Assoc. Prof. Dr. Bora Canbula



https://github.com/canbula/NumericalAnalysis/

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Key Features of NumPy

Binary Representation of Numbers

IEEE 754 Representation of Numbers

Precisions in IEEE 754 Representation

Introduction to Numerical Derivatives

Finite Difference Approach

System of Linear Equations

Bisection Method

Newton - Raphson Method

Introduction to Numerical Integration

Gaussian Quadrature Method

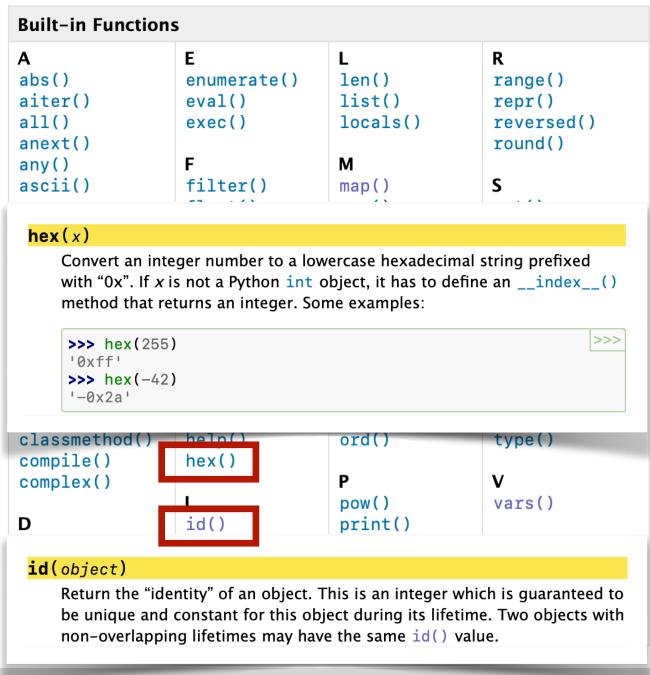
System of Nonlinear Equations

Variables

Variables are symbols for memory addresses.

Built-in Functions

The Python interpreter has a number of functions and types built into it that are always available. They are listed here in alphabetical order.



https://docs.python.org/3/library/functions.html

Identifier Names

For variables, functions, classes etc. we use identifier names. We <u>must</u> obey some <u>rules</u> and we <u>should</u> follow some naming <u>conventions</u>.

Rules

- Names are case sensitive.
- Names can be a combination of letters, digits, and underscore.
- Names can only start with a letter or underscore, can not start with a digit.
- Keywords can not be used as a name.

keyword — Testing for Python keywords

Source code: Lib/keyword.py

This module allows a Python program to determine if a string is a keyword or soft keyword.

keyword.iskeyword(s)

Return True if s is a Python keyword.

keyword.**kwlist**

Sequence containing all the keywords defined for the interpreter. If any keywords are defined to only be active when particular __future__ statements are in effect, these will be included as well.

keyword.issoftkeyword(s)

Return True if s is a Python soft keyword.

New in version 3.9.

keyword.softkwlist

Sequence containing all the soft keywords defined for the interpreter. If any soft keywords are defined to only be active when particular __future__ statements are in effect, these will be included as well.

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https://peps.python.org/

Python Enhancement Proposals Python » PEP Index » PEP 8



PEP 8 - Style Guide for Python Code

Author: Guido van Rossum < guido at python.org >, Barry Warsaw

<barry at python.org>, Nick Coghlan <ncoghlan at</pre>

gmail.com>

Status: Active

Type: Process

Created: 05-Jul-2001

Post-History: 05-Jul-2001, 01-Aug-2013

Identifier Names

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Conventions

- Names to Avoid
 - Never use the characters 'l' (lowercase letter el), 'O' (uppercase letter oh), or 'l' (uppercase letter eye) as single character variable names.
- Packages
 - Short, all-lowercase names without underscores
- Modules
 - Short, all-lowercase names, can have underscores
- Classes
 - CapWords (upper camel case) convention
- Functions
 - snake case convention
- <u>Variables</u>
 - snake_case convention
- Constants
 - ALL_UPPERCASE, words separated by underscores

Leading and Trailing Underscores

- _single_leading_underscore Weak "internal use" indicator.
 - from M import * does not import objects whose names start with an underscore.
- single_trailing_underscore_ Used by convention to avoid conflicts with keyword.
- __double_leading_underscore When naming a class attribute, invokes name mangling (inside class FooBar, __boo becomes _FooBar__boo)
- __double_leading_and_trailing_underscore__ "magic" objects or attributes that live in user-controlled namespaces (__init__, __import__, etc.). Never invent such names; only use them as documented.

Variable Types

Python is <u>dynamically typed</u>. Python does not have primitive types. Everything is an object in Python, therefore, a variable is purely a <u>reference</u> to an object with the specified value.

Numeric Types

- Integer
- Float
- Complex
- Boolean

Formatted Output

- print("static text = ", variable)
- print("static text = %d" % (variable))
- print("static text = {0}".format(variable))
- print(f"static text = {variable}")
- print(f"static text = {variable:5d}")

Variable Types

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Sequences

print(k)

print(k, v)

print(k, v)

- **Strings**
- List
- **Tuple**
- Set
- **Dictionary**

Week02/IntroductoryPythonDataStructures.pdf

INTRODUCTORY PYTHON: DATA STRUCTURES IN PYTHON

ASSOC. PROF. DR. BORA CANBULA MANISA CELAL BAYAR UNIVERSITY

LISTS IN PYTHON: Ordered and mutable sequence of values indexed by integers Initializing a_list = list() ## empty a_list = [3, 4, 5, 6, 7] ## filled Finding the index of an item a_list.index(5) ## 2 (the first occurence) Accessing the items a_list[1] ## 4 a_list[-1] ## 7 a list[2:] ## [5, 6, 7] a_list[:2] ## [3, 4] a_list[1:4] ## [4, 5, 6] a_list[0:4:2] ## [3, 5] a_list[4:1:-1] ## [7, 6, 5] Adding a new item a_list.append(9) ## [3, 4, 5, 6, 7, 9] a_list.insert(2, 8) ## [3, 4, 8, 5, 6, 7, 9] a_list[2] = 1 ## [3, 4, 1, 5, 6, 7, 9] Remove the list or just an item a_list.pop() ## last item a_list.pop(2) ## with index del a_list[2] ## with index a_list.remove(5) ## first occurence of 5 a_list.clear() ## returns an empty list del a_list ## removes the list completely Extend a list with another list list_1 = [4, 2] list_2 = [1, 3] list_1.extend(list_2) ## [4, 2, 1, 3] Reversing and sorting list_1.reverse() ## [3, 1, 2, 4] list_1.sort() ## [1, 2, 3, 4] list_1.count(4) ## 1 list_1.count(5) ## 0 list_1 = [3, 4, 5, 6, 7] list_2 = list_1 list_3 = list_1.copy() list_1.append(1) list_2 ## [3, 4, 5, 6, 7, 1] list_3 ## [3, 4, 5, 6, 7]



```
1. What is the correct writing of the
                                             6. What is the output of the code below?
                                             x = set([int(i/2) for i in range(8)])
programming language that we used in this
course?
                                             print(x)
( ) Phyton
                                             () {0, 1, 2, 3, 4, 5, 6, 7}
( ) Pyhton
                                             () {0, 1, 2, 3}
( ) Pthyon
                                             () {0, 0, 1, 1, 2, 2, 3, 3}
( ) Python
                                             () {0.5, 1, 1.5, 2, 2.5, 3, 3.5, 4}
2. What is the output of the code below?
                                             7. What is the output of the code below?
                                             x = set(i for i in range(0, 4, 2))
my name = "Bora Canbula"
                                             y = set(i for i in range(1, 5, 2))
print(my_name[2::-1])
                                              print(x^y)
() alu
( ) ula
                                             () {0, 1, 2, 3}
( ) roB
                                             () {}
() Bor
                                             () {0, 8}
                                             ( ) SyntaxError: invalid syntax
3. Which one is not a valid variable name?
                                             8. Which of the following sequences is
( ) for
                                             immutable?
( ) Manisa_Celal_Bayar_University
                                             () List
                                             () Set
( ) IF
( ) not
                                             ( ) Dictionary
                                             ( ) String
4. What is the output of the code below?
                                             9. What is the output of the code below?
for i in range(1, 5):
                                             print(int(2 999 999.999))
  print(f"{i:2d}{(i/2):4.2f}", end='')
                                             () 2
                                             ( ) 3000000
( ) 010.50021.00031.50042.00
                                             ( ) ValueError: invalid literal
( ) 10.50 21.00 31.50 42.00
                                             ( ) 2999999
( ) 1 0.5 2 1.0 3 1.5 4 2.0
( ) 100.5 201.0 301.5 402.0
5. Which one is the correct way to print
                                             10. What is the output of the code below?
Bora's age?
                                             x = (1, 5, 1)
profs = \Gamma
                                             print(x, type(x))
  {"name": "Yener", "age": 25},
                                             ( ) [1, 2, 3, 4] <class 'list'>
  {"name": "Bora", "age": 37},
                                             ( ) (1, 5, 1) <class 'range'>
  {"name": "Ali", "age": 42}
                                             ( ) (1, 5, 1) <class 'tuple'>
                                             ( ) (1, 2, 3, 4) <class 'set'>
]
() profs["Bora"]["age"]
( ) profs[1][1]
( ) profs[1]["age"]
( ) profs.age[name="Bora"]
```

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Iterables - Sequences - Iterators

An **iterable** is any object that can be looped over. It represents a collection of elements that can be accessed one by one.

An object is considered iterable if:

- It implements the __iter__() method which returns an iterator, or
- It defines the __getitem() method that can fetch items using integer indices starting from zero.

A **sequence** is a subtype of iterables. It's an ordered collection of elements that can be indexed by numbers.

- Ordered: Elements in a sequence have a specific order.
- Indexable: You can get any item using an index my_sequence[5].
- Slicable: Supports slicing to get some of items my_sequence[2:5].

An **iterator** is an object that produces items (one at a time) from its associated iterable.

- Stateful: An iterator remembers its state between calls. Once an element is consumed, it can't be accessed again without reinitializing the iterator.
- Lazy Evaluation: Items are not produced from the source iterable until the iterator's __next__() method is called.
- Iterators raise a StopIteration exception when there are no more items to return.
- An iterator's __iter__() method returns the iterator object itself.
- While all iterables must be able to produce an iterator (with __iter__() method), not all iterators are directly iterable without using a loop.

Numpy Arrays

Numerical Python (**NumPy**)is a powerful library for numerical computing. Its key feature is multi dimensional arrays (**ndarrays**).

Traditional Python Lists

- Dynamically Typed: Lists can store elements of mixed types in a single list.
- Resizable: Lists can be resized by appending or removing elements.
- **General-purpose:** Lists are general-purpose containers for items of any type.
- Memory: Lists have a larger memory overhead because of their general-purpose nature and dynamic typing.
- **Performance:** Basic operations on lists may not be as fast as those on NumPy arrays because they aren't optimized for numerical operations.

NumPy Arrays

- Typed: All elements in a NumPy array are of the same type.
- **Size:** The size of a NumPy array is fixed upon creation. However, one can create a new array with a different size, but resizing inplace (like appending in lists) isn't directly supported.
- **Efficiency:** NumPy arrays are memory-efficient as they store elements in contiguous blocks of memory.
- **Performance:** Operations on NumPy arrays are typically faster than lists, especially for numerical tasks, due to optimized C and Fortran extensions.
- **Vectorized Operations:** Supports operations that apply to the entire array without the need for explicit loops (e.g., adding two arrays element-wise).
- Broadcasting: Advanced feature allowing operations on arrays of different shapes.
- Extensive Functionality: Beyond just array storage, NumPy provides a vast range of mathematical, logical, shape manipulation, and other operations.
- Interoperability: Can interface with C, C++, and Fortran code.

Homework

Week04/arrays_firstname_lastname.py



Function Description

replace_center_with_minus_one(d, n, m)

This function creates an n-by-n numpy array populated with random integers that have up to d digits. It then replaces the central m-by-m part of this array with -1.

Parameters

- d: Number of digits for the random integers.
- n: Size of the main array.
- m: Size of the central array that will be replaced with −1.

Returns

A modified numpy array with its center replaced with −1.

Exceptions

 ValueError: This exception is raised in the following scenarios:

```
If m > nIf d <= 0</li>If n < 0</li>
```

 \circ If m < 0

<pre>1. What is the correct way to create a NumPy array? () np.list([1, 2, 3]) () np([1, 2, 3]) () np.array([1, 2, 3]) () np(array([1, 2, 3]))</pre>	<pre>6. What is the output of the code below? n_1 = np.array([1, 2, 3]) n_2 = np.array([4, 5, 6]) n_3 = np.array([7, 8, 9]) print(np.array([n_1, n_2, n_3]).ndim)</pre> Your answer:
<pre>2. Which of the following arrays is a 2-D array? () [3, 5] () [[3], [5]] () [{1, 3}, {5, 7}] () [2]</pre>	<pre>7. What is the output of the code below? n_1 = np.array([1, 2, 3]) n_2 = np.array([4, 5, 6]) n_3 = np.array([7, 8, 9]) print(np.array([n_1 + n_2 + n_3]).shape) Your answer:</pre>
<pre>3. What is the correct way to print 5 from the array given below? a = np.array([[1, 2], [3, 4], [5, 6]]) () print(a[3, 1]) () print(a[2, 0]) () print(a[1, 2]) () print(a[1, 3])</pre>	<pre>8. Which of the following is created with the code given below? np.array([[1, 2, 3], [4, 5, 6]]) () 1-d array of shape 6 x 1 () 2-d array of shape 2 x 3 () 3-d array of shape 3 x 2 () 3-d array of shape 2 x 3</pre>
<pre>4. What is the correct way to print every other item from the array given below? a = np.arange(5) () print(a[1:3:5]) () print(a[::2]) () print(a[1:5]) () print(a[0:2:4]</pre>	9. What is the output of the code below? print(np.arange(10).reshape(2, -1))
5. What does the shape mean of a NumPy array?() Number of columns() Total number of items() Number of items in each dimension() Number of rows	<pre>10. What is the output of the code below? Print(np.array([0.5, 1.5, 2.5]).dtype)</pre>

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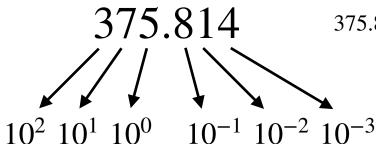
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Binary Representation of Floating-Point Numbers



$$375.814 = (3 \cdot 10^{2}) + (7 \cdot 10^{1}) + (5 \cdot 10^{0}) + (8 \cdot 10^{-1}) + (1 \cdot 10^{-2}) + (4 \cdot 10^{-3})$$

Integer Part

$$375 \% 2 = 1$$
 $187 \% 2 = 1$
 $93 \% 2 = 1$
 $46 \% 2 = 0$
 $23 \% 2 = 1$
 $11 \% 2 = 1$
 $5 \% 2 = 1$
 $2 \% 2 = 0$
 1

Decimal Part

$$0.814 \cdot 2 = 1.628 \rightarrow 1$$

 $0.628 \cdot 2 = 1.256 \rightarrow 1$
 $0.256 \cdot 2 = 0.512 \rightarrow 0$
 $0.512 \cdot 2 = 1.024 \rightarrow 1$
 $0.024 \cdot 2 = 0.048 \rightarrow 0$
 $0.048 \cdot 2 = 0.096 \rightarrow 0$
 $0.096 \cdot 2 = 0.192 \rightarrow 0$
 $0.192 \cdot 2 = 0.384 \rightarrow 0$
 $0.384 \cdot 2 = 0.768 \rightarrow 0$
 $0.768 \cdot 2 = 1.536 \rightarrow 1$
 $0.036 \cdot 2 = 0.072 \rightarrow 0$
:

 $(375.814)_{10} = (101110111.11010000010...)_2$



Homework

Week05/bra_firstname_lastname.py



Binary Representation API

Your task is to create a Python application that exposes an API endpoint to convert floating-point numbers into their binary representation. This application will be a Flask web service that can accept GET requests with a floating-point number and respond with its binary representation. The binary representation should separate the integer and fractional parts with a dot.

Objectives

- Implement a BinaryRepresentation class that can take a float and provide methods to convert both the integer and decimal parts into binary.
- Develop a Flask API with a route that accepts a floating-point number as a query parameter and returns its binary representation.
- Ensure that your code passes a series of tests that will be run against it.
- All the details that you can't understand from this assignment should be extracted from the tests: Week05/test bra.py

Requirements

1. BinaryRepresentation Class

- The class should be initialized with one float parameter.
- Implement a method **integer2binary** that converts the integer part of the float to binary.
- Implement a method **decimal2binary** that converts the decimal part of the float to binary up to 10 places.
- Implement the <u>__str__</u> method to return the binary representation as a string, separating the integer and decimal parts with a dot.

2. Flask API

- Set up a Flask application.
- Define a route that listens to GET requests and expects a number query parameter.
- Validate that the number parameter is a **float** and return an appropriate response if not.
- Utilize the BinaryRepresentation class to return the binary representation of the number.

3. Error Handling

• Ensure that the application correctly handles cases where the number is not provided, or is not a valid float.

In binary system, which of the following digits are used to represent a number?
 1 and 2
 0 and 1
 1 and 2
 A and B
 Which of the following codes gives a binary representation of 97?
 binary(97)
 (97).binary()

6. Use the codes given in the question **4** as a starting point and write Python codes which converts the decimal of a base-10 number into binary system.

3. What is the name of the NumPy method
which converts a number to binary system?
() np.binary()
() np.bin()
() np.binary_representation()
() np.binary_repr()

4. The code given below produces this output:

() f"{97:b}"
() to binary(97)

```
> 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 1 = 97
```

Complete the code with appropriate statements for the lines given with (1) and (2).

```
n = 16;r = 97;r_0 = r;b = [0]*n
for i in range(n-1, -1, -1):
    x = 2**i
    if r >= x:
        (1)
        (2)
b = b[::-1]
print(*b, end='')
print(f" = {r_0}")
```

5. Modify the code given in question **4** to avoid fixing the number of digits (n). Hint: use bit_length() method of integer object.

7. Try to write a general function which converts a base-10 floating point number into any base including the decimal part.

```
def to_any_base(r: float, b: int) -> str:
    '''This function returns the base-b '''
    '''conversion of r, which is a
    '''floating-point number.
    '''Example:
    ''' to_any_base(3.5, 2) -> '11.1'
```

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Python Ba	sics
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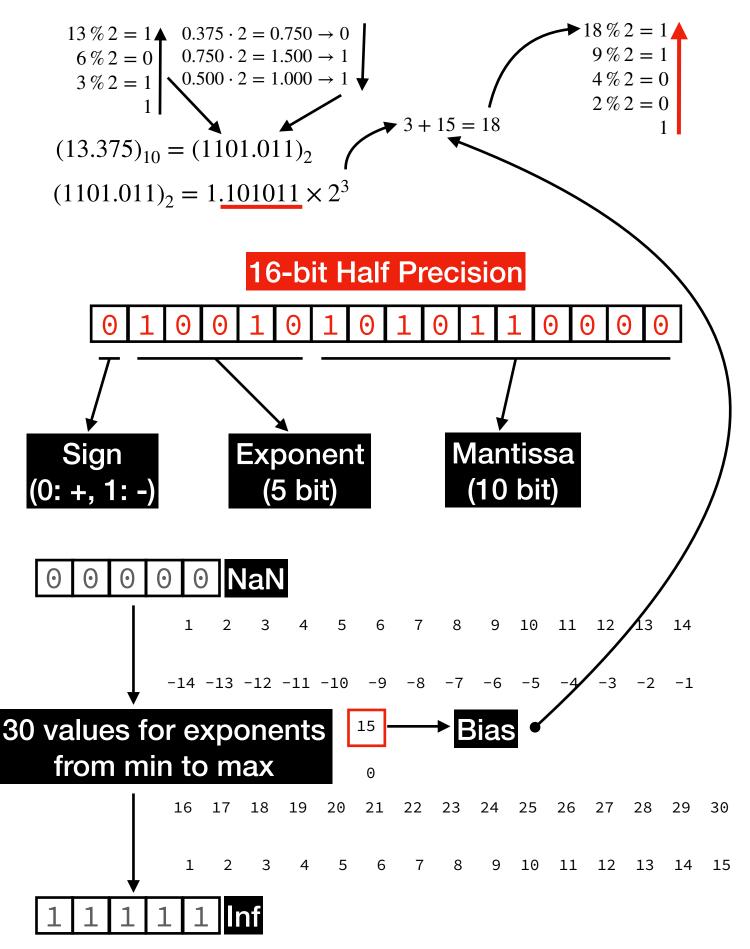
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- 1. Find the smallest and the largest value that you can represent with 16-bit IEEE 754 standard?
- 4. Use a custom IEEE 754 representation as 1-bit for the sign of the number and (4-bit exponent) + (20-bit mantissa). Convert 0.17 into this representation and compare the result with the previous question.

2. Find the 16 bit IEEE 754 representation of -5.875.

- 3. Calculate the error if we use 16 bit IEEE 754 representation to store the value 0.17 in memory.
- 5. Calculate the bias for the 8 bit exponent part.