



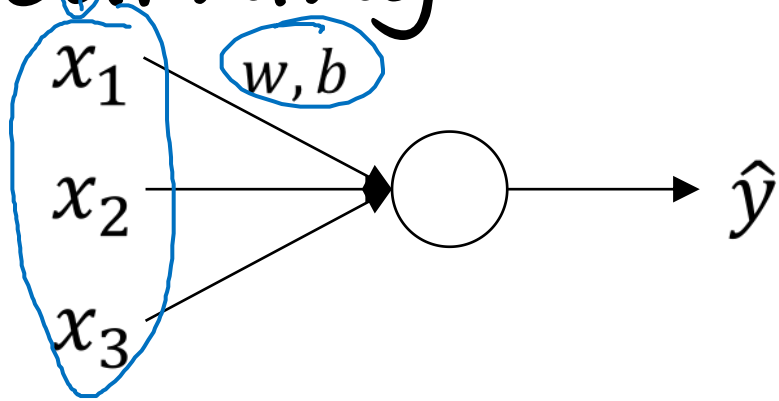
deeplearning.ai

# Batch Normalization

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Normalizing activations  
in a network

# Normalizing inputs to speed up learning

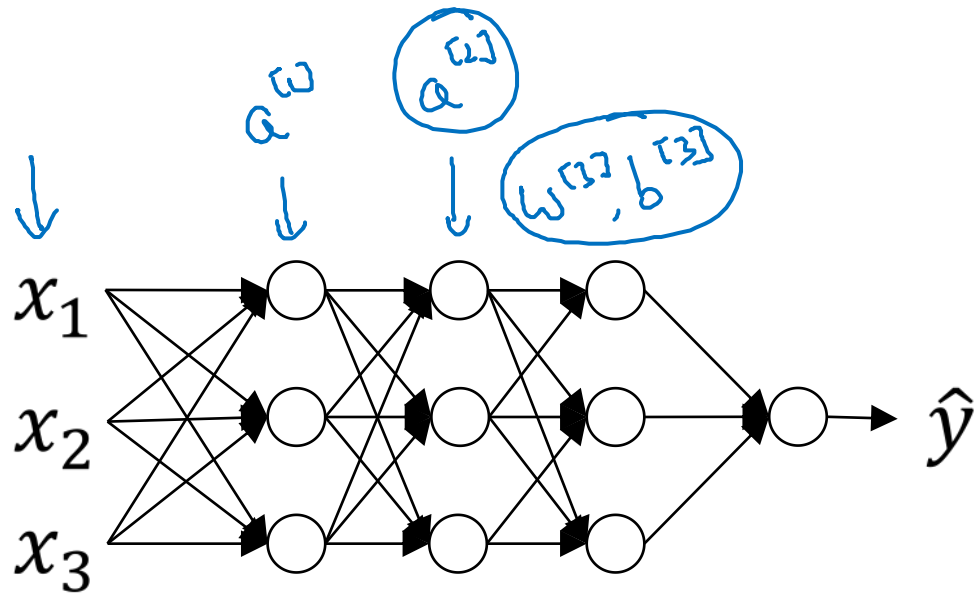
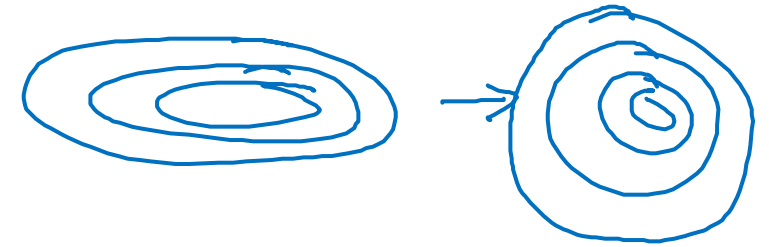


$$\mu = \frac{1}{n} \sum_i x^{(i)}$$

$$X = X - \mu$$

$$\sigma^2 = \frac{1}{n} \sum_i x^{(i)2} \quad \leftarrow \text{element-wise}$$

$$X = X / \sigma^2$$



Can we normalize  $\frac{a^{[2]}}{w^{[2]}, b^{[2]}}$  so as to train faster

Normalize  $\frac{z^{[2]}}{\uparrow}$

# Implementing Batch Norm

Given some intermediate values in NN

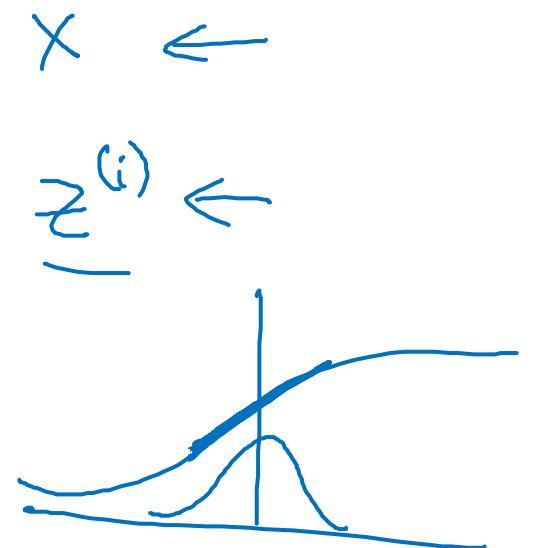
$$z^{(1)}, \dots, z^{(m)}$$

$$z^{[l]}(i)$$

$$\begin{aligned} \mu &= \frac{1}{m} \sum_i z^{(i)} \\ \sigma^2 &= \frac{1}{m} \sum_i (z^{(i)} - \mu)^2 \\ z_{\text{norm}}^{(i)} &= \frac{z^{(i)} - \mu}{\sqrt{\sigma^2 + \epsilon}} \\ \hat{z}^{(i)} &= \gamma z_{\text{norm}}^{(i)} + \beta \end{aligned}$$

$$\begin{aligned} \text{If } \gamma &= \sqrt{\sigma^2 + \epsilon} \\ \beta &= \mu \\ \text{then } \hat{z}^{(i)} &= z^{(i)} \end{aligned}$$

learnable parameters of model.



Use  $\hat{z}^{[l]}(i)$  instead of  $z^{[l]}(i)$