

## F. New Year and Finding Roots

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

**This is an interactive problem. In the interaction section below you will find the information about flushing the output.**

The New Year tree of height  $h$  is a perfect binary tree with vertices numbered 1 through  $2^h - 1$  in some order. In this problem we assume that  $h$  is at least 2. The drawing below shows one example New Year tree of height 3:

Polar bears love decorating the New Year tree and Limak is no exception. To decorate the tree, he must first find its root, i.e. a vertex with exactly two neighbours (assuming that  $h \geq 2$ ). It won't be easy because Limak is a little bear and he doesn't even see the whole tree. Can you help him?

There are  $t$  testcases. In each testcase, you should first read  $h$  from the input. Then you can ask at most 16 questions of format "`? x`" (without quotes), where  $x$  is an integer between 1 and  $2^h - 1$ , inclusive. As a reply you will get the list of neighbours of vertex  $x$  (more details in the "Interaction" section below). For example, for a tree on the drawing above after asking "`? 1`" you would get a response with 3 neighbours: 4, 5 and 7. Your goal is to find the index of the root  $y$  and print it in the format "`! y`". You will be able to read  $h$  for a next testcase only after printing the answer in a previous testcase and flushing the output.

Each tree is fixed from the beginning and it doesn't change during your questions.

### Input

The first line of the input contains a single integer  $t$  ( $1 \leq t \leq 500$ ) — the number of testcases.

At the beginning of each testcase you should read from the input a single integer  $h$  ( $2 \leq h \leq 7$ ) — the height of the tree. You can't read the value of  $h$  in a next testcase until you answer a previous testcase.

### Interaction

To ask a question about neighbours of vertex  $x$ , print "`? x`" (without quotes) on a separate line. Note, you must print an end-of-line character after the last character of the line and flush your output to get a response.

The response will consist of two lines. The first line will contain a single integer  $k$  ( $1 \leq k \leq 3$ ) — the number of neighbours of vertex  $x$ . The second line will contain  $k$  distinct integers  $t_1, \dots, t_k$  ( $1 \leq t_1 < \dots < t_k \leq 2^h - 1$ ) — indices of neighbours of vertex  $x$ , gives in the increasing order.

After asking at most 16 questions you have to say  $y$  — the index of the root. Print "`! y`" (without quotes) and an end-of-line character, and flush the output.

Each tree is fixed from the beginning and it doesn't change during your questions.

You can get `Idleness Limit Exceeded` if you don't print anything or if you forget to flush the output.

To flush you can use (just printing a query/answer and end-of-line):

- `fflush(stdout)` in C++;
- `System.out.flush()` in Java;
- `stdout.flush()` in Python;
- `flush(output)` in Pascal;
- See the documentation for other languages.

In any moment if the program reads  $h = 0$  or  $k = 0$  it should immediately terminate normally (for example, calling `exit(0)`). It means that the system detected incorrect request/output from your program and printed 0 because it can't

process your requests anymore. In this case you'll receive verdict "Wrong Answer", but if you ignore case  $h = 0$  or  $k = 0$  it could lead to "Runtime Error", "Time/Memory limit exceeded" or any other verdict because your program could read a trash from the closed input stream.

**Hacking.** To hack someone, use the following format:

The first line should contain a single integer  $t$  equal to 1 (only one testcase is allowed in hacks). The second line should contain a single integer  $h$ . Each of next  $2^h - 2$  lines should contain two distinct integers  $a_i$  and  $b_i$  ( $1 \leq a_i, b_i \leq 2^h - 1$ ), denoting two nodes connected with an edge. The printed edges must form a perfect binary tree of height  $h$ .

Of course, contestant programs will not be able to see this input.

**Examples**

input
1 3 3 4 5 7 2 1 2 1 2
output
? 1 ? 5 ? 6 ! 5

input
2 2 1 3 2 1 2 2 1 2 4 3 3 12 13
output
? 1 ? 3 ? 3 ! 3 ? 6 ! 1

**Note**

In the first sample, a tree corresponds to the drawing from the statement.

In the second sample, there are two two testcases. A tree in the first testcase has height 2 and thus 3 vertices. A tree in the second testcase has height 4 and thus 15 vertices. You can see both trees on the drawing below.