

Oral Presentation:

전산재료과학



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창원컨벤션센터(CECO)



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**Computational analysis on quantum diffusivity of hydrogen in bcc iron:
Application of machine learning interatomic potential**

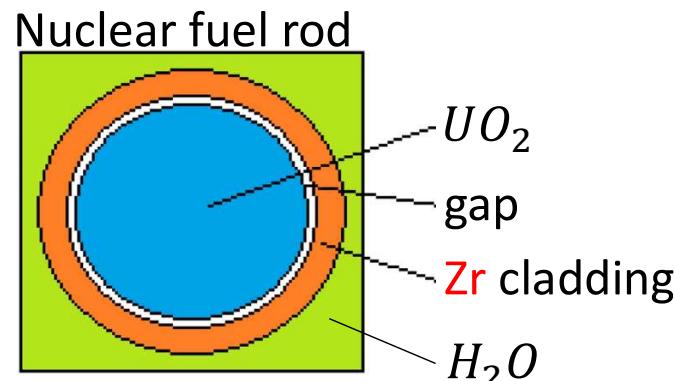
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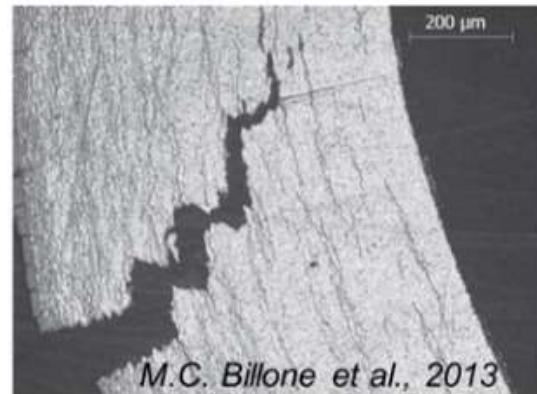
Introduction

■ Hydrogen and nuclear engineering

- Nuclear materials are always exposed to hydrogen gas.



Corrosion Reaction



Corrosion reaction of Zr cladding in nuclear reactor

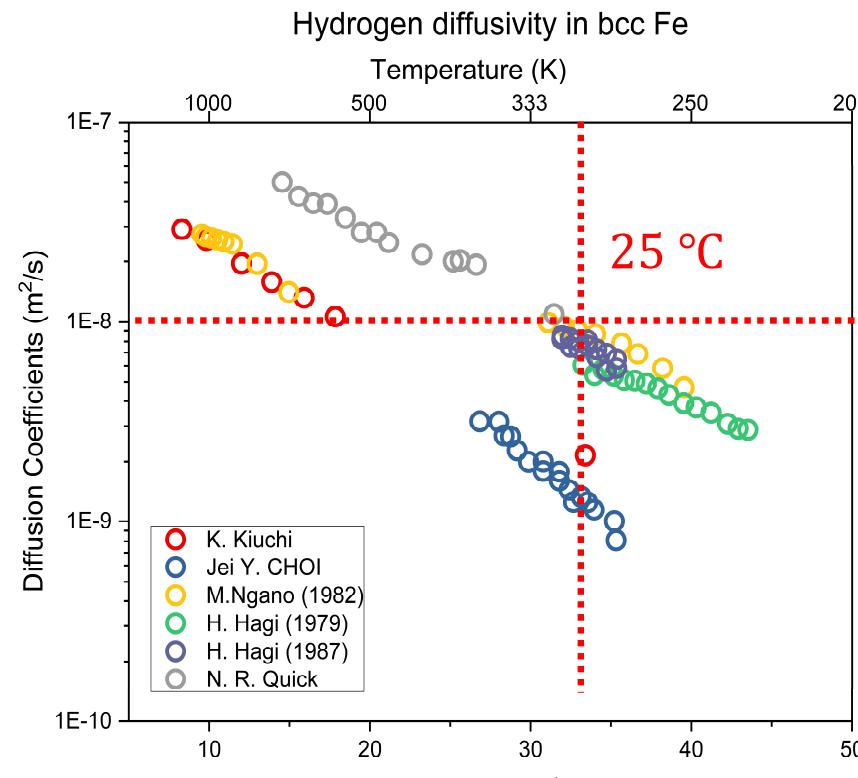




Introduction

■ Hydrogen diffusivity in metals

- Generally, hydrogen diffusivity in metals is so large that their mechanical properties can be degraded.



If $D \cong 10^{-8} m^2 s^{-1}$ at room temperature,

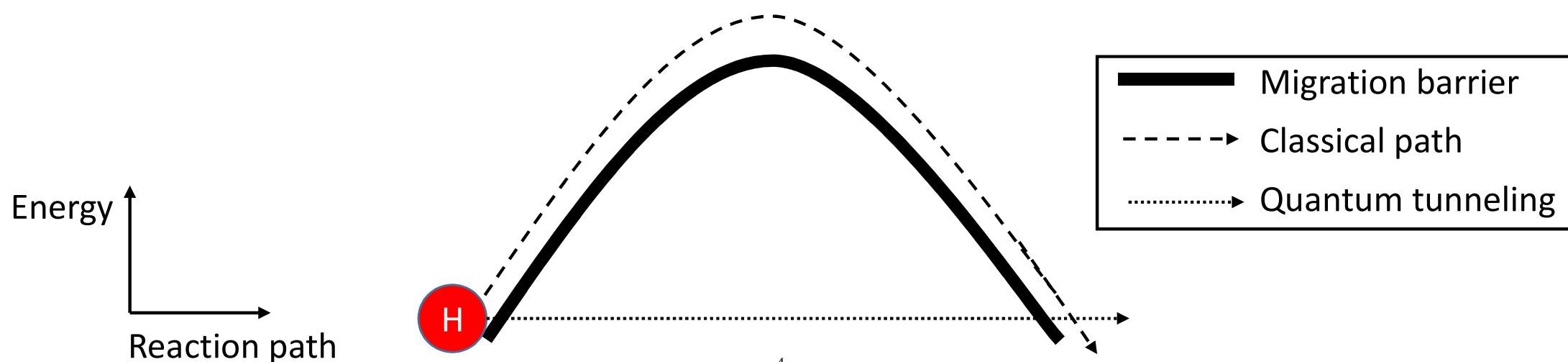
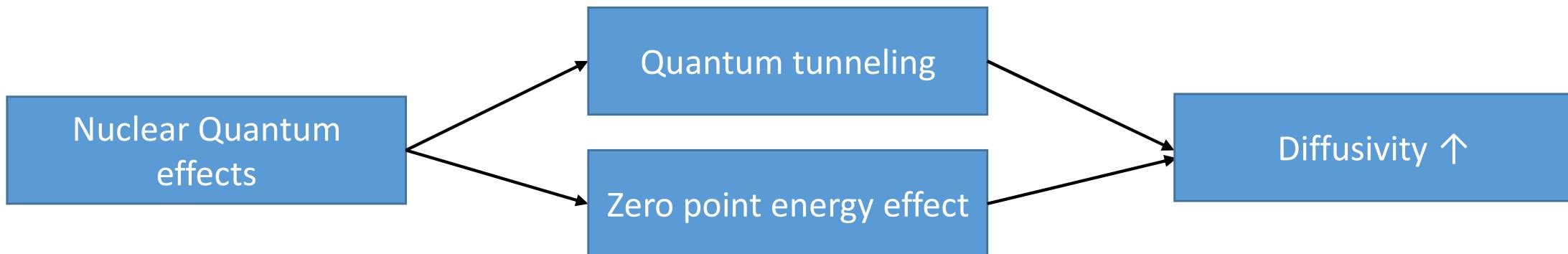
average migration distance per H atom is around **3 cm per day (1 m per month)**



Introduction

■ Nuclear Quantum Effects (NQEs)

- Light nuclei sometimes show considerable quantum effects even at room temperature.



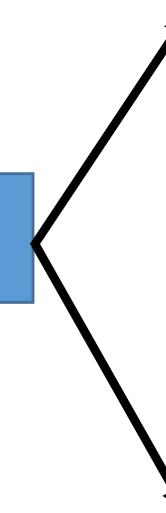


Introduction

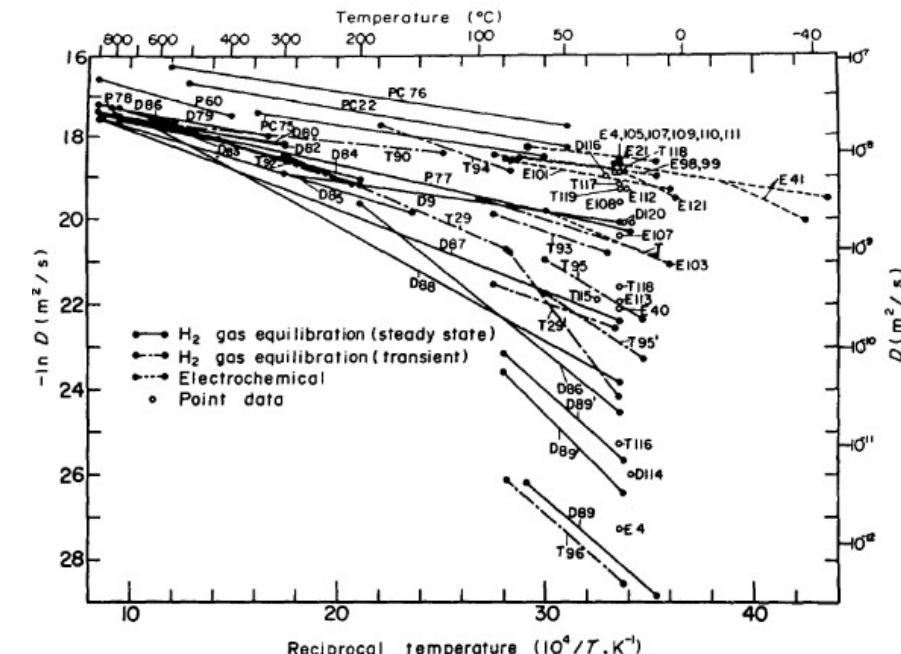
■ Preceding research about H diffusion in metals

Preceding research

Experiments:
Too scattered



Computation:
path integral theory



H diffusivity in bcc iron (Ref. [7])



Ab-initio path integral
molecular dynamics

Objective

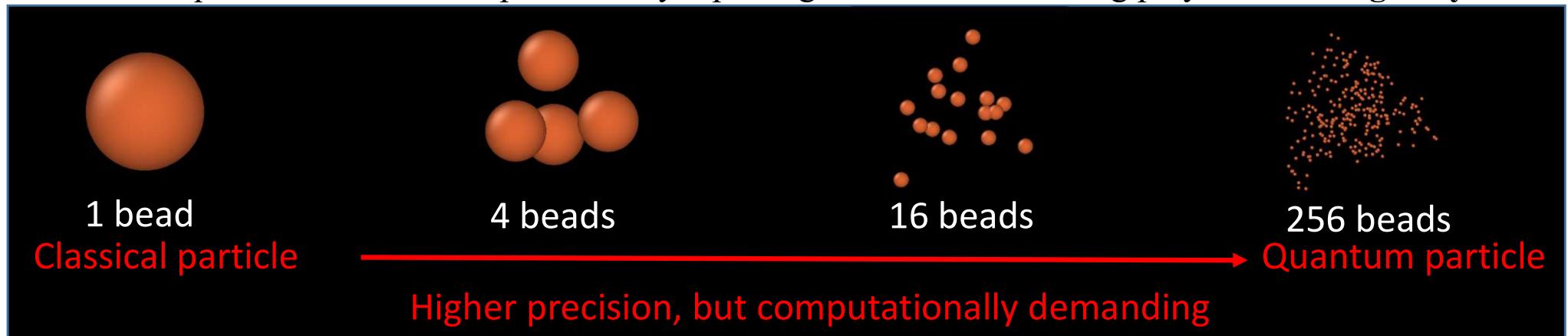
- Estimate H diffusivity in bcc metals with machine learning potential & path integral theory to reproduce nuclear quantum effects (NQEs).
- bcc Fe (α -Fe) was selected as a test case due to its high resistivity to radiation damage.



Path integral formulation

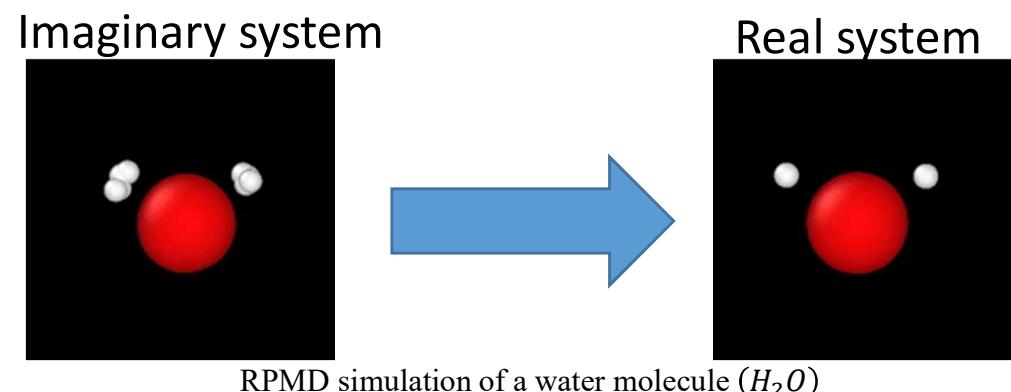
■ Classical isomorphism

- Nuclear quantum effects are reproduced by replacing **a nucleus** with a ring polymer of **imaginary beads**



■ Centroid path integral molecular dynamics (CMD)

- CMD is a approximate quantum dynamics theory for dynamic quantities in real-time.

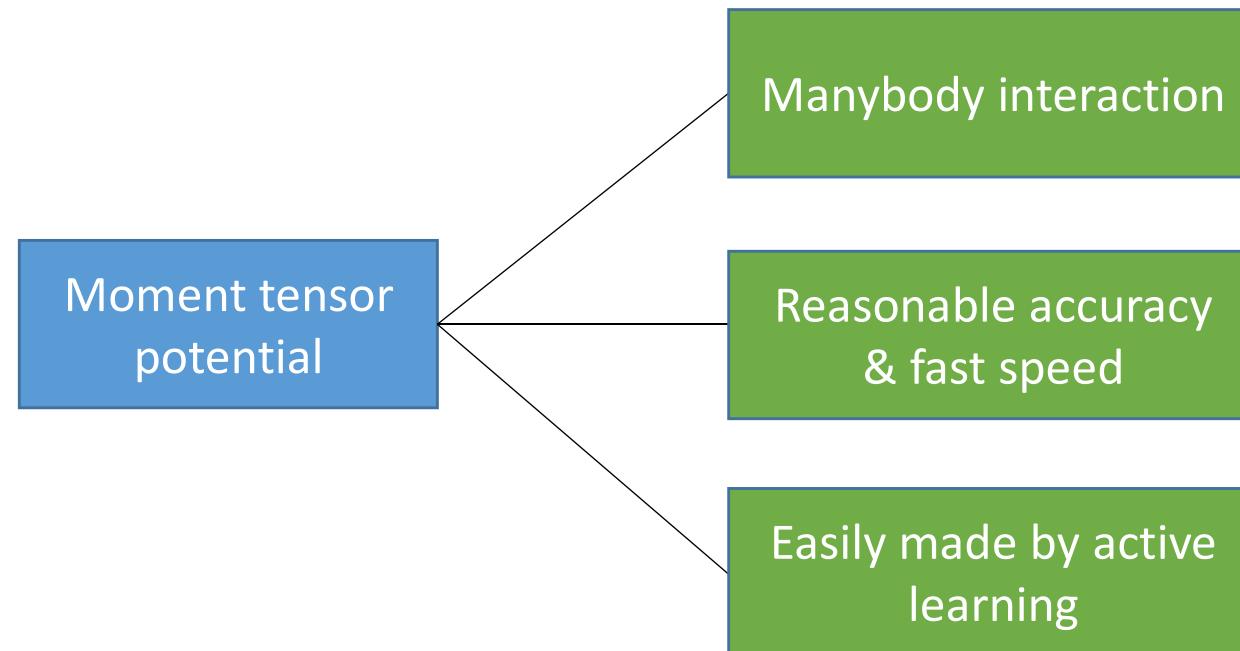




Generation of moment tensor potential (MTP)

■ Machine learning potential: Moment tensor potential (MTP)

- MTP was invented by A. V. Shapeev (2016).
- It can be trained to **imitate** a target force field (DFT-PBE) with a set of polynomials



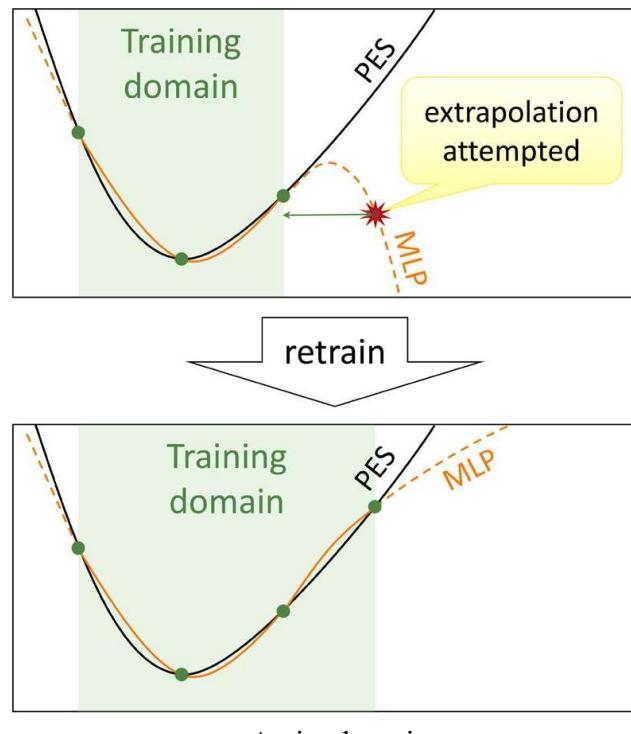
Three major advantages of MTP



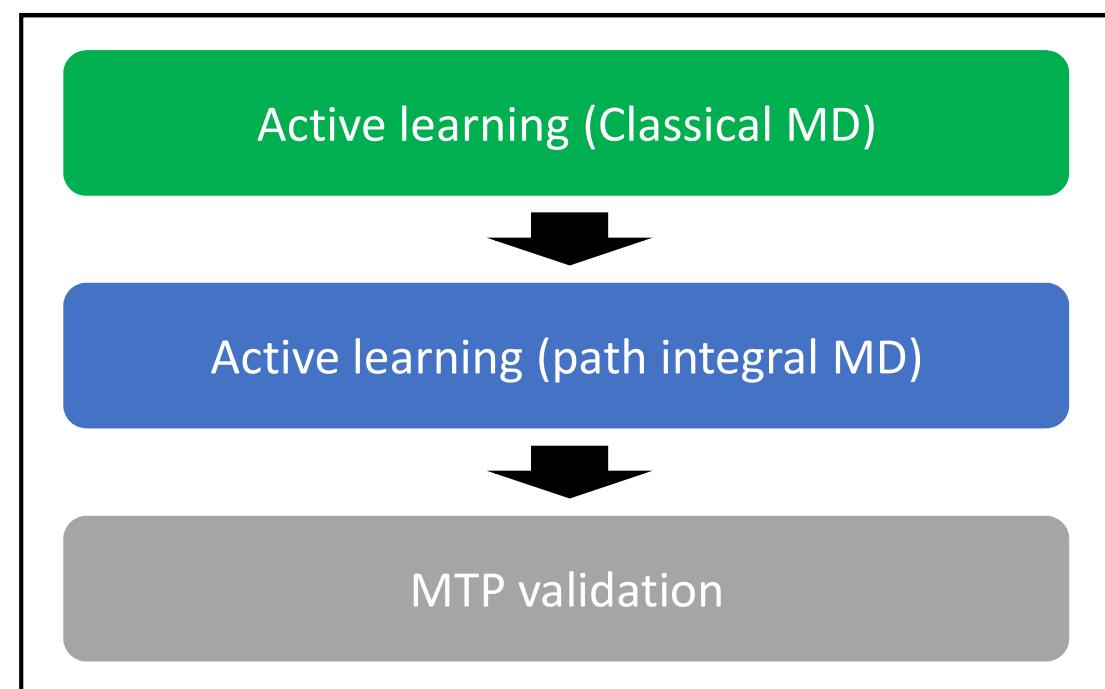
Generation of moment tensor potential (MTP)

■ Active learning

- The optimal training set for generating MTP was collected from **active learning**.



Active learning



MTP generation & validation scheme



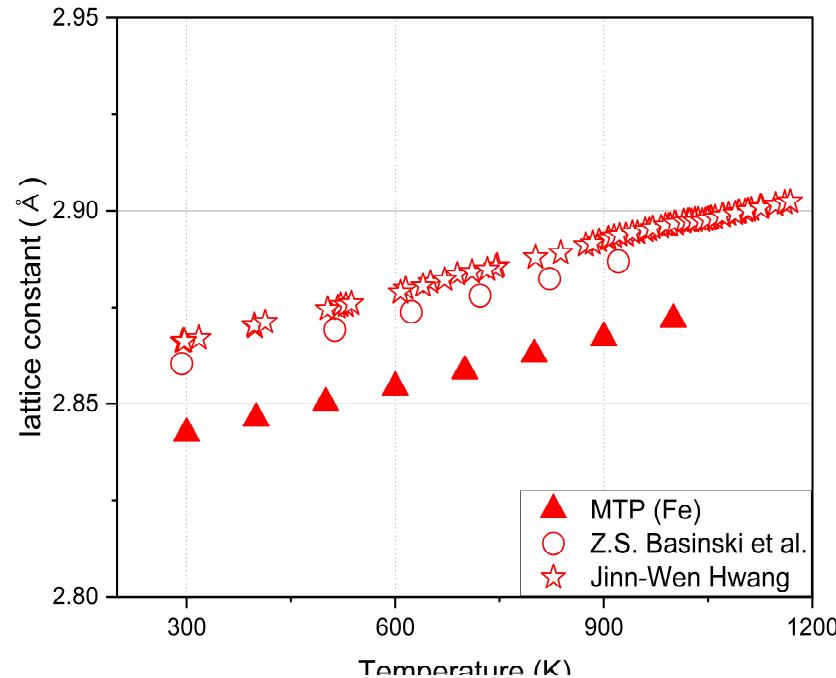
Validation of moment tensor potential (MTP)

■ Lattice & Elastic constants of bcc Fe without H

Comparison of MTP, DFT, and experiments	MTP	DFT	Experiments
Lattice constant	2.832 Å	2.832 Å	2.860 Å (293 K)
Elastic constant (C_{11})	258 GPa	278 GPa	240 GPa
Elastic constant (C_{12})	142 GPa	148 GPa	136 GPa
Elastic constant (C_{44})	96 GPa	98 GPa	131 GPa

■ Lattice thermal expansion

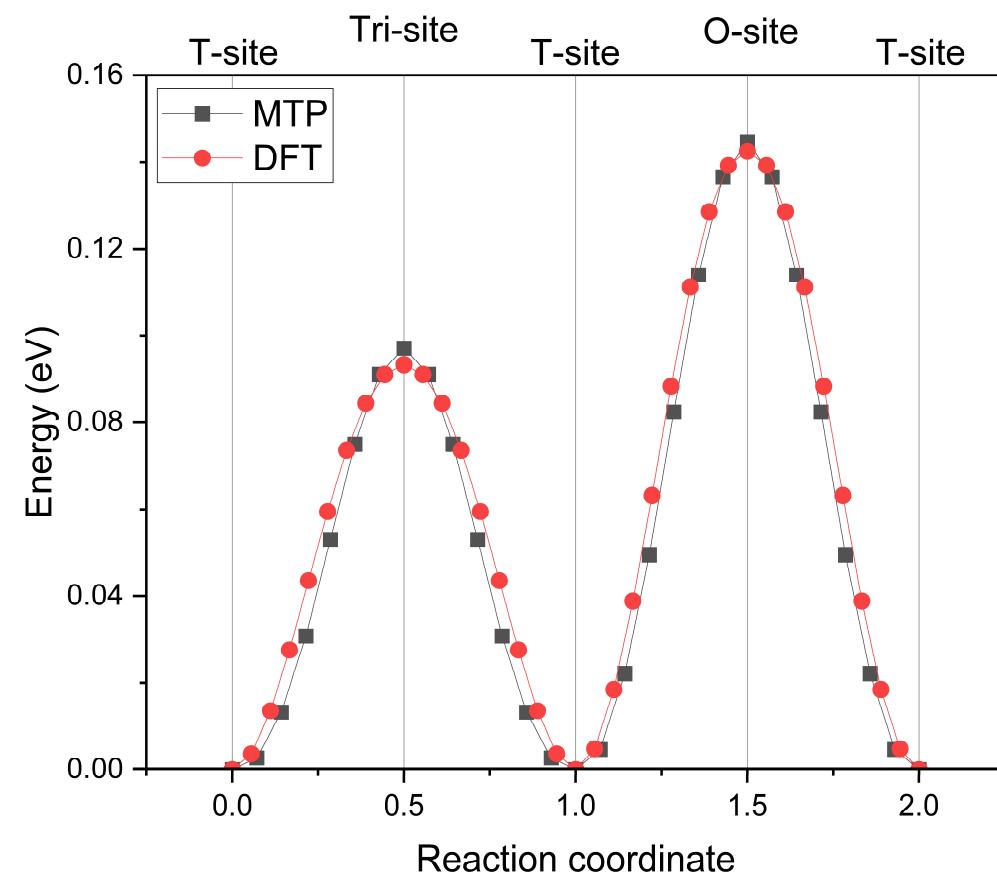
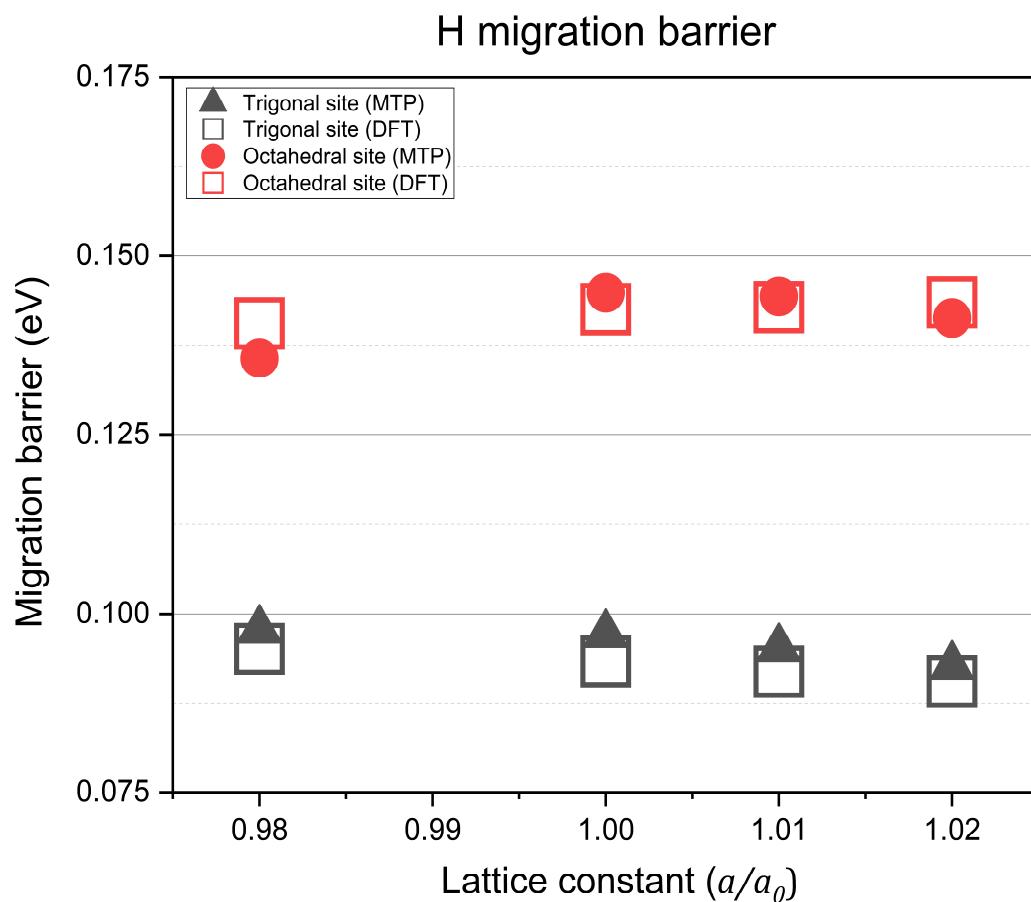
Lattice thermal expansion of bcc Fe





Validation of moment tensor potential (MTP)

■ Migration barrier





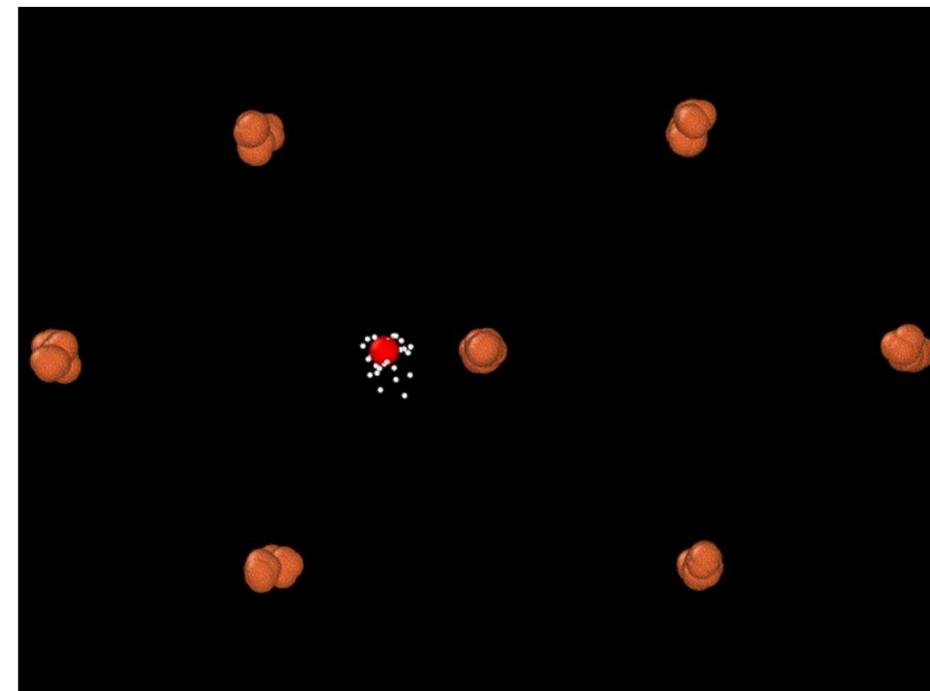
Simulation conditions

Note that

Classical Physics → classical MD

Quantum Physics → centroid path integral MD (CMD)

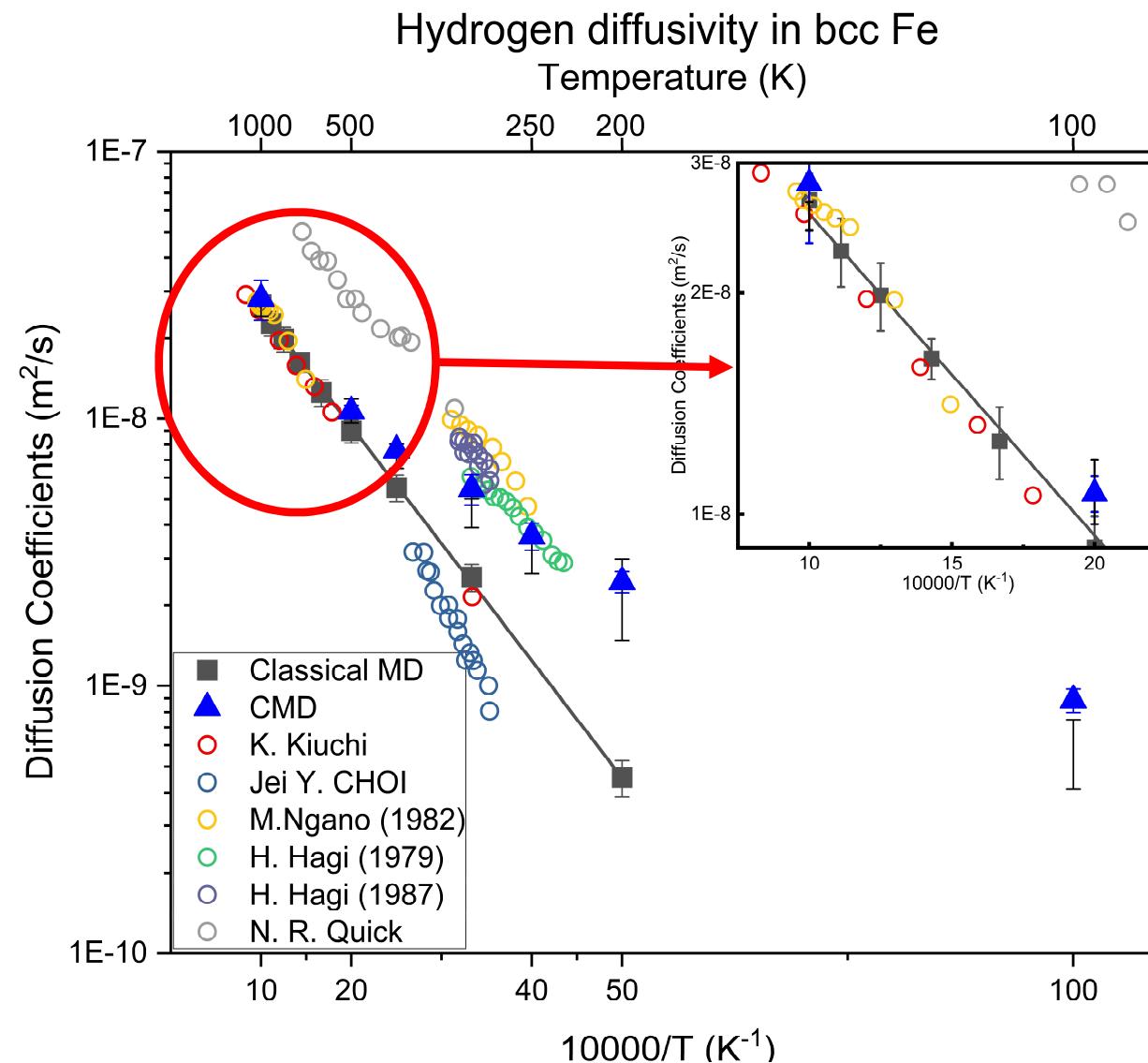
Simulation conditions	Experiments
Structure	one H in $4 \times 4 \times 4$ bcc Fe (periodic boundary condition)
Ensemble	NVT
Number of imaginary beads	64
Production time	30 ns



Animation of RPMD
(red ball: centroid position, white beads: imaginary beads)



H diffusivity in bcc Fe

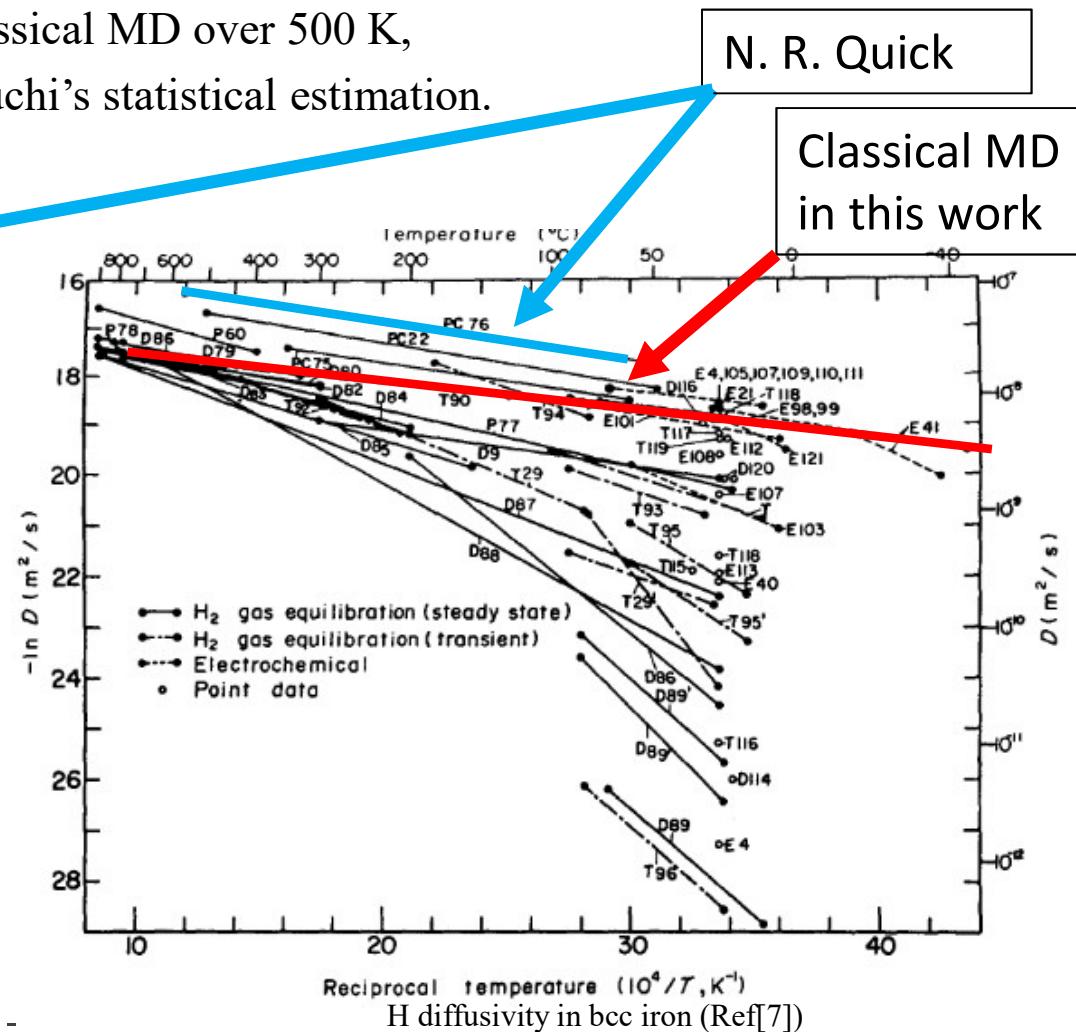
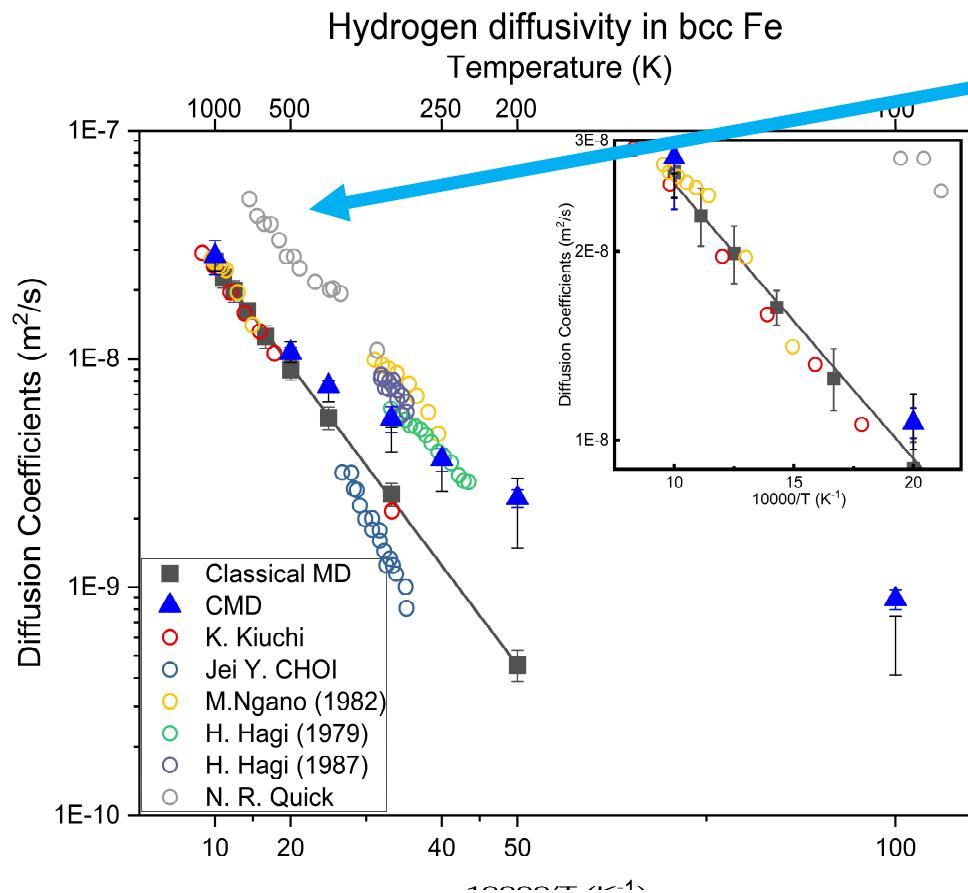




H diffusivity in bcc Fe

■ Diffusivity at high temperature (Classical region)

- Classical MD showed linear Arrhenius equation as the classical rate theory says.
 - Centroid path integral MD (CMD) converged to classical MD over 500 K,
 - Classical MD results were comparable to the K. Kiuchi's statistical estimation.

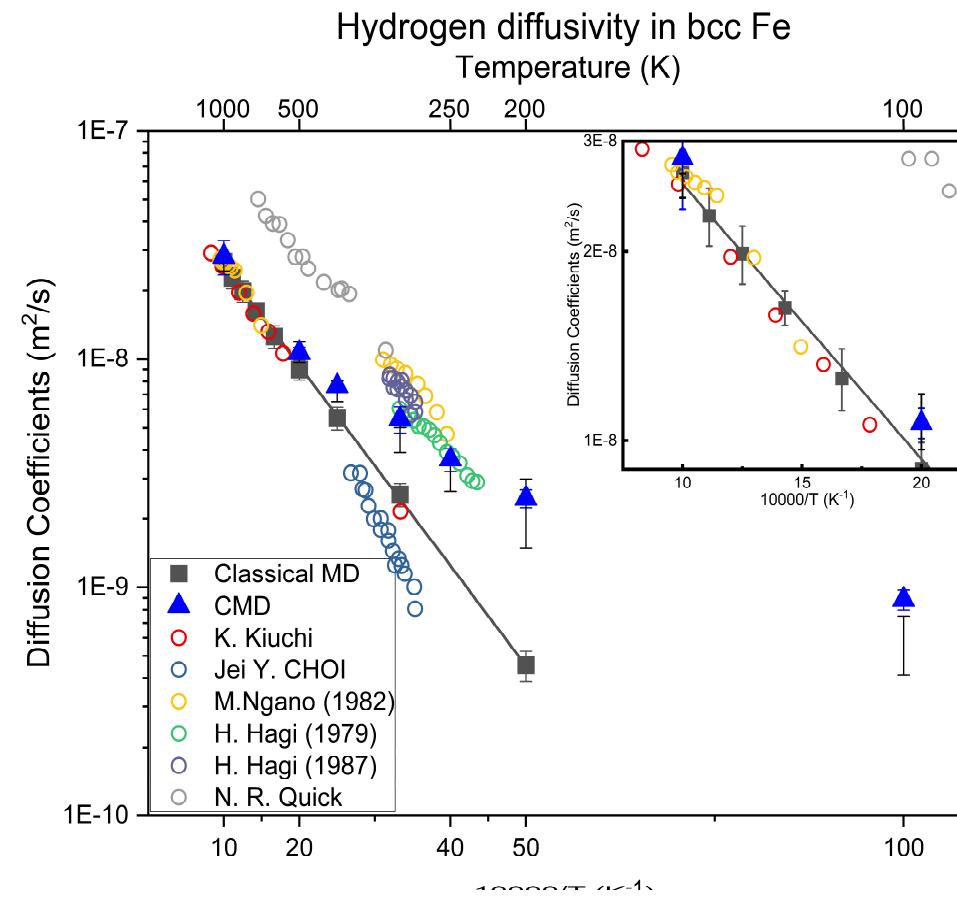




H diffusivity in bcc Fe

■ Diffusivity at low temperature (Nuclear Quantum effects)

- The diffusivity difference between centroid path integral MD (CMD) and classical MD was visible **below 500 K**.
- Experimental data are too scattered due to trapping effects.

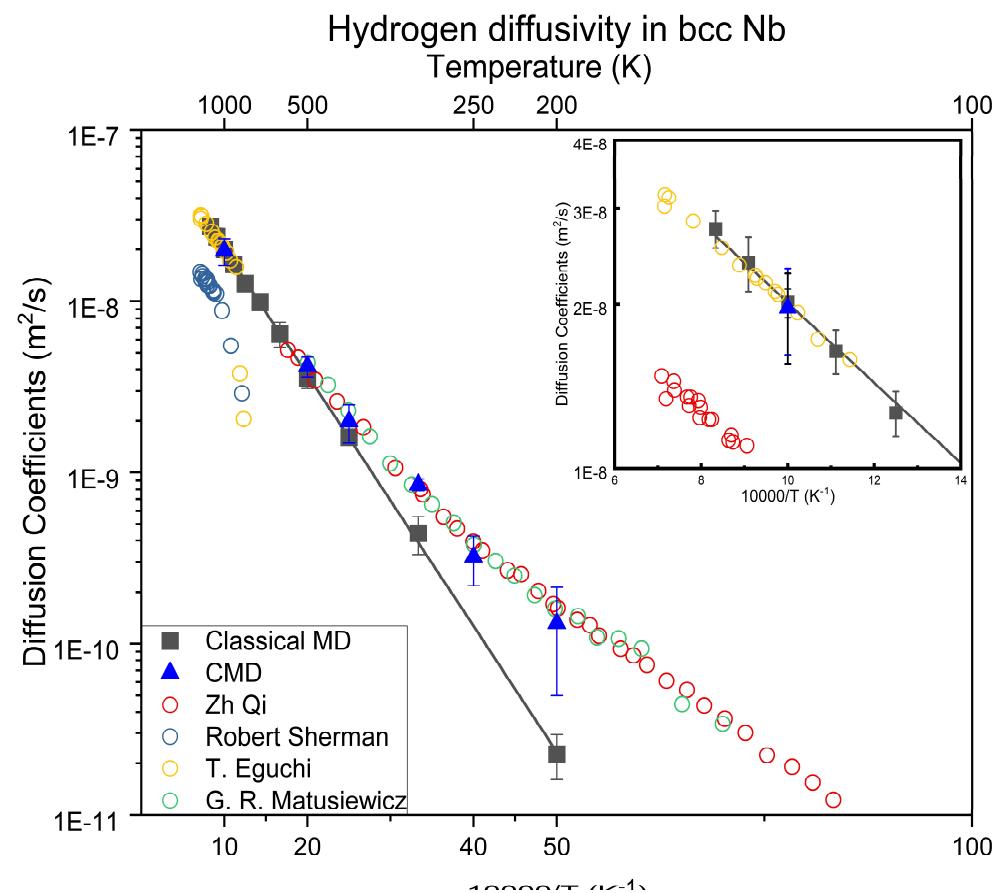
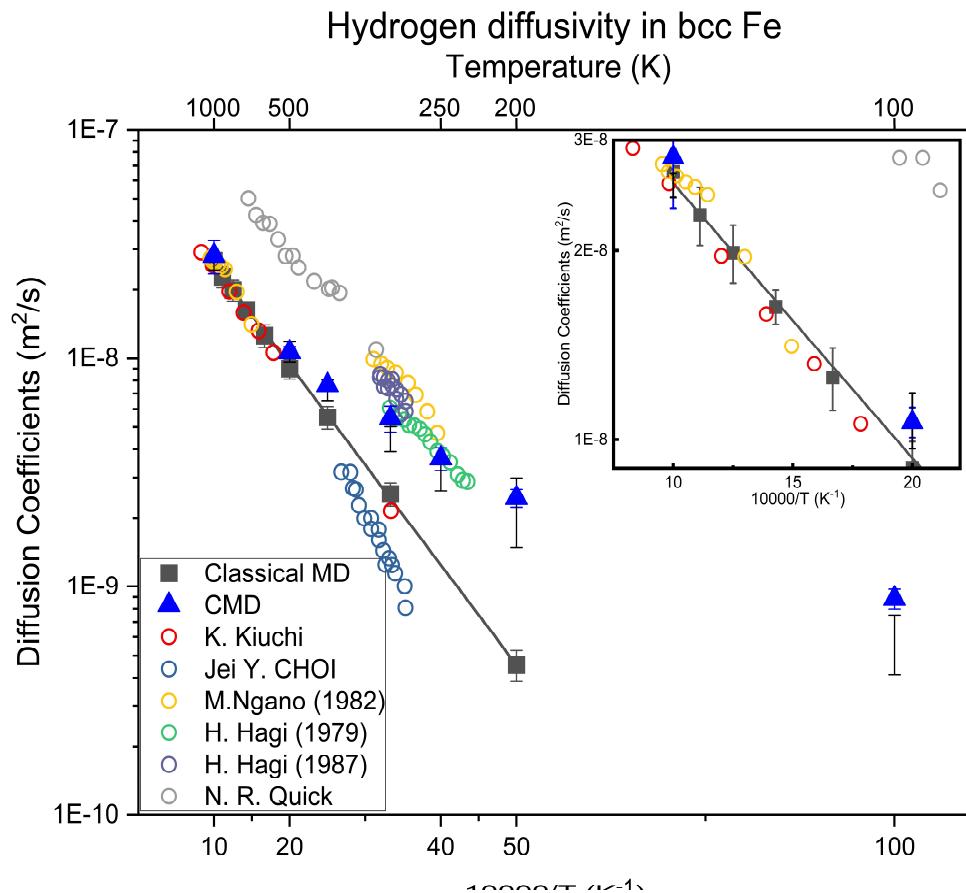




H diffusivity in bcc Fe

■ Diffusivity at low temperature (Nuclear Quantum effects)

- Similar method was applied to Nb, and it showed good agreement to experiments where data were consistent even at low temperature.





Conclusion

■ Machine learning interatomic potential

- Moment tensor potential (MTP) was generated from active learning.
- Accuracy of MTP was validated by comparing key quantities to DFT values.

■ Nuclear quantum effects

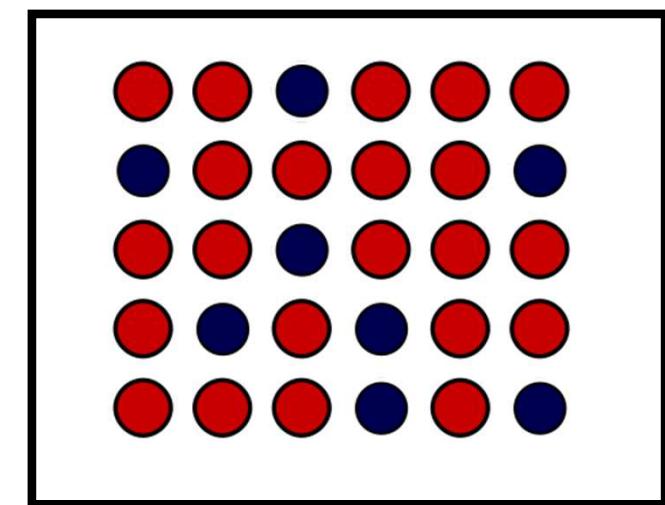
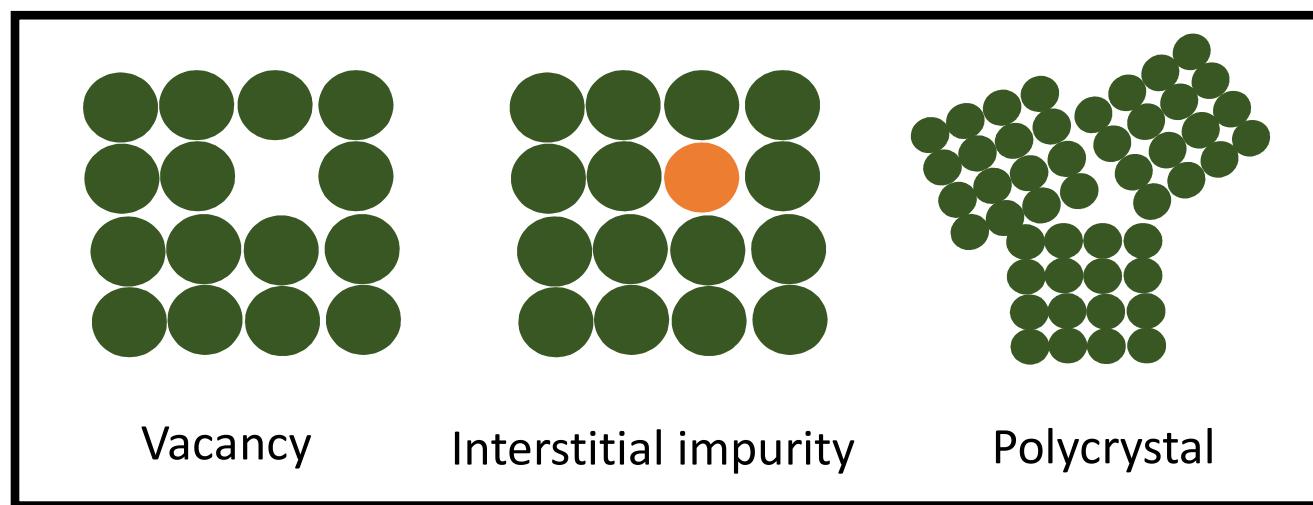
- Although experimental data are highly scattered due to trapping effects, ($T > 500$ K) both classical MD and CMD were comparable to overall measurements. ($100 \text{ K} < T < 500 \text{ K}$) CMD of H in bcc Nb showed good agreement with experiments.
- Classical-Quantum crossover temperature was around **500 K**.
(centroid MD produced about **35 %** larger diffusion coefficient than classical MD at 400 K.)



Future work

■ Potential value of machine-learning interatomic potentials

- Although only perfect bcc crystal was considered, our methodology can be further applied to more complex systems with a high level of transferability.
- Practical problems (e.g. hydrogen embrittlement) can be analyzed by this methodology.





Acknowledgement

- ① I would like to express my deepest gratitude to my supervisor, Prof. Oda for his careful instructions.
- ② Furthermore, I would like to acknowledge Dr. Shiga and Prof. Kimizuka for their active discussion about path integral MD.
- ③ Finally, I am so indebted to the HPCI of Japan for support of the supercomputer Fugaku.



Reference

- [1] Basinski, Z. S. Series A, Mathematical and Physical Sciences, Volume 229, Issue 1179, pp. 459-467 (1955)
- [2] B.N. Dutta, phys. stat. sol. 8, 2253 (1963)
- [3] Choi, J.Y. Diffusion of hydrogen in iron. Metall Mater Trans B 1, 911–919 (1970).
- [4] H. Hagi, Transactions of the Japan Institute of Metals: 1979 Volume 20 Issue 7 Pages 349-357
- [5] H. Kimizuka, PHYSICAL REVIEW B 83, 094110 (2011)
- [6] Ivan S Novikov et al 2021 Mach. Learn.: Sci. Technol. 2 025002 (2021)
- [7] Kiuchi, K. Kiuchi, R.B. McLellan, The solubility and diffusivity of hydrogen in well-annealed and deformed iron, Acta Metallurgica, Volume 31, Issue 7, 1983, Pages 961-984,
- [8] M. Nagano, Y. Hayashi, N. Ohtani, M. Isshiki, and K. Igaki, Scripta Metall. 16, 973 (1982)
- [9] Quick, Nathaniel R. and Herbert H. Johnson. “Hydrogen and deuterium in iron, 49–506°C.” Acta Metallurgica 26 (1978): 903-907.
- [10] Shapeev A V, Simul. 14 1153–73 (2016)