

## Communication Systems (25751-4)

### Problem Set 04

Fall Semester 1402-03

Department of Electrical Engineering

Sharif University of Technology

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*Due on Aban 24, 1402 at 17:00*

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(\*) starred problems are optional and have a bonus mark!

## 1 DSB Modulation with Periodic Waveforms

A DSB signal is generated by multiplying the message signal  $m(t)$  with the periodic rectangular waveform shown in Figure 2 and filtering the product with a bandpass filter tuned to the reciprocal of the period  $T_p$ , with bandwidth  $2W$ , where  $W$  is the bandwidth of the message signal.

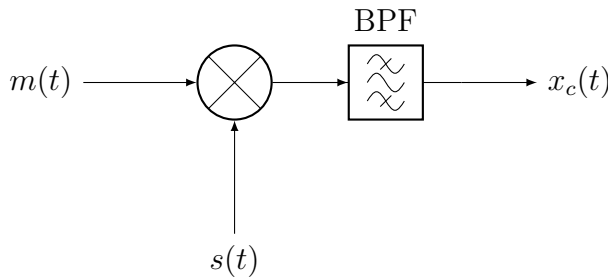


Figure 1: DSB Modulator

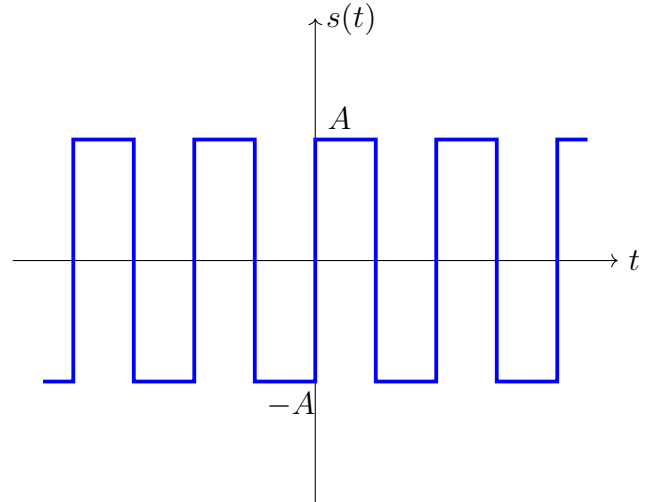


Figure 2:  $s(t)$

1. Demonstrate that the output  $x_c(t)$  of the BPF is the desired DSB signal

$$x_c(t) = A_c m(t) \sin(2\pi f_c t)$$

where  $f_c = \frac{1}{T_p}$ , and find  $A_c$ .

2. Show that it is not necessary that the periodic signal be rectangular. This means that any periodic signal with period  $T_p$  can substitute for the rectangular signal in Figure 2.

## 2 Weaver's SSB Modulator

Weaver's SSB modulator is illustrated in Figure 3. By taking the input signal as  $x(t) = \cos(2\pi f_m t)$ , where  $f_m < W$ , demonstrate that by proper choice of  $f_1$  and  $f_2$  the output is a SSB signal.

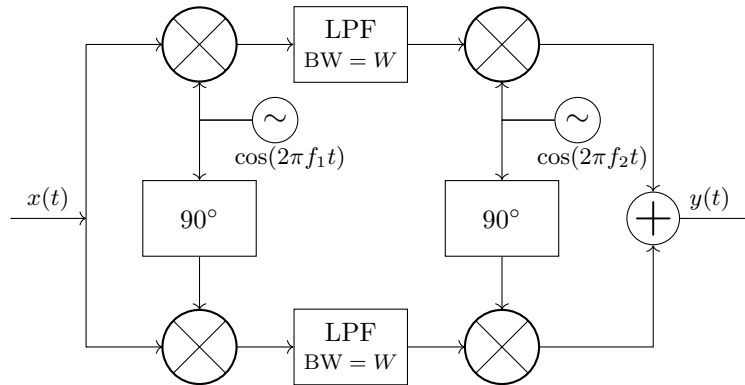


Figure 3: Weaver's SSB Modulator

## 3 SSB Signal

A USB signal is generated by using the phase shift method.

1. If the input to this system is  $\hat{m}(t)$  instead of  $m(t)$ , what will be the output?
2. Can this signal be demodulated (to get back  $m(t)$ )? If so, how?

## 4 VSB Signal

A VSB signal  $y(t)$  is as below.  $\alpha$  is a non negative constant less than one.

$$y(t) = \frac{\alpha}{2} \cos(2\pi(f_c + f_m)t) + \frac{1 - \alpha}{2} \cos(2\pi(f_c - f_m)t) + \cos(2\pi f_c t)$$

1. Prove that the envelop of the signal can be calculated as below.  $d(t)$  represents the distortion.

$$e(t) = \left[1 + \frac{1}{2} \cos(2\pi f_m t)\right] d(t)$$

$$d(t) = \sqrt{1 + \left[\frac{(1 - 2\alpha) \sin(2\pi f_m t)}{2 + \cos(2\pi f_m t)}\right]^2}$$

2. Find  $\alpha$  such that it maximize  $d(t)$ .

## 5 VSB Modulation System

A vestigial sideband modulation system is shown in figure 4. The bandwidth of the message signal  $m(t)$  is  $W$  and the transfer function of the bandpass filter is shown in the figure 5.

1. Determine  $h_{lp}(t)$ , the lowpass equivalent of  $h(t)$ , where  $h(t)$  represents the impulse response of the bandpass filter.
2. Derive an expression for the modulated signal  $x_c(t)$ .

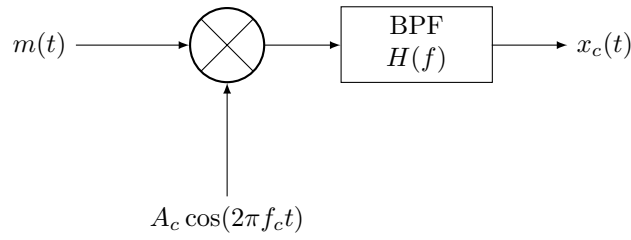


Figure 4: VSB Modulator

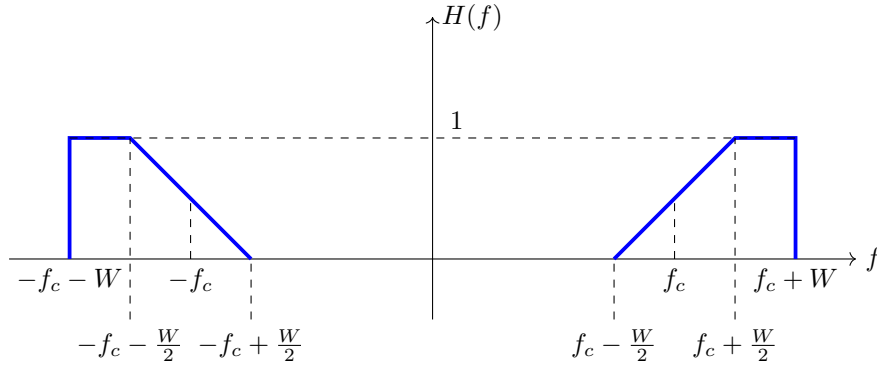


Figure 5:  $H(f)$

## 6 Practical VSB Systems

A vestigial filter  $H_i(f)$  in the transmitter of a VSB system has a transfer function as shown in figure 6. The carrier frequency is  $f_c = 10$  kHz, and the baseband signal bandwidth is 4 kHz. find the corresponding transfer function of the equalizer filter  $H_o(f)$  in the receiver.

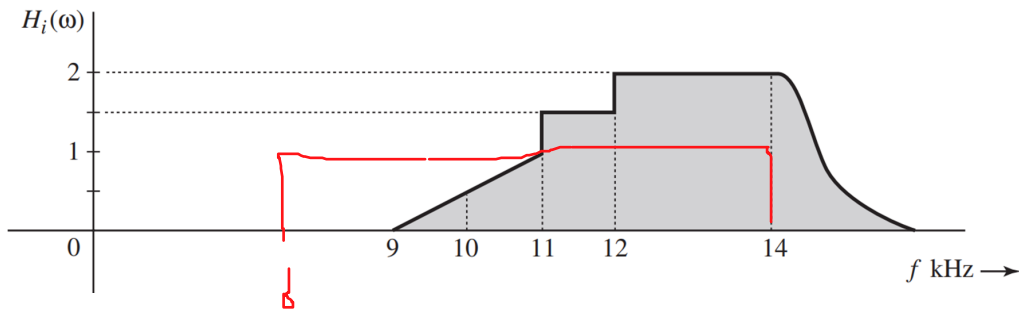


Figure 6: Frequency response of the transmitter filter

## 7 (\*) Modulation within Nonlinear Channels

Assume that the channel between a transmitter and a receiver has a non-linear characteristic as

$$y(t) = ax(t) + bx^2(t)$$

also we have just oscillator, adder, inverter and tunable band pass filter.(no mixer or multiplier).

1. design a system that can produce the DSB modulated signal at carrier frequency  $f_c$  in output.
2. now consider the channel has characteristic of the form

$$y(t) = ax(t) + bx^2(t) + cx^3(t)$$

again design a system that can produce the DSB modulated signal carrier frequency  $f_c$  in output.