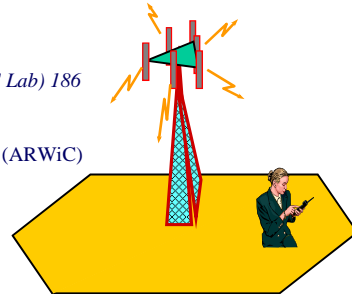




## Radio Transmission (Large-Scale Fading)

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## Radio Wave Propagation

- Mechanisms very diverse
  - reflection, diffraction and scattering
- In urban areas where there is no direct LOS, high rise buildings cause severe diffraction loss
- Waves travel along different paths of varying lengths
  - interaction causes multi-path fading
- Strength decreases as the distance between the transmitter and receiver increases



## Propagation Models

- Have traditionally focused on predicting the average received signal strength in close spatial proximity to a particular location
- Models that predict mean signal strength for an arbitrary transmitter receiver (T-R) separation
  - Useful for estimating the radio coverage area of a transmitter - *large-scale* models

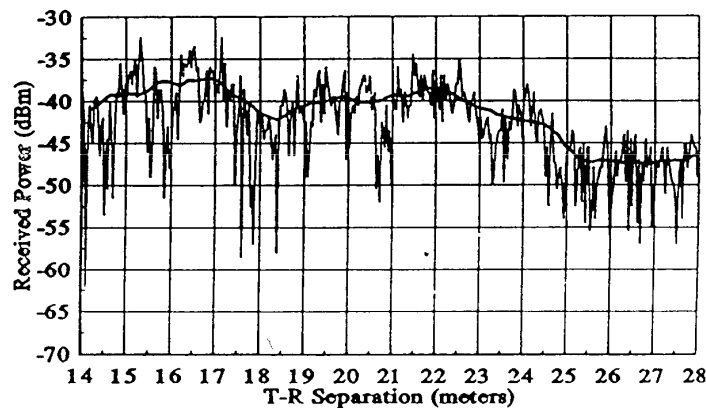


## Propagation Models 2

- *Large scale* models have T-Rs of several hundred or thousands of meters
- Models that can characterize the rapid fluctuations of received signal strength over short distances (few wavelengths) or short duration (second) are called *small-scale* or *fading* models



## Typical Look



## Free Space Propagation Model

- Predicts received signal strength when Transmitter (T) and Receiver (R) have direct Line of Sight (LOS)
- Satellite & Microwave LOS radio links
- As with most large scale models, the free space model predicts that the received power decays as a function of T-R separation raised to some power (power law function)



## Isotropic Antenna

$$G = 1$$

$$G = \frac{4\pi}{\lambda^2} A_{ea}$$

$$A_{ea} = \frac{\lambda^2}{4\pi}$$



## Free Space Equation

– For a T-R distance of  $d$

$$P_r(d) = \frac{P_t}{4\pi d^2} \frac{\lambda^2}{4\pi}$$

The equation is annotated with arrows:  $W_{rav} = P_r \cdot A_{ea}$  points to the product of the two fractions, and  $P_r(d)$  points to the entire right-hand side of the equation.

- $P_t$  - transmitted power,
- $P_r(d)$  - received power (change of notation !!  $P_r(d) \equiv W_{rav}$ ),

**Isotropic receiver and transmitter antenna used**



## Friis Free Space Equation

– For a T-R distance of  $d$

$$P_r(d) = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 d^2 L}$$

–  $P_t$  - transmitted power,

–  $P_r(d)$  - received power,

–  $G_t$  &  $G_r$  - transmitter & receiver antenna gains,  
 $L$  - system loss factor not related to propagation  
 ( $L \geq 1$ ),  $\lambda$  - wavelength in meters



## Antenna Gain

- The gain of an antenna is related to its effective aperture,  $A_e$ , by:

$$G = \frac{4\pi}{\lambda^2} A_e$$

- $A_e$  is related the physical size of the antenna, and  
 $\lambda$  is related to the carrier frequency by:

$$\lambda = \frac{c}{f} = \frac{2\pi c}{\omega_c}$$

$f$  - the carrier frequency in Hz,  
 $\omega_c$  - carrier frequency in radians/sec,  
 $c$  - speed of light in m/sec

EXAMPLE

$$f = 1 \text{ GHz} \rightarrow \lambda = \frac{3 \cdot 10^8 \text{ m/s}}{10^9 \text{ 1/s}} = 0.3 \text{ m} = 30 \text{ cm}$$



## Units

- $P_t$  and  $P_r$  must be in the same units [W, mW]
- $G_t$  &  $G_r$  are dimensionless
- $L$  is due to transmission line attenuation, filter & antenna losses
- Friis shows that the received power falls off as the square of  $d$  - 20 dB/decade



## EIRP

- Isotropic radiator is an ideal antenna which radiates power with unit gain uniformly in all directions - reference antenna gain in wireless systems
- Effective Isotropic Radiated Power (EIRP)** is defined as

$$\text{EIRP} = P_t G_t$$

- Represents the maximum radiated power available from the transmitter in the direction of antenna gain as compared to an isotropic radiator

## ERP



- In practice, *effective radiated power* (ERP) is used instead to denote the max radiated power as compared to an half-wave-dipole antenna
- Dipole antenna gain = 1.64, ERP will be 2.15dB smaller than the EIRP for the same transmission system
- dB*i - dB gain wrt to an isotropic source
- dB*d - dB gain wrt to a half wave dipole

## Path Loss



- Path Loss represents signal attenuation as a positive quantity measured in dB

$$PL(dB) = 10 \log \frac{P_t}{P_r} = -10 \log \left[ \frac{G_t G_r \lambda^2}{(4\pi)^2 d^2} \right]$$

If antenna gains  $G_t$  are  $G_r$  equal to 1

$$PL(dB) = -10 \log \left[ \frac{\lambda^2}{(4\pi)^2 d^2} \right]$$

## Far Field



- Friis model is only valid for received powers,  $P_r$  at distances  $d$ , which are in the *far field* or *Fraunhofer* region.
- Far field of a transmitting antenna is defined as the region beyond the far field distance  $d_f$ , which is related to the largest linear dimension of the antenna aperture and/or carrier wavelength.

## Fraunhofer Distance



- Fraunhofer distance is given by

$$d_f = \frac{2 D_l^2}{\lambda}$$

- $D_l$  is the largest physical linear dimension of the antenna
- To be in the far-field region,  $d_f$  must satisfy
- $d_f \gg D_l$  and  $d_f \gg \lambda$



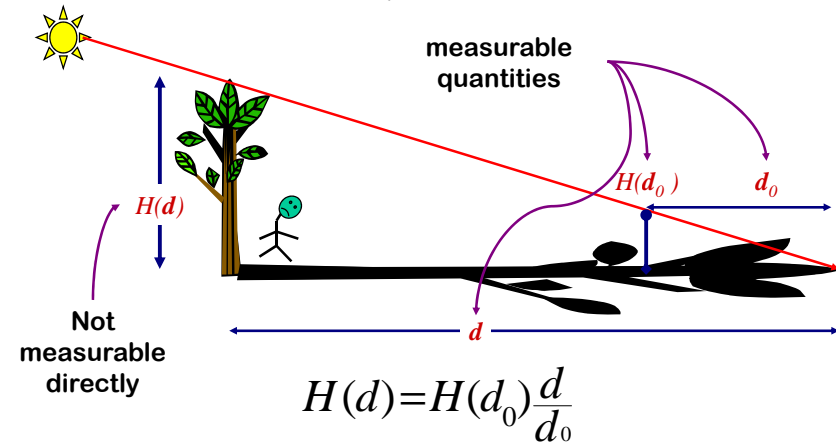
## Distance $d = 0$

- The received power equation does not hold for  $d = 0$ .
- Large scale models use a close-in distance  $d_0$  - *received power reference point*
- The received power at any distance  $d > d_0$  may be related to  $P_r(d_0)$  at  $d_0$
- $P_r(d_0)$  may be predicted or determined through empirical measurements



## Proportions

Calculating height of an inaccessible point



## Received power $P_r(d)$

$$P_r(d) = \frac{\lambda^2}{(4\pi)^2} \cdot \frac{P_t}{d^2}$$

$$P_r(d) = \text{con} \cdot \frac{P_t}{d^2} \quad P_r(d_0) = \text{con} \cdot \frac{P_t}{d_0^2} \Rightarrow \text{con} = P_r(d_0) \cdot \frac{d_0^2}{P_t}$$

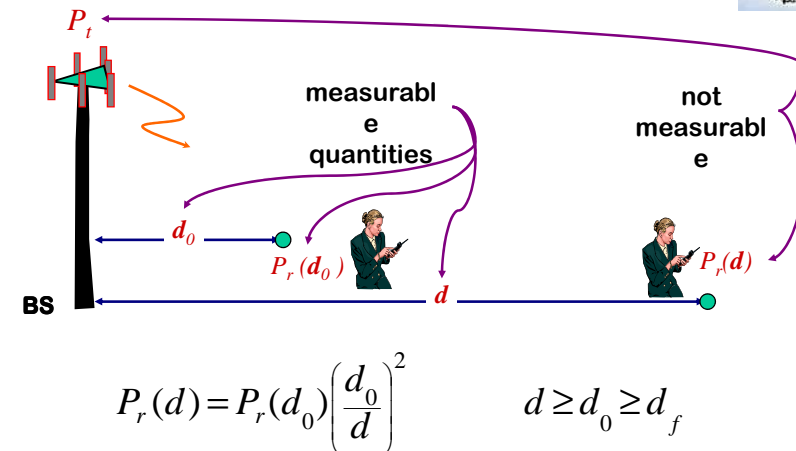
- $d_0$  must be chosen to be in the far-field region

$$P_r(d) = P_r(d_0) \left( \frac{d_0}{d} \right)^2 \quad d \geq d_0 \geq d_f$$

$$P_r(d) [\text{dBm}] = 10 \log \left[ \frac{P_r(d_0)}{0.001 \text{ W}} \right] + 20 \log \left( \frac{d_0}{d} \right); \quad d \geq d_0 \geq d_f$$



## Received power $P_r(d)$

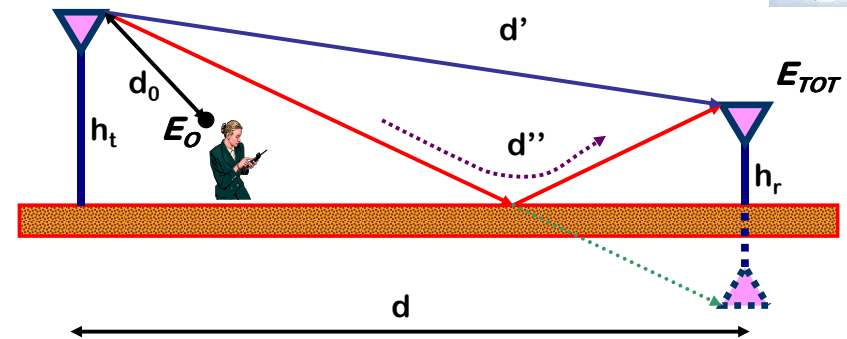


## Ground Reflection (2-ray) Model



- In a mobile radio channel, a single direct path between the base station and a mobile is exception rather than rule
- Two ray ground reflection model is reasonably accurate for predicting the large scale signal strength over distances of several kilometers for mobile radio systems

## Two Ray Model



$$E_{TOT}(d, t) = \frac{E_0 d_0}{d'} \cos\left(\omega_c \left(t - \frac{d'}{c}\right)\right) - \frac{E_0 d_0}{d''} \cos\left(\omega_c \left(t - \frac{d''}{c}\right)\right)$$

## Two Ray Model



$$P_r(d) = P_r(d_0) \left(\frac{d_0}{d}\right)^2 \quad d \geq d_0 \geq d_f$$

$$E_\theta(d) = \frac{E_0 d_0}{d} \quad (d > d_0 > d_f) \quad \mathbf{d_0 - reference distance}$$

$$E_\theta(d, t) = \frac{E_0 d_0}{d} \cos\left(\omega_c \left(t - \frac{d}{c}\right)\right) \quad (d > d_0)$$

$$E_{TOT}(d, t) = E_{LOS}(d', t) - E_{REF}(d'', t)$$

$$E_{TOT}(d, t) = \frac{E_0 d_0}{d'} \cos\left(\omega_c \left(t - \frac{d'}{c}\right)\right) - \frac{E_0 d_0}{d''} \cos\left(\omega_c \left(t - \frac{d''}{c}\right)\right)$$

## Two Ray Model Approximations



$$d' = \sqrt{(h_t - h_r)^2 + d^2}; \quad d'' = \sqrt{(h_t + h_r)^2 + d^2};$$

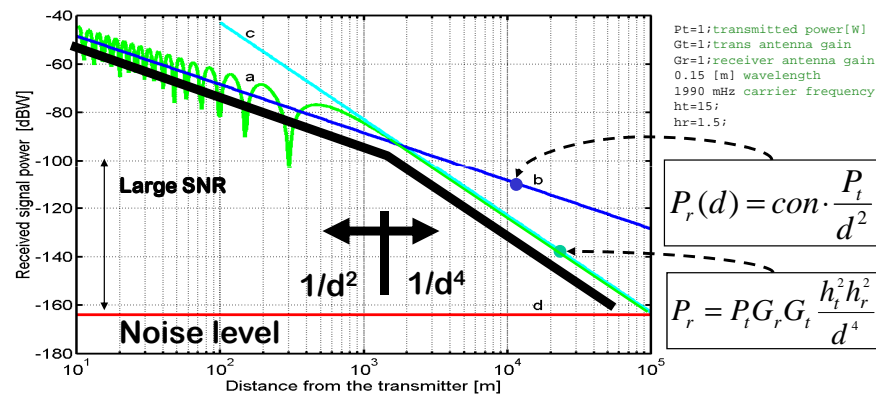
$$d \gg h_t + h_r; \Rightarrow d'' - d' \approx \frac{2h_t h_r}{d}; \Rightarrow \left|\frac{E_0 d_0}{d}\right| \approx \left|\frac{E_0 d_0}{d'}\right| \approx \left|\frac{E_0 d_0}{d''}\right|$$

$$E_{TOT}(d) = 2 \frac{E_0 d_0}{d} \sin\left(\frac{2\pi h_t h_r}{\lambda d}\right) \quad \text{for } \frac{2\pi h_t h_r}{\lambda d} < 0.3 \text{ rad}$$

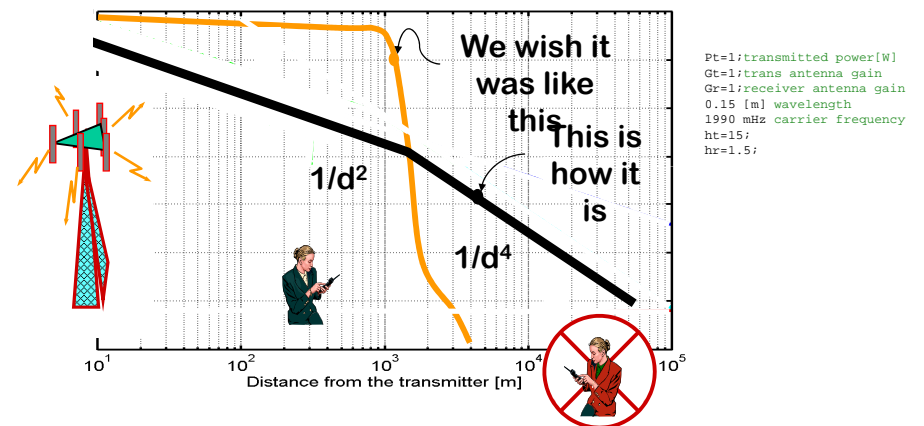
$$E_{TOT}(d) = \frac{4\pi E_0 d_0}{\lambda} \frac{h_t h_r}{d^2}$$

$$P_r = P_t G_r G_t \frac{h_t^2 h_r^2}{d^4}$$

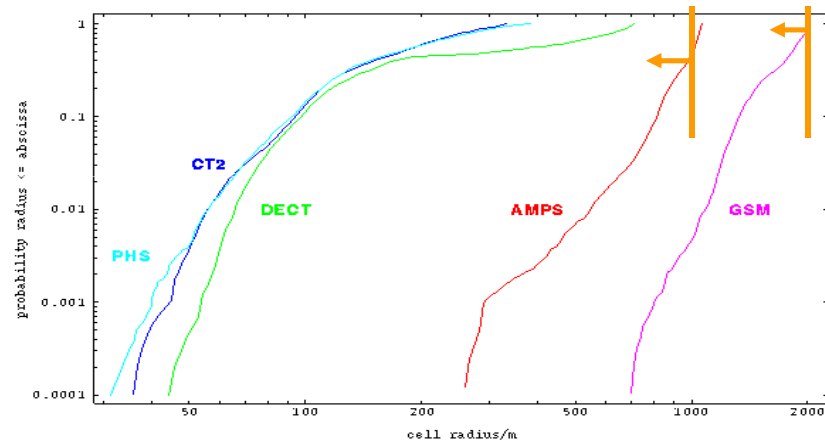
## Two Ray Model Path Loss



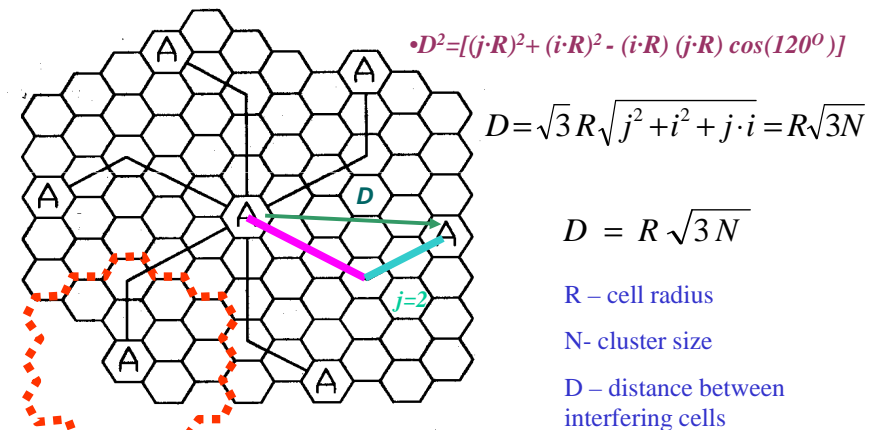
## Two Ray Model -The Model of 'Distance Filtering'



## Actual Cell Size



## Distance between interfering cells





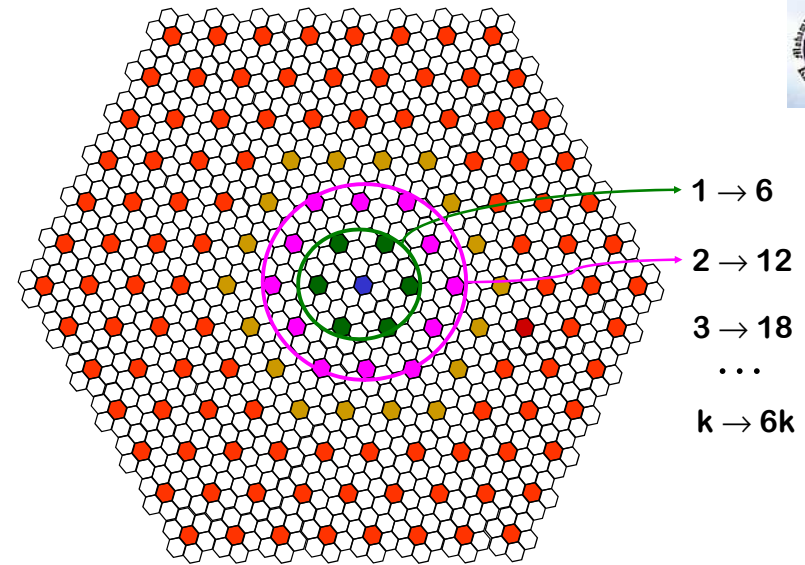


## Simpler SIR

- Considering only the first layer of interfering cells & if all these BS are equidistant

$$\frac{S}{I} = \frac{(D/R)^n}{i_0} = \frac{(\sqrt{3N})^n}{i_0}$$

- $i_0$  - number of neighboring/interfering co-channel cells



## Interference Limitation

$$\frac{S}{I} = \frac{R^{-n}}{\sum_{i=1}^{i_0} (D_i)^{-n}}$$

$$D_k < kR \sqrt{3N}$$

$$\frac{S}{I} = \frac{R^{-n}}{\sum_{k=0}^K 6 \cdot k (kR \sqrt{3N})^{-n}}$$

$$\frac{S}{I} = \frac{(\sqrt{3N})^n}{6 \cdot \sum_{k=0}^K k^{1-n}}$$

$k$  – circle of interfering cels



## Interference Limitation

$$\frac{S}{I} = \frac{(\sqrt{3N})^n}{6 \cdot \sum_{k=0}^K k^{1-n}}$$

- Considering  $K$  layers of interfering cells
- For  $N$  fixed,  $n=2$  and the number of layers  $K \rightarrow \infty$ ;  $S/I \rightarrow 0$

$$I = \lim_{K \rightarrow \infty} O \left( \sum_{k=0}^K \frac{1}{k} \right) = \infty$$



## Log-distance Path Loss Model



- Average received power decreases as the  $n$ -th power of the relative distance between the transmitter and the receiver
- The average large scale path loss for an arbitrary T-R separation is expressed as function of distance using a path-loss exponent

$$\overline{PL}(d) \propto \left(\frac{d}{d_0}\right)^n$$

$$\overline{PL} [dB] = \overline{PL}(d_0) + 10 n \log\left(\frac{d}{d_0}\right)$$

## Log-distance Path Loss Model



- $n$  - the rate at which the path loss increases
  - For free space  $n=2$
- $d_0$  – close-in reference distance
- The value of  $n$  depends on the specific propagation environment

## Example



Environment	Path Loss Exponent, $n$
Free space	2
Urban area cellular radio	2.7 to 3.5
Shadowed urban cellular radio	3 to 5
Inbuilding LOS	1.6 to 1.8
Obstructed in building	4 to 6
Obstructed in factories	2 to 3

## Log-normal Shadowing 1



- The log distance Model does not consider the effects of environmental clutter
  - Large discrepancies
- It has been shown that path loss at a particular location is random, and distributed *log-normally*

$$PL(d) = \overline{PL}(d) + X_\sigma = \overline{PL}(d_0) + 10n \log\left(\frac{d}{d_0}\right) + X_\sigma$$



## Log-normal Shadowing 2

$$P_r = P_t - PL(d)$$

- $X_\sigma$  - zero mean Gaussian distributed random variable (dB) with standard deviation  $\sigma$  (dB)
- $d_0$ ,  $n$  and  $\sigma$  statistically describe the path loss model for an arbitrary location



## Log-normal Shadowing 3

- $n$  and  $\sigma$  are in practice computed from measured data using linear regression (fitting)
- $PL(d_0)$  is based either on close-in measurements or on a free space assumption from transmitter to  $d_0$
- A number of practical models exist for predicting path loss in “real” propagation conditions



## A Cell Design Problem

A GSM-1800 operator provides cellular coverage in Karachi (Area: 2500 km<sup>2</sup>) with 49 microcells of similar hexagonal geometry. If a mobile unit is considered to be located at the edge of a cell, find the Signal to Noise Ratio (SNR) that is ensured for 90% of the time at the mobile unit.

Assume the following: The close-in reference distance  $d_0 = 1$  km. Transmitter power  $P_t = 10$ W, the receiver and the transmitter antenna gains are  $G_t = 3$  dB and  $G_r = 0$  dB, respectively. The propagation beyond the close-in distance occurs with a path loss exponent  $n=4$  and follows a log-normal distribution with standard deviation  $\sigma=6.5$ dB. Normal temperature in Karachi is 27°C and the noise figure of the mobile unit is 10dB.



## Okumura Model 1

- Okumura 1963;
- Okumura-Hata; ITU-R recommendation P.529-2; pages 5-7, 1995.
- Applicable for frequencies in the range 150 MHz to 1920 MHz
- Distances of 1 km to 100 km
- Effective antenna heights from 30m to 1000m (hills!!)



## Okumura Model 2

- Set of curves giving the median attenuation  $G$ 
  - relative to free space –  $A_{mu}$  (Graph)
  - in an urban area over quasi-smooth terrain
  - mobile antenna height of 3m
- Developed from extensive measurements
- Path loss is calculated by determining  $A_{mu}$  from the curves and adding correction factors
  - Type of terrain



## Okumura Model 3

$$L_{50}(dB) = L_F + A_{mu}(f, d) - G(h_{te}) - G(h_{re}) - G_{AREA}$$

- $L_{50}$  - 50th percentile value of the propagation path loss (median “average” not mean-square average)
- $L_F$  Free space propagation loss (Formula)
- $A_{mu}$  - Median attenuation relative to free space (G)
- $G(h_{te})$  - Base station antenna height gain factor (F)
- $G(h_{re})$  - Mobile antenna height gain factor (F)
- $G_{AREA}$  - Gain due to the type of environment (G)



## Free Space Propagation Loss

$$L_{50}(dB) = L_F + A_{mu}(f, d) - G(h_{te}) - G(h_{re}) - G_{AREA}$$

- The free space propagation loss is given by formula:

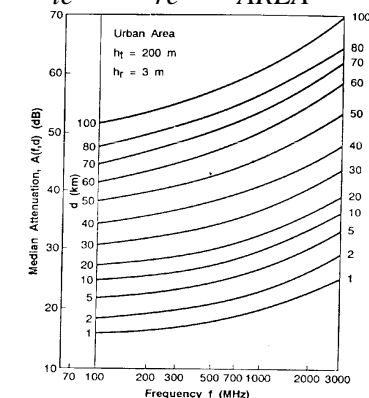
$$L_F [dB] = -10 \log \left[ \frac{G_t G_r \lambda^2}{(4\pi)^2 d^2} \right]$$



$A_{mu}$

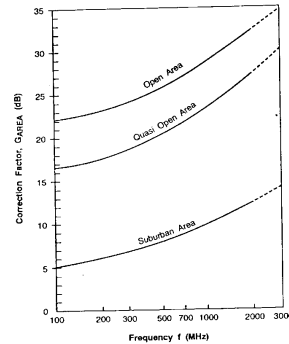
$$L_{50}(dB) = L_F + A_{mu}(f, d) - G(h_{te}) - G(h_{re}) - G_{AREA}$$

Median attenuation  
with respect to free  
space loss



## G<sub>AREA</sub>

Gain due to  
the type of  
environment



$$L_{50}(dB) = L_F + A_{mu}(f,d) - G(h_{te}) - G(h_{re}) - G_{AREA}$$

## Antenna gain factors $G(h_{te}), G(h_{re})$

Okumura found that for heights less than 3 m

- $G(h_{te})$  - varies at a rate of 20 dB/decade
- $G(h_{re})$  - varies 10dB/decade

$$G(h_{te}) = 20 \log \left( \frac{h_{te}}{200} \right) \quad 1000m > h_{te} > 10m$$

$$G(h_{re}) = 10 \log \left( \frac{h_{re}}{3} \right) \quad h_{re} \leq 3m$$

$$G(h_{re}) = 20 \log \left( \frac{h_{re}}{3} \right) \quad 10m > h_{re} > 3m$$

## Other Corrections

- Can be applied to Okumura's model
  - Terrain undulation height
  - Isolated ridge height
  - Average slope of terrain and
  - Mixed land-sea parameters
- All available as Okumura curves (Oku68)

## Okumura Model Summary

- Okumura's model is wholly based on measured data (empirical)
- Extrapolations can be made to obtain values outside the measurement range
- Simplest and the best in terms of accuracy (the best tradeoff in terms of simplicity-accuracy)
- Major disadvantage – decreased accuracy in situations of rapid changes in terrain



## Hata Propagation Model

- An empirical formulation of graph path loss data provided by Okumura
- Curves from Okumura model replaced by formulas
- Valid from 150 to 1500 MHz
- Presents an urban area propagation loss as a standard formula
  - correction equations for application to other situations



## Urban Path Loss Equation

$$L_{50}(\text{urban})(\text{dB}) = 69.55 + 26.16 \log f_c - 13.82 \log h_{te} - a(h_{re}) + (44.9 - 6.55 \log h_{te}) \log d$$

- $f_c$  - Frequency in MHz from 150-1500MHz
- $h_{te}$  - BS antenna height in meters from 30-200 m
- $h_{re}$  - MS antenna height in meters from 1-10 m
- $d$  - T-R separation distance in km
- $a(h_{re})$  - correction factor for effective MS antenna height (size of the coverage area)



## Mobile antenna correction factor $a(h_{re})$

- Small to medium size city

$$a(h_{re}) = (1.1 \log f_c - 0.7) h_{re} - (1.56 \log f_c - 0.8) \text{ dB}$$

- Large city

$$a(h_{re}) = 8.29(\log 1.54 h_{re})^2 - 1.1 \text{ dB} \quad \text{for } f_c \leq 300 \text{ MHz}$$

$$a(h_{re}) = 3.2(\log 11.75 h_{re})^2 - 4.97 \text{ dB} \quad \text{for } f_c \geq 300 \text{ MHz}$$



## Suburban and Rural Path Loss Equation

- Suburban area

$$L_{50}(\text{dB}) = L_{50}(\text{urban}) - 2[\log(f_c / 28)]^2 - 5.4$$

- Open rural area

$$L_{50}(\text{dB}) = L_{50}(\text{urban}) - 4.78(\log f_c)^2 - 18.33 \log f_c - 40.98$$



## Hata-model Summary

- Simple and sufficiently accurate
- Presents significant practical value
- Compares very favorably with Okumura's model for  $d > 1$  km (in fact it has been derived from Okumura model)
- Suitable for large cell mobile systems planning
- Extensions and corrections for smaller cells are available