## **Time Domain Modelling in MATLAB**

**LAB # 07** 



# Fall 2024 CSE-310L Control Systems Lab

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Class Section: C

"On my honor, as student of University of Engineering and Technology, I have neither given nor received unauthorized assistance on this academic work."

Submitted to:

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Date:

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## **Objectives:**

The objective of this lab is to:

• model the system in time domain.

## **State Space Representation:**

State Space representation is one of the unified method for modeling, analyzing and designing a wide range of systems.

6.1 Use the MATLAB code to form an LTI state space representation from the transfer function. The matrix A, B and C are shown below.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -24 & -26 & -9 \end{bmatrix} \quad \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} r$$

$$y = \begin{bmatrix} b_0 & b_1 & b_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 & 7 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

## **Code:**

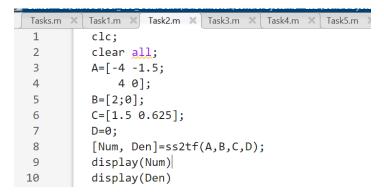
```
A = [0 \ 1 \ 0;
 1
 2
          0 0 1;
          -24 -26 -9];
 3
 4
 5
        B = [0; 0; 1];
        C = [2 7 1];
 6
 7
        D = 0;
        [Num, Den]=ss2tf(A,B,C,D);
 8
 9
        display(Num)
        display(Den)
10
```

#### **Output:**

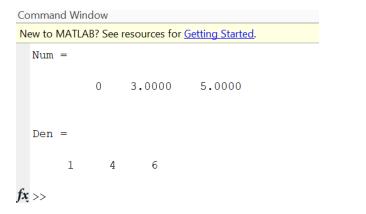
6.2 Use the MATLAB to convert the state space representation to the transfer function for the following

$$\mathbf{x} = \begin{bmatrix} -4 & -1.5 \\ 4 & 0 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 2 \\ 0 \end{bmatrix} u(t)$$
$$y = \begin{bmatrix} 1.5 & 0.625 \end{bmatrix} \mathbf{x}$$

## Code:



### **Output:**



6.3 Write the MATLAB code for the conversion of transfer function to the state space representation of the following system

$$\begin{array}{c|c}
R(s) & 8s+10 & C(s) \\
\hline
s^4 + 5s^3 + s^2 + 5s + 13 & \end{array}$$

## Code:

```
Editor - D:\GitHUb\UET_CSE_DataPack4\7thSemester\Control Systems - Lab\Contro
 Tasks.m X Task1.m X Task2.m X Task3.m X Task4.m X Task5
 1
            num3=[0 0 0 0 8 10];
 2
            denum3=[1 5 1 5 13];
            [A3,B3,C3,D3] = tf2ss(num3,denum3);
 3
 4
            display(A3)
 5
            display(B3)
 6
            display(C3)
 7
            display(D3)
```

## **Output:**

```
>> Task3
 A3 =
    -5
        -1
             -5 -13
         0
              0
                0
     1
         1
             0
                  0
            1
 B3 =
     1
     0
     0
 C3 =
     0
        0 8 10
D3 =
```

**6.4** Write the MATLAB code for the conversion of transfer function to the state space representation of the following system

$$\begin{array}{c|c}
R(s) & s^4 + 2s^3 + 12s^2 + 7s + 6 \\
\hline
s^5 + 9s^4 + 13s^3 + 8s^2
\end{array}$$

### Code:

```
Editor - D:\GitHUb\UET_CSE_DataPack4\7thSemester\Control Systems - Lab\ControlSystem
Tasks.m X Task1.m X Task2.m X Task3.m X Task4.m X Task5.m
           num4=[0 1 2 12 7 6];
 1
 2
           denum4=[1 9 13 8 0 0];
           [A4,B4,C4,D4] = tf2ss(num4,denum4);
 3
 4
           display(A4)
 5
           display(B4)
 6
           display(C4)
 7
           display(D4)
```

## **Output:**

6.5 Write the MATLAB code for the conversion of state space representation to the transfer function for the following

$$\dot{\mathbf{x}} = \begin{bmatrix} 0 & 1 & 5 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -7 & -9 & -2 & -3 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 5 \\ 8 \\ 2 \end{bmatrix} \mathbf{r}$$
$$\mathbf{y} = \begin{bmatrix} 1 & 3 & 6 & 6 \end{bmatrix} \mathbf{x}$$

#### Code:

```
Task1.m × Task2.m × Task3.m × Task4.m ×
                                                 Task5.m
Tasks.m
 1
          A = [0 \ 1 \ 5 \ 0;
 2
                 0 0 1 0;
 3
                 0001;
                 -7 -9 -2 -3];
 4
 5
          B = [0; 5; 8; 2];
 6
          C = [1 \ 3 \ 6 \ 6];
 7
          D = 0;
 8
          [Num, Den]=ss2tf(A,B,C,D);
 9
          display(Num)
10
          display(Den)
```

## **Output:**

```
>> Task5
Num = 1.0e+03 *

0 0.0750 -0.0960 -2.3310 -0.2100

Den = 1.0000 3.0000 2.0000 44.0000 7.0000
```

# 6.6 Write the MATLAB code for the conversion of state space representation to the transfer function for the following

$$\dot{\mathbf{x}} = \begin{bmatrix} 3 & 1 & 0 & 4 & -2 \\ -3 & 5 & -5 & 2 & -1 \\ 0 & 1 & -1 & 2 & 8 \\ -7 & 6 & -3 & -4 & 0 \\ -6 & 0 & 4 & -3 & 1 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 2 \\ 7 \\ 8 \\ 5 \\ 4 \end{bmatrix} \mathbf{r}$$
$$\mathbf{y} = \begin{bmatrix} 1 & -2 & -9 & 7 & 6 \end{bmatrix} \mathbf{x}$$

## **Code:**

```
🚪 Editor - D:\GitHUb\UET_CSE_DataPack4\7thSemester\Control Systems - Lab\ControlSystemLab7\Task6.m
  Tasks.m × Task1.m × Task2.m × Task3.m × Task4.m × Task5.m × Task6.m ×
  1
            A = [3 \ 1 \ 0 \ 4 \ -2;
                   -3 5 -5 2 -1;
  2
  3
                   0 1 -1 2 8;
  4
                   -7 6 -3 -4 0;
  5
                   -6 0 4 -3 1];
            B = [27854]';
  6
  7
            C = [1 -2 -9 7 6];
  8
            D = 0;
  9
            [Num, Den]=ss2tf(A,B,C,D);
            display(Num)
 10
 11
            display(Den)
```

## **Output:**

```
>> Task6
Num =

1.0e+04 *

0 -0.0025 -0.0292 0.1680 1.6282 3.1875

Den =

1.0e+03 *

0.0010 -0.0040 -0.0320 0.1480 -1.1530 -4.4800

>>
```