# Syntax Analysis(Parser)

A Syntax analyzer is formally defined as:

An Algorithm that Groups the Set of Tokens Sent by the Scanner to Form **Syntax Structures** Such As Expressions, Statements, Blocks, etc.

Simply put, the parser examines if the source code written follows the grammar(production rules) of the language.

The Syntax structure of programming languages and even spoken languages can be expressed in what is called  ${\bf BNF}$  notation, which stands for  ${\bf Bakus\ Naur\ Form.}$ 

For example, in spoken English, we can say the following:

```
sentence \rightarrow noun-phrase verb-phrase noun-phrase \rightarrow article noun article \rightarrow THE | A | ... noun \rightarrow STUDENT | BOOK | ... verb-phrase \rightarrow verb noun-phrase verb \rightarrow READS | BUYS | ....
```

Note : The BNF Notation uses different symbols, for example, a sentence is defined as :

```
< sentence > ::= < noun-phrase > < verb-phrase >
```

But this is very cumbersome, so we use the first notation, since its easier to use.

Now, let us derive a sentence:

```
sentence -> noun-phrase verb-phrase
```

- -> **article** noun verb-phrase
- -> THE **noun** verb-phrase
- -> THE STUDENT verb-phrase
- -> THE STUDENT **verb** noun-phrase
- -> THE STUDENT READS noun-phrase
- -> THE STUDENT READS article noun
- -> THE STUDENT READS A noun
- -> THE STUDENT READS A BOOK

In the same way, the parser tries to **derive** your source program from the starting symbol of the grammar.

Lets say we have these sentences:

THE BOOK BUYS A STUDENT

THE BOOK WRITES A DISH

THE DISH TAKES A STROLL

Syntax-wise, all of these sentences are correct. However, their meaning is not correct, and they are not useful. What differentiates 2 sentences that are grammatically correct is their meaning or their **semantics**. You and I can agree that the meaning of a grammatically correct sentence is not correct, but how does the computer do it?

### Grammar

A grammar G=(VN, VT, S, P) where:

- 1. VN : A finite set of nonterminals (nonterminals set).
- 2. VT: A finite set of terminals (terminals set).
- 3. S VN: The Starting symbol of the grammar.
- 4. P = A set of **production rules**(productions).<- Pending <==> Basically the whole grammar.

Note:

- 1. VN VT = .
- 2. VN VT = V(the vocabulary of the grammar).

Note: We will use

- 1. Uppercase Letters A,B,...,Z for non-terminals.
- 2. Lowercase Letters a,b,...,z for terminals.
- 3. Greek letters  $\,$ ,  $\,$ ,  $\dots$  for strings formed from VN OR VT = V. eg,

$$if\ VN=\{S,\!A,\!B\},$$

$$VT = \{0,1\}$$

then

- = 0A11B
- = S110B
- = 0010

### **Productions**

1. A Production -> (alpha derives beta) is a rewriting rule such that the occurrence of can be substituted by in any string.

Note that must contain at least one nonterminal from, VN.

For example, Assume we have the string ,

->

- 2. A Derivation is a sequence of strings 0, 1, 2, 3,..., n, then:
  - 0 \*-> n, n = 0.
  - 0 -+-> n, n 1.

Given a grammar G, then:

L(G) = Language Generated By the Grammar.

for example, Given the Grammar,  $G = (\{S,B,C\},\{a,b,c\},S,P)$ 

P:

$$S \rightarrow aSBC$$

$$S \rightarrow abC$$

$$CB \rightarrow BC$$

$$bB \rightarrow bb$$

$$bC \rightarrow bc$$

$$cC \rightarrow CC$$

$$L(G)=?$$

Lets follow through on the derivations

$$S \rightarrow abC \rightarrow abc(all terminals) L(G) \leftarrow A sentence$$

S -> aSBC -> aabCBC -> aabbcBC -> blocked, so we try another path

S -> aSBC ->......->aaabbbccc 
$$\ \, L(G) < --$$
 A sentence

Therefore, 
$$L(G) = \{an, bn, cn | n 1\}$$

As another Example, we have these productions

E -> E+T <- we can write the productions 1 and 2 as a single production E -> E+T | T

$$E \rightarrow T$$

T -> T\*F

T -> F

F -> (E) <- we can write the productions 5 and 6 as a single production F -> (E)  $\mid$  n

$$F -> n$$

Lets follow through some derivations

$$E \rightarrow T \rightarrow F \rightarrow n \quad L(E)$$

$$E -> E+T -> T+T -> T+F -> T+n -> F+n -> n+n \quad L(E)$$

$$E -> E+T -> T+T -> F+T -> n+T -> n+F -> n + (E) -> n+(T) -> n+(T^*F) -> n+(F^*F) -> n+(n^*F) -> n+(n^*n) L(E)$$

Therefore,  $L(G) = \{Any \text{ arithmetic expression with * and + operations}\}$ , n is an operand here.

Note that, if we add the productions

$$E \rightarrow E+T \mid E-T \mid T$$

$$T -\!\!> T^*F \mid T/F \mid T\%F$$

We would have a language to express all arithmetic expressions with  $(*, \cdot, +, -)$  operations.

Lets Take another Example(things in double quotes are terminals)

```
Program -> block "#"

block -> "{" stmt-List "}"

stmt-List -> statement ";" stmt-List |

statement -> if-stmt | while-stmt | read-stmt | write-stmt |

assignment-stmt | block

if-stmt -> "if" condition....

while-stmt -> "while" condition....

....

read-stmt -> "read"

write-stmt -> "write"
```

 $\label{eq:VN} VN = \{ Program, block, stmt-List, statement, if-stmt, while-stmt, read-stmt, write-stmt, assignment-stmt \}$ 

Lets Follow through some derivations :

```
Program \rightarrow block \# \rightarrow { stmt-list } \# \rightarrow { statement ; stmt-list} \# \rightarrow {statement ; statement ; \# \rightarrow {READ-statement ; } \# \rightarrow {READ ; write-statement ;} \# \rightarrow {READ ; WRITE ;} \# \rightarrow {READ ; WRITE ;} \# \rightarrow {READ ; WRITE ;}
```

We can write this as

```
{ READ;
 WRITE;
}#
```

The language of this language is defined as

 $L(G) = \{ \text{Set of all programs that can be written in this language} \}.$ 

This is only a simple example, of a simple language. For something more complex such as C or Pascal, there are hundreds of productions.

### Algorithms for Derivation

A Leftmost derivation is a derivation in which we replace the **left-most** nonterminal in each derivation step.

A Rightmost derivation is a derivation in which we replace the **right-most** nonterminal in each derivation step.

For example, given the grammar

$$\begin{split} V -> S & R \$ \\ S -> + |-| \\ R -> .dN & | dN.N \\ N -> dN & | \\ VN &= \{V,R,S,N\} \\ VT &= \{+,-,.,d,\$\} \end{split}$$

Lets follow through on the leftmost derivation

Lets follow through on the rightmost derivation

$$V -> SR\$ -> SdN.N -> SdN.dN\$ -> SdN.d\$ -> sddN.d\$ -> sdddN.d\$ -> sdddN.d\$ -> sddd.d\$ -> -ddd.d\$ <- A sentence.$$

#### **Derivation Trees**

A Derivation Tree is a Tree that displays the derivation of some sentence in the language. For example, lets look at the tree for the previous example

#### INSERT IMAGE OF TREE FOR -ddd.d\$

Note that if we traverse the tree in order, recording **only** the leaves, we obtain the sentence.

#### Classes of Grammars

According to Chomsky, There are 4 classes of grammars:

- 1. Unrestricted Grammars: No restrictions whatsoever except the restriction by definition that the left side of the production contains at least one nonterminal from Vs. This grammar is not practical and we cannot work with it.
- 2. Context-Sensitive Grammars: For each production -> B, | | | B|, ie, the length of alpha() is less than or equal to the length of Beta(B). This means that in this class of grammar, there are no productions in the form A -> &lambda, since | | = 0 and A 1.

They Say that Fortran has a context-sensitive grammar.

It is very difficult to work with this class of grammars.

3. Context-Free Grammar(CFG): Each production in this grammar class is of the form A -> , where A VN and V\* that is to say, the left hand side is **only** one nonterminal.

This is the most important class of grammar. Most programming languages's structures are context-free.

We will mostly be working with this class of grammar. Most of the examples we have taken are CFG.

4. Regular Grammar (Regular Expressions) : Each production in this grammar class is of the form A->aB or A->a, where A,B-VN and a-VT, with the exception of S->

For example, lets say we have the grammar

$$A \rightarrow aA$$

$$A \rightarrow a$$

Therefore, we get

$$G(L)=a+$$

However, adding the production

Results in the grammar

$$G(L)=a^*$$

# Parsing Techniques

There are 2 main parsing techniques used by a compiler.

#### **Top-Down Parsing**

In Top-Down Parsing, the parser builds the derivation tree from the root(S: the starting symbol) down to the leaves(sentence).

In Simple words, the parser tries to derive the sentence using leftmost derivation. For example, say we have this grammar:

$$V -> SR\$ \\ S -> + | - | \\ R -> .dN | dN.N \\ N -> dN |$$

Lets examine if the sentence

dd.d\$

is derived from this grammar.

V -> 
$$\mathbf{S}$$
R\$ -> + $\mathbf{R}$ \$ ->  $d\mathbf{N}$ .N\$ ->  $dd$ .N\$ ->  $dd.d$ **N**\$ ->  $dd.d$ **N**\$

Therefore, this sentence is derived from the grammar.

However, this approach is very computationally intensive, and more importantly, this requires knowing the source code in advance. The Parser doesnt know which production it should select in each derivation statement. We will learn how to solve these issues later in the course.

### Bottom-Up Parsing

In Bottom-Up Parsing, the parser builds the derivation tree from the leaves(sentence) up to the root(S: Starting Symbol). This type of tree, built from the leaves to the root, is called a B-Tree.

In Simple words, the parser starts with the given sentence, does **reduction**(opposite of derivation) steps, until the starting symbol is reached.

Note that the string is present everywhere in the string, and we can use it wherever we like.

Lets follow the reduction of the example given above.

Which means that the sentence is in the grammar.

Note that we can run into deadlocks here. say we took this path instead:

$$+dd.d\$ -> +dd.d\$ -> +dN.d\$ -> +dN.d\$ -> +dN.d\$ -> +dN.d\$ -> +dN.d\$ -> +dN.dN\$ -> +dNR\$ -> +Deadlock$$

This technique also has a major problem : Which substring should we select to reduce in each reduction step?

how do we slove this?

# Ambiguity

Given the following grammar :

$$\begin{array}{l} num -> num \ d \\ \\ num -> d \end{array}$$

Let us draw the derivation tree for the sentence dddd

```
** TODO INSERT TREE**
```

Question: is there another derivation tree that represents the sentence?

The answer is **no**.

If there is only one derivation tree representing the sentence, this means there is only one way to derive the sentence.

Based on this, we can say that :

A Grammar G is said to be ambiguous if there is one sentence with more than one derivation tree.

That is, there is more than one way to derive the sentence.

This means that our algorithm is **non-deterministic**.

Say we have this grammar

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E -> (E) | a$$

Take the sentence:

$$a + a * a$$

Lets draw the derivation tree

#### TODO INSERT DERIVATION TREE 1 and 2

Due to the fact that we have 2 trees that give the same result, we can say that this grammar is ambiguous.

In this case, to enforce the associativity rule, this grammar can be re-written as  $\dot{}$ 

$$E -> E + E \mid T$$
 $T -> T*T \mid F$ 

Now, Take the sentence a + a \* a and find the derivation tree now.

\*\* INSERT NEW DERIVATION TREE \*\*

There is only 1 possible derivation tree now. This solves the associativity issue of the grammar before with the + and \* operations.

But lets say we have the sentence:

$$a + a + a$$

Lets try to find the derivation tree and any alternative trees.

#### TODO INSERT DERIVATION TREES

We can see here that there is more than 1 derivation tree, and the language is still ambiguous.

We can solve this if we rewrite the grammar with the left-associative rule

$$E \rightarrow E + T \mid T$$
 $T \rightarrow T * F \mid F$ 
 $F \rightarrow (E) \mid a$ 

The resultant grammar is left-associative.

This grammar solves the problems of :

- ambiguity.
- precedence.
- · associativity.

Lets try rewriting it with the right-associative rule

$$E -\!\!> T + E \mid T$$

$$T \rightarrow F * T \mid F$$

Lets try creating the derivation tree of a + a \* a

\*\* INSERT THE TREE of a+a\*a\*\*

Now lets draw the derivation tree of a + a + a

\*\* INSERT THE TREE OF a+a+a\*\*

This new grammar is not ambiguious, however, as we can tell from the derivation trees, there are precedence issues now. It's not technically wrong, but it doesnt not follow standard arithmetic rules.

Back to the left-associative grammar now. This grammar is called **left-recursive**. This causes problems when it omes to top-down parsing techniques (we will see why later).

A grammar is said to be left recursive if there is a production of the form:

$$A->A$$

Conversely, a grammar is right-recursive if there is a production of the form:

$$A \rightarrow A$$

And causes no problems in top-down parsing.

our grammar has 2 rules of the form

$$A->A$$

The solution is to transform the grammar to a grammar which is not left-recursive.

This has an algorithm to it.

Given that

$$A->B1|B2|B3|...|Bn$$

To do this, we must introduce a new non-terminal, say A'.

The grammar now becomes:

and

For example, say we have

$$A->Ab$$

$$A->a$$

$$L(G)=ab^*$$

Then according to the above

$$A->aA'$$

which results in the same grammar.

Lets apply this to the grammar:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

This results in :

$$E' \rightarrow + T E'$$

$$T \rightarrow F T'$$

This grammar is now **perfect**. It solves all our ambiguity issues, and this is a grammar we can use to construct the production rules for our programming language.

Another ambiguity in programming languages is the if...else statement.

Lets take a generic if statement in a generic language:

stmt 
$$->$$
 if-stmt  $\mid$  while-stmt  $\mid$  ....

if-stmt  $\rightarrow$  IF condition stmt

if-stmt -> IF condition stmt ELSE stmt

condition -> C

$$stmt -> S$$

This grammar is ambiguous.

Lets take the nested if...else statement:

IF C

IF C

S

ELSE

This statement results in 2 derivations trees:

# INSERT TREES OF THIS STATEMENT

Both these trees result in the same traversal, but they have different meanings. The first results in the ELSE belonging to the first IF, while the second results int he ELSE belonging to the second IF. We as humans know that the ELSE belongs to the second IF, since we know that the ELSE statement follows the nearest IF. but how can the compiler know?

There are a bunch of solutions to this problem:

1. Add a delimiter to the IF statement, such as ENDIF or END or FI to the end of the statement, resulting in these productions : > if-stmt -> IF condition stmt ENDIF >> if-stmt -> IF condition stmt ELSE stmt ENDIF

Resulting in this statement :

The grammar is now unambigious, since we have to clearly state when an IF statement ends. However, this is not a pretty solution, and is extra work for both the programmar and compiler, and results in less readable code.

2. In C and Pascal, the compiler **always** prefers to shift the ELSE when it sees it in the source code so it follows the nearest IF. We will learn about this in more detail later.

Another thing about this grammar is **left factoring**.

#### Left Factoring

Consider the productions:

A ->

A ->

Note how the first part of the productions is the same. This grammar can be transformed by introducing a new non-terminal, So what happens now is:

For our grammar, this results in

```
if\text{-stmt} \rightarrow IF \text{ condition stmt}
```

if-stmt -> IF condition stmt ELSE stmt

becoming

```
if-stmt -> IF conditon stmt else-part else-part -> ELSE stmt |
```

Does this solve the ambiguity? No, but it helps in removing choices, since the if-stmt is now one production. If we look at the statement :

```
IF C
IF C
ELSE
```

It still has 2 derivation trees

#### TODO INSERT THE 2 DERIVATION TREES

# More Ways of Expressing Programming Languages

#### **Extended BNF Notation**

So far, we have been using **BNF Notation**(Production rules) to express languages. However, there is another form to Express a language, which is **Extended BNF Notation** 

if there is repetition in the grammar, say in the example of the grammar

$$E \rightarrow E + T \mid T$$
 $T \rightarrow T * F \mid F$ 
 $F \rightarrow (E) \mid a$ 

which can give us a derivation in the form of

$$\begin{array}{l} E \rightarrow > E + T \rightarrow > E + T + T \rightarrow > E + T + T + T \rightarrow T + T + T + T + T \\ T....+T \end{array}$$

or in the same line,

We can express this grammar as:

We know that [x] means that we take x 0 or 1 time only.

However,  $\{x\}$  means we take x zero or any number of times. This is equivalent to  $(x)^*$ 

We can also express this grammar as:

$$E \rightarrow T (+ T)^*$$
 $T \rightarrow F (* F)^*$ 
 $F \rightarrow (E) \mid a$ 

### **Syntax Diagrams**

Another way to express languages are **Syntax Diagrams**. These are used only with Extended-BNF notation.

Lets say we have want to express the Expression  ${\bf E}$ , using the Terms  ${\bf T}$  and the Factors  ${\bf F}$  of the form

#### TODO INSERT DRAWINGS OF SYNTAX TREES.

As we can see, A square shape represents a nonterminal and an oval shape represents a terminal.

## Parsing Techniques (Continued)

Recall: The parser is an algorithm which accepts or rejects a sentence in the programming language.

Recall: There are 2 kinds of parsers:

- 1. Top-Down Parsers: In This parsing technique, The parser starts with S using leftmost derivation to derive the sentence. The Major problem with this parsing technique is that the parser doesn't know which production it should select in each derivation step.
- 2. Bottom-Up Parsers: The parser in this parsing technique starts from the sentence, doing reduction steps, until it reaches the starting symbol S of

the grammar. The Major problem with this technique is that the parser doesn't know which substring the parser should select in each reduction step.

In Top-Down parsing, we have 2 available algorithms for parsing:

- 1. Recursive Descent Parsing.
- 2. LL(1) Predictive Parsing.

In Bottom-Up parsing, we have 2 available algorithms for parsing :

- 1. LR Parsers.
- 2. Operator Precedence Parsers -> Uses matrix manipulation.

Before we continue, we need to define a few functions

## The FIRST() Function

Given a string V\*, then

FIRST() = { a | 
$$-*->$$
 aw, a VT,w V\*}

in addition, if -> , then we add to FIRST(), that is

That is to say, FIRST( ) = Set of all terminals that may begin strings derived from  $% \left( 1\right) =1$  .

For example

$$-*-> cBx$$

$$-*-> ayD$$

$$-*-> ab$$

Then

$$FIRST() = \{c,a,d\}$$

Assume as well that

then

$$FIRST() = \{c,a,d,\}$$

That is to say, appears in the FIRST() function.

Lets take an example of this.

### The FOLLOW() Function

We define the FOLLOW() function for **only** nonterminals. That is to say

Given

$$S - *-> uA$$
,  $u VT*, A VN, V*$ 

then

That is to say, FOLLOW(A) = The set of all terminals that may appear after A in the derivation.

$$S - *-> aaXdd$$

$$S - *-> Xa$$

$$S - *-> BXc$$

Then

$$FOLLOW(X) = \{d,a,c\}$$

### Rules To Compute FIRST() and FOLLOW() Sets

- 1.  $FIRST() = \{ \}.$
- 2.  $FIRST(a) = \{ a \}.$
- 3.  $FIRST(a) = \{ \}.$
- 4. FIRST(XY) = FIRST(FIRST(X).FIRST(Y)) **OR** FIRST(X.FIRST(Y)) **OR** FIRST(FIRST(X).Y).
- 5. Given the production  $A \rightarrow X$ , Then:
  - a. FIRST() FOLLOW(X) if
  - b. FOLLOW(A) FOLLOW(X) if = .

Note that the FIRST() and FOLLOW() sets are made of terminals only

By these rules, say we have

$$A -> XB, XVN$$

and say we want FOLLOW(X)

Then

We say it is a subset because we can have other productions involving X.

Assuming that B =, Things are different.

Say that we have a production that leads to this derivation is

and following through this results in this derivation:

Therefore,

This is because whatever follows A can follow X if there is nothing between them.

Notes:

- 1. **may** appear in FIRST() but it doesn't appear in FOLLOW(). We will see this when we define augmented grammars.
- 2. Generally, we start computing the FIRST() from bottom to top, But follow from top to bottom.
- 3. When we compute FOLLOW(X), we search for X in the right side of any production.

# **Augmented Grammars**

Given the grammar G=(VN,VT,S,P), then the augmented grammar G'=(VN',VT',S',P') can be obtained from G as follows:

- 1.  $VN' = VN \{S'\}.$
- 2.  $VT' = VT \{ \$ \}$ .
- 3. S' = new starting point.
- 4. P= P ∪  $\{S\setminus ->S\}$

For example:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

Becomes:

$$G \rightarrow E$$
\$

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F -> (E) | a$$

This is because we want to create a FOLLOW() set for S.

Lets take another example:

$$S^{*} -> S \$$$

$$S -> AB$$

$$A -> a \mid$$

$$B -> b \mid$$
Lets compute the FIRST() sets for this grammar :
$$FIRST(A) = \{a, \}$$

$$FIRST(B) = \{b, \}$$

$$FIRST(S) = FIRST(AB) = FIRST(FIRST(A).FIRST(B))$$

$$= FIRST(\{a, \}, \{b, \})$$

$$= \{a,b, \}$$

$$FIRST(S^{*}) = FIRST(S) = FIRST(FIRST(S).FIRST())$$

$$= FIRST(\{a,b, \}.) = FIRST(a,b,)$$

$$= \{a,b,\$\}$$
Now Lets compute the FOLLOW() sets for this grammar :
$$FOLLOW(S) = \{\$\}$$

$$FOLLOW(A) = \{b,\$\}$$

$$FOLLOW(B) = \{\$\}$$

$$FOLLOW(B) = \{\$\}$$

$$Lets Take another, slightly more complex example :
$$S^{*} -> S \$$$

$$S -> Abc$$

$$A -> b \mid c \mid$$
Lets take the FIRST() for this grammar :
$$FIRST(A) = \{b,c, \}$$

$$FIRST(S) = FIRST(aAcb) FIRST(Abc) = \{a, \} \& cup \{b,c\}$$

$$= \{a,b,c\}$$$$

FIRST(S') = FIRST(S) = FIRST(FIRST(S).FIRST())

 $= FIRST({a,b,c}.{\$})$ 

 $= \{a,b,c\}$ 

```
Now lets take the FOLLOW():
```

$$FOLLOW(S) = \{\$\}$$
$$FOLLOW(A = \{c,b\}$$

Say we have the grammar

$$G \rightarrow E$$
\$
 $E \rightarrow E + T \mid T$ 
 $T \rightarrow T * F \mid F$ 
 $F \rightarrow (E) \mid a$ 

Lets calculate FIRST():

$$\begin{split} & FIRST(F) = \{(,a\} \\ & FIRST(T) = FIRST(T*F) \ FIRST(F) = FIRST(T*F) \ \{(,a\} \\ & = \{(,a\} \ (Because \ every \ T \ will \ eventually \ become \ an \ F) \\ & FIRST(E) = FIRST(E+T) \quad FIRST(T) = \{(,a\} \quad \{(,a\} \\ & = \{(,a\} \ FIRST(G) = FIRST(E\$) = \{(,a\} \ \end{cases} \end{split}$$

Now lets Calculate FOLLOW():

$$\begin{split} & FOLLOW(E) = \{\$,+,)\} \\ & FOLLOW(T) = FOLLOW(E) \quad \{*\} = \{\$,+,*,)\} \\ & FOLLOW(F) = FOLLOW(T) = \{\$,+,*,)\} \end{split}$$

But what makes all this so important?

Well, All of the parsing techniques we are going to learn will heavily rely on FIRST() and FOLLOW().

Top-Down Parsing(continued)

#### Recursive Descent Parsing

Recursive Descent Parsing is very simple. It works like this:

- 1. Divide the grammar into primitive/simple components
  - 1. For the token "a" :

```
If(token == "a"){\{}
      get-next()
  else{}
  report-error()
2. For X = 1, 2, ..., n:
       code(X):{}
       code(1);
       code{2}; ...
       code(n); }
   Then
       If(token FIRST(1))
       code(1)
       else If(token FIRST(2))
       \operatorname{code}(\ 2)\ \dots
       ... If(token FIRST(n))
       code(n)
       else{
       report-error(); }
   So we say, the code for x = *, we say
       while(token FIRST(*)){
       call(&alpha*);
       /}
```

# Notes:

- 1. Every nonterminal has a code(a function).
- 2. S' in augmented grammar is represented by the function "main".
- 3. We only start with calling "get-token" in function "main".

For Example, lets say we have

```
G \rightarrow E\$
E \rightarrow T( + T)^*
T \rightarrow F( * F)^*
F \rightarrow (E) | a
```

Then we can say:

```
main(){//represents G
 get-token;
 call E();
 if(token!="$")
   Error;
 }
 else{
    SUCCESS;
 }
}
 function E(){//Represents E -- T (+ T)*}
    call T();
    while(token == "+"){
        get-token();
        call T()
   }
 }
 function T(){//T--> F (* F)*}
    call F();
    while(token == "*"){
        get-token();
        call F();
    }
 }
 function F(){
    if(token == "(")
```

```
{
       get-token();
       call E();
       if(token == ")")
       {
           get-token();
       else
       {
           ERROR;
       }
   }
   else if(token=="a")
       get-token();
   else
   {
       ERROR;
   }
}
```

Note that ERROR is a function we should write.

Lets take another example now.

```
Given the grammar:
```

```
Program \rightarrow body .
body \rightarrow Begin stmt (; stmt)* End
stmt \rightarrow Read | Write | body |
```

where we will represent  $\,$  as 1 from now on in the example;

and

```
\begin{split} & \text{VN} = \{ \text{ Program, body, stmt, block} \} \\ & \text{VT} = \{ \text{ ., Begin, ;, End, Read, Write} \} \end{split}
```

examples of programs of this language would be

Begin Read;

```
Write;
    Read;
    Write;
End.
or
Begin
    Read;
End.
or
Begin
    Read;
    Begin
        Read;
        Write;
    End.
    Write;
End.
or
Begin;
End.
Lets write the code for this programming language.
main(){
    get-token();
    call body();
    if(token != "."){
        ERROR;
    }
    else{
        SUCCESS;
    }
}
```

```
function body(){
    call Begin();
    if(token == "Begin"){
        get-token();
        call stmt();
        while(token ==";"){
            get-token();
            call stmt();
        }
        if(token == "End"){
            get-token();
        else{
            ERROR;
        }
    }
    else{
        ERROR;
    }
}
function stmt(){
    if(token == "Read"){
        get-token();
    else if(token == "Write"){
        get-token();
    }
    else if(token == "Begin"){
        call body();
    }
    else if(token != ";" || token != "End" ){
        ERROR();
    }
}
```

# LL(1) Parsing

This Parsing method is a table-driven parsing method. The LL(1) parsing table selects which production to choose for the next derivation step.

But how do we build the LL(1) parsing table?

# LL(1) Parsing Table Building Algorithm

- 1. For each production  $A \rightarrow$  in the grammar G,
- 2. Add to the table entry T[A,a] the production  $A \rightarrow$ , where  $A \rightarrow FIRST()$
- 3. If FIRST( ), Add to the table entry T[A,b] the production A  $-\!\!>$   $-\!\!>$  b FOLLOW(A).
- 4. All Remaining Entries are Error Entries.

The table looks like

VN/VT	test
A	

For example, given the grammar :

$$V \rightarrow SR \$1$$

$$S -> +2 \mid -3 \mid 4$$

$$R \rightarrow dN.N5 \mid .dN6$$

$$N \rightarrow dN7 = 8$$

note that the superscript denotes the production number.

Then the table will look like this

$$FIRST(SR \$) = \{+,-,d,.\}$$

$$FIRST(+) = \{+\}$$

$$FOLLOW(S) = \{d,.\}$$

$$FIRST(R) = \{., \$\}$$

$$FIRST(d) = \{ - \}$$

$$FOLLOW(N) = \{., \$\}$$

$\overline{\mathrm{VN/VT}}$	+	-	d		\$
V	1	1	1	1	
S	2	3	4	4	
R			5	5	
N			7	8	8

There should be no conflict(multiple entries) in the LL(1) table.

L(G) of this grammar = all floating point numbers.

The parser works like this

Stack	Remaining Input	Action
$\overline{V}$	-dd.d\$	Production 1
SR\$	-dd.d\$	Production 3
-R\$	-dd.d\$	Pop & advance input
$\mathbb{R}$ \$	dd.d\$	Production 5
dN.N\$	dd.d\$	Pop & advance input
N.N\$	d.d\$	Production 7
dN.N\$	d.d\$	Pop & advance input
N.N\$	d	Production 8
.N\$	d	Pop & advance input
N\$	d\$	Production 7
dN\$	d\$	Pop & advance
N\$	\$	Production 8
\$	\$	Pop and Advance
		Accept

If at any point the parser reaches a place where the input and the stack have 2 different terminal symbols, it throws a syntax error.

Lets Take another example. Let the Grammar be :

```
program -> block $1
```

block -> { declarations stmnts } 2

decls  $\rightarrow$  D ; decls 3 | 4

 $stmnts \rightarrow statement \ ; \ stmts \ 5 \ | \ \ 6$ 

statement –> if 7 | while 8 | ass 9 | scan 10 | print<br/>11 | block 12 | 13

 $VT = \{\$, \{,\}, D, ;; if, while, ass, scan, print\}$ 

VN/VT	if	while	ass	scan	print	{	}	D	;	\$
Program						1				
block decls	4	4	4	4	4	2 4	4	3	4	
stmts statement	5 7	5 8	5 9	5 10	5 11	$\frac{5}{2}$	6		5 13	

No conflict.