# E. DZY Loves Fibonacci Numbers

time limit per test: 4 seconds memory limit per test: 256 megabytes input: standard input output: standard output

In mathematical terms, the sequence  $F_n$  of Fibonacci numbers is defined by the recurrence relation

$$F_1 = 1$$
;  $F_2 = 1$ ;  $F_n = F_{n-1} + F_{n-2}$   $(n > 2)$ .

DZY loves Fibonacci numbers very much. Today DZY gives you an array consisting of n integers:  $a_1, a_2, ..., a_n$ . Moreover, there are m queries, each query has one of the two types:

- 1. Format of the query "1 l r". In reply to the query, you need to add  $F_{i-l+1}$  to each element  $a_i$ , where  $l \le i \le r$ .
- 2. Format of the query "2 l r". In reply to the query you should output the value of modulo 1000000009 ( $10^9 + 9$ ).

Help DZY reply to all the gueries.

#### Input

The first line of the input contains two integers n and m ( $1 \le n$ ,  $m \le 300000$ ). The second line contains n integers  $a_1, a_2, ..., a_n \ (1 \le a_i \le 10^9)$  — initial array a.

Then, m lines follow. A single line describes a single guery in the format given in the statement. It is guaranteed that for each query inequality  $1 \le l \le r \le n$  holds.

#### **Output**

For each guery of the second type, print the value of the sum on a single line.

## **Examples**

# input

4 4 1 2 3 4

1 1 4

2 1 4

1 2 4 2 1 3

## output

17 12

### **Note**

After the first query, a = [2, 3, 5, 7].

For the second query, sum = 2 + 3 + 5 + 7 = 17.

After the third query, a = [2, 4, 6, 9].

For the fourth query, sum = 2 + 4 + 6 = 12.