

## E. Surprise me!

time limit per test: 8 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Tired of boring dates, Leha and Noora decided to play a game.

Leha found a tree with  $n$  vertices numbered from 1 to  $n$ . We remind you that tree is an undirected graph without cycles. Each vertex  $v$  of a tree has a number  $a_v$  written on it. Quite by accident it turned out that all values written on vertices are distinct and are natural numbers between 1 and  $n$ .

The game goes in the following way. Noora chooses some vertex  $u$  of a tree uniformly at random and passes a move to Leha. Leha, in his turn, chooses (also uniformly at random) some vertex  $v$  from remaining vertices of a tree ( $v \neq u$ ). As you could guess there are  $n(n - 1)$  variants of choosing vertices by players. After that players calculate the value of a function  $f(u, v) = \varphi(a_u \cdot a_v) \cdot d(u, v)$  of the chosen vertices where  $\varphi(x)$  is Euler's totient function and  $d(x, y)$  is the shortest distance between vertices  $x$  and  $y$  in a tree.

Soon the game became boring for Noora, so Leha decided to defuse the situation and calculate expected value of function  $f$  over all variants of choosing vertices  $u$  and  $v$ , hoping of at least somehow surprise the girl.

Leha asks for your help in calculating this expected value. Let this value be representable in the form of an irreducible fraction . To further surprise Noora, he wants to name her the value .

Help Leha!

### Input

The first line of input contains one integer number  $n$  ( $2 \leq n \leq 2 \cdot 10^5$ ) — number of vertices in a tree.

The second line contains  $n$  different numbers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq n$ ) separated by spaces, denoting the values written on a tree vertices.

Each of the next  $n - 1$  lines contains two integer numbers  $x$  and  $y$  ( $1 \leq x, y \leq n$ ), describing the next edge of a tree. It is guaranteed that this set of edges describes a tree.

### Output

In a single line print a number equal to  $P \cdot Q^{-1}$  modulo  $10^9 + 7$ .

### Examples

input
3 1 2 3 1 2 2 3
output
33333338

input
5 5 4 3 1 2 3 5 1 2 4 3 2 5
output

## Note

Euler's totient function  $\varphi(n)$  is the number of such  $i$  that  $1 \leq i \leq n$ , and  $\gcd(i, n) = 1$ , where  $\gcd(x, y)$  is the greatest common divisor of numbers  $x$  and  $y$ .

There are 6 variants of choosing vertices by Leha and Noora in the first testcase:

- $u = 1, v = 2, f(1, 2) = \varphi(a_1 \cdot a_2) \cdot d(1, 2) = \varphi(1 \cdot 2) \cdot 1 = \varphi(2) = 1$
- $u = 2, v = 1, f(2, 1) = f(1, 2) = 1$
- $u = 1, v = 3, f(1, 3) = \varphi(a_1 \cdot a_3) \cdot d(1, 3) = \varphi(1 \cdot 3) \cdot 2 = 2\varphi(3) = 4$
- $u = 3, v = 1, f(3, 1) = f(1, 3) = 4$
- $u = 2, v = 3, f(2, 3) = \varphi(a_2 \cdot a_3) \cdot d(2, 3) = \varphi(2 \cdot 3) \cdot 1 = \varphi(6) = 2$
- $u = 3, v = 2, f(3, 2) = f(2, 3) = 2$

Expected value equals to . The value Leha wants to name Noora is  $7 \cdot 3^{-1} = 7 \cdot 333333336 = 333333338$  .

In the second testcase expected value equals to , so Leha will have to surprise Noora by number  $8 \cdot 1^{-1} = 8$  .