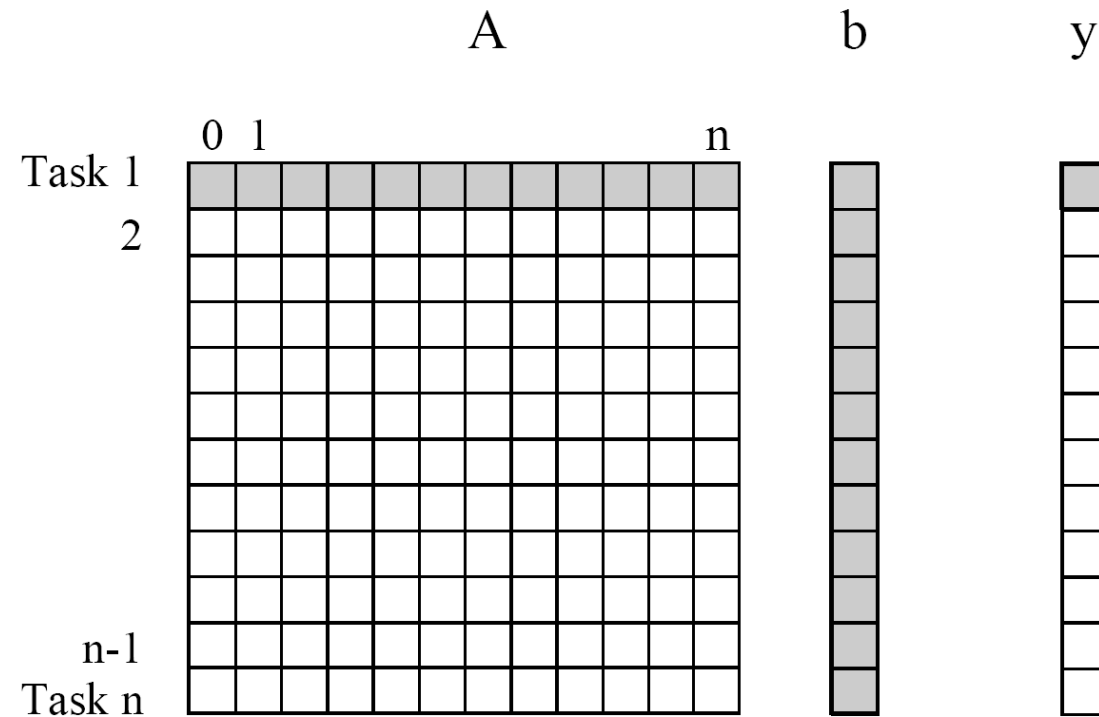
# Principles of Parallel Algorithm Design

- **Decomposition:**

- The process of dividing a computation into smaller parts, some or all of which may potentially be executed in parallel.

- **Tasks**

- **Programmer-defined units of computation** into which the main computation is subdivided by means of decomposition
- Tasks can be of **arbitrary size**, but once defined, they are regarded as **indivisible units of computation**.
- The tasks into which a problem is decomposed ***may not all be*** of the ***same size***
- ***Simultaneous execution of multiple tasks*** is the key to reducing the time required to solve the entire problem.



**Figure 3.1** Decomposition of dense matrix-vector multiplication into  $n$  tasks, where  $n$  is the number of rows in the matrix. The portions of the matrix and the input and output vectors accessed by Task 1 are highlighted.

- *Problem can be decomposed into  $n$  tasks*
- *Computation of each element of vector  $y$  is independent of other elements*
- *No control dependencies so no task-dependency graph*

# Vector Multiplication ( $n \times 1$ )

- So the multiplication program like:

```
for (row = 0; row < n; row++)  
    y[row] = dot_product( get_row(A, row), get_col(b));
```

can be transformed to:

```
for (row = 0; row < n; row++)  
    y[row] = create_thread( dot_product(get_row(A, row), get_col(b)));
```

- In this case, one may think of the thread as an instance of a function that returns before the function has finished executing

# Vector Multiplication (n x n)

```
for (row = 0; row < n; row++)  
    for (column = 0; column < n; column++)  
        c[row][column] = dot_product( get_row(a, row), get_col(b, col));
```

## Multithreaded:

```
for (row = 0; row < n; row++)  
    for (column = 0; column < n; column++)  
        c[row][column] = create_thread( dot_product(get_row(a, row), get_col(b, col)));
```

# Task-Dependency Graph

- The tasks in the previous examples are independent and can be performed in any sequence.
- In most of the problems, some sort of dependency exists between the tasks.
- An abstraction used to express such **dependencies** among tasks and their **relative order of execution** is known as a **task-dependency graph**
- It is a **directed acyclic graph** in which nodes are tasks and the directed edges indicate the dependencies between them
- The task corresponding to a node can be executed when all tasks connected to this node by incoming edges have completed.

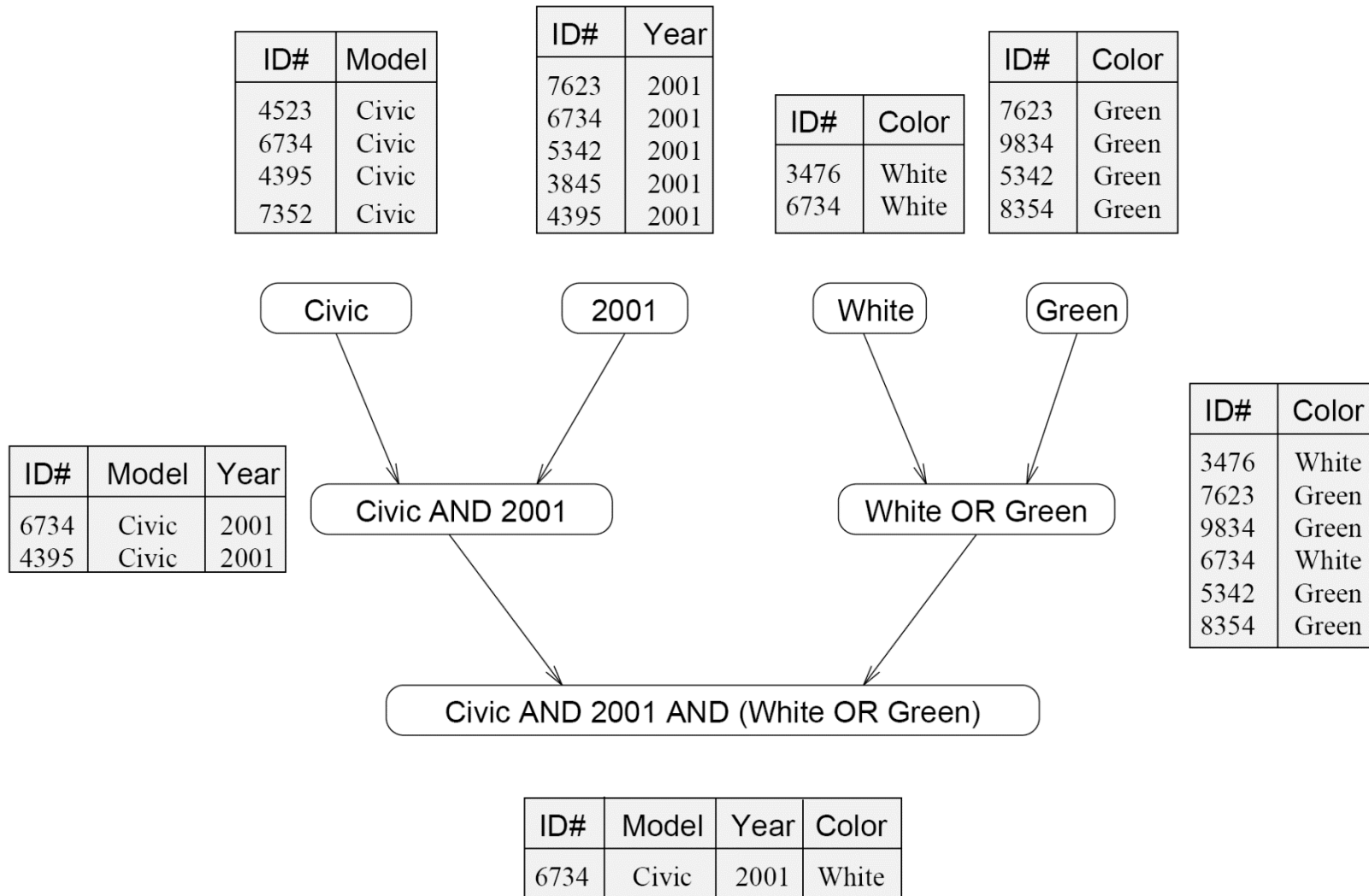
# DB Query

ID#	Model	Year	Color	Dealer	Price
4523	Civic	2002	Blue	MN	\$18,000
3476	Corolla	1999	White	IL	\$15,000
7623	Camry	2001	Green	NY	\$21,000
9834	Prius	2001	Green	CA	\$18,000
6734	Civic	2001	White	OR	\$17,000
5342	Altima	2001	Green	FL	\$19,000
3845	Maxima	2001	Blue	NY	\$22,000
8354	Accord	2000	Green	VT	\$18,000
4395	Civic	2001	Red	CA	\$17,000
7352	Civic	2002	Red	WA	\$18,000

**Table 3.1** A database storing information about used vehicles.

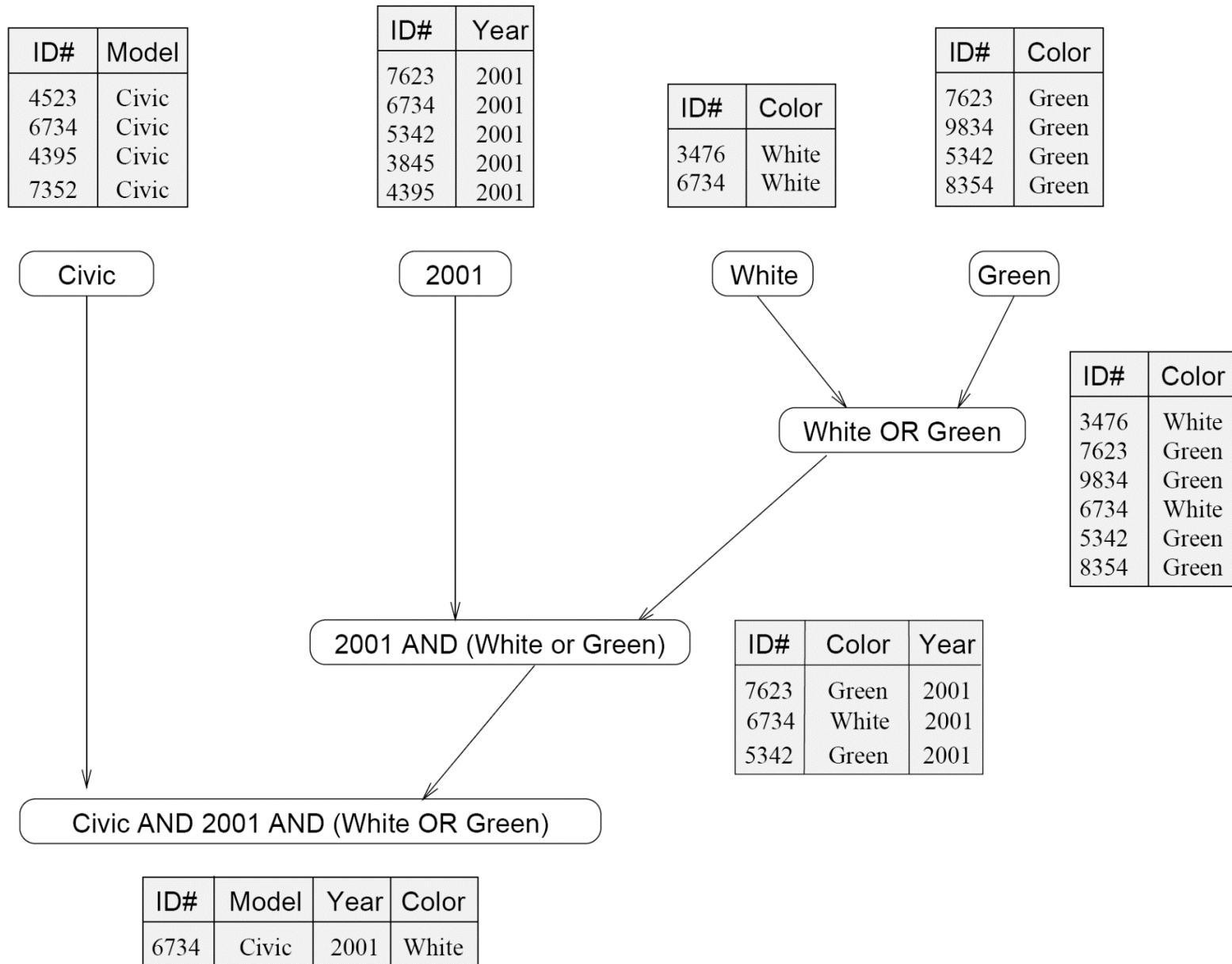
Execution of the query:

MODEL = “CIVIC” AND YEAR = 2001 AND (COLOR = “GREEN” OR COLOR = “WHITE”)



**Figure 3.2** The different tables and their dependencies in a query processing operation.



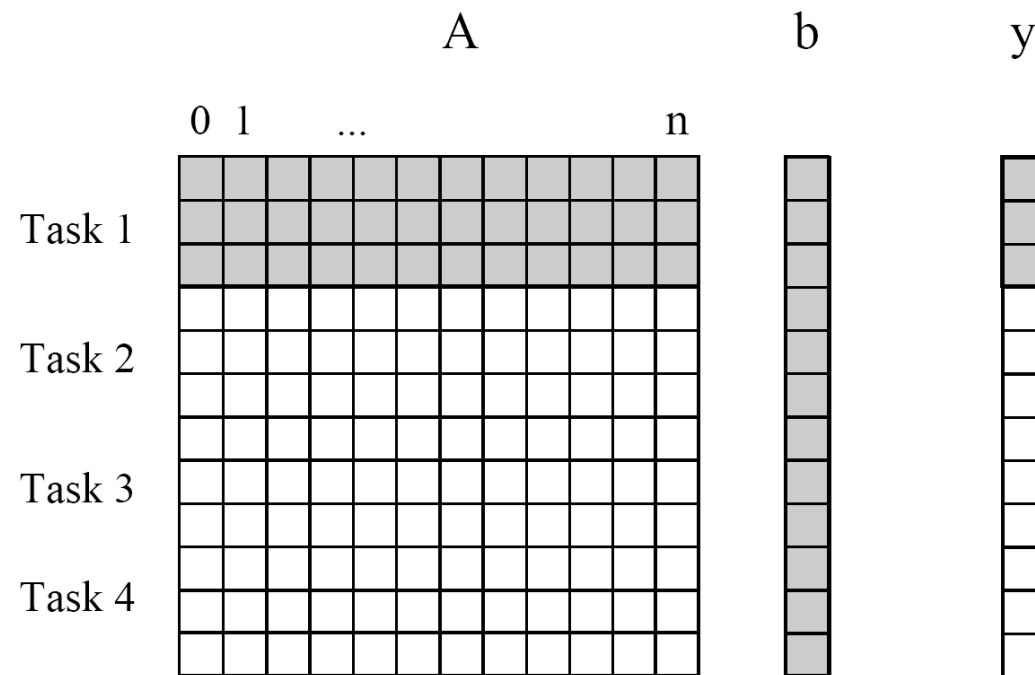


**Figure 3.3** An alternate data-dependency graph for the query processing operation.

# Principles of Parallel Algorithm Design

## Granularity

- The **number** and **sizes** of tasks into which a problem is decomposed determines the ***granularity*** of the decomposition
  - A decomposition into a large number of small tasks is called ***fine-grained***
  - A decomposition into a small number of large tasks is called ***coarse-grained***
- For matrix-vector multiplication Figure 3.1 would usually be considered ***fine-grained***
- Figure 3.4 shows a ***coarse-grained*** decomposition as each task computes  $n/4$  of the entries of the output vector of length  $n$



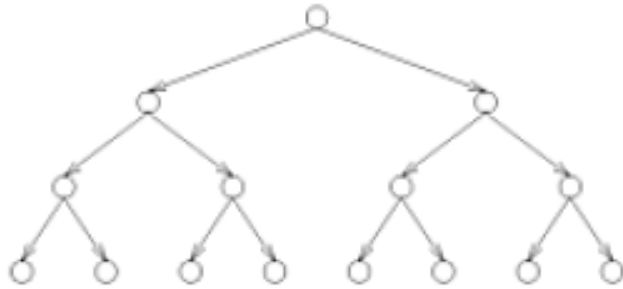
**Figure 3.4** Decomposition of dense matrix-vector multiplication into four tasks. The portions of the matrix and the input and output vectors accessed by Task 1 are highlighted.

# Maximum Degree of Concurrency

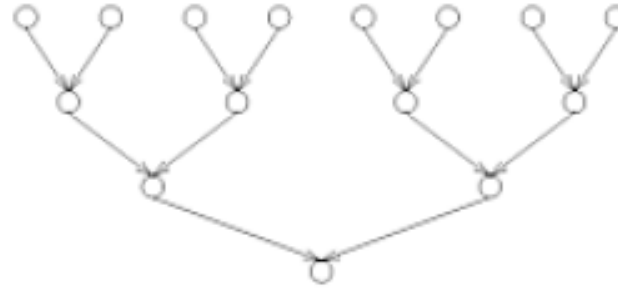
- The *maximum number of tasks* that can be executed *simultaneously* in a parallel program at any given time is known as its *maximum degree of concurrency*
- Usually, it is always less than total number of tasks due to dependencies.
- E.g., max-degree of concurrency in the task-graphs of Figures 3.2 and 3.3 is 4.
- **Rule of thumb:** For task-dependency graphs that are trees, the maximum degree of concurrency *is always equal to the number of leaves in the tree*

# Maximum Degree of Concurrency

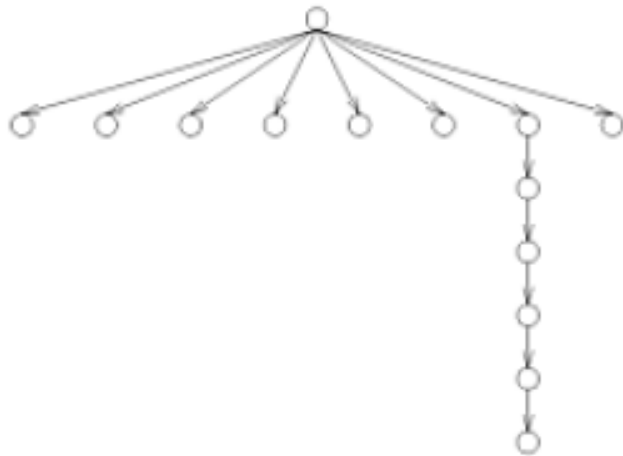
**Determine the Maximum Degree of Concurrency?**



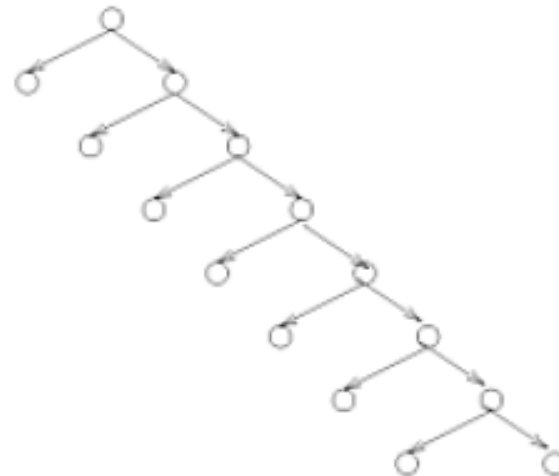
(a)



(b)



(c)



(d)

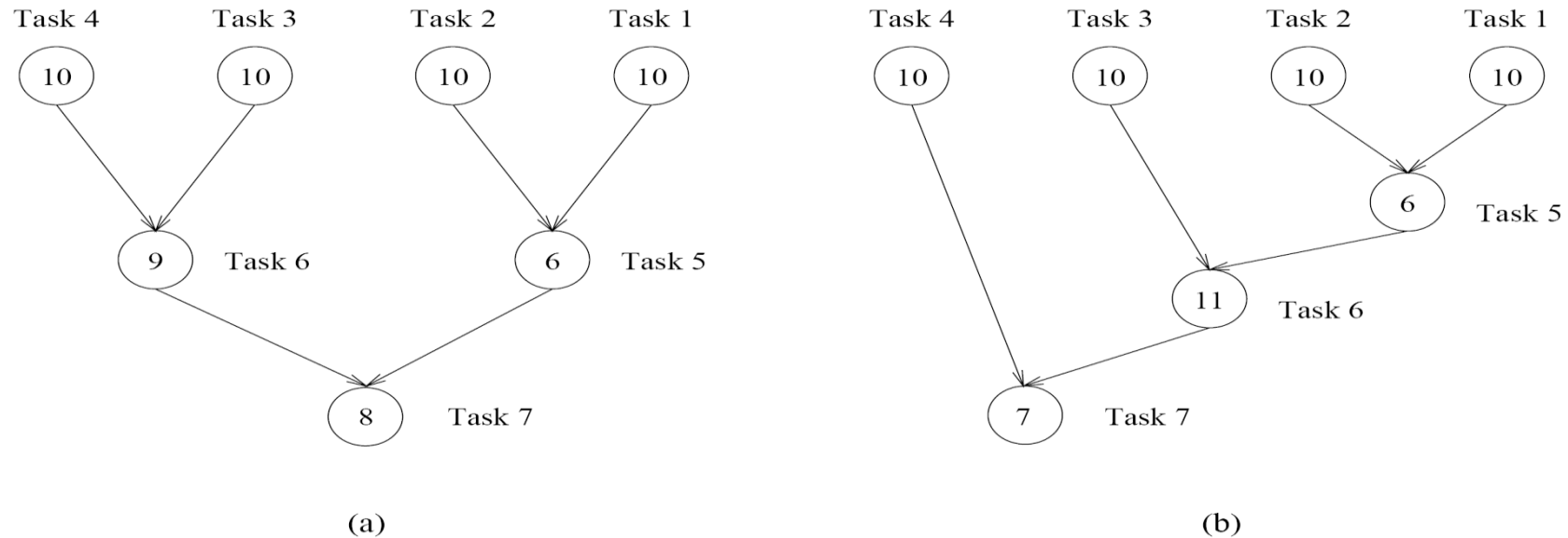
# Average Degree of Concurrency

- A relatively *better measure* for the performance of a parallel program
- The average number of tasks that can run concurrently over the entire duration of execution of the program
- The ratio of the *total amount of work* to the *critical-path length*
  - So, what is the critical path in the graph?

# Critical Path

- ***Critical Path***: The longest directed path between any pair of start and finish nodes is known as the *critical path*.
- ***Critical Path Length***: The *sum of the weights of nodes* along this path
  - the weight of a node is the *size or the amount of work associated* with the corresponding task.
- A shorter critical path favors a *higher average-degree of concurrency*.
- Both, *maximum* and *average degree of concurrency* increases as tasks become smaller (finer)

# Average Degree of Concurrency



**Figure 3.5** Abstractions of the task graphs of Figures 3.2 and 3.3, respectively.

**Critical path lengths:** 27 and 34

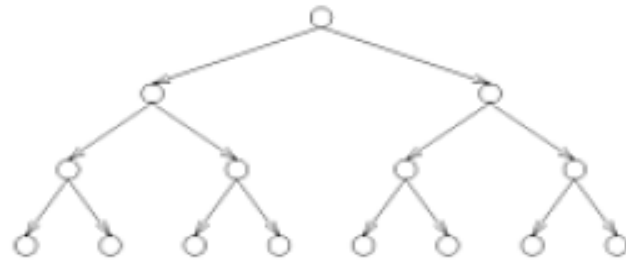
**Total amount of work:** 63 and 64

**Average degree of concurrency:** 2.33 and 1.88

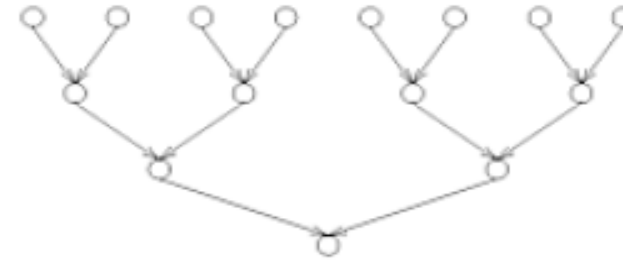


# Principles of Parallel Algorithm Design

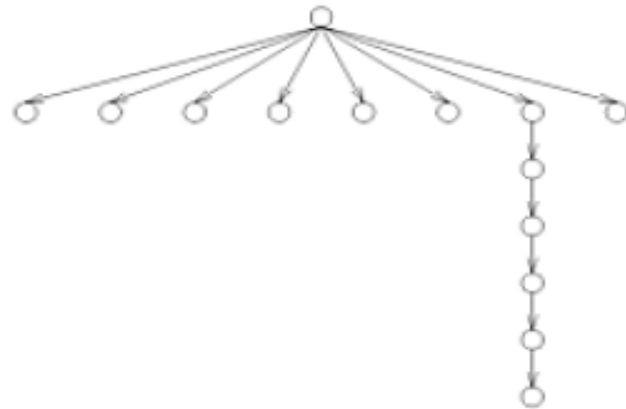
**Determine critical path length and average-concurrency?**



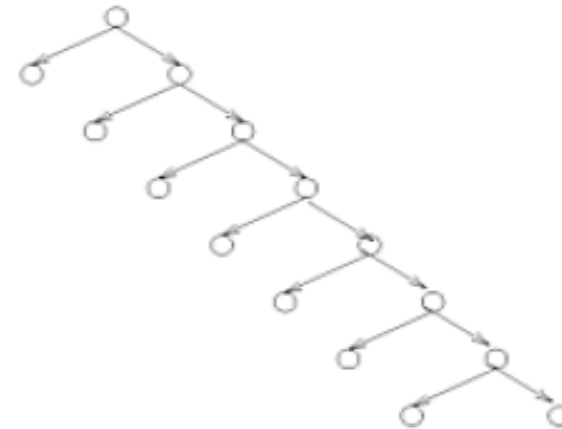
(a)



(b)



(c)



(d)

# Task Interaction Graph

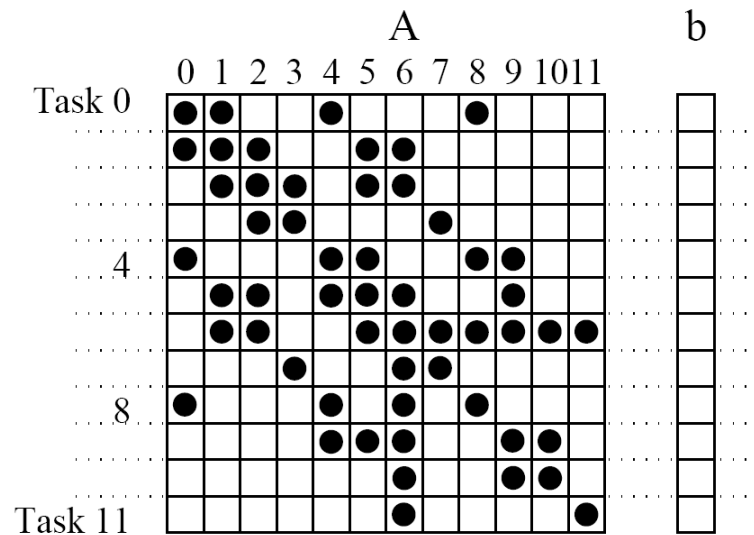
- Depicts pattern of interaction between the tasks
- *Dependency graphs* only show how the *output of the first task* becomes the *input to the next level task*.
- The *task interaction graph* depicts how the tasks interact with each other to access *distributed data*
- The **nodes** in a *task-interaction graph represent tasks*
- The **edges** connect *tasks that interact with each other*

# Task Interaction Graph

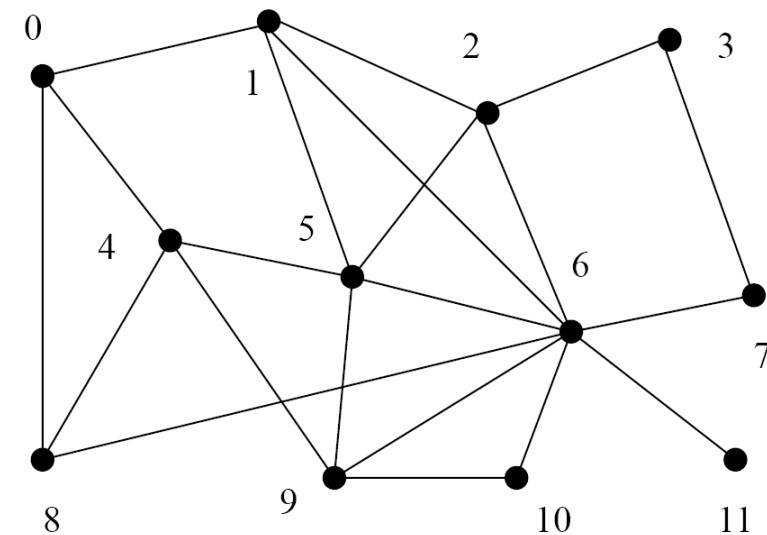
- The **edges** in a task interaction graph are usually *undirected*
  - But directed edges can be used to indicate the direction of flow of data, if it is *unidirectional*.
- The **edge-set** of a task-interaction graph is usually a *superset* of the **edge-set** of the *task-dependency graph*
- In the database query processing example, the *task-interaction graph* is the **same** as the *task-dependency graph*.

# Principles of Parallel Algorithm Design

## Task Interact Graph (Sparse-matrix multiplication)



(a)



(b)

**Figure 3.6** A decomposition for sparse matrix-vector multiplication and the corresponding task-interaction graph. In the decomposition Task  $i$  computes  $\sum_{0 \leq j \leq 11, A[i,j] \neq 0} A[i,j] \cdot b[j]$ .

# Sources

- Slides of Dr. Rana Asif Rahman & Dr. Haroon Mahmood, FAST
- (Chapter 2) Kumar, V., Grama, A., Gupta, A., & Karypis, G. (1994). Introduction to parallel computing (Vol. 110). Redwood City, CA: Benjamin/Cummings.
- Quinn, M. J. Parallel Programming in C with MPI and OpenMP,(2003).