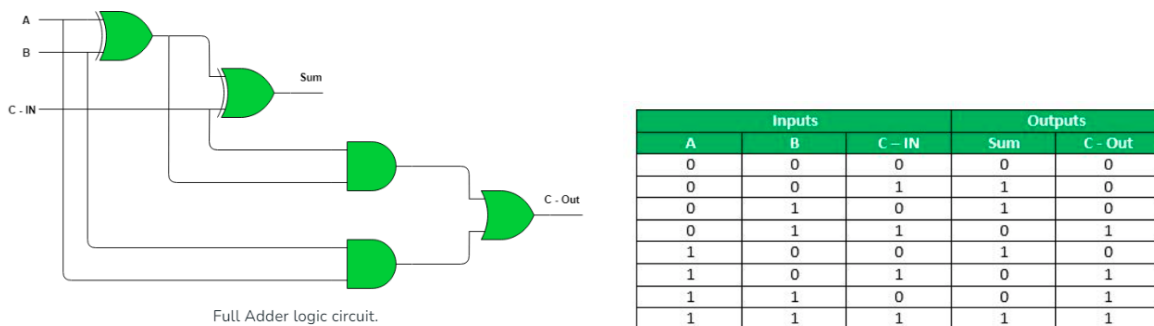


Half Adder



Logical Expression for SUM: $= A' B' C\text{-IN} + A' B C\text{-IN}' + A B' C\text{-IN}' + A B C\text{-IN} = C\text{-IN} (A' B' + A B) + C\text{-IN}' (A' B + A B') = C\text{-IN} \text{ XOR } (A \text{ XOR } B) = (1,2,4,7)$

Logical Expression for C-OUT: $= A' B C\text{-IN} + A B' C\text{-IN} + A B C\text{-IN}' + A B C\text{-IN} = A B + B C\text{-IN} + A C\text{-IN} = (3,5,6,7)$

Another form in which C-OUT can be implemented: $= A B + A C\text{-IN} + B C\text{-IN} (A + A') = A B C\text{-IN} + A B + A C\text{-IN} + A' B C\text{-IN} = A B (1 + C\text{-IN}) + A C\text{-IN} + A' B C\text{-IN} = A B + A C\text{-IN} + A' B C\text{-IN} = A B + A C\text{-IN} (B + B') + A' B C\text{-IN} = A B C\text{-IN} + A B + A B' C\text{-IN} + A' B C\text{-IN} = A B (C\text{-IN} + 1) + A B' C\text{-IN} + A' B C\text{-IN} = A B + A B' C\text{-IN} + A' B C\text{-IN} = A B + C\text{-IN} (A' B + A B')$

Therefore $C_{OUT} = AB + C\text{-IN} (A \text{ EX - OR } B)$

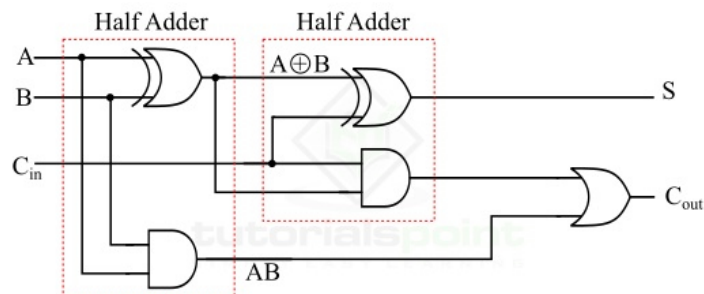
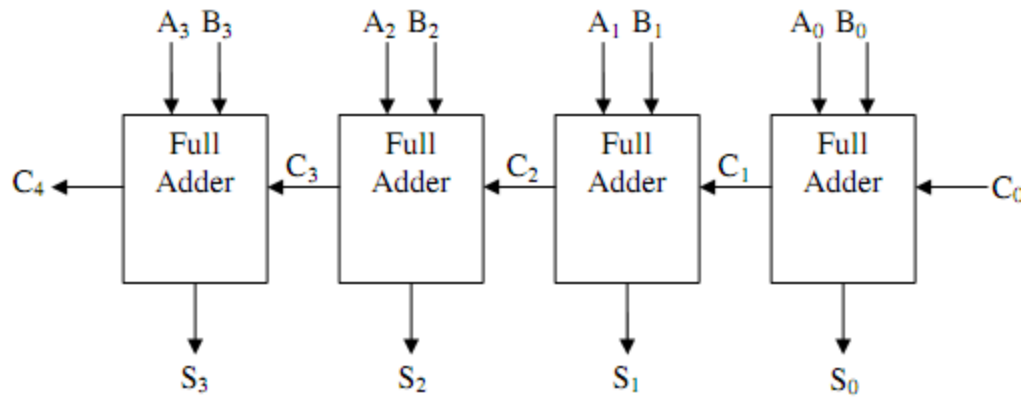
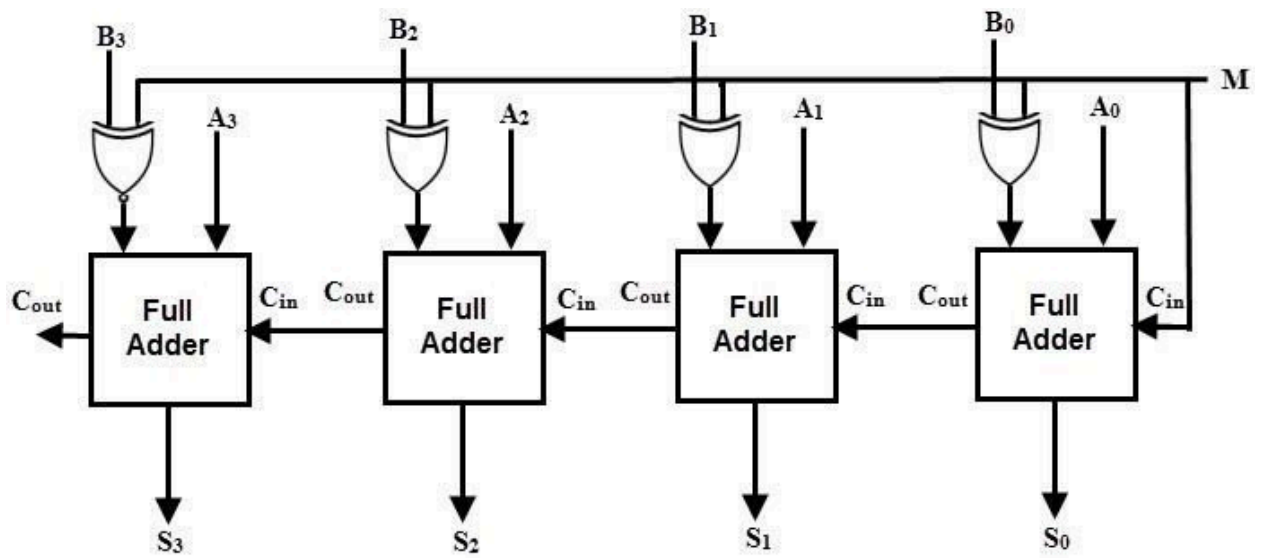


Figure 3 - Logic Diagram of Full Adder using Half Adder

Full Adder



4 bit parallel adder



Adder + Subtractor