

# CARCA: Context and Attribute-Aware Next-Item Recommendation via Cross-Attention

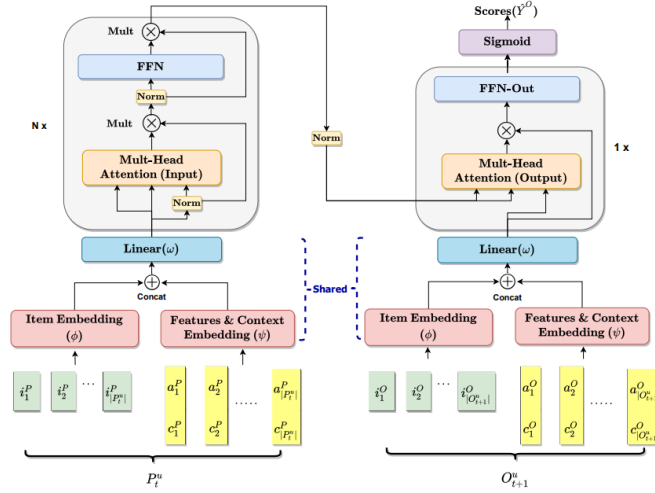


Figure 1: Illustration of the CARCA model, which is composed of two main branches, namely the profile-level features extraction branch on the left and the target items cross-attention scoring branch on the right.

## Problem Definition

An item recommendation problem consists of a set  $\mathcal{U} := \{1, \dots, U\}$  of **users**, a set  $\mathcal{I} := \{1, \dots, I\}$  of **items** and a sequence  $\mathcal{D} = ((u_1, i_1), \dots, (u_N, i_N)) \in (\mathcal{U} \times \mathcal{I})^*$  of their past **interactions** originating from an unknown distribution  $p$  on user/item pairs (with  $U, I, N \in \mathbb{N}$ ). Sought is a model  $\hat{p}: \mathcal{U} \rightarrow (\mathbb{R}_0^+)^I$  for the unknown conditional density  $p(i | u)$ , i.e., given a loss function  $\mathcal{L}: \mathcal{I} \times (\mathbb{R}_0^+)^I \rightarrow \mathbb{R}$  with minimal expected loss

$$\mathbb{E}_{(u,i) \sim p} \mathcal{L}(i, \hat{p}(u))$$

One calls the problem **having item attributes**, if additionally there is a given matrix  $A^{IT} \in \mathbb{R}^{I \times j}$  containing for item an attribute vector with  $j \in \mathbb{N}$  attribute values each.

One calls the problem **having context**, if each interaction has additional attributes, i.e.,  $\mathcal{D} = ((u_1, i_1, c_1), \dots, (u_N, i_N, c_N)) \in (\mathcal{U} \times \mathcal{I} \times \mathbb{R}^l)^*$  (with  $l \in \mathbb{N}$ ) is a sample from an unknown distribution on user/item/context triples and the goal is to find a model  $\hat{p}: \mathcal{U} \times \mathbb{R}^l \rightarrow (\mathbb{R}_0^+)^I$  for the unknown conditional density  $p(i | u, c)$ , i.e., given a loss function  $\mathcal{L}$  with minimal expected loss

$$\mathbb{E}_{(u,i,c) \sim p} \mathcal{L}(i, \hat{p}(u, c))$$

The most frequently encountered context is an absolute **time-stamp** at which the user interacted with an item (for example measured as a real number in Unix Time).

Sequential approaches usually consider all users to have profiles  $P_t^u$  that contain the sequence of their previously interacted items  $P_t^u := \{i_1^P, \dots, i_{|P_t^u|}^P\}$  along with their attributes  $A_t^u \in \mathbb{R}^{|P_t^u| \times j}$  and their interactions' contextual features  $C_t^u \in \mathbb{R}^{|P_t^u| \times l}$  such as timestamps. The main goal of the sequential item recommendation task will be to rank a target list of items  $O_{t+1}^u := \{i_1^O, \dots, i_{|O_{t+1}^u|}^O\}$  based on their likelihood of being interacted with by the target user  $u$  at time  $t + 1$  while similarly considering their attributes and contextual features existing at that time point.

## Model Design

### Embedding

We utilize two separate dedicated embedding functions  $\phi$  and  $\psi$ . The first embedding function  $\phi: \mathbb{R}^1 \rightarrow \mathbb{R}^d$  is used to extract the first half of the item's latent features  $z_i \in \mathbb{R}^d, i \in P_t^u \cup O_{t+1}^u$  from the item's one-hot encoded vectors  $x_i \in \mathbb{R}^I$ . The second function  $\psi: \mathbb{R}^{j+l} \rightarrow \mathbb{R}^g$  extracts the second half of the latent features  $q_i \in \mathbb{R}^g$  from the item's contextual features  $c_i \in \mathbb{R}^l$  and attributes  $a_i \in \mathbb{R}^j$ . After extracting the two partial latent feature vectors, both of them are concatenated and fed into a third embedding layer  $\omega: \mathbb{R}^{g+d} \rightarrow \mathbb{R}^d$  to generate the final item's latent features  $e_i \in \mathbb{R}^d$  as follows:

$$z_i = \phi(x_i) = x_i W^\phi + b^\phi, \quad W^\phi \in \mathbb{R}^{I \times d}, \quad b^\phi \in \mathbb{R}^d \quad (1)$$

$$q_i = \psi(a_i, c_i) = \text{concat}_{\text{col}}(a_i, c_i) W^\psi + b^\psi, \quad W^\psi \in \mathbb{R}^{(j+l) \times g}, \quad b^\psi \in \mathbb{R}^g \quad (2)$$

$$e_i = \omega(z_i, q_i) = \text{concat}_{\text{col}}(z_i, q_i) W^\omega + b^\omega, \quad W^\omega \in \mathbb{R}^{(g+d) \times d}, \quad b^\omega \in \mathbb{R}^d \quad (3)$$

The embedding pipeline is shared between user profile  $P_t^u$  and target items  $O_{t+1}^u$ .

### Self-Attention Blocks

#TODO

### Sampling and Loss Function

For each user we exclude his last interaction and we convert the user profile sequence into a fixed-length input list of items  $P^u := \{i_1^P, \dots, i_{|P_t^u|-1}^P\}$  via truncation or padding.

The list of target items is constructed by combining a list of positive items  $O^{u(+)}$  and another list of negative items  $O^{u(-)}$  with equal length. The positive items list is constructed by right shifting the input list  $P^u$  to include the user's last interaction  $O^{u(+)} := \{i_2^P, \dots, i_{|P_t^u|}^P\}$  while the negative items list is generated by selecting random negative items  $i \notin P^u$  and they are given the same contextual features as their corresponding positive ones.

Finally, we optimize the CARCA model by minimizing the binary cross-entropy loss using an ADAM optimizer, and the padded items are masked to prevent them from contributing to the loss function.

$$\mathcal{L} = - \sum_{u \in U} \sum_{r \in O^{u(+)} \cup O^{u(-)}} \left( Y_r^O \log(\hat{Y}_r^O) + (1 - Y_r^O) \log(1 - \hat{Y}_r^O) \right) \quad (11)$$

## Experiments

**Table 2: Performance comparison of the CARCA against state-of-the-art sequential (SEQ), context (CXT) and attribute-aware (ATT) recommendation models.**

Model	ATT	CXT	SEQ	Men		Fashion		Games		Beauty	
				HR@10	NDCG@10	HR@10	NDCG@10	HR@10	NDCG@10	HR@10	NDCG@10
Random				0.098	0.044	0.099	0.045	0.100	0.045	0.099	0.045
TopPop				0.415	0.269	0.407	0.262	0.519	0.314	0.451	0.261
EASE [22]				0.193	0.133	0.213	0.146	0.623	0.465	0.299	0.222
GraphRec [16]	✓			0.374	0.219	0.419	0.244	0.613	0.400	0.435	0.273
DeepFM [6]	✓	✓		0.334	0.237	0.283	0.185	0.736	0.494	0.464	0.266
SASRec [12]			✓	0.397	0.259	0.381	0.245	0.742	0.541	0.485	0.322
OAR [26]		✓	✓	0.355	0.225	0.340	0.214	0.704	0.496	0.485	0.329
TiSASRec [13]		✓	✓	0.333	0.194	0.384	0.234	0.748	0.533	0.492	0.333
BERT4Rec [23]			✓	0.315	0.193	0.328	0.209	0.705	0.509	0.478	0.318
SSE-SASRec [27]			✓	0.397	0.257	0.385	0.248	0.754	0.549	0.481	0.330
SSE-PT [28]			✓	0.397	0.258	0.381	0.246	0.748(0.775)	0.545(0.566)	0.443(0.502)	0.302(0.337)
S <sup>3</sup> Rec [36]	✓		✓	0.365	0.238	0.367	0.239	<u>0.765</u>	<u>0.549</u>	0.538	<u>0.371</u>
SASRec++ (Our extension)	✓	✓	✓	<u>0.500</u>	<u>0.315</u>	<u>0.546</u>	<u>0.344</u>	0.752	0.533	<u>0.545</u>	0.351
CARCA (w/o CA) (Ours)	✓	✓	✓	0.521	0.322	0.568	0.359	0.738	0.517	0.556	0.358
CARCA (Ours)	✓	✓	✓	<b>0.550*</b>	<b>0.349*</b>	<b>0.591*</b>	<b>0.381*</b>	<b>0.782*</b>	<b>0.573*</b>	<b>0.579*</b>	<b>0.396</b>
Improv. vs best published baseline (%)				38.65	35.87	53.71	53.24	2.20	4.38	7.70	6.74
Improv. vs SASRec++ (%)				10.09	10.79	8.25	10.67	3.96	7.64	6.31	12.95

(\*) Significantly outperforms the best baseline at the 0.01 levels.  
Published results of SSE-PT are indicated in parentheses.

## Ablation Study

**Table 4: Ablation analysis between different CARCA configurations on the Men dataset.**

Configuration	HR@10	NDCG@10
Default (1)	<b>0.550</b>	<b>0.349</b>
Additive residual connections (2)	0.513	0.325
Concat. all features (3)	0.543	0.340
Concat. item features (4)	0.540	0.339
Positional encoding (5)	<u>0.544</u>	<u>0.345</u>
Additional self-attention blocks on output (6)	0.427	0.231
CARCA with single target split (7)	0.394	0.233
CARCA with transformer architecture (8)	0.459	0.276

## Runtime Comparison

**Table 6: Runtime Comparison on Games Dataset**

Model	Average batch runtime in seconds
$S^3$ Rec	0.580
SSE-PT	0.008
SASRec	0.013
TiSASRec	0.075
SSE-SASRec	0.015
OAR	0.018
SASRec++	0.028
CARCA (w/o CA)	0.015
CARCA	0.026