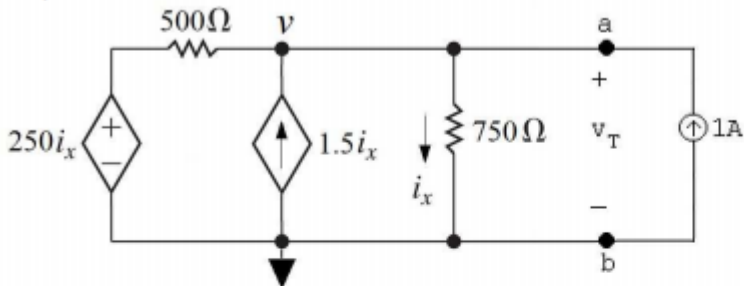


## Homwork 3 جواب سوالات

-۲

$V_{Th} = 0$  since there are no independent sources in the circuit. Thus we need only find  $R_{Th}$ .



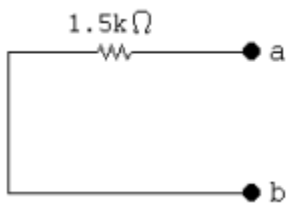
$$\frac{v - 250i_x}{500} - 1.5i_x + \frac{v}{750} - 1 = 0$$

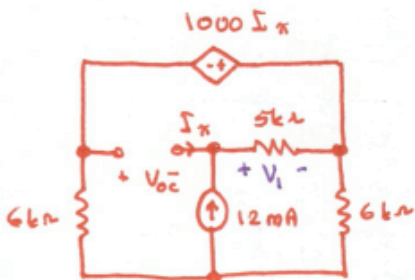
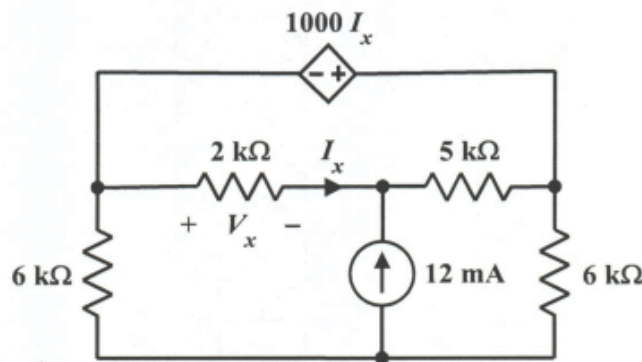
$$i_x = \frac{v}{750}$$

Solving,

$$v = 1500 \text{ V}; \quad i_x = 2 \text{ A}$$

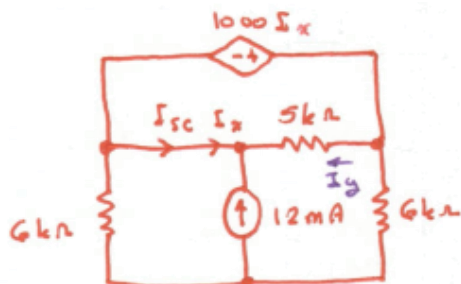
$$R_{Th} = \frac{v}{1 \text{ A}} = 1500 = 1.5 \text{ k}\Omega$$





$$I_x = 0 \Rightarrow V_1 = (5k\Omega)(12mA) = 60V$$

$$\Rightarrow 1000 I_x = 0 \Rightarrow V_{oc} = -V_1 = -60V$$



$$I_y = \frac{1000 I_x}{5k\Omega} = \frac{1}{5} I_x$$

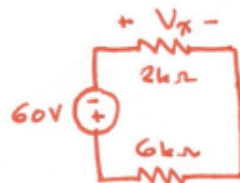
$$I_y + I_x = -12mA \Rightarrow 1.2 I_x = -12mA$$

$$\therefore I_x = -10mA$$

$$I_{sc} = I_x = -10mA$$

$$V_T = V_{oc} = -60V$$

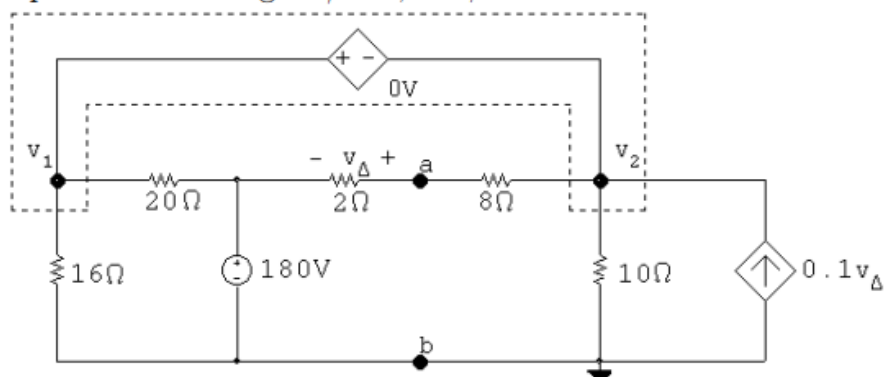
$$R_T = \frac{V_{oc}}{I_{sc}} = \frac{-60V}{-10mA} = 6k\Omega$$



$$V_x = - \frac{2k\Omega}{2k\Omega + 6k\Omega} (60V) = -15V$$

[a] First find the Thévenin equivalent with respect to  $R_o$ .

Open circuit voltage:  $i_\phi = 0$ ;  $184\phi = 0$



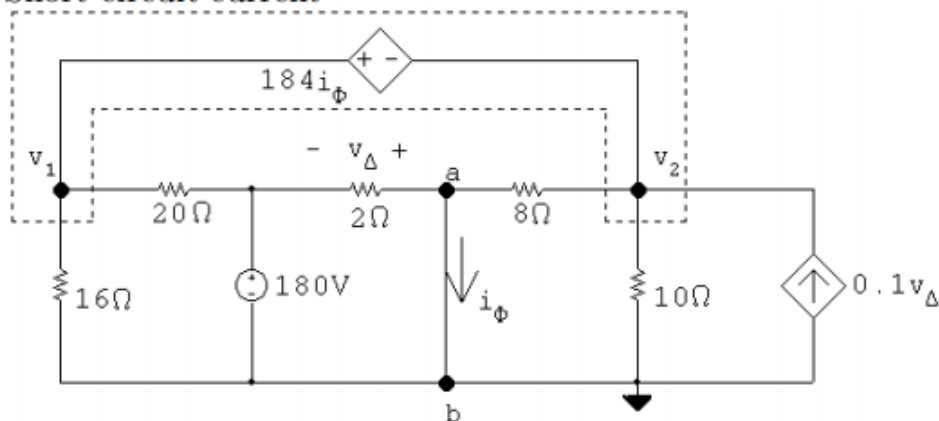
$$\frac{v_1}{16} + \frac{v_1 - 180}{20} + \frac{v_1 - 180}{10} + \frac{v_1}{10} - 0.1v_\Delta = 0$$

$$v_\Delta = \frac{v_1 - 180}{10}(2) = 0.2v_1 - 36$$

$$v_1 = 80 \text{ V}; \quad v_\Delta = -20 \text{ V}$$

$$V_{\text{Th}} = 180 + v_\Delta = 180 - 20 = 160 \text{ V}$$

Short circuit current



$$\frac{v_1}{16} + \frac{v_1 - 180}{20} + \frac{v_2}{8} + \frac{v_2}{10} - 0.1(-180) = 0$$

$$v_2 + 184i_\phi = v_1$$

$$i_\phi = \frac{180}{2} + \frac{v_2}{8} = 90 + 0.125v_2$$

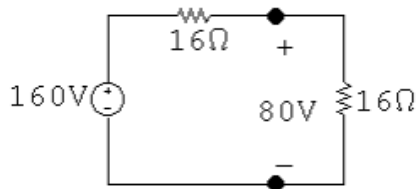
$$v_2 = -640 \text{ V}; \quad v_1 = 1200 \text{ V}$$

$$i_{\phi} = i_{sc} = 10 \text{ A}$$

$$R_{Th} = V_{Th}/i_{sc} = 160/10 = 16 \Omega$$

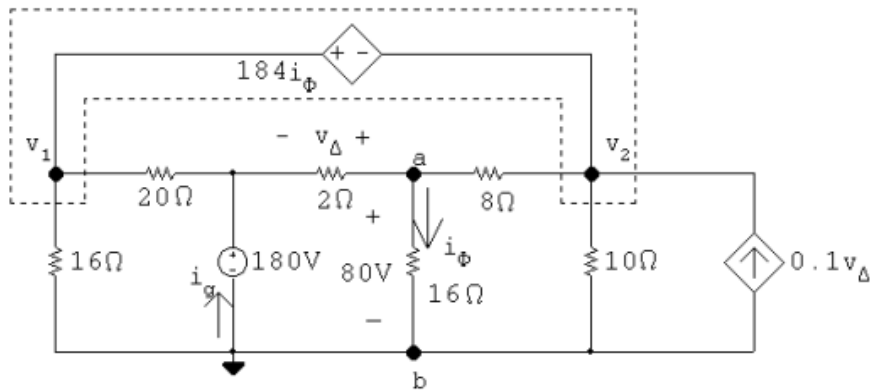
$$\therefore R_o = 16 \Omega$$

[b]



$$p_{\max} = (80)^2/16 = 400 \text{ W}$$

[c]



$$\frac{v_1}{16} + \frac{v_1 - 180}{20} + \frac{v_2 - 80}{8} + \frac{v_2}{10} - 0.1(80 - 180) = 0$$

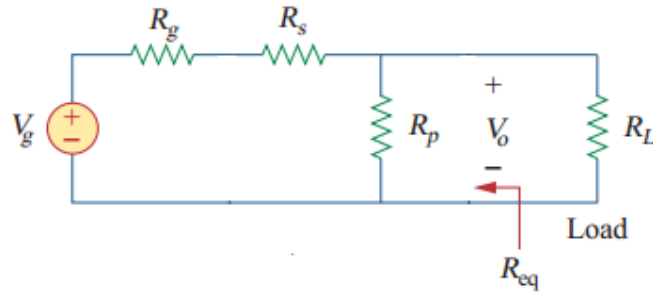
$$v_2 + 184i_{\phi} = v_1; \quad i_{\phi} = 80/16 = 5 \text{ A}$$

Therefore,  $v_1 = 640 \text{ V}$  and  $v_2 = -280 \text{ V}$ ; thus,

$$i_g = \frac{180 - 80}{2} + \frac{180 - 640}{20} = 27 \text{ A}$$

$$p_{180\text{V}} (\text{dev}) = (180)(27) = 4860 \text{ W}$$

$$400 \cdot 100 / 4860 = 8.23 \%$$



(a) 
$$V_o/V_g = R_p/(R_g + R_s + R_p) \quad (1)$$

$$R_{eq} = R_p || (R_g + R_s) = R_g$$

$$R_g = R_p(R_g + R_s)/(R_p + R_g + R_s)$$

$$R_g R_p + R_g^2 + R_g R_s = R_p R_g + R_p R_s$$

$$R_p R_s = R_g(R_g + R_s) \quad (2)$$

From (1), 
$$R_p/\alpha = R_g + R_s + R_p$$

$$R_g + R_s = R_p((1/\alpha) - 1) = R_p(1 - \alpha)/\alpha \quad (1a)$$

Combining (2) and (1a) gives,

$$R_s = [(1 - \alpha)/\alpha]R_{eq} \quad (3)$$

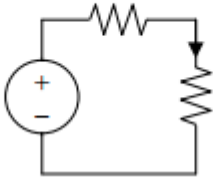
$$= (1 - 0.125)(100)/0.125 = \underline{\underline{700 \text{ ohms}}}$$

From (3) and (1a),

$$R_p(1 - \alpha)/\alpha = R_g + [(1 - \alpha)/\alpha]R_g = R_g/\alpha$$

$$R_p = R_g/(1 - \alpha) = 100/(1 - 0.125) = \underline{\underline{114.29 \text{ ohms}}}$$

(b)

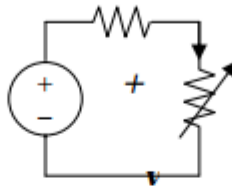


$$V_{Th} = V_s = 0.125V_g = 1.5 \text{ V}$$

$$R_{Th} = R_g = 100 \text{ ohms}$$

$$I = V_{Th}/(R_{Th} + R_L) = 1.5/150 = \underline{\underline{10 \text{ mA}}}$$

We replace the box with the Thevenin equivalent.



$$V_{Th} = v + iR_{Th}$$

When  $i = 1.5$ ,  $v = 3$ , which implies that  $V_{Th} = 3 + 1.5R_{Th}$  (1)

When  $i = 1$ ,  $v = 8$ , which implies that  $V_{Th} = 8 + 1R_{Th}$  (2)

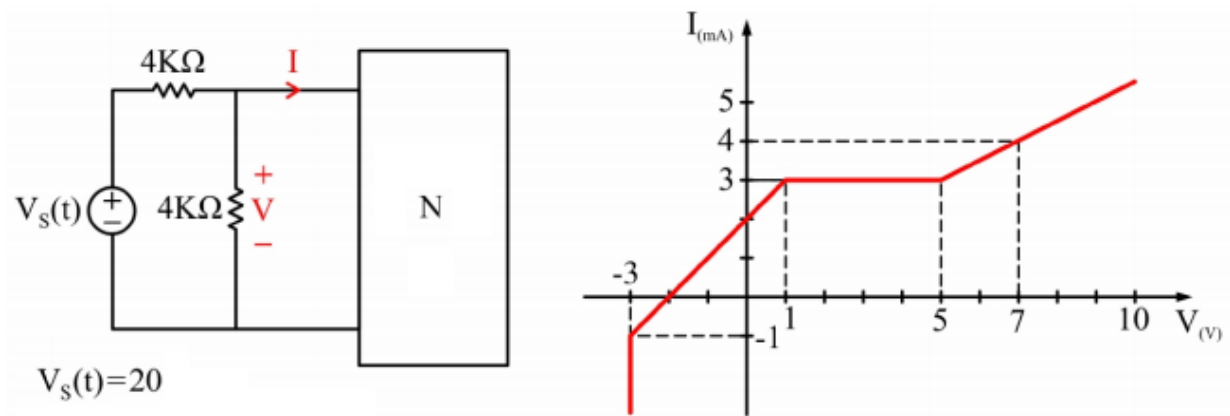
From (1) and (2),  $R_{Th} = 10$  ohms and  $V_{Th} = 18$  V.

(a) When  $R = 4$ ,  $i = V_{Th}/(R + R_{Th}) = 18/(4 + 10) = \underline{\underline{1.2857 \text{ A}}}$

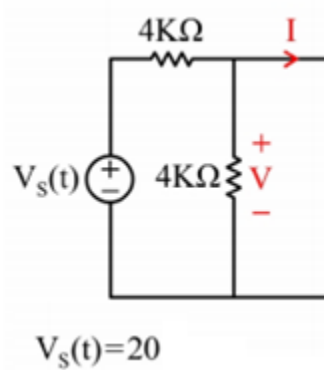
(b) For maximum power,  $R = R_{Th}$

$$P_{max} = (V_{Th})^2/4R_{Th} = 18^2/(4 \times 10) = \underline{\underline{8.1 \text{ watts}}}$$

-V



First find the Thévenin equivalent



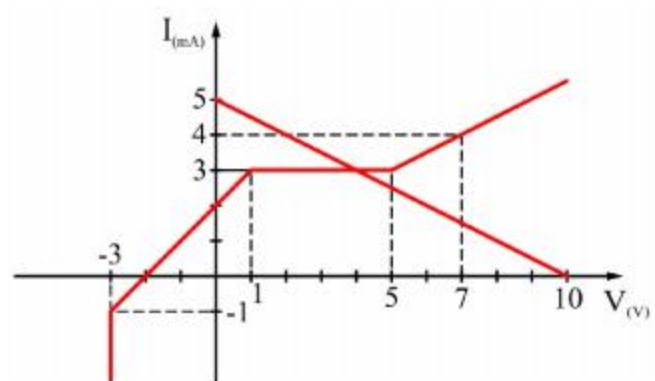
$$R_{th} = 2K\Omega, \quad e_{oc} = \frac{V_s}{2} \Rightarrow V = 2I + \frac{V_s}{2}$$

The relationship between voltage and current for the above figure is obtained as follows

$$V = -2I + 10$$

Then we obtain the intersection point of this equation with the V-I diagram of bipolar N:





$$\Rightarrow i=3 \Rightarrow V = -2 \times 3 + 10 = 4$$