

## Assignment 2

**Subject: Complex Variables and Transforms (BSI- 362 )**

**Maximum Marks=100**

**CLO 1/PLO 1 [Knowledge]**

1. **Determine** the set of points  $S$  where each function is continuous

$$f(z) = \frac{z-1}{z^7 + z^4 + z^3 + 1}$$

2. **Determine** where  $f(z) = \frac{1+z}{1-z}$  is non analytic.

3. **Find**  $\operatorname{Re} f$  and  $\operatorname{Im} f$ . Are following functions analytic? (Riemann Equations)

a)  $f(z) = (1+2i)z^5 - (-1-i)z^4 + 4iz + (-1+4i)$

b)  $w = \frac{1}{(z-a)^n}$ , (hint s.  $x-a = r \cos \theta$ ,  $y = r \sin \theta$ )

4. **Determine**  $a, b$ , and  $c$  such that given functions are harmonic and find a harmonic conjugate.

a)  $u = ax^3 + bxy$

b)  $u(x, y) = ax^3 + by^3$

c)  $u = \sin x \cosh cy$

5. **Find** all solutions

a)  $e^z = 1$ .

b)  $e^z = 4 + 3i$

**6.** Find the principal value of the given expression

**c)**  $(1+i)^{-1+i}$  .

**d)**  $(1+3i)^i$