

## F. Coprime Permutation

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Two positive integers are coprime if and only if they don't have a common divisor greater than 1.

Some bear doesn't want to tell Radewoosh how to solve some algorithmic problem. So, Radewoosh is going to break into that bear's safe with solutions. To pass through the door, he must enter a permutation of numbers 1 through  $n$ . The door opens if and only if an entered permutation  $p_1, p_2, \dots, p_n$  satisfies:

In other words, two different elements are coprime if and only if their indices are coprime.

Some elements of a permutation may be already fixed. In how many ways can Radewoosh fill the remaining gaps so that the door will open? Print the answer modulo  $10^9 + 7$ .

### Input

The first line of the input contains one integer  $n$  ( $2 \leq n \leq 1\,000\,000$ ).

The second line contains  $n$  integers  $p_1, p_2, \dots, p_n$  ( $0 \leq p_i \leq n$ ) where  $p_i = 0$  means a gap to fill, and  $p_i \geq 1$  means a fixed number.

It's guaranteed that if  $i \neq j$  and  $p_i, p_j \geq 1$  then  $p_i \neq p_j$ .

### Output

Print the number of ways to fill the gaps modulo  $10^9 + 7$  (i.e. modulo 1000000007).

### Examples

<b>input</b>
4 0 0 0 0
<b>output</b>
4
<b>input</b>
5 0 0 1 2 0
<b>output</b>
2
<b>input</b>
6 0 0 1 2 0 0
<b>output</b>
0
<b>input</b>
5 5 3 4 2 1
<b>output</b>
0

**Note**

In the first sample test, none of four element is fixed. There are four permutations satisfying the given conditions:  $(1,2,3,4)$ ,  $(1,4,3,2)$ ,  $(3,2,1,4)$ ,  $(3,4,1,2)$ .

In the second sample test, there must be  $p_3 = 1$  and  $p_4 = 2$ . The two permutations satisfying the conditions are:  $(3,4,1,2,5)$ ,  $(5,4,1,2,3)$ .