

# N. April Fools' Problem (medium)

time limit per test: 4 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

The marmots need to prepare  $k$  problems for HC<sup>2</sup> over  $n$  days. Each problem, once prepared, also has to be printed.

The preparation of a problem on day  $i$  (at most one per day) costs  $a_i$  CHF, and the printing of a problem on day  $i$  (also at most one per day) costs  $b_i$  CHF. Of course, a problem cannot be printed before it has been prepared (but doing both on the same day is fine).

What is the minimum cost of preparation and printing?

## Input

The first line of input contains two space-separated integers  $n$  and  $k$  ( $1 \leq k \leq n \leq 2200$ ). The second line contains  $n$  space-separated integers  $a_1, \dots, a_n$  — the preparation costs. The third line contains  $n$  space-separated integers  $b_1, \dots, b_n$  — the printing costs.

## Output

Output the minimum cost of preparation and printing  $k$  problems — that is, the minimum possible sum  $a_{i_1} + a_{i_2} + \dots + a_{i_k} + b_{j_1} + b_{j_2} + \dots + b_{j_k}$ , where  $1 \leq i_1 < i_2 < \dots < i_k \leq n$ ,  $1 \leq j_1 < j_2 < \dots < j_k \leq n$  and  $i_1 \leq j_1, i_2 \leq j_2, \dots, i_k \leq j_k$ .

## Example

input
8 4 3 8 7 9 9 4 6 8 2 5 9 4 3 8 9 1
output
32

## Note

In the sample testcase, one optimum solution is to prepare the first problem on day 1 and print it on day 1, prepare the second problem on day 2 and print it on day 4, prepare the third problem on day 3 and print it on day 5, and prepare the fourth problem on day 6 and print it on day 8.