

## **Assignment 4**



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**CSE-408 Digital Image Processing**

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## Question 1: Frequency Domain Sharpening (Highpass Filtering)

Apply and analyze **sharpening filters** in the frequency domain using Python/ MATLAB. Observe how edges and details are enhanced using different high-pass filtering approaches.

### Instructions:

1. Use the same grayscale image as in Assignment 03.
2. Implement and apply the following **Highpass Filters** in the frequency domain:
  - Ideal Highpass Filter (IHPF)
  - Butterworth Highpass Filter (BHPF) with order = 2
  - Gaussian Highpass Filter (GHPF)
3. Use a common cutoff frequency  $D_0 = 50$
4. Perform inverse FFT to reconstruct the image.
5. Display and compare:
  - Original image
  - Sharpened outputs
  - Their corresponding magnitude spectra

### Analysis:

- Compare edge enhancement and noise amplification.
- Which filter gives sharp results without introducing strong artifacts? Explain.

### Code:

```
Assignment4.py × Assignment3.py
Assignment4.py > ...
1  import numpy as np
2  import matplotlib.pyplot as plt
3  from skimage import data
4
5  # Load grayscale image
6  image = data.camera()
7
8  # Step 1: Fourier Transform
9  dft = np.fft.fft2(image)
10 dft_shift = np.fft.fftshift(dft)
11 magnitude_spectrum = 20 * np.log(np.abs(dft_shift) + 1)
12
13 # Step 2: Prepare Distance Matrix
14 M, N = image.shape
15 u = np.arange(M)
16 v = np.arange(N)
17 U, V = np.meshgrid(u, v, indexing='ij')
18 D = np.sqrt((U - M//2)**2 + (V - N//2)**2)
19
20 # Step 3: Define Highpass Filters
21 D0 = 50
22 n = 2 # Butterworth order
23
24 # Ideal Highpass Filter
25 H_ihpf = np.ones((M, N))
```

```

Assignment4.py > ...
25 H_ihpf = np.ones((M, N))
26 H_ihpf[D <= D0] = 0
27
28 # Butterworth Highpass Filter
29 H_bhpf = 1 / (1 + (D0 / (D + 1e-5))**(2 * n)) # Add small epsilon to avoid div/0
30
31 # Gaussian Highpass Filter
32 H_ghpf = 1 - np.exp(-(D**2) / (2 * D0**2))
33
34 # Step 4: Apply Filters in Frequency Domain
35 filtered_ihpf = dft_shift * H_ihpf
36 filtered_bhpf = dft_shift * H_bhpf
37 filtered_ghpf = dft_shift * H_ghpf
38
39 # Step 5: Compute magnitude spectra of filtered images
40 mag_ihpf = 20 * np.log(np.abs(filtered_ihpf) + 1)
41 mag_bhpf = 20 * np.log(np.abs(filtered_bhpf) + 1)
42 mag_ghpf = 20 * np.log(np.abs(filtered_ghpf) + 1)
43
44 # Step 6: Inverse FFT to get sharpened images
45 sharpened_ihpf = np.abs(np.fft.ifft2(np.fft.ifftshift(filtered_ihpf)))
46 sharpened_bhpf = np.abs(np.fft.ifft2(np.fft.ifftshift(filtered_bhpf)))
47 sharpened_ghpf = np.abs(np.fft.ifft2(np.fft.ifftshift(filtered_ghpf)))
48
49 # =====
50 # Figure 1: Original Image + Spectrum
51 # =====
52 plt.figure(figsize=(10, 5))
53
54 plt.subplot(1, 2, 1)
55 plt.imshow(image, cmap='gray')
56 plt.title('Original Image')
57 plt.axis('off')
58
59 plt.subplot(1, 2, 2)
60 plt.imshow(magnitude_spectrum, cmap='viridis')
61 plt.title('Original Spectrum')
62 plt.axis('off')
63
64 plt.tight_layout()
65
66
67 # =====
68 # Figure 2: IHPF Image + Spectrum
69 # =====
70 plt.figure(figsize=(10, 5))
71
72 plt.subplot(1, 2, 1)
73 plt.imshow(sharpened_ihpf, cmap='gray')
74 plt.title('IHPF Filtered')

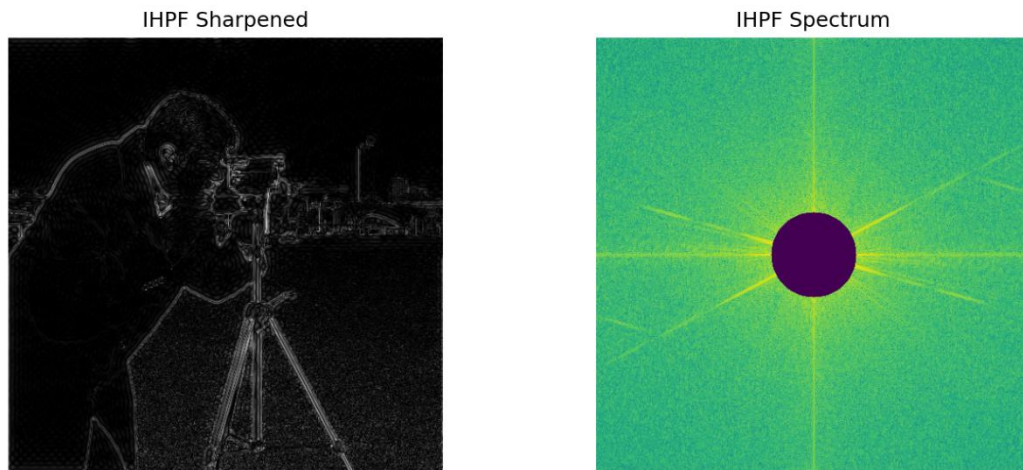
```

```

74 plt.title('ILPF Filtered')
75 plt.axis('off')
76
77 plt.subplot(1, 2, 2)
78 plt.imshow(mag_ihpf, cmap='viridis')
79 plt.title('ILPF Spectrum')
80 plt.axis('off')
81
82 plt.tight_layout()
83
84 # =====
85 # Figure 3: BHPF Image + Spectrum
86 # =====
87 plt.figure(figsize=(10, 5))
88
89 plt.subplot(1, 2, 1)
90 plt.imshow(sharpened_bhpf, cmap='gray')
91 plt.title('BLPF Filtered (n=2)')
92 plt.axis('off')
93
94 plt.subplot(1, 2, 2)
95 plt.imshow(mag_bhpf, cmap='viridis')
96 plt.title('BLPF Spectrum')
97 plt.axis('off')
98
99 plt.tight_layout()
100
101 # =====
102 # Figure 4: GHPF Image + Spectrum
103 # =====
104 plt.figure(figsize=(10, 5))
105
106 plt.subplot(1, 2, 1)
107 plt.imshow(sharpened_ghpf, cmap='gray')
108 plt.title('GLPF Filtered')
109 plt.axis('off')
110
111 plt.subplot(1, 2, 2)
112 plt.imshow(mag_ghpf, cmap='viridis')
113 plt.title('GLPF Spectrum')
114 plt.axis('off')
115
116 plt.tight_layout()
117
118 # Show all figures
119 plt.show()
120

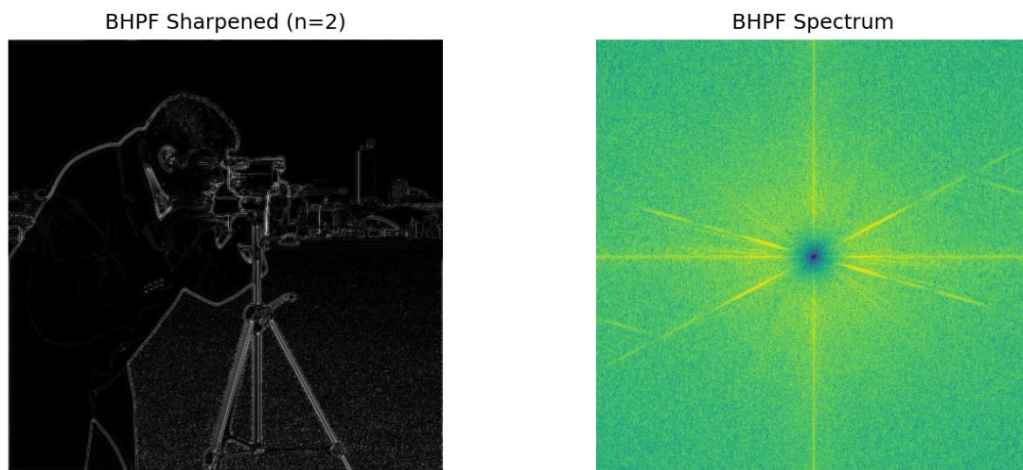
```

**Output:**



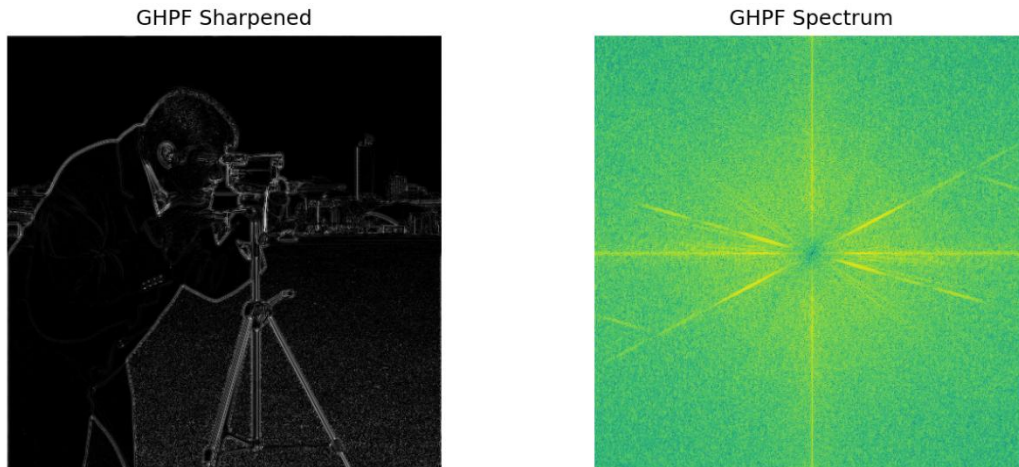
**Figure 1: Ideal Highpass Filter (IHPF) Output and Spectrum**

*The left image shows the result of applying an Ideal Highpass Filter with cutoff  $D_0=50$ . This filter removes all low-frequency components below the cutoff sharply, enhancing edges and fine details. The right image displays the filtered magnitude spectrum, showing a ring-like pattern due to the ideal circular cutoff.*



**Figure 2: Butterworth Highpass Filter (BHPF) Output and Spectrum**

*This figure shows the result of applying a second-order Butterworth Highpass Filter. Compared to IHPF, BHPF provides a smoother transition between low and high frequencies, avoiding sharp artifacts. The corresponding spectrum shows a gradual suppression of central (low-frequency) components.*



**Figure 3: Gaussian Highpass Filter (GHPF) Output and Spectrum**

*The Gaussian Highpass Filter offers the smoothest frequency attenuation among the three. The output image exhibits edge enhancement with minimal ringing artifacts. The spectrum on the right shows a soft, radial attenuation around the center, consistent with the Gaussian function.*

## **Analysis:**

### **Ideal High-Pass Filter (IHPF)**

The sharpened image using the Ideal High-Pass Filter exhibits strong edge enhancement. However, this comes at the cost of introducing ringing artifacts, especially around high-contrast boundaries. The frequency spectrum of the IHPF clearly shows a hard cutoff, with the central low-frequency region completely removed. This abrupt transition causes the Gibbs phenomenon, leading to unnatural visual artifacts in the filtered image.

### **Butterworth High-Pass Filter (BHPF)**

The image processed with the Butterworth High-Pass Filter shows smoother and more natural sharpening. It enhances edges without introducing the harsh ringing seen with IHPF. The filter's spectrum illustrates a gradual attenuation of low frequencies, avoiding the sharp cutoff and thereby reducing spatial domain distortions. This smooth frequency transition helps maintain visual quality while still sharpening the image effectively.

### **Gaussian High-Pass Filter (GHPF)**

The Gaussian High-Pass Filter provides the most balanced and visually pleasing result among the three. It gently enhances image details and edges without introducing significant artifacts or distortions. The associated frequency spectrum shows an even smoother transition, reflecting the exponential decay of

the Gaussian function. This leads to a natural-looking enhancement, preserving both fine detail and overall image coherence.

## **Conclusion**

Among the three high-pass filters, the Gaussian High-Pass Filter (GHPF) delivers the best trade-off between edge enhancement and artifact avoidance. While the Ideal filter is aggressive and introduces noticeable ringing, and the Butterworth filter offers a compromise, the GHPF achieves visually appealing results with minimal side effects. For applications requiring both detail sharpening and artifact-free output, GHPF is the most effective choice.