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# Flow in O2 with the Generic Framework

O2 hands-on tutorial  
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THE VELUX FOUNDATIONS

VILLUM FONDEN  VELUX FONDEN



- ❖ What is the Generic Framework?
- ❖ The Generic Framework in O2
  - Initialisation
  - Correlator configurations
  - Filling and calculating correlations
- ❖ Walkthrough of the skeleton code
- ❖ Exercises

These slides, shell commands and solutions to the exercises can be found in

<https://github.com/AliceO2Group/analysis-tutorials/tree/master/o2at-2/PWGCF/GenericFramework>



# The Generic Framework

- ❖ Calculate m-particle correlations with recursive formula fast and exact

$$\begin{aligned} \langle m \rangle_{n_1, n_2, \dots, n_m} &\equiv \left\langle e^{i(n_1 \varphi_{k_1} + n_2 \varphi_{k_2} + \dots + n_m \varphi_{k_m})} \right\rangle \\ &\equiv \frac{\sum_{\substack{k_1, k_2, \dots, k_m=1 \\ k_1 \neq k_2 \neq \dots \neq k_m}}^M w_{k_1} w_{k_2} \dots w_{k_m} e^{i(n_1 \varphi_{k_1} + n_2 \varphi_{k_2} + \dots + n_m \varphi_{k_m})}}{\sum_{\substack{k_1, k_2, \dots, k_m=1 \\ k_1 \neq k_2 \neq \dots \neq k_m}}^M w_{k_1} w_{k_2} \dots w_{k_m}}. \end{aligned} \quad (7)$$

- ❖ Denominator trivially related to numerator

$$N\langle m \rangle_{n_1, n_2, \dots, n_m} \equiv \sum_{\substack{k_1, k_2, \dots, k_m=1 \\ k_1 \neq k_2 \neq \dots \neq k_m}}^M w_{k_1} w_{k_2} \dots w_{k_m} e^{i(n_1 \varphi_{k_1} + n_2 \varphi_{k_2} + \dots + n_m \varphi_{k_m})}, \quad (16)$$

$$D\langle m \rangle_{n_1, n_2, \dots, n_m} \equiv \sum_{\substack{k_1, k_2, \dots, k_m=1 \\ k_1 \neq k_2 \neq \dots \neq k_m}}^M w_{k_1} w_{k_2} \dots w_{k_m} \quad (17)$$

$$= N\langle m \rangle_{0, 0, \dots, 0}. \quad (18)$$

## Generic framework for anisotropic flow analyses with multi-particle azimuthal correlations

Ante Bilandzic,<sup>1</sup> Christian Holm Christensen,<sup>1</sup> Kristjan Gulbrandsen,<sup>1</sup> Alexander Hansen,<sup>1</sup> and You Zhou<sup>2,3</sup>

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(Dated: December 23, 2013)

We present a new generic framework which enables exact and fast evaluation of all multi-particle azimuthal correlations. The framework can be readily used along with a correction framework for systematic biases in anisotropic flow analyses due to various detector inefficiencies. A new recursive algorithm has been developed for higher order correlators for the cases where their direct implementation is not feasible. We propose and discuss new azimuthal observables for anisotropic flow analyses which can be measured for the first time with our new framework. The effect of finite detector granularity on multi-particle correlations is quantified and discussed in detail. We point out the existence of a systematic bias in traditional differential flow analyses which stems solely from the applied selection criteria on particles used in the analyses, and is also present in the ideal case when only flow correlations are present. Finally, we extend the applicability of our generic framework to the case of differential multi-particle correlations.

PACS numbers: 25.75.Ld, 25.75.Gz, 05.70.Fh

## Recursive algorithm

```

N⟨1⟩n1': return Qn1,1
N⟨m⟩n1,...,nm':
  C ← 0
  for k ← (m - 1), 1 do
    for each combination c = {c1, ..., ck} of {n1, ..., nm-1} do
      q ← ∑j not in c nj
      C ← C + (-1)m-k (m - k - 1)! × N⟨k⟩c1,...,ck' × Qq,m-k
    end for each c
  end for k
  return C .

```



# Initialisation

- ❖ The GFW class is a fast, reliable and easy to use c++ class

```
GFW* fGFW = new GFW();
```

Initialise like any c++ object

- ❖ Works with 'regions' of  $\eta$

Name of region    $\eta_{\min}$     $\eta_{\max}$     $N_{p_T}$    Bitmask

```
fGFW->AddRegion("full", -0.8, 0.8, 1, 1);
```

- ❖ Specify the desired correlations in the correlator configurations

Name of region   Harmonics   Correlator name    $p_T$  flag

```
corrconfigs.push_back(fGFW->GetCorrelatorConfig("full {2 -2}", "ChFull22", kFALSE));
```

- ❖ Finalize the initialisation with `fGFW->CreateRegions();`

More documentation at  
[https://github.com/vvislavi/GFW\\_Core](https://github.com/vvislavi/GFW_Core)



# Correlator configurations

- ❖ The general syntax for a single subevent is

“[POI] Ref [ | Overlap] {harm1[,harm2,...,harmN]}”

- ❖ Example: calculating  $p_T$ -differential flow

Define the required regions

```
fGFW->AddRegion("refN", -0.8, -0.4, 1, 1);  
fGFW->AddRegion("refP", 0.4, 0.8, 1, 1);  
fGFW->AddRegion("poiN", -0.8, -0.4, 1+fPtAxis->GetNbins(), 2);  
fGFW->AddRegion("olN", -0.8, -0.4, 1, 4);
```

Note: bitmasks for POI (2) and overlap (4) are different from ref (1), so that we can fill them with the correct particles

Fill the correlator configs, while specifying the POI and overlap

```
corrconfigs.push_back(fGFW->GetCorrelatorConfig("refN {2} refP {-2}", "ChGap22", kFALSE));  
corrconfigs.push_back(fGFW->GetCorrelatorConfig("poiN refN | olN {2} refP {-2}", "ChGap22", kTRUE));
```

More documentation at  
[https://github.com/vvislavi/GFW\\_Core](https://github.com/vvislavi/GFW_Core)



# Filling and calculating with the GFW

- ❖ Fill the GFW in the track loop

$\eta$        $p_T$  bin       $\varphi$       NUA/NUE      Bitmask

```
fGFW->Fill(track.eta(), 1, track.phi(), wacc * weff, 1);
```

- ❖ If we have POI then we can fill according to the bitmasks with some additional selection

```
bool WithinPtPOI = (cfgCutPtPOIMin<pt) && (pt<cfgCutPtPOIMax); //within POI pT range
bool WithinPtRef  = (cfgCutPtMin<pt) && (pt<cfgCutPtMax);    //within RF pT range
if(WithinPtRef) fGFW->Fill(track.eta(), fPtAxis->FindBin(pt)-1, track.phi(), wacc * weff, 1);
if(WithinPtPOI) fGFW->Fill(track.eta(), fPtAxis->FindBin(pt)-1, track.phi(), wacc * weff, 2);
if(WithinPtPOI && WithinPtRef) fGFW->Fill(track.eta(), fPtAxis->FindBin(pt)-1, track.phi(), wacc * weff, 4);
```

- ❖ Calculating the correlation values

Correlator config     $p_T$  bin    Harms to zero flag

```
dnx = fGFW->Calculate(corrconf, 0, kTRUE).real();
```

```
val = fGFW->Calculate(corrconf, 0, kFALSE).real()/dnx;
```

- ❖ This can then be filled in e.g. TProfile

More documentation at  
[https://github.com/vvislavi/GFW\\_Core](https://github.com/vvislavi/GFW_Core)



# Skeleton code

```
struct GfwTutorial {

    02_DEFINE_CONFIGURABLE(cfgCutVertex, float, 10.0f, "Accepted z-vertex range")
    02_DEFINE_CONFIGURABLE(cfgCutPtPOIMin, float, 0.2f, "Minimal pT for poi tracks")
    02_DEFINE_CONFIGURABLE(cfgCutPtPOIMax, float, 10.0f, "Maximal pT for poi tracks")
    02_DEFINE_CONFIGURABLE(cfgCutPtMin, float, 0.2f, "Minimal pT for ref tracks")
    02_DEFINE_CONFIGURABLE(cfgCutPtMax, float, 3.0f, "Maximal pT for ref tracks")
    02_DEFINE_CONFIGURABLE(cfgCutEta, float, 0.8f, "Eta range for tracks")
    02_DEFINE_CONFIGURABLE(cfgCutChi2prTPCcls, float, 2.5, "Chi2 per TPC clusters")
    02_DEFINE_CONFIGURABLE(cfgUseNch, bool, false, "Use Nch for flow observables")
    02_DEFINE_CONFIGURABLE(cfgNbootstrap, int, 10, "Number of subsamples")

    ConfigurableAxis axisVertex{"axisVertex", {20, -10, 10}, "vertex axis for histograms"};
    ConfigurableAxis axisPhi{"axisPhi", {60, 0.0, constants::math::TwoPI}, "phi axis for histograms"};
    ConfigurableAxis axisEta{"axisEta", {40, -1., 1.}, "eta axis for histograms"};
    ConfigurableAxis axisPt{"axisPt", {VARIABLE_WIDTH, 0.2, 0.25, 0.30, 0.40, 0.45, 0.50, 0.55, 0.60, 0.65, 0.70, 0.75,
    0.80, 0.85, 0.90, 0.95, 1.00, 1.10, 1.20, 1.30, 1.40, 1.50, 1.60, 1.70, 1.80, 1.90, 2.00, 2.20, 2.40, 2.60, 2.80, 3.00}, "pt axis for histograms"};
    ConfigurableAxis axisMultiplicity{"axisMultiplicity", {VARIABLE_WIDTH, 0, 5, 10, 20, 30, 40, 50, 60, 70, 80, 90}, "centrality axis for histograms"};

    Filter collisionFilter = nabs(aod::collision::posZ) < cfgCutVertex;
    Filter trackFilter = (nabs(aod::track::eta) < cfgCutEta) && (aod::track::pt > cfgCutPtMin) && (aod::track::pt < cfgCutPtMax) &&
    ((requireGlobalTrackInFilter()) || (aod::track::isGlobalTrackSDD == (uint8_t) true)) && (aod::track::tpcChi2NCl < cfgCutChi2prTPCcls);

    // Connect to ccdb
    Service<ccdb::BasicCCDBManager> ccdb;
    Configurable<int64_t> nolaterthan{"ccdb-no-later-than", std::chrono::duration_cast<std::chrono::milliseconds>(std::chrono::system_clock::now().
    time_since_epoch()).count(), "latest acceptable timestamp of creation for the object"};
    Configurable<std::string> url{"ccdb-url", "http://ccdb-test.cern.ch:8080", "url of the ccdb repository"};

    // Define output
    HistogramRegistry registry{"registry"};

    // define global variables
    GFW* fGFW = new GFW();
    std::vector<GFW::CorrConfig> corrconfigs;

    using aodCollisions = soa::Filtered<soa::Join<aod::Collisions, aod::EvSels, aod::CentRun2V0Ms>>;
    using aodTracks = soa::Filtered<soa::Join<aod::Tracks, aod::TrackSelection, aod::TracksExtra>>;
```

Configurables  
(Can be overwritten in  
the configuration.json)

Track and collision filters

Output objects and  
gobal variables

aliases for tracks and  
collision tables



# Skeleton code

```
void init(InitContext const&)
{
    ccdb->setURL(url.value);
    ccdb->setCaching(true);
    ccdb->setCreatedNotAfter(nolaterthan.value);

    // Add some output objects to the histogram registry
    registry.add("hPhi", "", {HistType::kTH1D, {axisPhi}});
    registry.add("hEta", "", {HistType::kTH1D, {axisEta}});
    registry.add("hVtxZ", "", {HistType::kTH1D, {axisVertex}});
    registry.add("hMult", "", {HistType::kTH1D, {{3000, 0.5, 3000.5}}});
    registry.add("hCent", "", {HistType::kTH1D, {{90, 0, 90}}});
    registry.add("c22", "", {HistType::kTProfile, {axisMultiplicity}});

    fGFW->AddRegion("full", -0.8, 0.8, 1, 1);
    corrconfigs.push_back(fGFW->GetCorrelatorConfig("full {2 -2}", "ChFull22", kFALSE));
    fGFW->CreateRegions();
}
```

Initialise objects in the  
histogram registry

Initialise the GFW



# Skeleton code

```
void process(aodCollisions::iterator const& collision, aod::BCsWithTimestamps const&, aodTracks const& tracks)
{
    int Ntot = tracks.size();
    if (Ntot < 1)
        return;
    if (!collision.sel7())
        return;
    float vtxz = collision.posZ();
    registry.fill(HIST("hVtxZ"), vtxz);
    registry.fill(HIST("hMult"), Ntot);
    registry.fill(HIST("hCent"), collision.centRun2V0M());
    fGFW->Clear();
    const auto cent = collision.centRun2V0M();
    float weff = 1, wacc = 1;
    for (auto& track : tracks) {
        registry.fill(HIST("hPhi"), track.phi());
        registry.fill(HIST("hEta"), track.eta());

        fGFW->Fill(track.eta(), 1, track.phi(), wacc * weff, 1);
    }

    // Filling c22 with ROOT TProfile
    FillProfile(corrconfigs.at(0), HIST("c22"), cent);
}
```

Track loop

Fill the GFW

Fill correlation values



# Skeleton code

```
template <char... chars>
void FillProfile(const GFW::CorrConfig& corrconf, const ConstStr<chars...>& tarName, const double& cent)
{
    double dnx, val;
    dnx = fGFW->Calculate(corrconf, 0, kTRUE).real();
    if (dnx == 0)
        return;
    if (!corrconf.pTDif) {
        val = fGFW->Calculate(corrconf, 0, kFALSE).real() / dnx;
        if (TMath::Abs(val) < 1)
            registry.fill(tarName, cent, val, dnx);
        return;
    }
    return;
}
```

Calculate normalisation

Check for division by zero

Calculate correlation value

Fill TProfile



# Running the task

- ❖ The provided scripts will take care of downloading and running the tasks with the correct configurations
- ❖ Download AO2D data files with the downloadAOD.sh script

```
$> sh downloadAOD.sh
```

- ❖ Run the task with the run.sh script

```
$> sh run.sh
```

- ❖ To run on Run3 data specify <run3> as argument - will only work if the proper adjustments have been made in the task

```
$> sh downloadAOD.sh run3
```

```
$> sh run.sh run3
```



1. Add more correlations to calculate  $v_3$ ,  $v_4$ ,  $v_2\{4\}$ , etc.

*Add new correlation configurations*

2. Add subevents with varying  $|\eta|$  gaps

*Add new regions*

3. Add  $p_T$ -differential flow

*Add regions for POI, reference and overlap*

4. Run the previous exercises on run3 data

*Use the appropriate configuration and data file*

*Change to a run3 centrality estimator (FT0C) and remove trigger selection*

5. Add PID flow

*Add PID tables to the tracks*

6. (Optional) Run a flow analysis using the FlowContainer to store the correlations



- ❖ Container that holds the correlations in 2D histogram (correlator config. vs centrality)
  - Handles cumulants calculations,  $v_n$  calculations, subsamples for bootstrapping, etc.

- ❖ Initialise the FlowContainer

```
TObjArray* oba = new TObjArray();
oba->Add(new TNamed("ChGap22", "ChGap22"));
for(Int_t i=0;i<fPtAxis->GetNbins();i++)
|   oba->Add(new TNamed(Form("ChGap22_pt_%i",i+1),"ChGap22_pTDiff"));
fFC->SetName("FlowContainer");
fFC->SetXAxis(fPtAxis);
fFC->Initialize(oba, axisMultiplicity, cfgNbootstrap);
delete oba;
```

ObjArray holds each correlator

For  $p_T$ -differential we add each  $p_T$  bin

Setting name and X-axis for  $p_T$ -differential

Initialise with the ObjArray, centrality axis, and number of subsamples

- ❖ Fill the flow container

Correlator config name

Value

Random number for subsamples

```
fFC->FillProfile(corrconf.Head.c_str(), cent, val, dnx, rndm);
```

Centrality

Normalisation



❖ After receiving the analysis output file

- Fetch the FlowContainer from the file

```
FlowContainer* fc = (FlowContainer*)f->Get("gfw-tutorial/FlowContainer");
```

- Set the name for the current ID

```
fc->SetIDName("ChGap");
```

- If not using bootstrap errors, set propagation of errors

```
fc->SetPropagateErrors(kTRUE);
```

❖ Callers for getting most common observables

```
TH1D* GetVN2VsMulti(int n = 2, int l_pta = 0)
TH1D* GetVN2VsPt(int n = 2, double min = -1, double max = -1)
TH1D* GetCN4VsMulti(int n = 2, int pti = 0)
TH1D* GetCN4VsPt(int n = 2, double min = -1, double max = -1)
TH1D* GetVN4VsMulti(int n = 2, int pti = 0)
TH1D* GetVN4VsPt(int n = 2, double min = -1, double max = -1)
TH1D* GetVN6VsMulti(int n = 2, int pti = 0)
TH1D* GetVN6VsPt(int n = 2, double min = -1, double max = -1)
TH1D* GetVN8VsMulti(int n = 2, int pti = 0)
TH1D* GetVN8VsPt(int n = 2, double min = -1, double max = -1)
```

Example



$p_T$ -integrated  $v_2$  as function of centrality

```
TH1D* hV22 = fc->GetVN2VsMulti(2);
TH1D* hV22pt_gap = fc->GetVN2VsPt(2, 0, 4.9);
```

$p_T$ -differential  $v_2$  in 0-5% centrality

❖ Callers for getting just the correlations

```
TH1D* GetHistCorrXXVsMulti(const char* order, int l_pti = 0)
TH1D* GetHistCorrXXVsPt(const char* order, double lminmulti = -1, double lmaxmulti = -1)
```