



Alexandria University
— Faculty of Engineering —

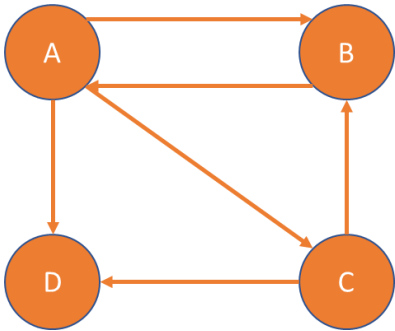
Assignment NO. 6

By:

Ali Mohamed Taima Hummus

Question1:

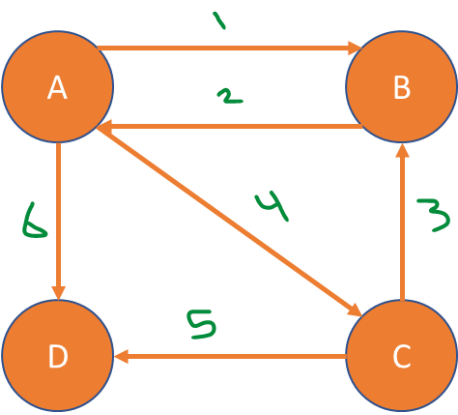
a)



b)

| | A | B | C | D |
|---|---|---|---|---|
| A | 0 | 1 | 1 | 1 |
| B | 1 | 0 | 0 | 0 |
| C | 0 | 1 | 0 | 1 |
| D | 0 | 0 | 0 | 0 |

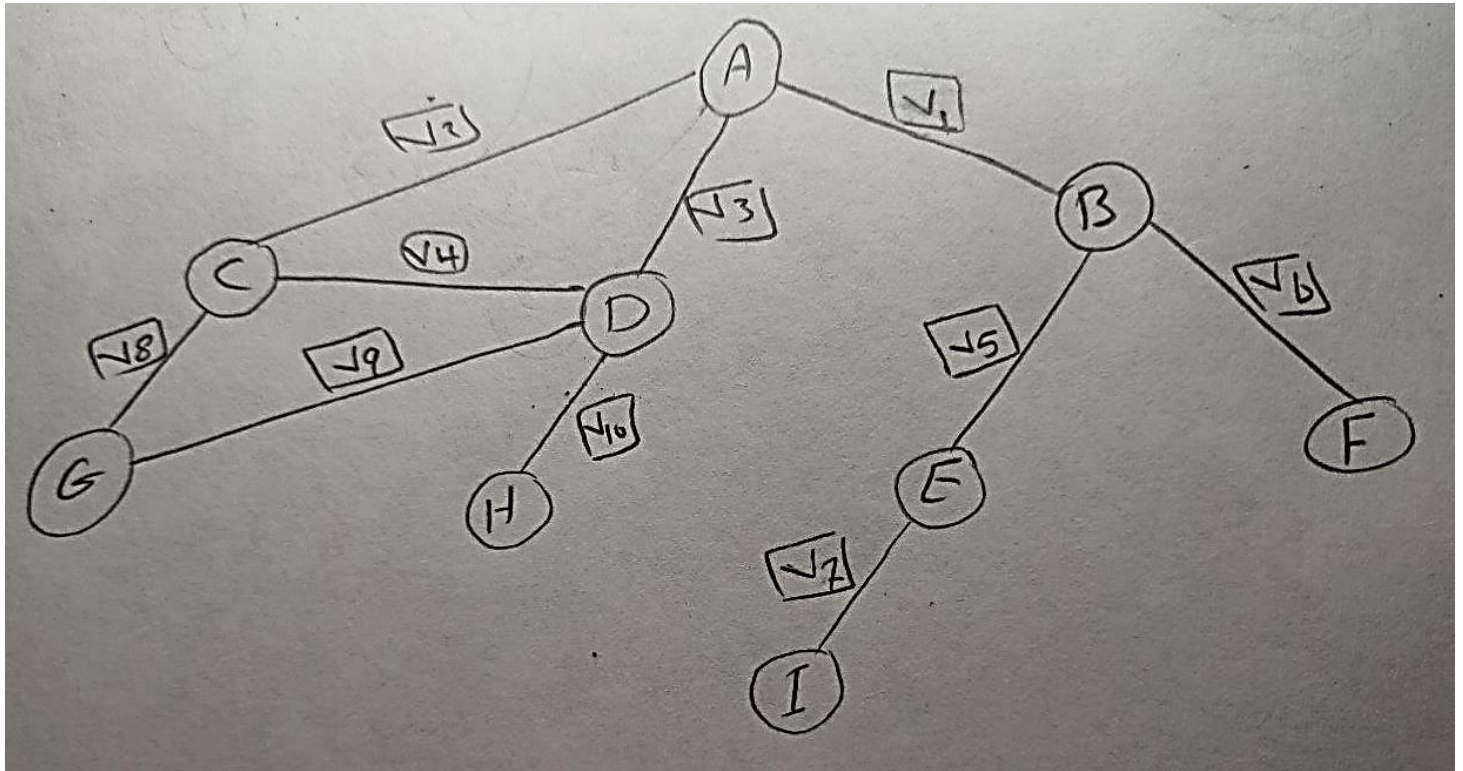
c)



| source | destination | edge |
|--------|-------------|------|
| A | B | 1 |
| A | C | 4 |
| A | D | 6 |
| B | A | 2 |
| C | B | 3 |
| C | D | 5 |

Question2:

a)



b)

| | A | B | C | D | E | F | G | H | I |
|---|---|---|---|---|---|---|---|---|---|
| A | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| C | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 |
| D | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |
| E | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| F | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| G | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| H | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| I | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |

c)

| | A | B | C | D | E | F | G | H | I |
|---|---|---|---|---|---|---|---|---|---|
| A | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| C | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 |
| D | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |
| E | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| F | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| G | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| H | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| I | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |

YES, because it undirected graph and the edge is for

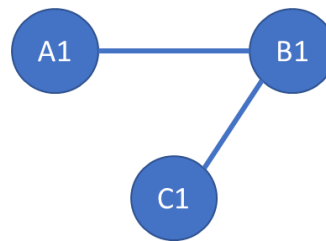
d)

It will be the number out-edges of vertex

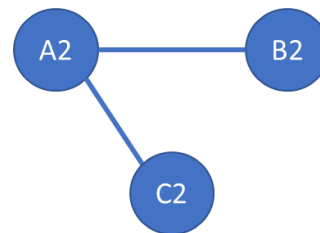
Question3:

a)

| | A1 | B1 | C1 |
|----|----|----|----|
| A1 | 0 | 0 | 1 |
| B1 | 0 | 0 | 1 |
| C1 | 1 | 1 | 0 |



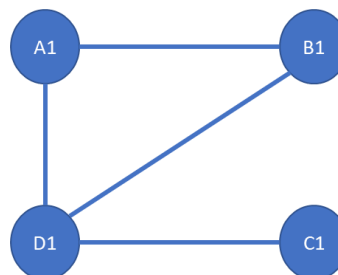
| | A2 | B2 | C2 |
|----|----|----|----|
| A2 | 0 | 1 | 1 |
| B2 | 1 | 0 | 0 |
| C2 | 1 | 0 | 0 |



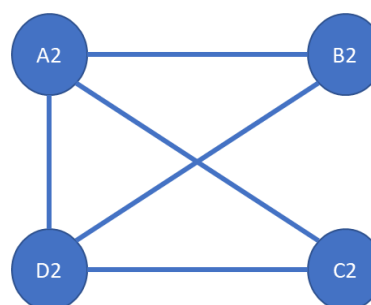
- The two graphs are isomorphism
 - Because the Isomorphism f from first to second graph is: $f(B1) = A2$, $f(A1) = B2$, $f(C1) = C2$

b)

| | A1 | B1 | C1 | D1 |
|----|----|----|----|----|
| A1 | 0 | 1 | 0 | 1 |
| B1 | 1 | 0 | 0 | 1 |
| C1 | 0 | 0 | 0 | 1 |
| D1 | 1 | 1 | 1 | 0 |



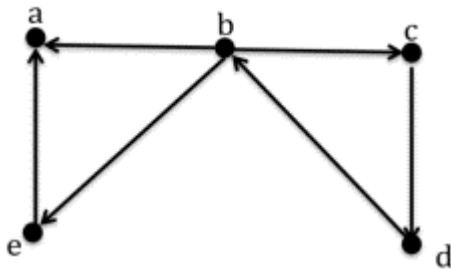
| | A2 | B2 | C2 | D2 |
|----|----|----|----|----|
| A2 | 0 | 1 | 1 | 1 |
| B2 | 1 | 0 | 0 | 1 |
| C2 | 1 | 0 | 0 | 1 |
| D2 | 1 | 1 | 1 | 0 |



- The two graphs are not isomorphism
 - Because the number of edges of the first graph are 4 but in second graph are 5

Question4:

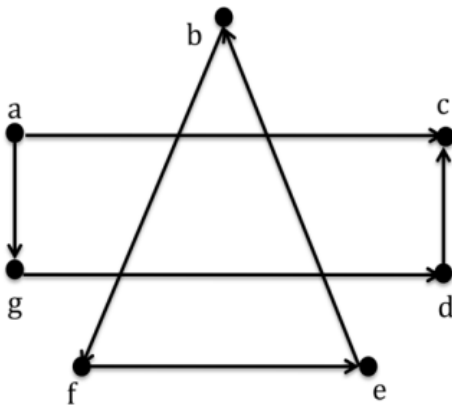
a)



This graph is **weakly** connected, because **there is a path from b to a** but there is **no path** from **a to b**, and **there is a path from b to e** but there is **no path** from **e to b**

We can call the **subgraph acd** is a **strongly** connected, because there are paths between all possible pairs of vertices

b)

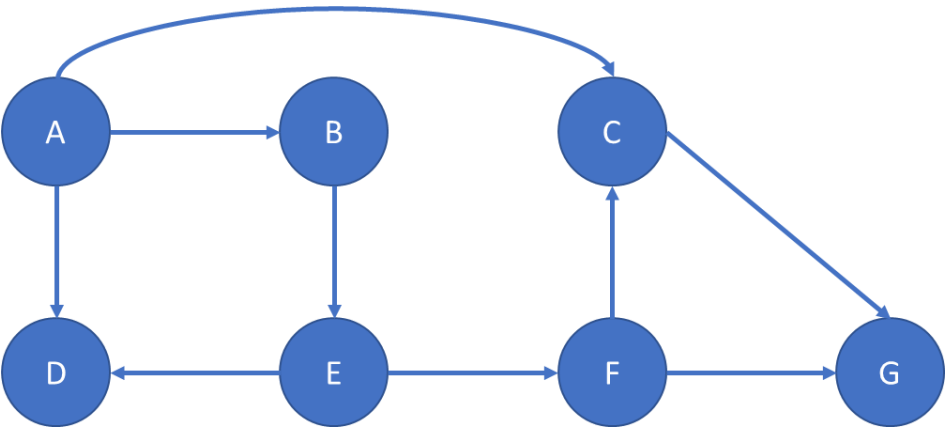


This graph is **NOT** connected

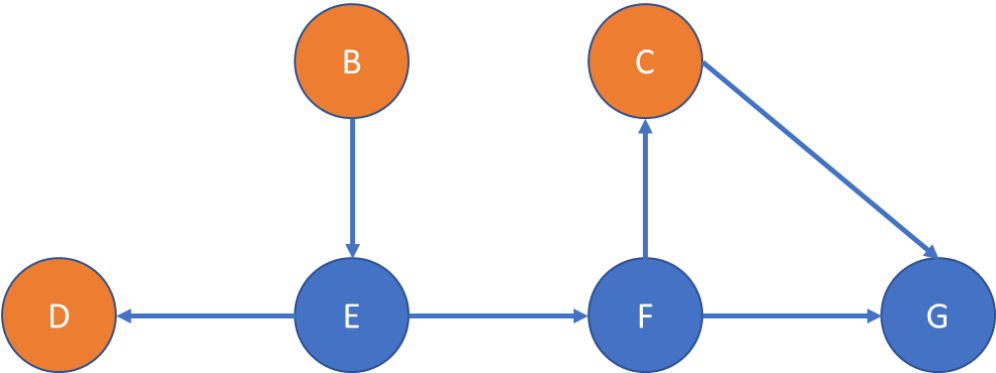
We can call **the subgraph acdg** is **weakly** connected, because **there is a path from a to c** but there is no path from **c to a**, path from **a to g** but no path from **g to a**, path from **d to c** but no path from **c to d** and so on

We can call the **subgraph afe** is a **strongly** connected, because there are paths between all possible pairs of vertices

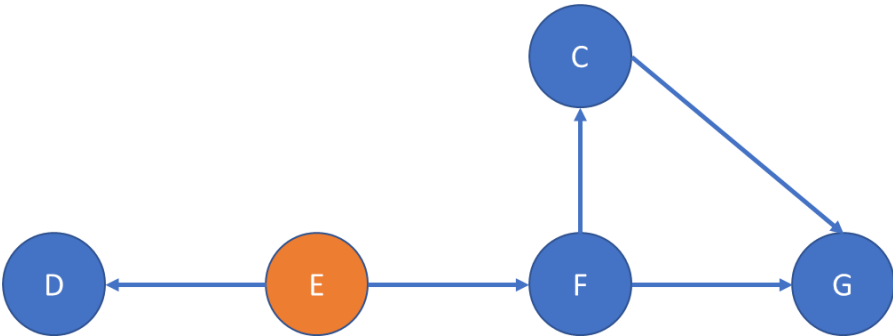
Question5:



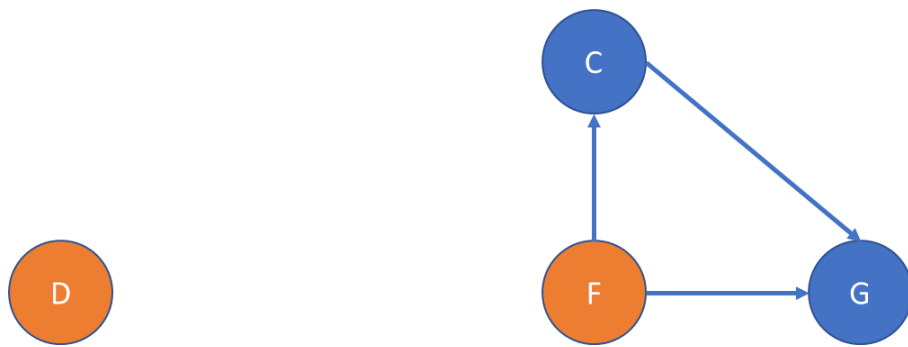
| Vertex | A | B | C | D | E | F | G | output |
|-----------|----|----|----|----|----|----|----|--------|
| Removed | NO | NO | NO | NO | NO | NO | NO | |
| In-degree | 0 | 1 | 2 | 2 | 1 | 1 | 2 | |



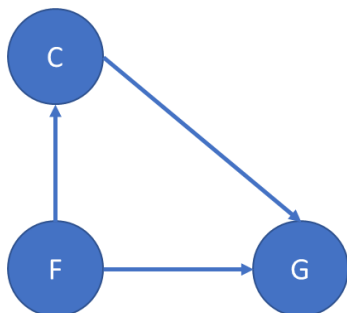
| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|----|----|----|----|----|----|----------|
| Removed | YES | NO | NO | NO | NO | NO | NO | A |
| In-degree | | 0 | 1 | 1 | 1 | 1 | 2 | |



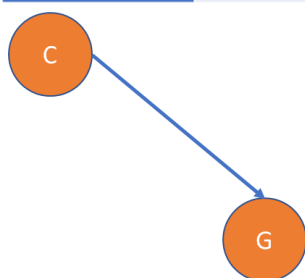
| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|----|----|----|----|----|-------------|
| Removed | YES | YES | NO | NO | NO | NO | NO | A, B |
| In-degree | | | 1 | 1 | 0 | 1 | 2 | |



| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|----|----|-----|----|----|---------|
| Removed | YES | YES | NO | NO | YES | NO | NO | A, B, E |
| In-degree | | | 1 | 0 | | 0 | 2 | |



| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|----|-----|-----|----|----|------------|
| Removed | YES | YES | NO | YES | YES | NO | NO | A, B, E, D |
| In-degree | | | 1 | | | 0 | 2 | |



| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|----|-----|-----|-----|----|---------------|
| Removed | YES | YES | NO | YES | YES | YES | NO | A, B, E, D, F |
| In-degree | | | 0 | | | | 1 | |



| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|-----|-----|-----|-----|----|------------------|
| Removed | YES | YES | YES | YES | YES | YES | NO | A, B, E, D, F, C |
| In-degree | | | | | | | 0 | |

| Vertex | A | B | C | D | E | F | G | output |
|-----------|-----|-----|-----|-----|-----|-----|-----|---------------------|
| Removed | YES | YES | YES | YES | YES | YES | YES | A, B, E, D, F, C, G |
| In-degree | | | | | | | | |

The final output is: A, B, E, D, F, C, G