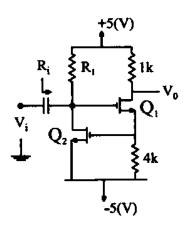
جواب سوالات Homwork 8



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$$v_0 = 4v \implies I_{D_1} = \frac{5-4}{1k} = 1 \text{ mA}$$

$$V_{Gs_2} = 4k(1 \text{ mA}) = 4V \implies I_D = k(V_{GS_2} - V_T)^2 = 1 \text{ mA}$$

$$R_1 = \frac{5 - (-5) - V_{GS_1} - V_{GS_2}}{1 \text{ mA}} = 2k\Omega$$

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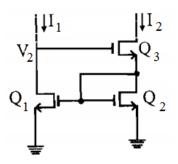
$$\begin{split} R_{i} &= \frac{V_{i}}{I_{i}} \\ v_{i} &= v_{gs_{1}} + g_{m}v_{gs_{1}}\left(4k\right) \quad , \quad g_{m} = k\left(V_{GS} - V_{T}\right) = i\frac{mA}{V} \\ V_{i} &= 5\left(V_{gs_{1}}\right) \quad , \quad V_{gs_{2}} = g_{m}v_{gs_{1}}\left(4k\right) = 4vgs_{1} \\ v_{j} &= \frac{5}{4}\left(v_{gs_{2}}\right) \\ I_{i} &= \frac{V_{i}}{R_{1}} + g_{m}v_{gs_{2}} \\ \frac{v_{j}}{I_{i}} &= R_{i} = 0.77 \ k\Omega \end{split}$$

$$\begin{split} &I_{D_{\eta}} = I_{D_{\eta}} \Rightarrow \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \Leftrightarrow \frac{K_{\eta}}{\tau} (V_{T_{\eta}} = V_{T_{\eta}})^{\tau} = (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \Rightarrow (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \Rightarrow V_{GS_{\eta}} = V_{GS_{\eta}} \\ & I_{D_{\eta}} = I_{D_{\eta}} \Rightarrow \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \Rightarrow (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \downarrow V_{S_{\eta}} = V_{O} \\ & V_{S_{\eta}} = V_{O} \\ & I_{D_{\eta}} = I_{D_{\eta}} \Rightarrow \frac{k_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{k_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \Leftrightarrow V_{GS_{\eta}} - V_{T_{\eta}} \Rightarrow \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} = \frac{K_{\eta}}{\tau} (V_{GS_{\eta}} - V_{T_{\eta}})^{\tau} \\ & \Rightarrow V_{GS_{\eta}} - V_{T_{\eta}} = \tau (V_{GS_{\eta}} - V_{T_{\eta}}) \\ & \Rightarrow (V_{S_{\eta}} = V_{O}) \\ & \Rightarrow (V_{S_{\eta}} = V_{O})$$

$$\Rightarrow (V_{GS_{\tau}} - f V_{T_{\tau}})^{\tau} = (V_{GS_{\tau}} - V_{T_{\tau}})^{\tau} \Rightarrow V_{GS_{\tau}} - f V_{T_{\tau}} = V_{GS_{\tau}} - V_{T_{\tau}}$$

$$\begin{cases} V_{G_{\tau}} = 1 \cdot \\ V_{S_{\tau}} = V_{O} \end{cases}, \quad \begin{cases} V_{G_{\tau}} = V_{O} \\ V_{S_{\tau}} = \cdot \end{cases} \Rightarrow (1 \cdot - V_{O} - f V_{T_{\tau}}) = (V_{O} - \cdot - V_{T_{\tau}}) \Rightarrow \tau V_{O} = 1 \cdot - r V_{T_{\tau}}$$

$$\Rightarrow V_{O} = \frac{1 \cdot - r V_{T_{\tau}}}{r}$$



$$I_1 = \frac{K_1}{\gamma} (V_{GS_1} - V_{T_1})^{\gamma} \Rightarrow 1 \text{ mA} = \frac{\gamma}{\gamma} (V_{GS_1} - \gamma)^{\gamma} \Rightarrow 1 = (V_{G_1} - V_{S_1} - \gamma)^{\gamma}$$

$$V_{S_1} = \langle V \Rightarrow 1 = (V_{G_1} - Y)^T \Rightarrow \begin{cases} V_{G_1} - Y = 1 \Rightarrow V_{G_1} = YV \\ V_{G_1} - Y = -1 \Rightarrow V_{G_1} = 1V \end{cases}$$

نمیباشد. $m V_{GS} =
m V >
m V_{T}$ قابل قبول نمیباشد چون $m V_{GS} =
m V
m V_{G_1} =
m V$

$$V_{G_1} = \Upsilon V$$
 قابل قبول $\Rightarrow V_1 = V_{G_1} = \Upsilon V$

$$I_{\gamma} = I_{D_{\gamma}} = I_{D_{\gamma}} = \frac{K_{\gamma}}{\gamma} (V_{GS_{\gamma}} - V_{T_{\gamma}})^{\gamma} \Rightarrow \begin{cases} V_{S_{\gamma}} = \bullet \\ V_{G_{\gamma}} = V_{G_{\gamma}} = \Upsilon V \end{cases}$$

$$\Rightarrow I_{\gamma} = \frac{\gamma}{\gamma} (\gamma - \gamma)^{\gamma} = \gamma mA$$

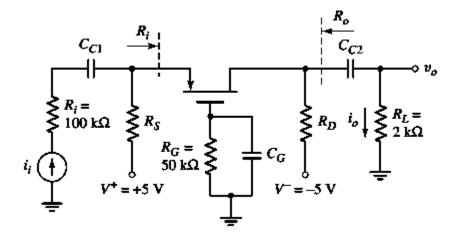
$$I_{D_{\tau}} = I_{D_{\tau}} = \mbox{\backslash mA$} \Rightarrow \mbox{$\backslash$ mA$} = \frac{K_{\tau}}{\gamma} (V_{GS_{\tau}} - V_{T_{\tau}})^{\gamma} \Rightarrow \mbox{\backslash mA$} = \frac{\gamma}{\gamma} (V_{G_{\tau}} - V_{S_{\tau}} - \gamma)^{\gamma}$$

ز طرفی
$$k V_{S_{\tau}} = V_1 = \pi V \Rightarrow V = (V_{G_{\tau}} - \pi - \tau)^{\tau} \Rightarrow$$

$$V_{G_{\gamma}}$$
 - ۵ = ± ۱ \Rightarrow $\begin{cases} V_{G_{\gamma}} = 9 \, V \\ V_{G_{\gamma}} = 4 \, V \Rightarrow \end{cases}$ قابل قبول نمىباشد

 $V_{GS_7}=$ ۴- ۳= ۱۷ بــاشد در ایــن صــورت $V_{GS_7}=$ ۴- ۳= $V_{GS_7}=$ مــیشود کــه از $V_{GS_7}=$ ۴۷ جا تال قبول نمیباشد پس داریم:

$$V_{G_r} = 9V \Rightarrow V_r = V_{G_r} = 9V$$



a.

$$I_{DQ} = K_p (V_{SG} + V_{TP})^2$$

$$0.75 = (0.5)(V_{SG} - 1)^2 \Rightarrow V_{SG} = 2.225 \text{ V}$$

$$5 = I_{DQ}R_S + V_{SG} \Rightarrow R_S = \frac{5 - 2.225}{0.75} \Rightarrow \underline{R_S} = 3.70 \text{ k}\Omega$$

$$V_{SDQ} = 10 - I_{DQ}(R_S + R_D)$$

$$6 = 10 - (0.75)(3.70 + R_D) \Rightarrow \underline{R_D} = 1.63 \text{ k}\Omega$$

b.

$$R_{i} = \frac{1}{g_{m}}$$

$$g_{m} = 2\sqrt{K_{p}I_{DQ}} = 2\sqrt{(0.5)(0.75)} = 1.225 \text{ mA/V}$$

$$R_{i} = \frac{1}{1.225} \Rightarrow \frac{R_{i} = 0.816 \text{ k}\Omega}{R_{o} = R_{D}} \Rightarrow \frac{R_{o} = 1.63 \text{ k}\Omega}{R_{o}}$$

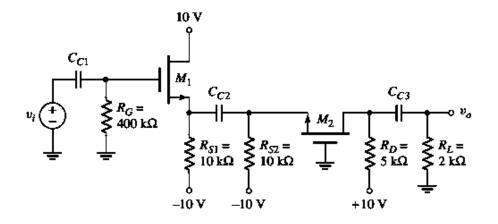
c.

$$i_{0} = \left(\frac{R_{D}}{R_{D} + R_{L}}\right) \left(\frac{R_{S}}{R_{S} + \left[1/g_{m}\right]}\right) \cdot i_{i}$$

$$i_{0} = \left(\frac{1.63}{1.63 + 2}\right) \left(\frac{3.70}{3.70 + 0.816}\right) i_{i}$$

$$i_{0} = 0.368 i_{i} = i_{0} = 1.84 \sin \omega t \left(\mu A\right)$$

$$v_{0} = i_{0} R_{L} = (1.84)(2) \sin \omega t \Rightarrow v_{0} = 3.68 \sin \omega t \left(\text{mV}\right)$$



(a)
$$I_{DQ1} = \frac{10 - V_{GS1}}{R_{S2}} = K_{n1} \left(V_{GS1} - V_{TN1} \right)^{2}$$

$$10 - V_{GS1} = (4) (10) \left(V_{GS1}^{2} - 4V_{GS1} + 4 \right)$$

$$40V_{GS1}^{2} - 159V_{GS1} + 150 = 0$$

$$V_{GS1} = \frac{159 \pm \sqrt{(159)^{2} - 4(40)(150)}}{2(40)} \Rightarrow V_{GS1} = 2.435 \text{ V}$$

$$I_{DQ1} = (4) (2.435 - 2)^{2} \Rightarrow I_{DQ1} = 0.757 \text{ mA}$$

$$V_{DSQ1} = 20 - (0.757)(10) \Rightarrow V_{DSQ1} = 12.4 \text{ V}$$
Also
$$I_{DQ2} = 0.757 \text{ mA}$$

$$V_{DSQ2} = 20 - (0.757)(10 + 5) \Rightarrow V_{DSQ2} = 8.65 \text{ V}$$
(b)
$$g_{m1} = g_{m2} = 2\sqrt{KI_{DQ}} = 2\sqrt{(4)(0.757)} \Rightarrow g_{m1} = g_{m2} = 3.48 \text{ mA/V}$$

$$V_{gs1} \longrightarrow g_{m1}V_{gs1}$$

$$R_{G} \longrightarrow g_{m2}V_{gs2}$$

$$R_{S1} \longrightarrow V_{gs2}$$

$$R_{S2} + \vdots$$

$$R_{D} \longrightarrow R_{L}$$

$$V_{0} = -\left(g_{m2}V_{gs2}\right)\left(R_{D} \| R_{L}\right)$$

$$V_{gs2} = \left(-g_{m1}V_{gs1} - g_{m2}V_{gs2}\right)\left(R_{S1} \| R_{S2}\right)$$

$$V_{i} = V_{gs1} - V_{gs2} \Rightarrow V_{gs1} = V_{i} + V_{gs2}$$

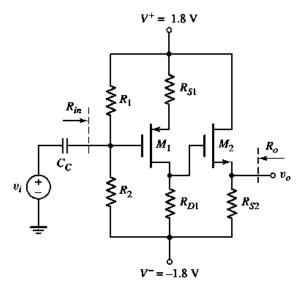
$$V_{gs2} + g_{m2}V_{gs2}\left(R_{S1} \| R_{S2}\right) = -g_{m1}\left(V_{i} + V_{gs2}\right)\left(R_{S1} \| R_{S2}\right)$$

$$V_{gs2} + g_{m2}V_{gs2}\left(R_{S1} \| R_{S2}\right) + g_{m1}V_{gs2}\left(R_{S1} \| R_{S2}\right) = -g_{m1}V_{i}\left(R_{S1} \| R_{S2}\right)$$

$$V_{gs2} = \frac{-g_{m1}V_{i}\left(R_{S1} \| R_{S2}\right)}{1 + g_{m2}\left(R_{S1} \| R_{S2}\right) + g_{m1}\left(R_{S1} \| R_{S2}\right)}$$

$$A_{v} = \frac{V_{0}}{V_{i}} = \frac{g_{m1}g_{m2}\left(R_{S1} \| R_{S2}\right)\left(R_{D} \| R_{L}\right)}{1 + \left(g_{m1} + g_{m2}\right)\left(R_{S1} \| R_{S2}\right)}$$

$$A_{v} = \frac{\left(3.48\right)^{2}\left(10 \| 10\right)\left(5 \| 2\right)}{1 + \left(3.48 + 3.48\right)\left(10 \| 10\right)} \Rightarrow A_{v} = 2.42$$



(a)
$$R_{S1} = \frac{0.6}{0.1} = 6 \text{ k }\Omega$$

 $V_{D1} = 1.8 - 0.6 - 1 = 0.2 \text{ V}$
 $R_{D1} = \frac{0.2 - (-1.8)}{0.1} = 20 \text{ k }\Omega$
 $I_{DQ1} = K_{p1} (V_{SGQ1} + V_{TP})^2$
 $0.1 = 0.4 (V_{SGQ1} - 0.4)^2 \Rightarrow V_{SGQ1} = 0.90 \text{ V}$
 $I_{DQ2} = K_{n2} (V_{GSQ2} - V_{TN})^2$
 $0.3 = 4 (V_{GSQ2} - 0.4)^2 \Rightarrow V_{GSQ2} = 0.6739 \text{ V}$
 $V_{G1} = 1.8 - 0.6 - V_{SGQ1} = 1.8 - 0.6 - 0.9 = 0.3 \text{ V}$
 $V_{G1} = \left(\frac{R_2}{R_1 + R_2}\right) (3.6) - 1.8$
 $0.3 = \frac{1}{R_1} (200)(3.6) - 1.8 \Rightarrow R_1 = 343 \text{ k }\Omega$

$$R_1 \| R_2 = 200 \text{ k } \Omega \implies R_2 = 480 \text{ k } \Omega$$

 $V_{D1} = 1.8 - 0.6 - 1.0 = 0.2 \text{ V}$
 $V_{S2} = V_{D1} - V_{GSQ2} = 0.2 - 0.6739 = -0.4739 \text{ V}$
 $R_{S2} = \frac{-0.4739 - (-1.8)}{0.3} = 4.42 \text{ k } \Omega$

(b)
$$A_{v} = \left(\frac{-g_{m1}R_{D1}}{1+g_{m1}R_{S1}}\right)\left(\frac{g_{m2}R_{S2}}{1+g_{m2}R_{S2}}\right)$$

 $g_{m1} = 2\sqrt{K_{p1}I_{DQ1}} = 2\sqrt{(0.4)(0.1)} = 0.4 \text{ mA/V}$
 $g_{m2} = 2\sqrt{K_{n2}I_{DQ2}} = 2\sqrt{(4)(0.3)} = 2.191 \text{ mA/V}$
 $A_{v} = \frac{-(0.4)(20)}{1+(0.4)(6)} \cdot \frac{(2.191)(4.42)}{1+(2.191)(4.42)} = -2.13$

(c)
$$R_o = \frac{1}{g_{m^2}} ||R_{S2}|| = \frac{1}{2.191} ||4.42|| = 0.4564 ||4.42|| \Rightarrow R_o = 414 \Omega$$