



Alexandria University
— Faculty of Engineering —

Assignment NO. 3

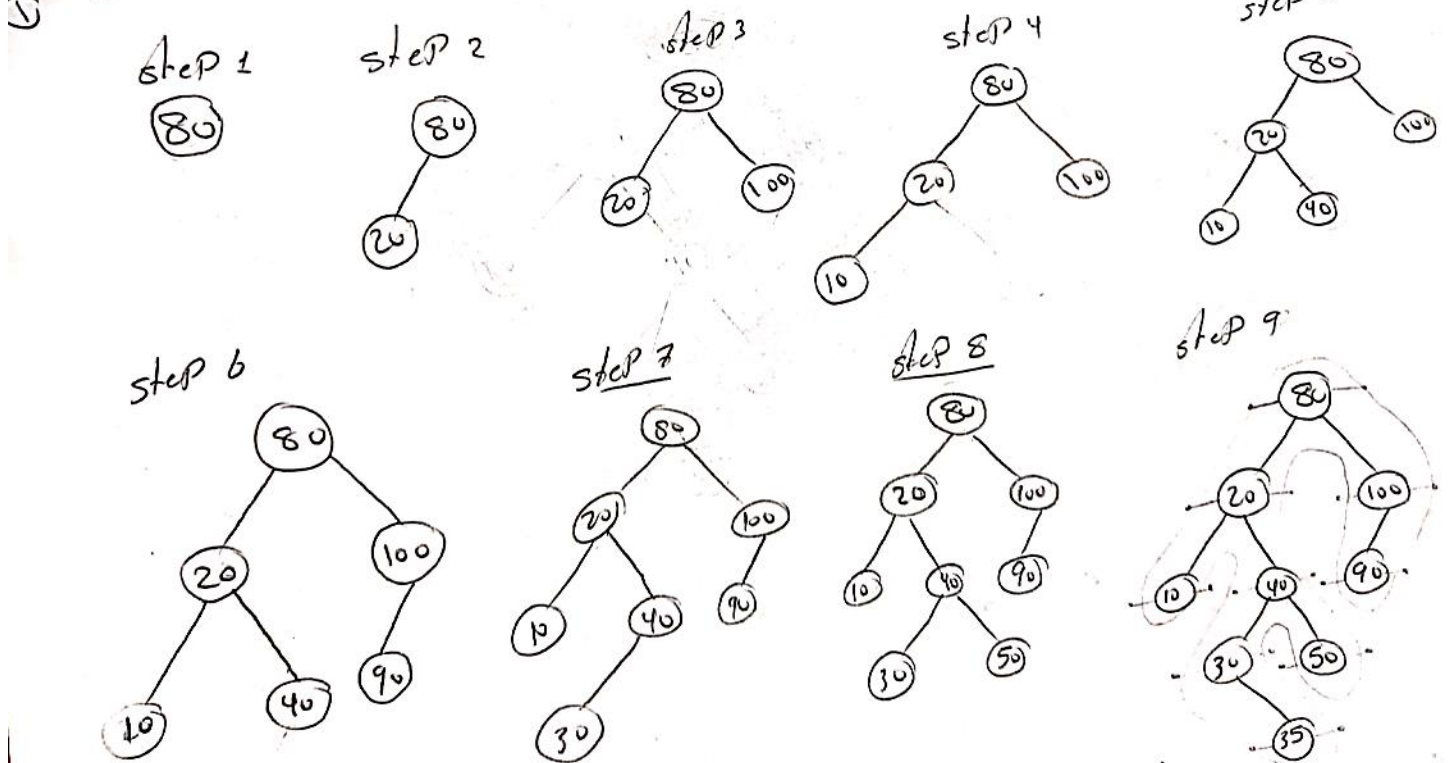
By:

Ali Mohamed Taima Hummus

Question 1

a)

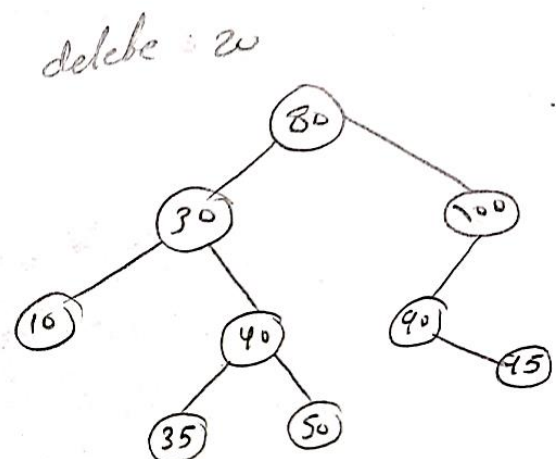
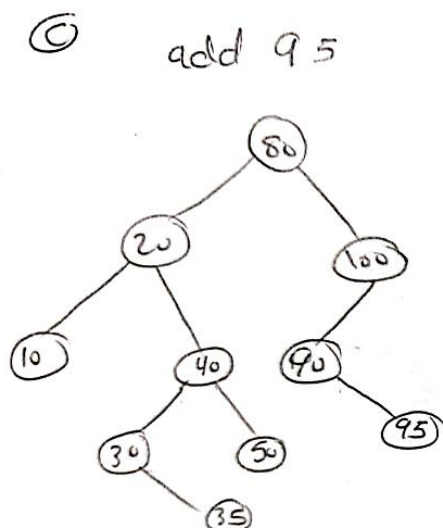
Q111



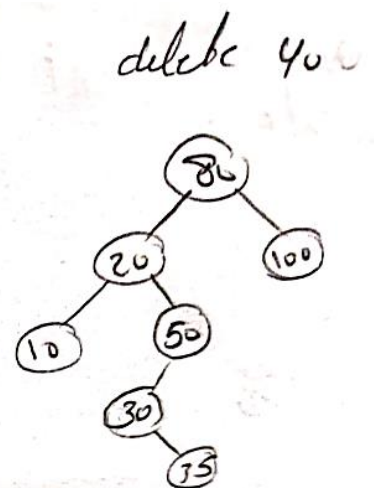
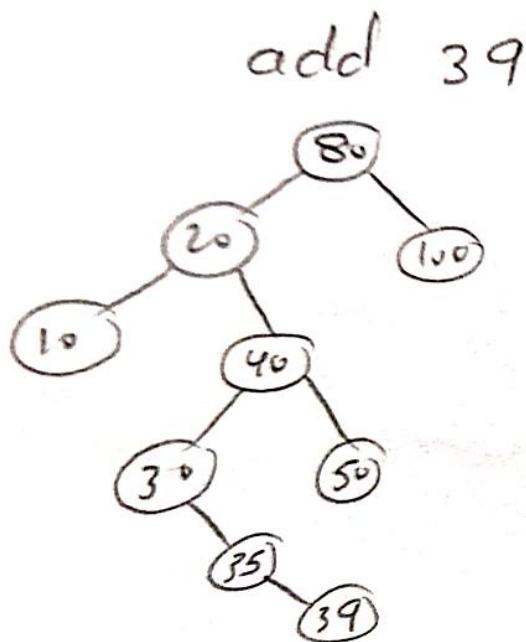
b)

- Pre-order:
 - Visit the root.
 - Visit the left subtree, using preorder.
 - Visit the right subtree, using preorder.
 - (80, 20, 10, 40, 30, 35, 50, 100, 80)
- Postorder:
 - Visit the left subtree, using postorder.
 - Visit the right subtree, using postorder.
 - Visit the root.
 - (10, 35, 30, 50, 40, 20, 90, 100, 80)

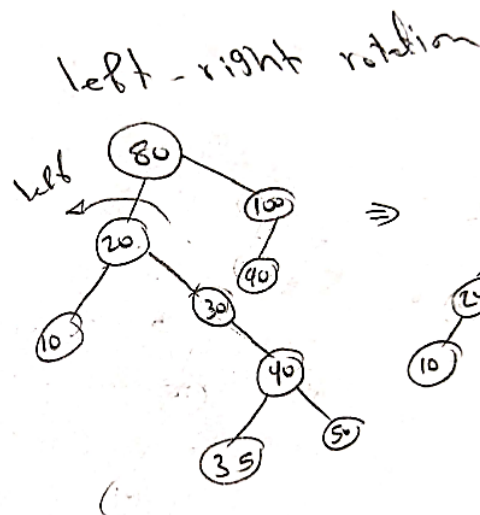
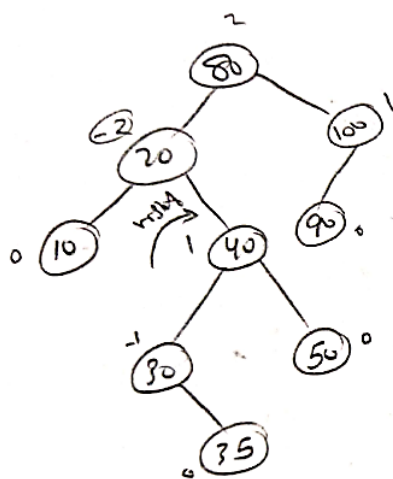
c)



d)



e)



Question 2

a) Preorder: (4, 3, 2, 1, 8, 6, 5, 7, 9)

b) Inorder: (1, 2, 3, 4, 5, 6, 7, 8, 9)

c) Postorder: (1, 2, 3, 5, 7, 6, 9, 8, 4)

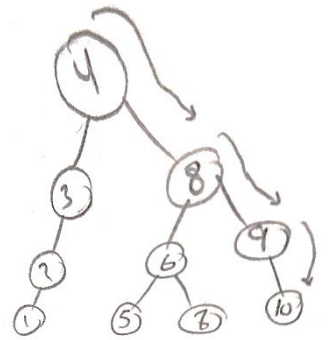
d)

1- check binary tree: **The tree is binary tree** as each node has at most 2 children

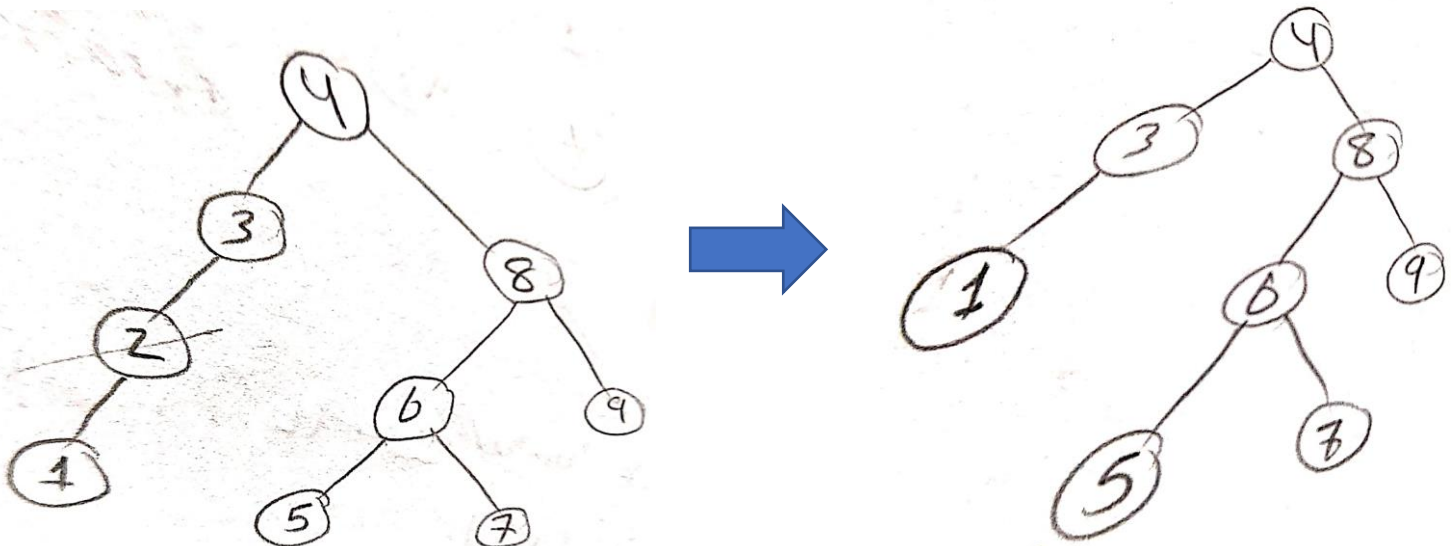
2- check BST: **The tree is BST** as all nodes of left subtree are less than the root(or parent) and all nodes of right subtree are greater than the root(or parent)

3- check AVL: **The tree is not an AVL tree**, as the **balance factor of node 3 is 2** and the condition of AVL tree that balance factor **must be (-1, 0, 1)** that means not greater than 1 or less than -1

e) 10 is less than 4, so negate to right subtree until 8, find that 10 is greater than 8, so navigate to right subtree until 9, again we find 10 is greater than 9, so navigate to right and there is no more nodes, so put 10 in the right of 9

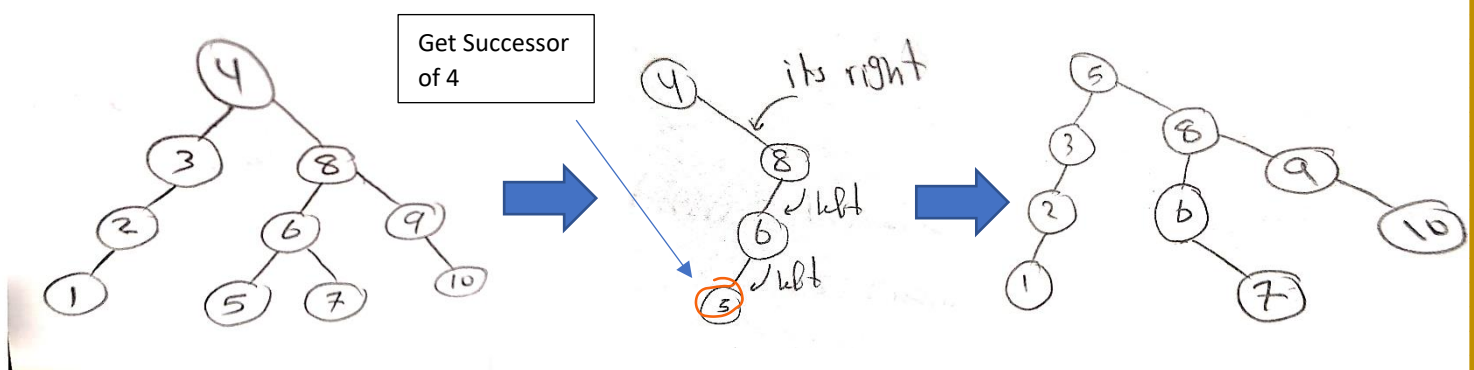


f) We want to delete 2, so we should search for its successor, but 2 doesn't have right subtree so doesn't have successor, so we will delete 2 and place the nodes smaller than it in its place, so we put 1 and delete 2

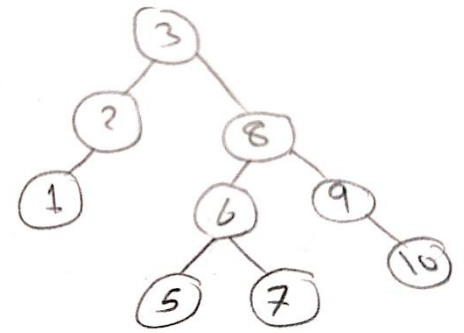


g) There are two methods to delete 4

1- To delete 4 we should put its successor in its position and delete the successor from its original position, in our tree the successor of 4 is 5, so we delete 4 and put 5 instead of it and delete 5 from down



2- To delete 4 we put the node tha less than the node that we want to delete in our tree the node is 3, so we delete 4 and put 3 instead of it and its subtrees



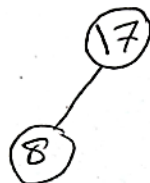
Question 3

a)

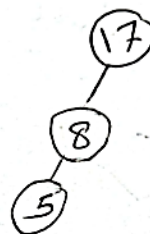
insert (17)



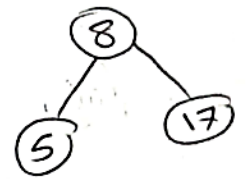
insert (8)



insert (5)

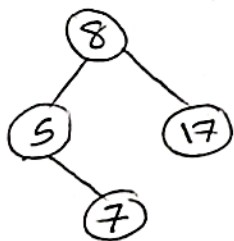


R.R

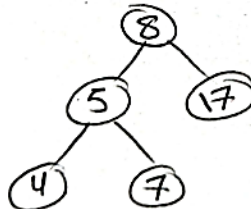


unbalance, make right rotation

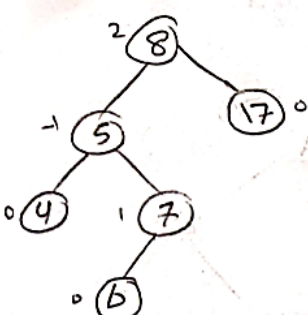
insert (7)



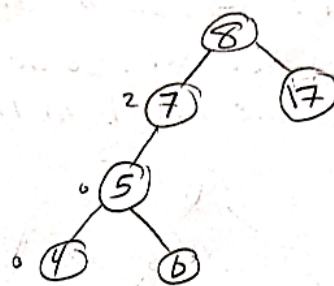
insert (4)



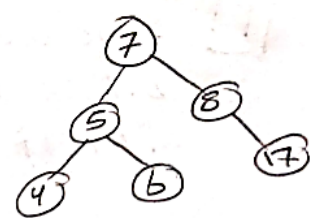
insert (6)



Left rotation 5



right rotation 7

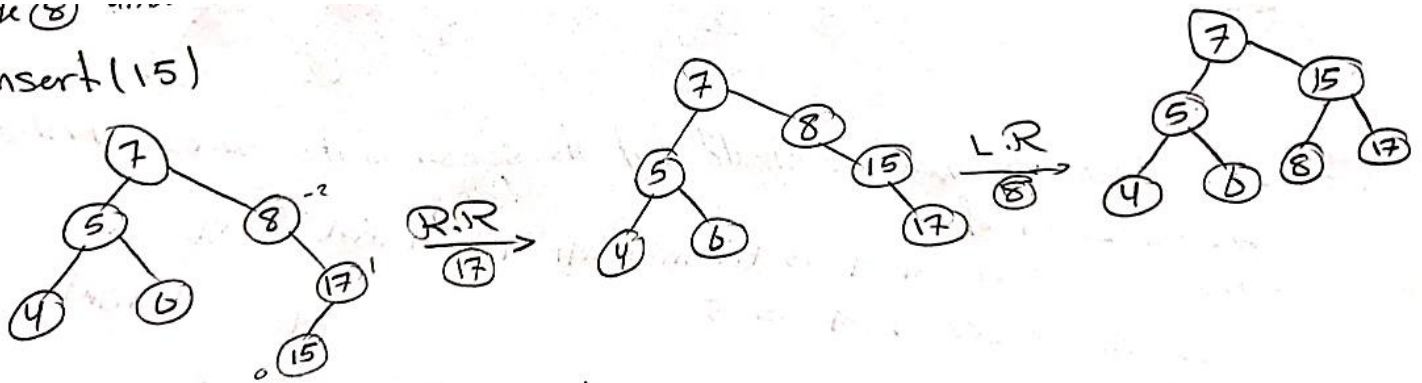


node 8 unbalanced (left right unbalance)

17

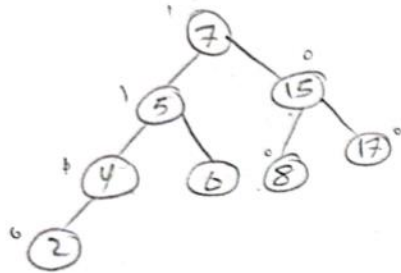
Node (8)

*insert (15)

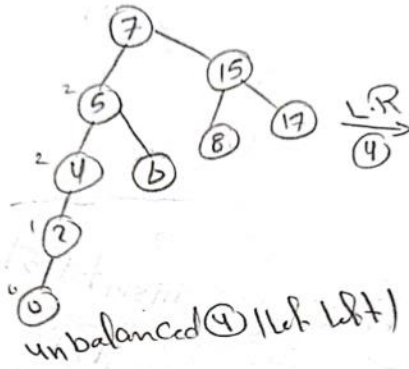


unbalanced (8) (right left unbalance)

*insert (12)

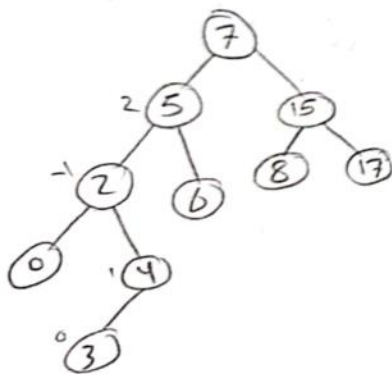


*insert (10)

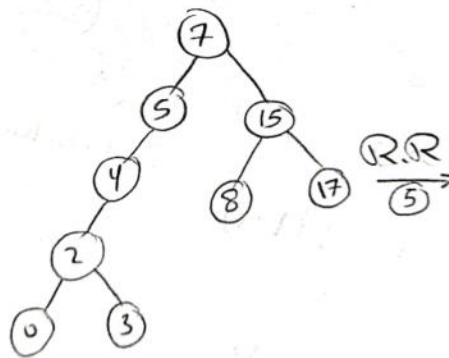


unbalanced (4) (left left)

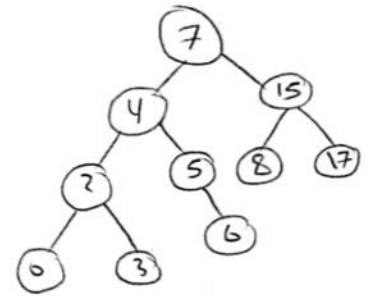
*insert (13)



R.L
2



R.R
5

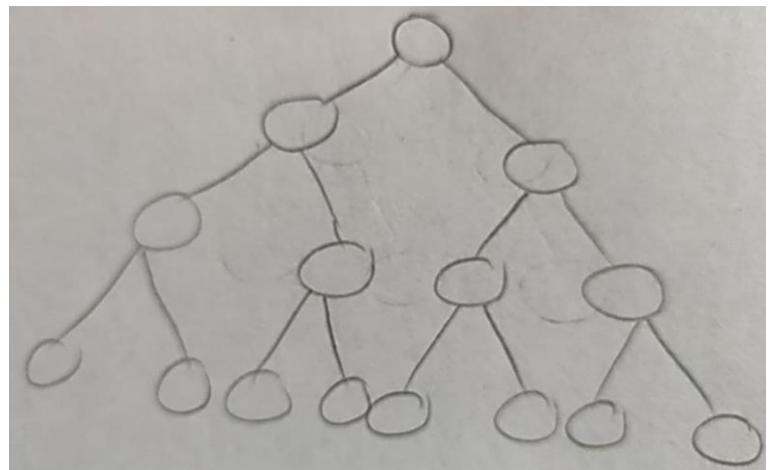


unbalanced (left right) (5)

b)

1- If height of AVL tree is h , maximum number of nodes can't exceed $2^{h+1} - 1$

- As we show in the picture the height is 3 and the number of nodes is 15 and we can't add any other nodes and have the same height (3)



2- Minimum number of nodes in a tree with height h can be represented as:

$N(h) = N(h-1) + N(h-2) + 1$ for $n > 2$ where $N(0) = 1$ and $N(1) = 2$.

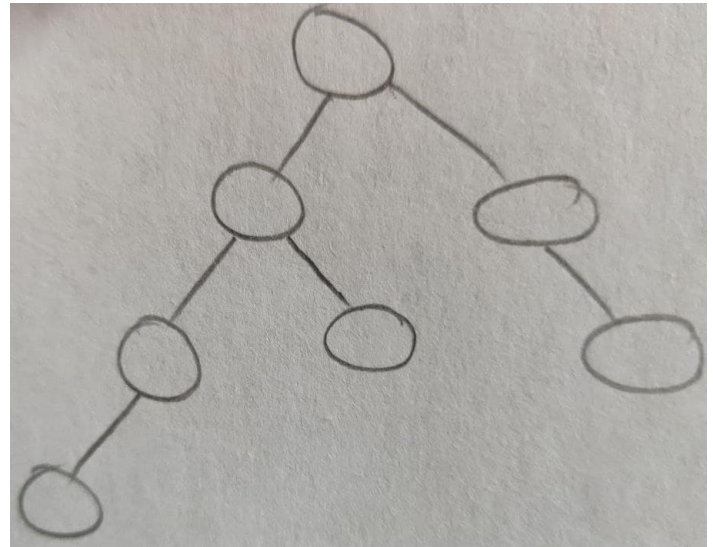
- The difference between height of left sub-tree and right sub-tree of any node can't be more than 1. This property gives balance factor which whose value should be from $(-1, 0, 1)$ in case of AVL tree
- In this example I suppose that height is 3 and I want to know the minimum nodes

- $N(3) = N(2) + N(1) + 1$

- $N(2) = N(1) + N(0) + 1 = 2 + 1 + 1 = 4$

- $N(3) = 4 + 2 + 1 = 7$

- so we can't delete any node because if we delete the balance factor will be more than 1 or less than -1



c)

1- If there are n nodes in AVL tree, minimum height of AVL tree is $\text{Floor}(\log_2(n+1) - 1)$

- Suppose we have 8 nodes $\text{Floor}(\log_2(7+1) - 1) = 2$
- For 2 nodes $\text{Floor}(\log_2(2+1) - 1) = 1$
- For 15 nodes $\text{Floor}(\log_2(15+1) - 1) = 3$
- For 16 nodes $\text{Floor}(\log_2(16+1) - 1) = 4$

2- If there are n nodes in AVL tree, maximum height can't exceed $1.44 \cdot \log_2 n$

- We can get Maximum height of tree is we put the minimum number of nodes in the tree
 - So if I want to calculate the height for 2 nodes the result will be $1.44 \cdot \log_2 2 = 1$
-

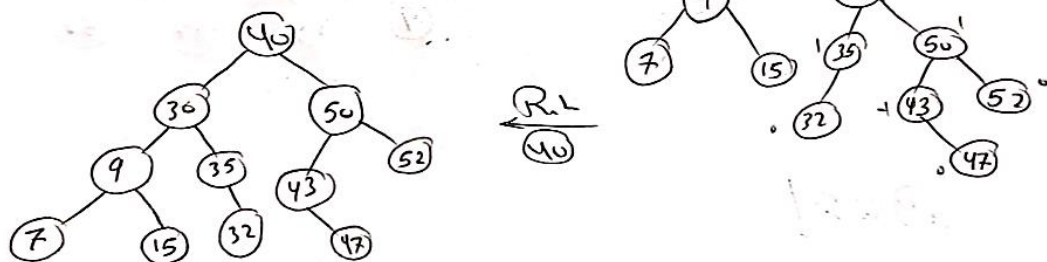
Question 4

Q14)

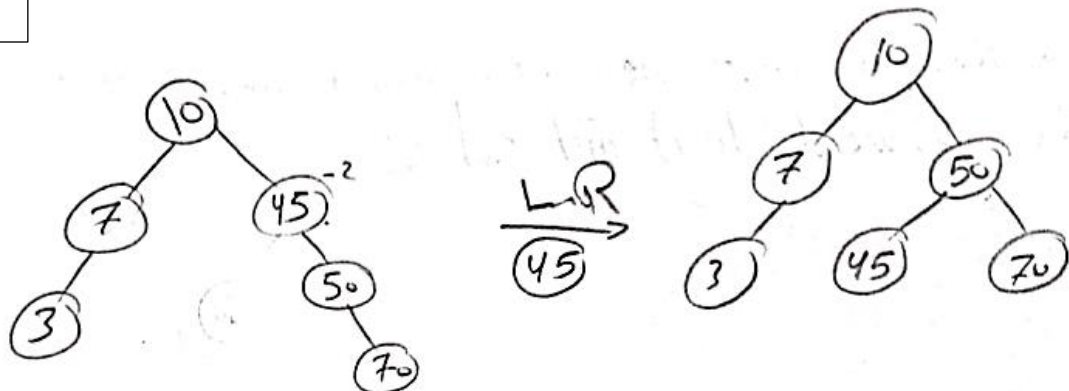
a



unbalanced (left right)

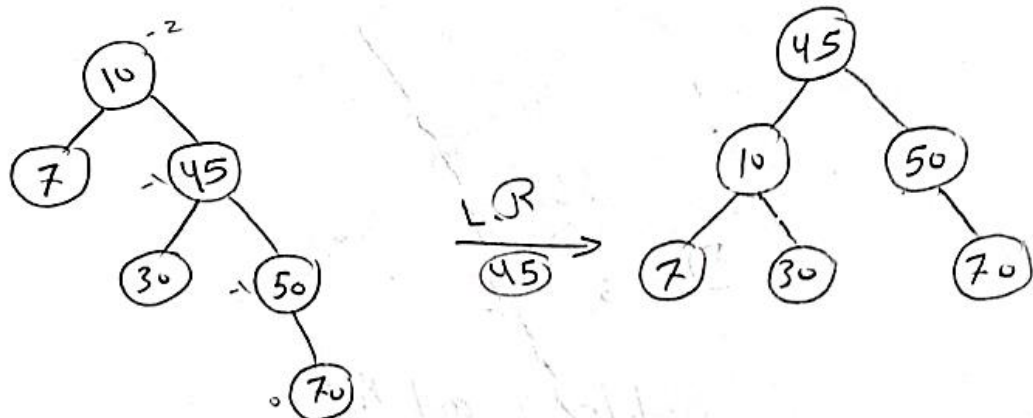


b



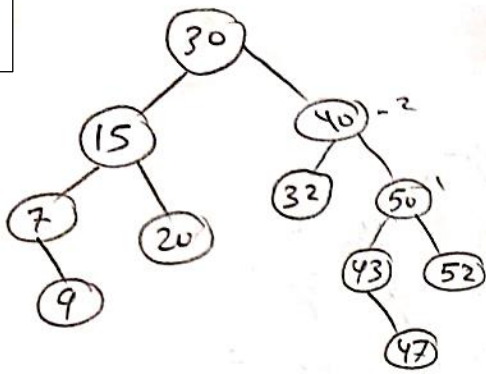
unbalanced (right-right)

c

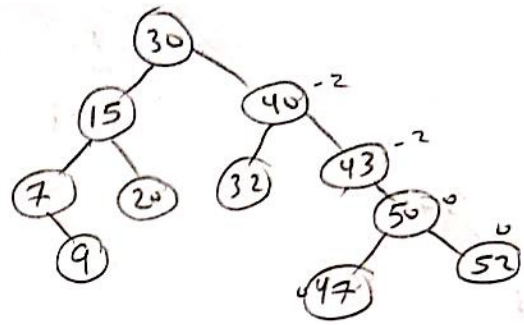


unbalanced (right-right)

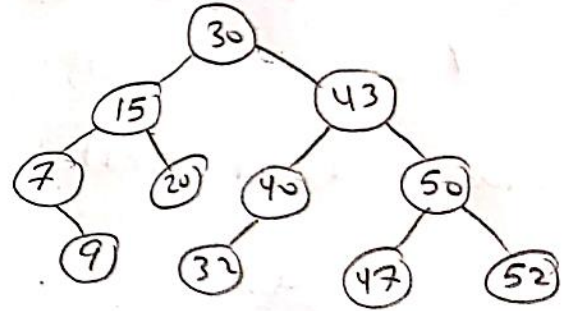
d



R.R
50



40 / R.L



unbalanced (right-left)