

Question 1

Given:

Annual Revenue = 10,000,00 for 10 years

Reduction after 10 years = 100000 each year

Interest rate = compounded annually = $i = 9.5\%$

Future worth = $F = ?$

For first 10 years, Annuity = 1000000

For next 10 years, Annuity = 9000,00

↳ For same 10 years, Geometric series = 100,000

Now

$$F_1 = 1000,000 (F/A, 9.5\%, 10) (F/P, 9.5\%, 10)$$

$$F_1 = 1000,000 \left\{ \frac{(1+i)^{10} - 1}{i} \right\} \{1+i\}^{10}$$

$$F_1 = 1000000 \left\{ \frac{(1.095)^{10} - 1}{0.095} \right\} (1.095)^{10}$$

$$F_1 = 1000000 (15.56) (2.47)$$

$$\Rightarrow F_1 = \$38433200$$

$$F_2 = 900000 (F/A, 9.5\%, 10)$$

$$900000 \left\{ \frac{(1+0.095)^{10} - 1}{0.095} \right\}$$

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$$= 900000(15.56)$$

$$F_2 = \$14004261.6$$

$$P = C_1(P/C_1, 9.5\%, 10)$$

$$= 100000 \left\{ \frac{(1+i)^{10} - i \times 10 - 1}{i^2 (1+i)^{10}} \right\}$$

$$= 100000 \left\{ \frac{(1.095)^{10} - 0.95 - 1}{(0.095)^2 (1.095)^{10}} \right\}$$

$$= 100000(23.61)$$

$$P = \$2361000$$

$$F_3 = 2361000(F/P, 9.5\%, 10)$$

$$= 2361000(2.47)$$

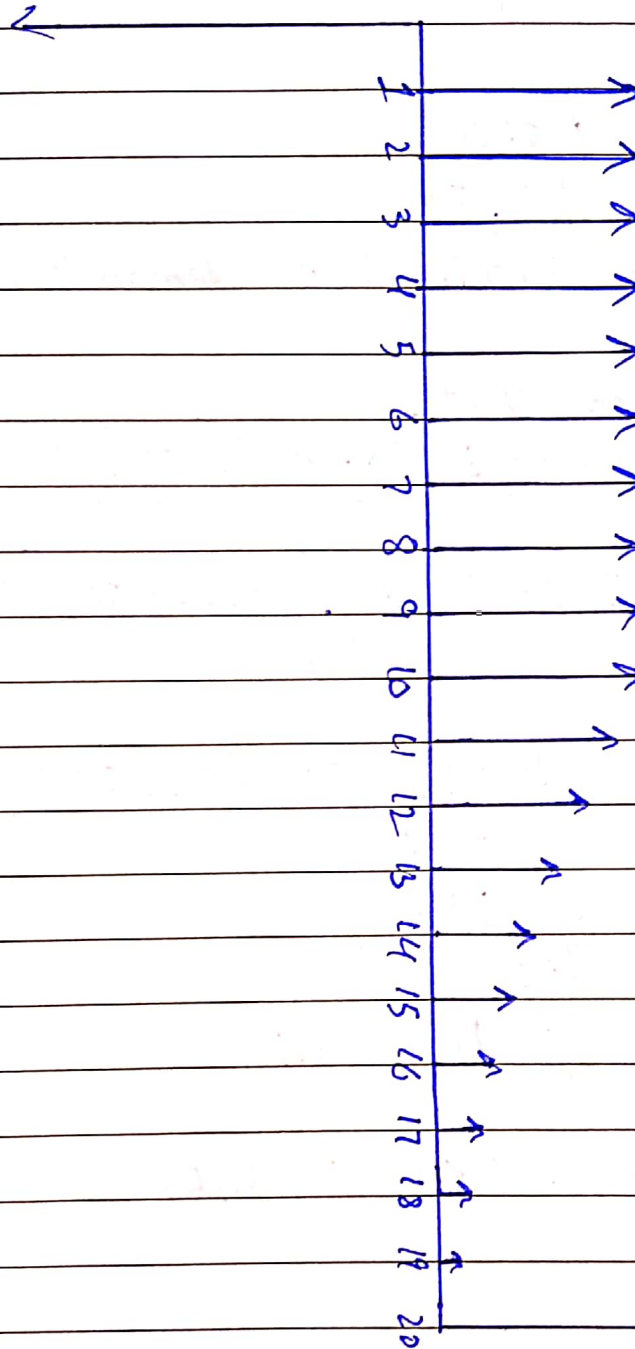
$$F_3 = \$5851095.39$$

$$F = F_1 + F_2 + F_3 = \$58288556.97$$

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Cash Flow Diagram:



\$58288556.99

No:

Date:

(Question 2)

Given:

$$P = \$10,000,000$$

$$i = 8.5\%$$

Annuaty = A for 1st 8 years

3A for next 5 years

5A for last 7 years

$$N = 20 \text{ years}$$

$$A = ?$$

Take Annuaty = A for 20 years

Take Annuaty = 2A for 5 years from 9th year

Take Annuaty = 2A for 7 years for last 7 years

Now

$$P_1 = A(P/A, i\%, N)$$

$$= A \left\{ \frac{(1+i)^N - 1}{i(1+i)^N} \right\} = A \left\{ \frac{(1.085)^{20} - 1}{0.085(1.085)^{20}} \right\}$$

$$\Rightarrow P_1 = 9.463 A$$

$$P_2 = 2A(P/A, 8.5\%, 12)(P/F, 8.5\%, 8)$$

$$= 2A \left\{ \frac{(1.085)^{12} - 1}{0.085 \times (1.085)^{12}} \right\} \left\{ (1.085)^{-8} \right\}$$

$$P_2 = 7.6487 A$$

$$P_3 = 2A(P/A, 8.5\%, 7)(P/F, 8.5\%, 13)$$

$$= 2A(5.118)(0.34)$$

$$P_3 = 3.48 A$$

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Now

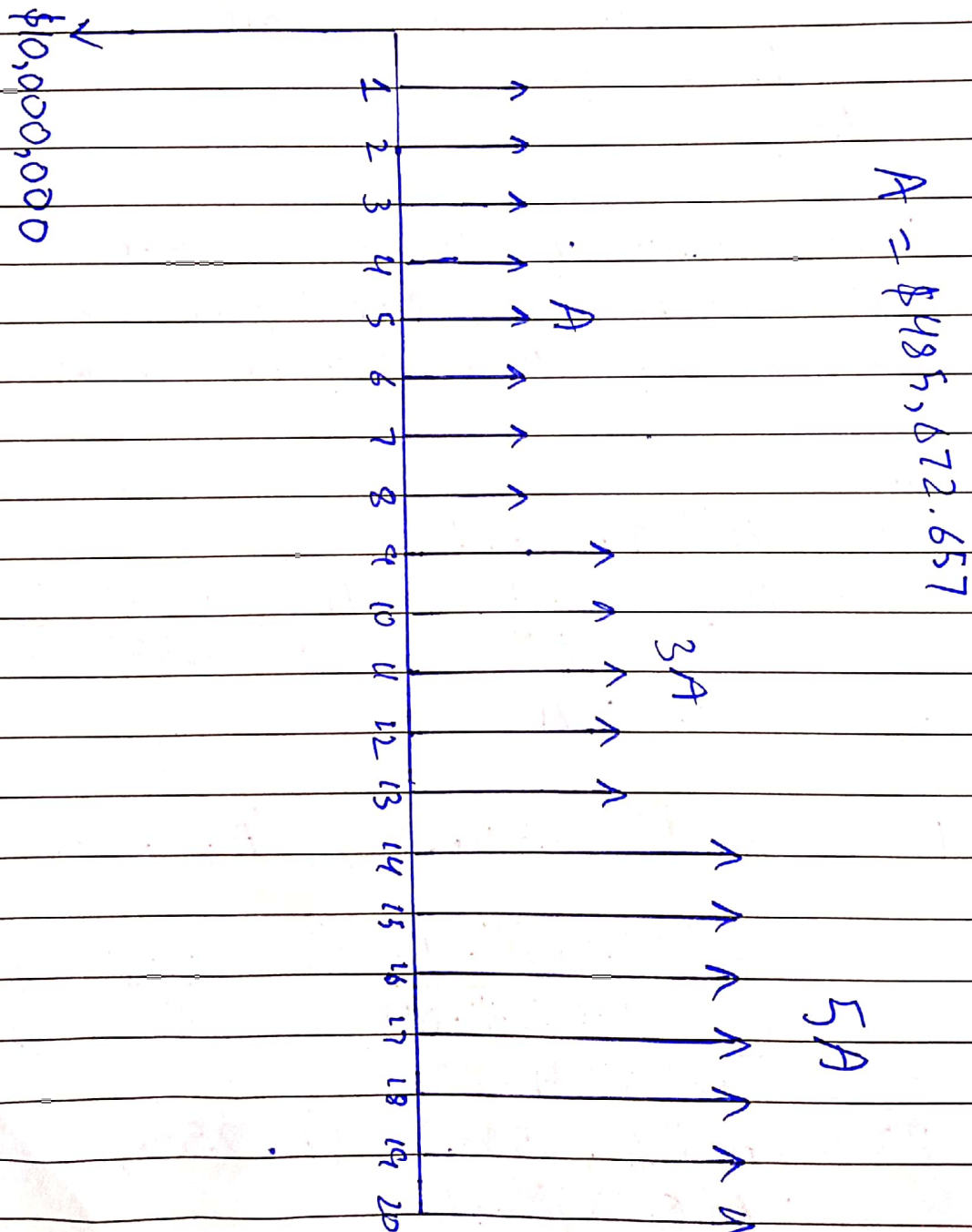
$$P_1 + P_2 + P_3 = P$$

$$9.46A + 7.65A + 3.48A = 10,000,000$$

$$20.59A = 10,000,000$$

$$A = \$485,672.657$$

Cash Flow Diagram:



No:

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(Question 3)

Solution:

$$a = 4500$$

$$b = 80$$

$$CV = \$850$$

$$CF = \$8,500$$

Range of Profitable demands = ?

As we know that

$$D = \frac{-(a - CV) \pm \sqrt{(a - CV)^2 - 4(-b)(-CF)}}{2(-b)}$$
$$= \frac{-(4500 - 850) \pm \sqrt{(4500 - 850)^2 - 4(-80)(-8500)}}{2(-80)}$$

$$= \frac{-3650 \pm \sqrt{13322500 - 2720000}}{-160}$$

$$D = \frac{-3650 \pm 3256.2}{-160}$$

$$D_1 = 2.46 \quad \& \quad D_2 = 43.16$$

$$\text{Range} = \{ 2.46 \leq D \leq 43.16 \}$$

No:

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(Question 4)

Solution:

Present worth = Total costs

$$\text{Total costs} = 500,000 + 650,000 + 550,000 + 250,000$$

Annual Revenue = 600,000 for 12 years

$$\text{Salvage value} = 500,000 + 250,000 + 60,000 + 625,000$$

Annual cost = \$435,000

MARR = 9.5%

Initial cost = \$1950,000

$$\text{Capital Recovery cost} = CR(i\%) = (I - S)(A/P, i\%, N) + S(i\%)$$

Net Annuatly = 600000 - 435000

Annual worth = \$165000 = R - E

Now

$$AW(i\%) = R - E - CR(i\%)$$

$$= \$165,000 - \{(I - S)(A/P, i\%, N) + S(i\%)\}$$

$$AW(9.5\%) = 165000 - \{(1950,000 - 1460,000)(A/P, 9.5\%, 12) + 1460000 \times 9.5\%\}$$

$$= 165000 - \left\{ 490 \left\{ \frac{(1.095)^{12} \times 0.095}{(1.095)^{12} - 1} \right\} + 138700 \right\}$$

$$= 165000 - \{ 490(0.143) + 138700 \}$$

$$= 165000 - 138770.16$$

Date:

$$AW(9.5\%) = \$26229.84$$

As AW is greater than 0 thus the project is accepted and the person should invest in this mall.