



deeplearning.ai

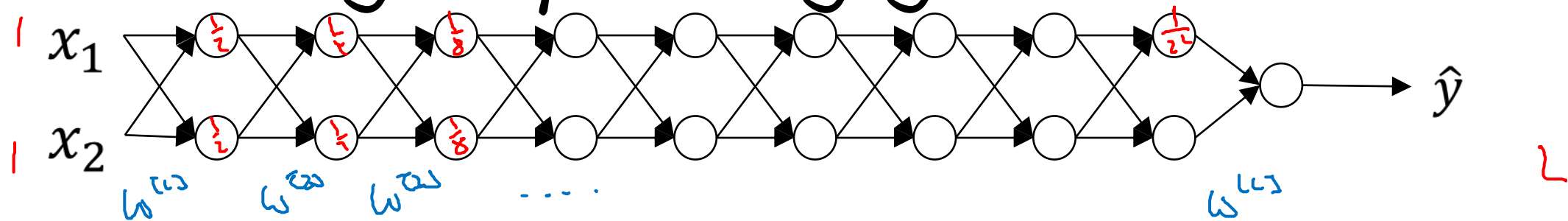
Setting up your  
optimization problem

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Vanishing/exploding  
gradients

# Vanishing/exploding gradients

$L=150$



$g(z) = z$        $b^{(L)} = 0$

$\hat{y} = w^{(L,L)} \underbrace{w^{(L-1,L)} w^{(L-2,L)} \dots w^{(2,L)}}_{\text{product of weights}} a^{(1,L)}$

$1.5^L$   
 $0.5^L$

$w^{(1,1)} > I$

$w^{(1,2)} < I$        $\begin{bmatrix} 0.9 & \\ & 0.9 \end{bmatrix}$

$w^{(1,2)} = \begin{bmatrix} 1.5 & 0 \\ 0 & 0.5 \end{bmatrix}$

$0.5$   
 $1.5$   
 $0.5$

$z^{(1)} = w^{(1,1)} x$

$a^{(1)} = g(z^{(1)}) = z^{(1)}$

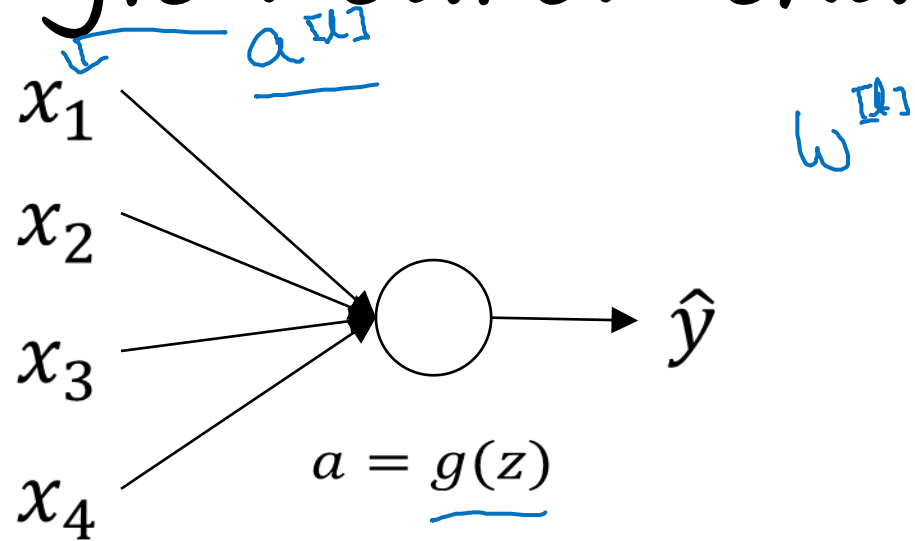
$a^{(2)} = g(z^{(2)}) = g(w^{(2,1)} a^{(1)})$

$\hat{y} = w^{(L,L)} \begin{bmatrix} 1.5 & 0 \\ 0 & 0.5 \end{bmatrix}^{L-1} x$

$0.5$   
 $1.5$   
 $0.5$

$1.5^{L-1} x$   
 $0.5^{L-1} x$

# Single neuron example



$$z = w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

large  $n \rightarrow$  Smaller  $w_i$

$$\text{Var}(w_i) = \frac{1}{n} \frac{2}{n}$$

$$\underline{w^{[L]}} = \text{np.random.randn}(\text{shape}) * \text{np.sqrt}\left(\frac{2}{n^{[L-1]}}\right)$$

ReLU  $g^{[L]}(z) = \text{ReLU}(z)$

Other variants:

$$\tanh \sqrt{\frac{2}{n^{[L-1]}}}$$

Xavier initialization ↑

$$\sqrt{\frac{2}{n^{[L-1]} + n^{[L]}}}$$

↑