



# Cellular Concept and Trunking

**Lecturer: Prof. Dr Noor M Khan**

*Department of Electronic Engineering,*

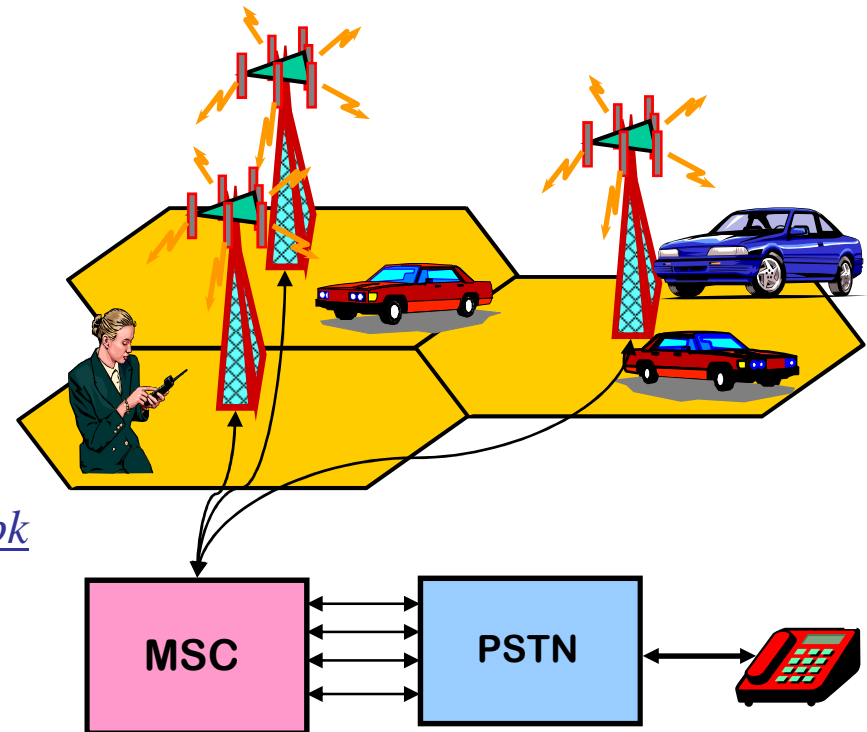
*Muhammad Ali Jinnah University,*

*Islamabad Campus, Islamabad, PAKISTAN*

*Ph: +92 (51) 111-878787*

*Ext. 129 (Office), Ext. 186 (ARWiC Lab)*

*email: [noor@ieee.org](mailto:noor@ieee.org), [noormkhan@jinnah.edu.pk](mailto:noormkhan@jinnah.edu.pk)*





# Cellular Concept

- Simple Solution
  - Single high powered transmitter on a tall tower
  - Good coverage but very low capacity
  - No frequency reuse
- High Capacity Solution
  - Cellular concept solves problem of low capacity
  - Replaces a single high power transmitter (large cell) with many low power transmitters (small cells)
  - Much smaller and more efficient mobile units



# Operation

- The Cellular Concept is a system level idea:
  - Each base station is allocated a portion of the total number of channels available to the entire system
  - Nearby base stations are assigned different groups of channels
  - All channels are assigned to a relatively small number of neighboring base stations
- The level of interference between base stations (and the mobile users) is controlled



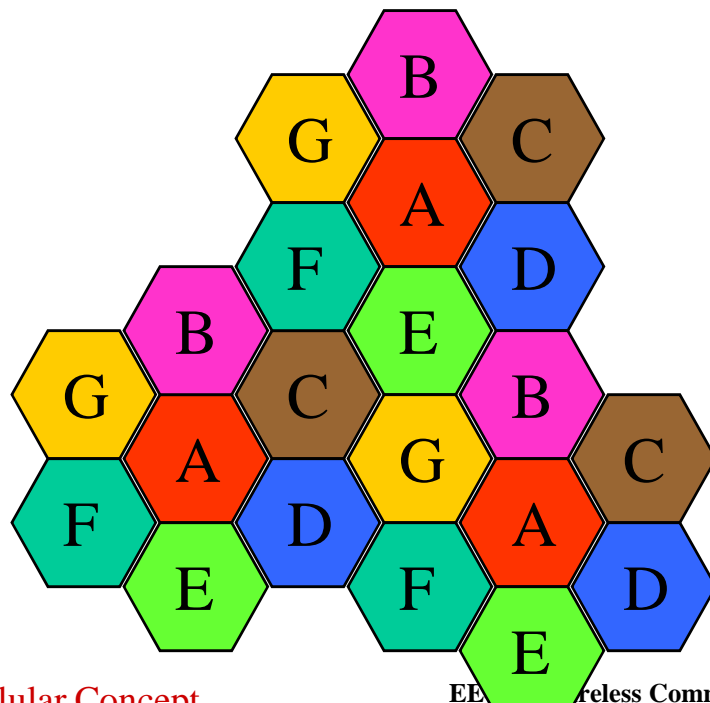
# Scalability

- Frequency can be re-used as many times as necessary as long as interference between co-channel stations can be kept within acceptable limits.
- As the demand increases, the number of base stations can be increased (with a corresponding decrease in transmitter power)
- This fundamental principal is the foundation of all modern wireless communication systems.



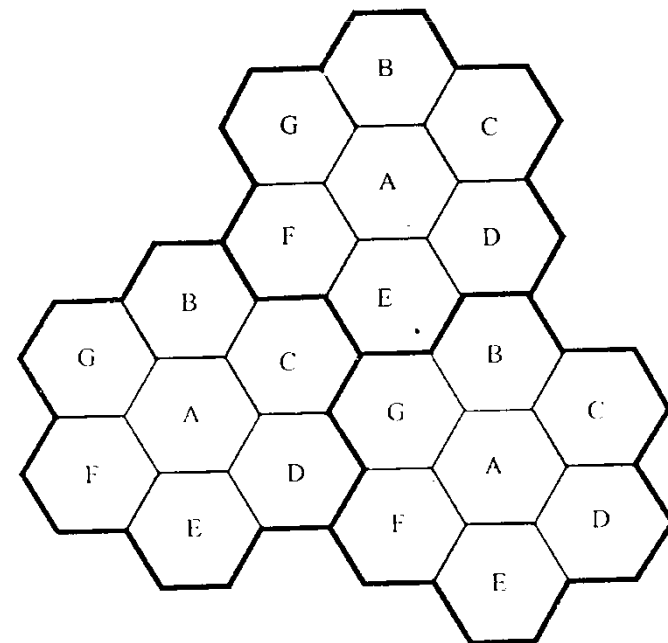
# Frequency Re-use

- The process of selecting and allocating channel groups for all base stations within a system is known as frequency re-use or frequency planning



Cellular Concept

EE, Wireless Communications  
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EE, MAJU

# Comments on Hexagonal Cells



- Hexagon geometry approximates omnidirectional base station with free space propagation
- When hexagons are used base stations can either be
  - in the center (center excited) - omnidirectional antennas or
  - on 3 of the six cell vertices (edge excited) - sectored directional antennas



# Simple Calculation

- Let  $S$  be the total number of duplex channels
- Let  $k$  be the number of channels in each cell
- $N$  cells collectively use the complete set of  $S$  available channels.
- $N$  is the *cluster size* ( $N=4, 7$  or  $12$ ), then  $S = kN$
- If a cluster is replicated  $M$  times
- Total number of duplex channels  $= MS = MkN$
- $1/N$  is called the *frequency re-use factor*



## More About Cellular Structure

- Each cell has exactly six equidistant neighbors
- Thus there is only certain cluster sizes and cell layouts possible
- It can be shown that the number of hexagonal cells per cluster is given by

$$N = i^2 + ij + j^2$$

- $i$  &  $j$  are non negative integers



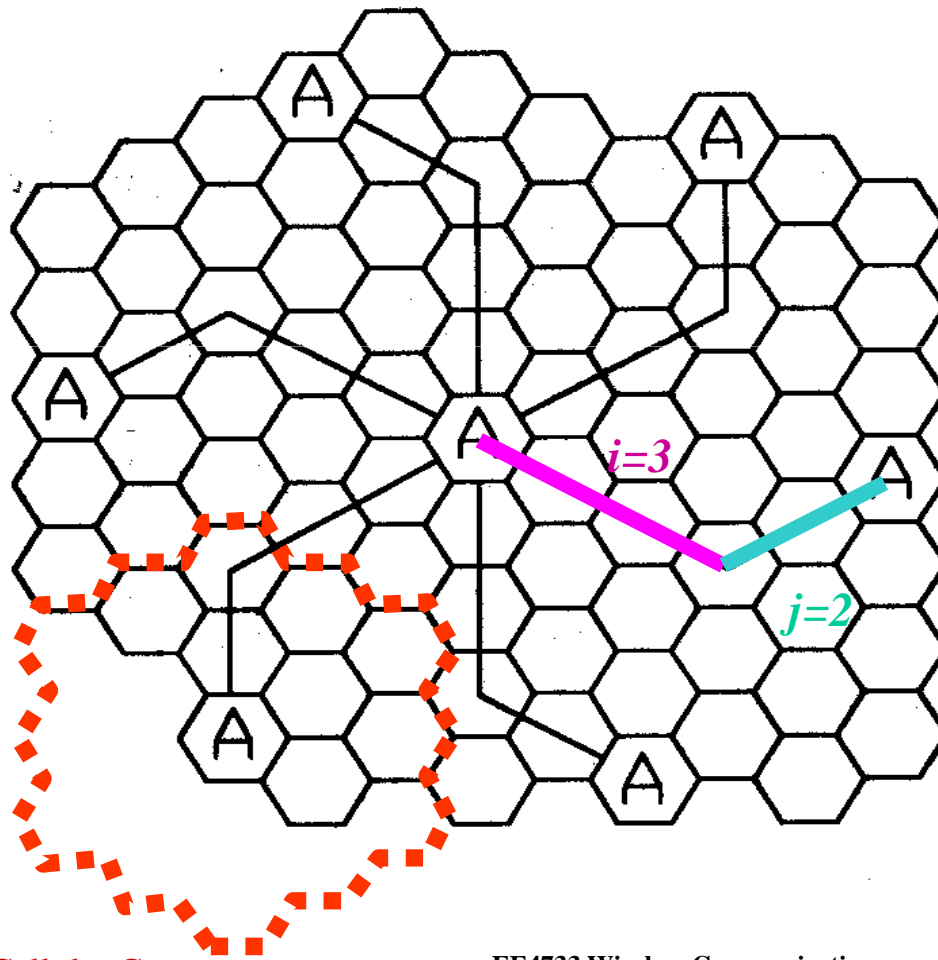


## $i$ & $j$ , Co-Channel Neighbors

- To find the nearest co-channel neighbors
- Move  $i$  cells along any chain of hexagons and then
- Turn 60 degrees counter clockwise, and move  $j$  cells



## Example



- $i=3$ , (move 3 cells along any chain of hexagons)

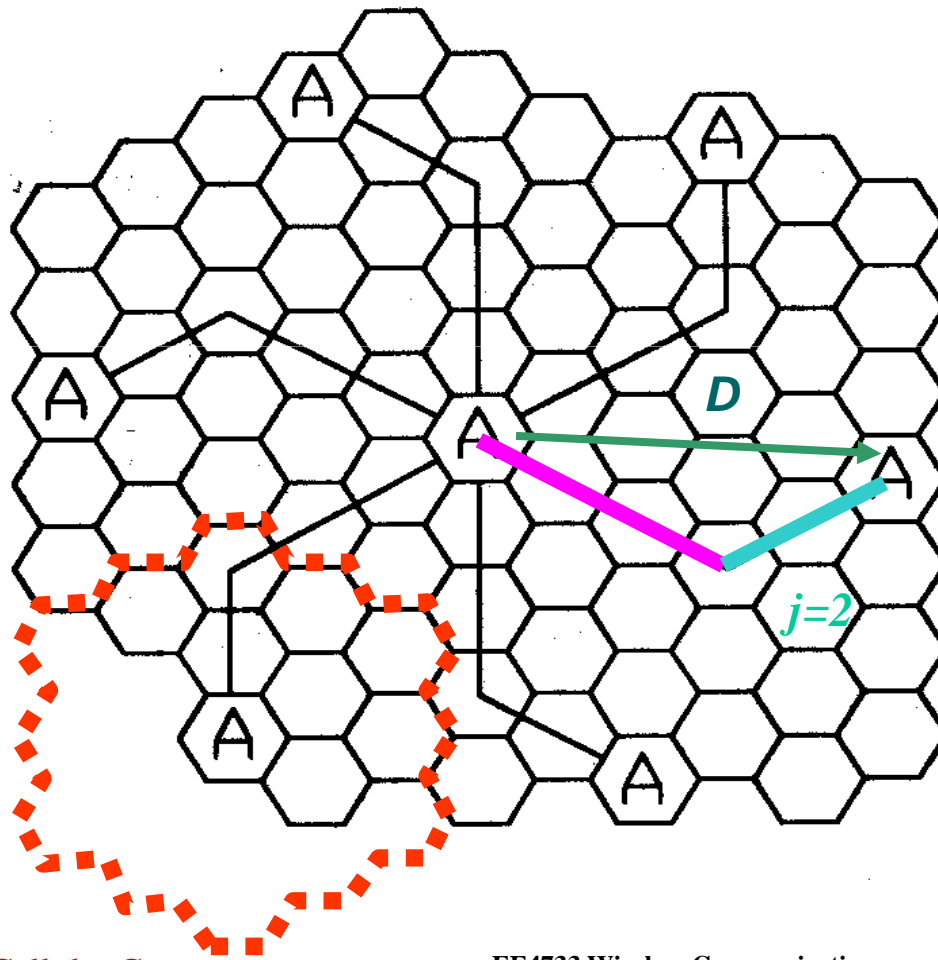
- $j=2$  (turn 60 degrees counter clockwise and move 2 cells);

- This is the way to find the central cell of the new cluster

- Number of cells in the cluster;  $N=9+3*2+4=19$ .



# Distance



$$D = \sqrt{3} R \sqrt{j^2 + i^2 + j \cdot i} = R \sqrt{3N}$$



# Channel Assignment

- Channel assignment (Frequency reuse)
  - efficient utilization of radio spectrum
  - increased capacity
  - minimized interference
- Channel assignment can be
  - *fixed*
  - *dynamic*
- Affects performance especially *handover* (*handoff*)



# Fixed Channel Assignment

- Each cell is allocated a predetermined set of channels
- Any call attempt within the cell can only be served by the unused channels in that cell
- Variations that allow channel borrowing exist
  - A cell is allowed to borrow from its neighbor
  - MSC supervises the borrowing procedure



# Dynamic Channel Assignment

- Each time a call is attempted, the serving BS request a channel from the MSC
- The lending algorithm take into account
  - likelihood of future blocking
  - frequency re-use of candidate channel
  - other cost functions
- Dynamic schemes reduces the call blocking probability and increases system capacity



# Implications

- Dynamic schemes require the MSC to collect real time data on all channels
  - Channel occupancy
  - Traffic distribution
  - Radio signal strength indications (RSSI)
- Makes the MSC more complex, and increases its storage and computational load



# Handover (Handoff)

- Need to be performed successfully and infrequently as possible and be transparent to users
- Need to decide the optimum signal level to perform handover
- Generally the level is decided the handover level is set slightly above it

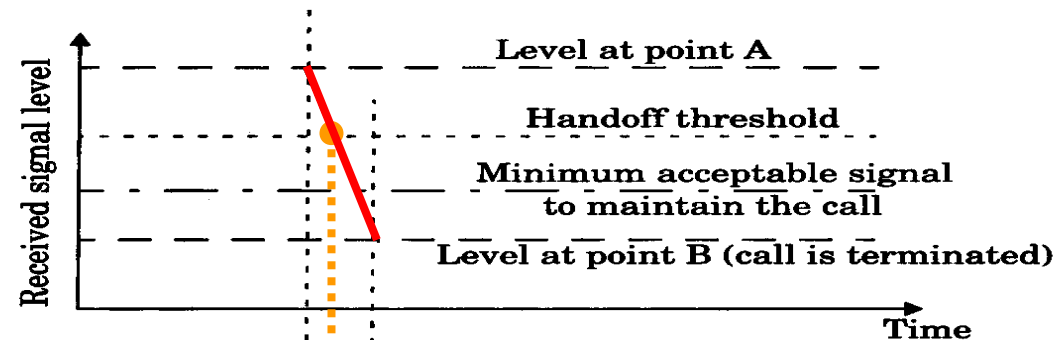
$$\Delta = P_{r \text{ handover}} - P_{r \text{ minimum usable}}$$



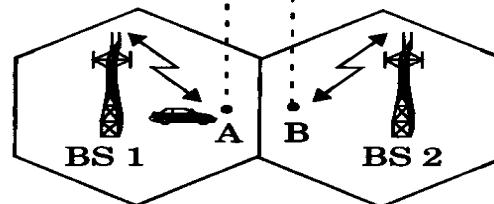
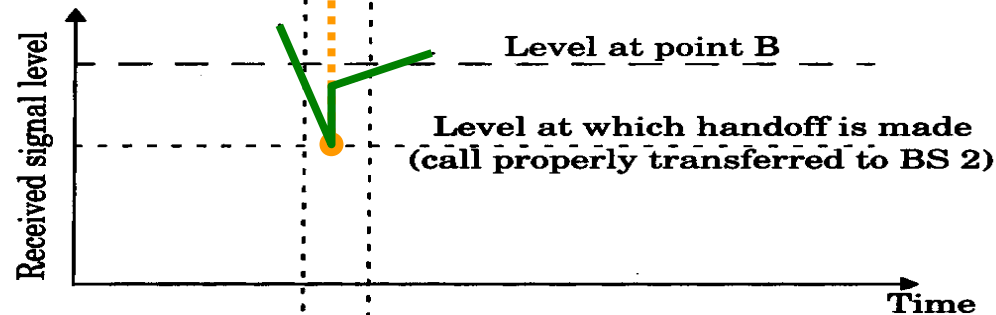


# Example

(a) Improper handoff situation



(b) Proper handoff situation





# Dwell Time

- The time a call may be maintained within a cell, without handover, is called the *dwell time*.
- Dwell time is dependent on a number of factors
  - propagation
  - interference
  - distance from BS etc.
- Therefore even a stationary subscriber may have a random and finite dwell time

# Mobile Assisted Handover (MAHO)



- In analog systems the signal strength was measured by the base station and supervised by the MSC,
- The MSC decides if a handover is necessary or not
- Digital systems handover decisions are mobile assisted
  - Mobile measures signal strength and reports to the serving BS
  - Handover is initiated when power received from the BS of a neighboring cell begins to exceed the power received from the current BS - certain level & duration



## Handover 2

- MAHO is faster and more suited for micro cellular environments
- It is also possible to have intersystem handover,
  - Handover from a cell of one MSC to a cell of another MSC
- Numerous issues
  - A local call (initially) may become a long distance call
  - Need to deal with incompatibility of the MSC

# Handover Policy



- Ways of handling handover requests
  - Same as all initial call requests
  - Give it higher priority
  - Queue requests
- Generally it is more annoying to have a call cut off in mid conversation than being blocked on a new call attempt
- Fraction of the total available channels in a cell is reserved for handover requests from ongoing calls
  - *guard channel*

# Practical Handover Considerations



- *Cell dragging* - pedestrian users that provide a very strong signal to the BS (LOS), but moved to a close range of another base station causing interference
- Difficulty in obtaining physical cell sites
  - Zoning laws (no high rise structures)
  - Public protest (radiation concerns) e.t.c
- Too many handoffs for high speed mobiles (on a vehicle)



# Handoff Improvements

- First generation mobile 10s to make handoff and  $\Delta = 6-12$  dB. ( $\Delta = P_{r \text{ handover}} - P_{r \text{ minimum usable}}$ )
- GSM (II generation) 1-2s to make handoff with  $\Delta = 0-6$  dB.
- Better system efficiency and handling high speed vehicles

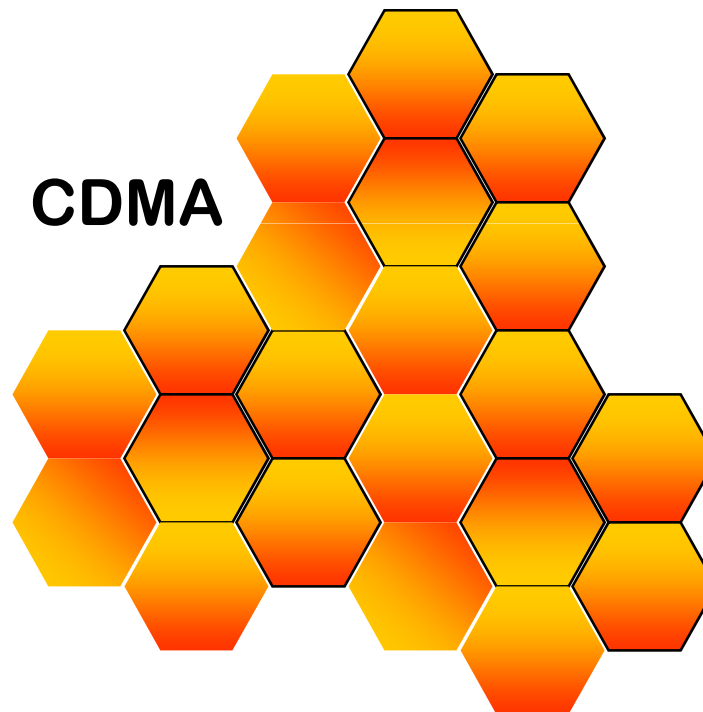
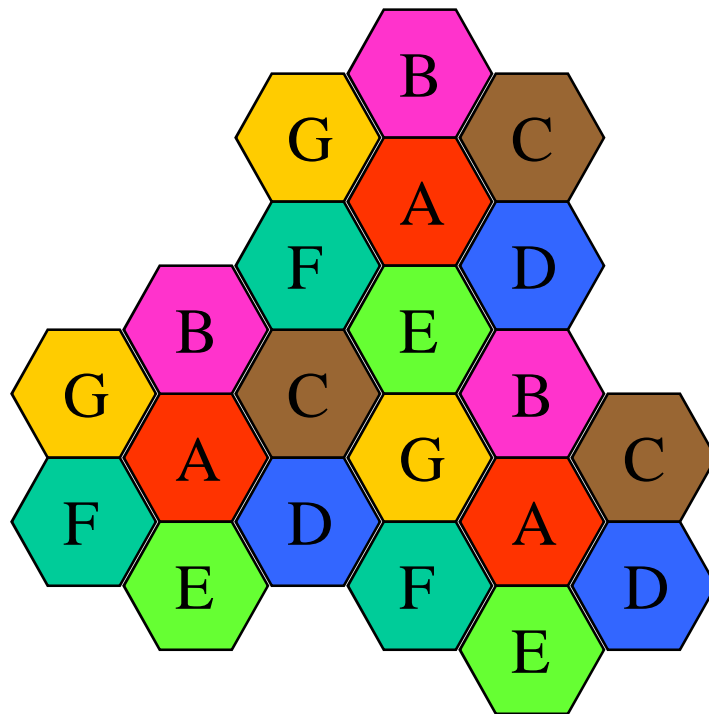


# Soft Handoff

- Channelized wireless systems (such as GSM) have to switch channels in the process of handoff
- There is always risk of losing the connection
- IS-95, Code Division Multiple Access (CDMA) system provides *Soft Handoff*.
- *Soft Handoff* does not mean changing the channel but rather deciding which base station will handle the connection
- This is a unique property of CDMA concept.



# CDMA Frequency Reuse Pattern





# Co-channel Interference

- There are several cells that use the same set frequencies
  - co-channel cells
- Interference between signals from these cells is called co-channel interference
- Unlike thermal noise, this cannot be overcome by increasing the signal power
- The co-channel cells must be physically separated



# Co-channel Interference

- Because the cell size is same, co-channel interference is independent of transmitted power
- It is a function of the radius of the cell ( $R$ ), and the distance to the center of the nearest co-channel cell ( $D$ )
- For hexagonal geometry, co-channel reuse ratio  $Q$  is given by

$$Q = \frac{D}{R} = \sqrt{3N}$$



# Carrier to Interference Ratio

- Carrier to Interference ratio (SIR or S/I) is also independent of transmitted power
- It is a function of the radius of the cell ( $R$ ), and the distance to the center of the nearest co-channel cell ( $D$ )
- For the first tier in hexagonal geometry, Carrier to Interference ratio is usually taken as

$$\frac{S}{I} \approx \frac{1}{6} \left( \frac{D}{R} \right)^4 = \frac{1}{6} (3N)^2$$



## Some Arithmetic Again

- Let  $i_0$  be the number of co channel interfering cells
- then carrier signal to interference ratio (SIR)

$$\frac{S}{I} = \frac{S}{\sum_{i=1}^{i_0} I_i}$$

- $S$  - desired signal power from desired BS;  $I_i$  - interference power caused by the  $i^{\text{th}}$  interfering co-channel cell BS



# Received Power

- Ave. received signal strength at any point decays as a power law of the distance of separation ( $d$ ) and is given by

$$P_r = P_0 \left( \frac{d}{d_0} \right)^{-n}$$

$$P_r(dBm) = P_0(dBm) - 10n \log \left( \frac{d}{d_0} \right)$$

- $P_0$  - Power received at a close-in reference point in the far field region of the antenna at a small distance;  $n$  - path loss component (2-4)



# SIR

- If  $D_i$  is the distance of the  $i^{\text{th}}$  interferer, the received power at a given mobile due to the  $i^{\text{th}}$  interfering cell will be proportional to  $(D_i)^{-n}$
- When the transmit power of each BS is equal and the path loss exponent is the same

$$\frac{S}{I} = \frac{R^{-n}}{\sum_{i=1}^{i_0} (D_i)^{-n}}$$



## Simpler SIR

- Considering only the first layer of interfering cells & if all these BS are equidistant

$$\frac{S}{I} = \frac{(D/R)^n}{i_0} = \frac{(\sqrt{3N})^n}{i_0}$$

- $i_0$  - number of neighboring/interfering co-channel cells



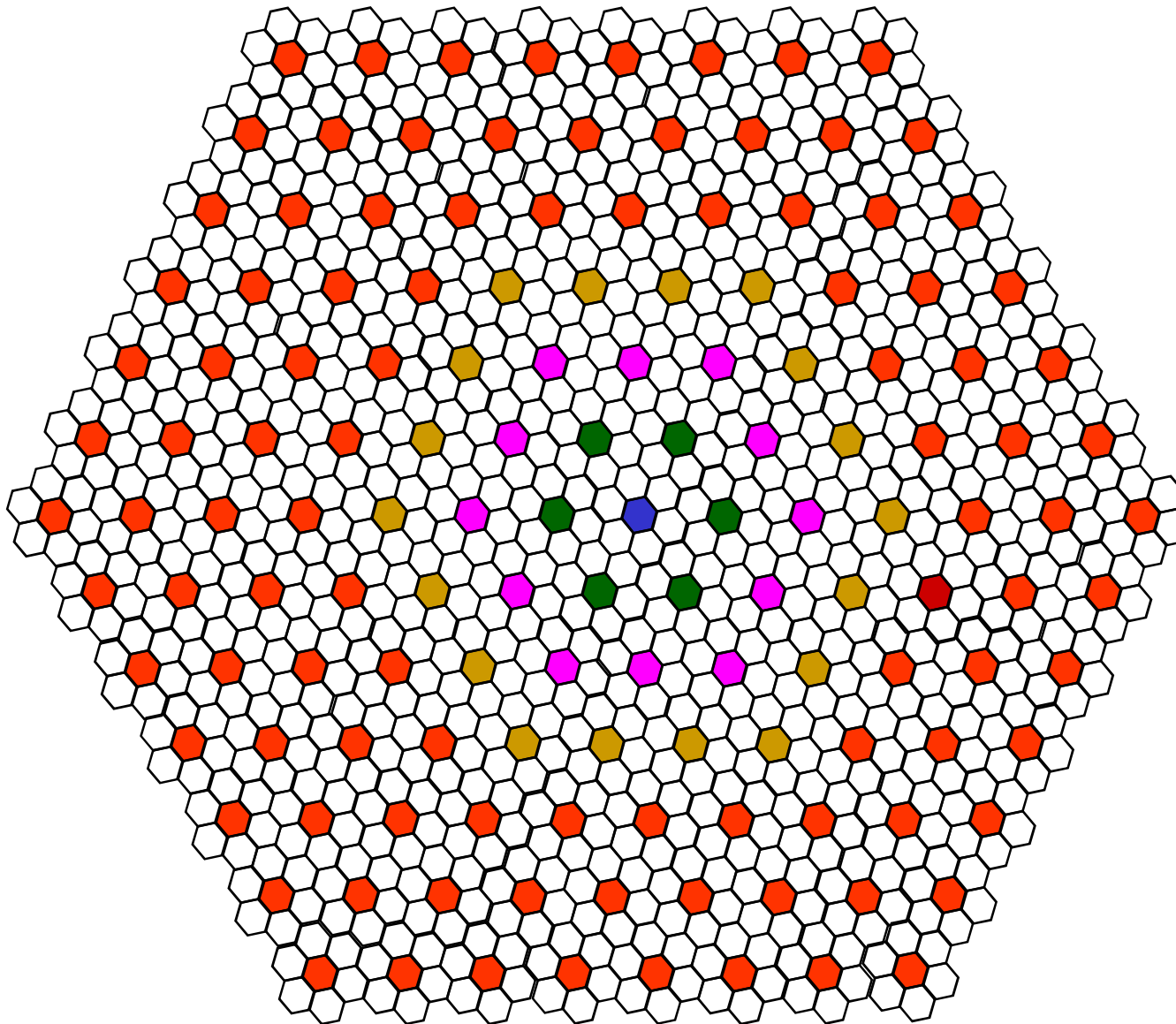
# Interference Limitation Example



- $i_0 = 6$  number of co-channel cells
- $N = 7$
- $n = 2$

$$\frac{S}{I} = \frac{3N}{6} = \frac{N}{2}$$

- Considering only the first layer of interfering cells & if all these BS are equidistant



$$1 \rightarrow 6$$

$$2 \rightarrow 12$$

$$3 \rightarrow 18$$

...

$$k \rightarrow 6k$$



# Interference Limitation

$$\frac{S}{I} = \frac{R^{-n}}{\sum_{i=1}^{i_0} (D_i)^{-n}}$$

$$D_K < kR \sqrt{3N}$$

$$\frac{S}{I} = \frac{R^{-n}}{\sum_{k=0}^K 6 \cdot k (kR \sqrt{3N})^{-n}}$$

$$\frac{S}{I} = \frac{(\sqrt{3N})^n}{6 \cdot \sum_{k=0}^K k^{1-n}}$$



# Interference Limitation

$$\frac{S}{I} = \frac{(\sqrt{3N})^n}{6 \cdot \sum_{k=0}^K k^{1-n}}$$

- Considering  $K$  layers of interfering cells
- For  $N$  fixed,  $n=2$  and the number of layers  $K \rightarrow \infty$ ;  $S/I \rightarrow 0$

$$I = \lim_{K \rightarrow \infty} O\left(\sum_{k=0}^K \frac{1}{k}\right) = \infty$$

# Adjacent Channel Interference 1



- Interference resulting from signals which are adjacent in frequency
- Results from imperfect receiver filters which allow nearby frequencies to leak
  - Particularly serious if an adjacent channel user is transmitting very close to the a receiver
- Referred to as the *near-far* effect
  - Nearby transmitter captures the receiver

# Adjacent Channel Interference 2

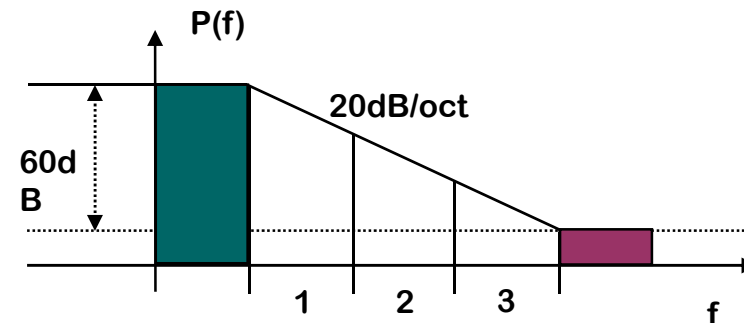
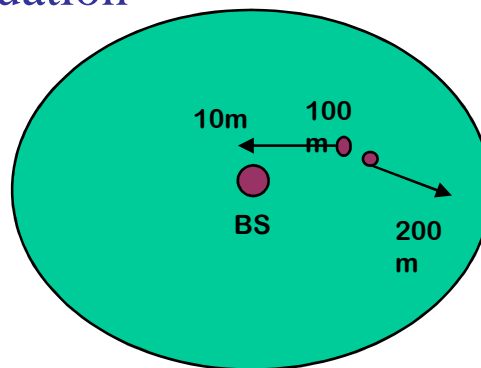


- Can be minimized by careful filtering & channel assignment
- If the frequency re-use factor is small, the separation between adjacent channels may not be sufficient to keep the adjacent channel interference level within tolerable limits



# Adjacent Channel Interference 3

- If a mobile is 20 times closer to the BS than another mobile
$$SIR = (20)^{-n}$$
- For  $n=4$ , this is equal to -52 dB
- If the intermediate filter has a slope of 20 dB/octave in the stop-band
- Adjacent channel must be displaced 3 times the pass-bandwidth from the center of the receiver frequency band-pass to achieve the 52 dB attenuation





# Power Control

- The power level transmitted by every mobile is controlled by the BS
- Enables to use the smallest power to maintain good link quality and reduces interference to other cells
- Increases battery lifetime before recharging ( talk time and stand-by time)
- CDMA requires very strict power control (1dB)





# Trunking

- Trunking is a statistical concept which allows a large number of users to share relatively small number of channels providing access on demand from a pool of available channels.
- Relatively small number of channels can serve a large number of users since all users are not demanding access and utilization of the system at the same time



# Grade of Service

- ***Grade of Service*** is a measure of the ability of a trunked system to give access to a user requiring service during the busiest hour (4-6pm, Thu, Fri)
- Grade of Service is usually measured in two ways
  1. Probability that a call is blocked
  2. Probability that a call will be delayed more than specified queuing time (some tolerable delay)



## Some Traffic Quantities

- $A_u$  - Traffic intensity

$$A_u = \lambda H$$

- $H$  - average duration of a call
- $\lambda$  - average number of calls per unit time
- For system with  $U$ , users total offered traffic intensity  $A$ , is

$$A = UA_u$$



# Blocked Calls Cleared

- Calls arrive as Poisson distributed
- All users may request service at any time
- $A$  - generated traffic
- $C$  - number of channels
- Grade of Service (Erlang B formula):

$$GOS = \Pr[blocking] = \frac{\frac{A^C}{C!}}{\sum_{k=0}^C \frac{A^k}{k!}}$$



# Capacity of Erlang B System

	Capacity in Erlangs for GOS			
No.of Channels	Pr=0.01	0.005	0.002	0.001
2	0.153	0.105	0.065	0.046
5	1.36	1.13	0.900	0.762
10	4.46	3.96	3.43	3.09
20	12.0	11.1	10.1	9.41
40	29.0	27.3	25.7	24.5
100	84.1	80.9	77.4	75.2



## Blocked Calls Delayed

- If a channel is not available immediately the call request may be put in a queue and delayed until a channel becomes available
- Erlang C formula:

$$\Pr[\text{delay} > 0] = \frac{A^C}{A^C + C! \left(1 - \frac{A}{C}\right) \sum_{k=0}^{C-1} \frac{A^k}{k!}}$$



# Grade of Service for Delayed Calls

$$\begin{aligned} GOS &= \Pr[ \textit{delay} > t ] \\ &= \Pr[ \textit{delay} > 0 ] \Pr[ \textit{delay} > t \mid \textit{delay} > 0 ] \\ &= \Pr[ \textit{delay} > 0 ] e^{-\frac{(C - A)t}{H}} \end{aligned}$$

# Average Delay in a Queued System



- The average delay  $D$  for all calls in a queued system is:

$$D = \Pr[\text{delay} > 0] \frac{H}{C - A}$$

– Where the average delay in the queue is  $H/(C-A)$

- $H$  – average duration of a call
- $C$  – number of channels
- $A$  – total offered traffic