## Solution 10

3.1

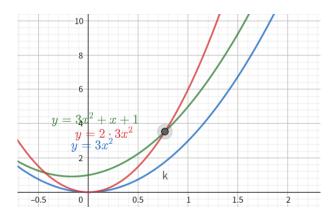
- 02. a) Lack finiteness.(The **while** loop lasts forerver.)
  - b) Lack effectiveness. (When n = 0, m := 1/n can not be computed.)
  - c) Lack definiteness. (i is not be definited.)
  - d) Lack definiteness.(It isn't determined.)
- 56. Each selection does not exceed the maximum number of current amounts.
  - a) Three quarters, leaving 12 cents. One dime, leaving 2 cents. Two pennies.
  - b) One quarter, leaving 24 cents. Two dimes, leaving 4 cents. Four pennies.
  - c) Three quarters, leaving 24 cents. Two dimes, leaving 4 cents. Four pennies.
  - d) One quarter, leaving 8 cents. One nickel, leaving 3 cents. Three pennies.

3.2

34. a)

$$x > 0, 3x^{2} \le 3x^{2} + x + 1$$
$$x > 1, 3x^{2} + x + 1 \le 2 \cdot 3x^{2}$$
$$1 \cdot 3x^{2} \le 3x^{2} + x + 1 \le 2 \cdot 3x^{2}$$

So, 
$$C_1 = 1, C_2 = 2, k = 1$$
  
b)  $k(\frac{\sqrt{13} + 1}{6}, \frac{\sqrt{13} + 7}{3})$ 



73.

$$\therefore n \leqslant (n-k)(k+1)$$

$$\therefore n^n \leqslant n((n-1)\cdot 2)\cdot ((n-2)\cdot 3)\cdots (2\cdot (n-1))\cdot n = (n!)^2$$

$$\therefore \log n! \leqslant n \log n \leqslant 2 \log n!$$

So,  $n \log n$  is  $O(\log n!)$ .

74. By 73.,  $n \log n$  is  $O(\log n!)$ .

$$\therefore n! \leqslant n^n$$
$$\therefore \log n! \leqslant n \log n$$

So,  $\log n!$  is  $O(n \log n)$ . So,  $\log n!$  is  $\Theta(n \log n)$ .

## 3.3

40. **procedure** change $(c_1, c_2, \ldots, c_r)$ : coin denominations; n: a positive integer) for i := 1 to r  $d_i := 0$ while  $n \ge c_i$   $d_i := d_i + 1$   $n := n - c_i$ 

The algorithm uses comparison of denominations of coins which is positive integer. Any positive integer is O(n). Each comparison takes some time, and there are at most n comparisons, since every comparison all decrease the number. Therefore, the greedy algorithm has O(n) complexity measured in terms of comparison needed.