

# Problem Set 5: Object Tracking and Pedestrian Detection

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March 4, 2022

## ASSIGNMENT DESCRIPTION

### Description

In Problem set 5, you are going to implement tracking methods for image sequences and videos. The main algorithms you will be using are the Kalman and Particle Filters. Methods to be used: You will design and implement a Kalman and a Particle filters from the ground up.

RULES: You may use image processing functions to find color channels, load images, find edges (such as with Canny), resize images. Don't forget that those have a variety of parameters and you may need to experiment with them. There are certain functions that may not be allowed and are specified in the assignment's autograder Piazza post.

Refer to this problem set's autograder post for a list of banned function calls.

Please do not use absolute paths in your submission code. All paths should be relative to the submission directory. Any submissions with absolute paths are in danger of receiving a penalty!

### Learning Objectives

- Identify which image processing methods work best in order to locate an object in a scene.
- Learn to how object tracking in images works.
- Explore different methods to build a tracking algorithm that relies on measurements and a prior state.
- Create methods that can track an object when occlusions are present in the scene.

### Starter Code

Obtain the starter code from canvas under files.

# INSTRUCTIONS

## Programming Instructions

Your main programming task is to complete the functions described in the file **PS5.py**. The driver program **experiment.py** helps you illustrate the results and will output the files needed for the writeup.

## Write-up Instructions

Create **ps5\_report.pdf** - a PDF file that shows all your output for the problem set, including images labeled appropriately (by filename, e.g. ps5-1-a-1.png) so it is clear which section they are for and the small number of written responses necessary to answer some of the questions (as indicated). You are required to use do the following when creating your report:

- Use the LATEX template provided.
- PLEASE be sure to add your name and email, exactly as it is on CANVAS as we need to know who did this work. ALSO, please change the term to current term of the class (Fall 2021, etc.)

## How to Submit

Two assignments have been created on Gradescope: one for the report - PS5\_report, and the other for the code - **PS5\_code**.

- Report: the report (PDF only) must be submitted to the PS5\_report assignment.
- Code: all files must be submitted to the PS5\_code assignment. DO NOT upload zipped folders or any sub-folders, please upload each file individually. Drag and drop all files into Gradescope.

### **note:**

You only need to submit ps5.py and experiment.py to Gradescope. Any functions added or modified in ps5\_utils.py will not be checked by gradescope and you may get an error if your implementation depends on them. However, you can still add any code in the ps5\_utils.py for local use/saving output etc.

## *Notes*

- You can only submit to the autograder **10** times in an hour. You'll receive a message like "You have exceeded the number of submissions in the last hour. Please wait for 36.0 mins before you submit again." when you exceed those 10 submissions. You'll also receive a message "You can submit 8 times in the next 53.0 mins" with each submission so that you may keep track of your submissions.
- If you wish to modify the autograder functions, create a copy of those functions and DO NOT mess with the original function call.

**YOU MUST SUBMIT your report and code separately, i.e., two submissions for the code and the report, respectively. Only your last submission before the deadline will be counted for each of the code and the report.**

## Grading

The assignment will be graded out of 100 points. The code portion (autograder) represents 75% of the grade and the report the remaining 25%.

## ASSIGNMENT QUESTIONS

### 1 THE KALMAN FILTER

The Kalman Filter (KF) is a method used to track linear dynamical systems with gaussian noise. Recall that both the predicted and the corrected states are gaussians, allowing us to keep the mean and covariance of the state in order to run this filter. Use the kalman filter on the provided images to track a moving circle.

First we need to define the KF's components. We will use the notation presented in the lectures for the N-dimensional case.

State vector:

We represent the filter's state using the current position and velocities in the x, y plane. We will not use acceleration in our exercise.

$$X = [x, y, v_x, v_y]$$

Dynamics Model transition 4x4 matrix  $D_t$ :

This matrix will map the equations below to the state components. Determine how this 4x4 matrix can be used to represent these equations using the state vector.

$$x_t = x(t-1) + v_x \Delta t$$

$$y_t = y(t-1) + v_y \Delta t$$

$\Delta t = 1$  for simplicity

State and Covariance prediction:

We assume that the state vector prediction is based on a linear transformation using the transition matrix  $D_t$ . And the covariance is obtained from the squaring operation plus the process noise  $\Sigma_{d_t}$ .

We will also assume this noise is independent from each component in the state vector.

$$X_t^- = D_t X_{t-1}^+$$

$$\Sigma_t^- = D_t \Sigma_{t-1}^+ D_t^T + \Sigma_{d_t}$$

$$\Sigma_{d_t} = \begin{bmatrix} \sigma_{d_x}^2 & 0 & 0 & 0 \\ 0 & \sigma_{d_y}^2 & 0 & 0 \\ 0 & 0 & \sigma_{d_{v_x}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{d_{v_y}}^2 \end{bmatrix}$$

Before we continue to the Correction state. We will define our sensor's function as a way to obtain the object's position. In our case we will use a template matching code to obtain these components. In order to make this a little more interesting, we will add some noise to these measurements.

Sensor measurement 2x4 matrix  $M_t$ :

This matrix maps the available measurements to the state vector defined above. Because we can only obtain two values, x and y, it contains two rows and four columns.

Kalman Gain  $K_t$  :

Using the measurement matrix, and the predicted covariance we can now compute the Kalman Gain. Here you will also define a measurement noise represented by  $\Sigma_{m_t}$ .

$$K_t = \Sigma_t^- M_t^T (M_t \Sigma_t^- M_t^T + \Sigma_{m_t})^{-1}$$

State and Covariance correction:

Now that we have all the components we need, you will proceed to update the state and the covariance arrays. Notice that in order to update the state you will use the residual represented by the difference between the measurements obtained from the sensor (template matching function)  $Y_t$  and the predicted positions  $M_t X_t^-$ .

$$X_t^+ = X_t^- + K_t(Y_t - M_t X_t^-), \text{ where } Y_t \text{ is the measurements at time } t$$
$$\Sigma_t^+ = (I - K_t M_t) \Sigma_t^-, \text{ where } I \text{ is the identity matrix}$$

In the next iteration the updated state and covariance will be used in the prediction stage.

This may seem like a lot but you will find coding this KF is not complicated. Complete the KalmanFilter class with the process described above. We will split the tasks the following way:

**a.**

Initialize the class defining the class arrays you will be using. Place these components in the `_init_(self, init_x, init_y)` function.

Here's a reminder of what should be included in this part:

- State vector (X) with the initial x and y values.
- Covariance 4x4 array ( $\Sigma$ ) initialized with a diagonal matrix with some value.
- 4x4 state transition matrix  $D_t$
- 2x4 measurement matrix  $M_t$
- 4x4 process noise matrix  $\Sigma_{d_t}$
- 2x2 measurement noise matrix  $\Sigma_{m_t}$

Code: `__init__(self, init_x, init_y)`

Complete the prediction state in `predict(self)`. Here you will replace the class variables for the state and covariance arrays with the prediction process.

Code: `predict(self)`

Finally, we need to correct the state and the covariances using the Kalman gain and the measurements obtained from our sensor.

Code: `correct(self)`

**b.**

The position estimation is performed by the function `process(self, measurement_x, measurement_y)` which uses the functions defined above. Now that you have finished creating the Kalman Filter, estimate the position of a bouncing circle. Use the images in the directory called 'circle' to find the circle's position at each frame.

Input: circle/0000.jpg to circle/0099.jpg.

Code: `part_1b()`

**c.**

Now let's try with a more complicated scene using the same filter. We will find and track pedestrians in a video. This means we need to update our sensor with a function that can locate people in an image. Fortunately, there is a function in OpenCV that can help us with this task using Histogram of Gradients (HoG) descriptors. This object contains a method called `detectMultiScale` that returns the bounding boxes for each person in the scene along with the detection weight associated to it.

Use the sequence of images in the 'walking' directory to detect and follow the man crossing the street using the output from the HoG detector as the measurements and the Kalman Filter.

Input directory: walking/001.jpg to walking/159.jpg

Code: `part_1c()`

## 2 THE PARTICLE FILTER

Recall that we need a variety of elements:

1. a model - this is the "thing" that is actually being tracked. Maybe it's a patch, a contour, or some other description of an entity;
2. a representation of state  $x_t$  that describes the state of the model at time  $t$ ;
3. a dynamics model  $p(x_t|x_{t-1})$  that describes the distribution of the state at time  $t$  given the state at  $t-1$ ;
4. a measurement  $z_t$  that somehow captures the data of the current image; and finally,
5. a sensor model  $p(z_t|x_t)$  that gives the likelihood of a measurement given the state. For Bayesian-based tracking, we assume that at time  $t-1$  we have a belief about the state represented as a density  $p(x_{t-1})$ , and that given some measurements  $z_t$  at time  $t$  we update our Belief by computing the posterior density:

$$Bel(x_t) \propto p(z_t|x_t)p(x_t|u_t, x_{t-1})Bel(x_{t-1})$$

In class we discussed both the theory and the implementation specifics behind particle filtering. The algorithm sketch is provided in the slides and it describes a single update of the particle filter. What is left up to the coder are several details including what is the model, what is the state, the number of particles, the dynamics/control function  $p(x_t|x_{t-1}, u_t)$ , the measurement function  $p(z_t|x_t)$ , and the initial distribution of particles.

For this question, you will need to track an image patch template taken from the first frame of the video. For this assignment the model is simply going to be the image patch, and the state will be only the 2D center location of the patch. Thus each particle will be a  $(u, v)$  pixel location

(where  $u$  and  $v$  are the row and column number respectively) representing a proposed location for the center of the template window.

We will be using a basic function to estimate the dissimilarity between the image patch and a window of equal size in the current image, the Mean Squared Error:

$$MSE(u_p, v_p) = \frac{1}{mn} \sum_{u=1}^m \sum_{v=1}^n (Template(u, v) - Image^t(u + u_p - \frac{m}{2}, v + v_p - \frac{n}{2}))^2$$

The funny indexing is just because  $(u, v)$  are indexed from 1 to  $M$  (or  $N$ ) but the state  $(u_p, v_p)$  is the location of the center. Notice the above equation can be simplified by using array operations. Remember you are calculating the Mean of the Squared Error between two images, a template and a patch of the image.

These images are color and you will convert them to grayscale can do the tracking in either the full color image, or in grayscale, or even in the green channel. If you use color, there would be an outer summation over the three color channels. If you want to use grayscale, you can use `cvtColor` in OpenCV or just use a weighted sum of R,G,B to get a luma value (try weights of 0.3, 0.58, and 0.12).

MSE, of course, only indicates how dissimilar the image patch is, whereas we need a similarity measure so that more similar patches are more likely. Thus, we will use a squared exponential equation (Gaussian) to convert this into a usable measurement function:

$$p(z_t | x_t) \propto \exp\left(\frac{-MSE}{2\sigma_{MSE}^2}\right)$$

To start out, you might use a value of  $\sigma_{MSE} = 10$  (for grayscale in 0-255 range) but you might need to change this value.

For the dynamics we're going to use normally distributed noise since the object movements can be unpredictable and often current velocity isn't indicative of future motion; so our dynamics model is merely

$$x_t = x_{t-1} + \delta_t, \text{ where } \delta_t \sim N(0, \Sigma_d), \Sigma_d = \begin{bmatrix} \sigma_d^2 & 0 \\ 0 & \sigma_d^2 \end{bmatrix}$$

which is just a fancy way to say you add a little bit of Gaussian noise to both  $u$  and  $v$  independently.

The number of particles and initial distribution are up to you to figure out. You may need to tune your parameters for these to get better tracking/performance.

In order to visualize the tracker's behavior you will need to overlay each successive frame with the following elements:

- Every particle's  $(x,y)$  location in the distribution should be plotted by drawing a colored dot point on the image. Remember that this should be the center of the window, not the corner.
- Draw the rectangle of the tracking window associated with the Bayesian estimate for the current location which is simply the weighted mean of the  $(x,y)$  of the particles.
- Finally we need to get some sense of the standard deviation or spread of the distribution. First, find the distance of every particle to the weighted mean. Next, take the weighted sum of these distances and plot a circle centered at the weighted mean with this radius.

You are encouraged to produce these visuals for selected frames. You will not have to submit the entire video.

For reading the frames OpenCV users should look at the class `VideoCapture`. For sampling

based on a distribution, see the functions `numpy.random.multinomial` or `numpy.random.choice`.

**a.**

Implement the particle filter. You can find the bounding box for the initial position in `template_rect` - this is your template. Tweak the parameters including window size until you can get the tracker to follow this object. Run the tracker and save the video frames described below with the visualizations overlaid.

Classes, methods: Define a class `ParticleFilter`, with the following methods:

- `_init_(frame, template, **kwargs)` : (constructor) Initialize particle filter object.
- `get_error_metric(template, frame_cutout)` : Calculates the error metric used (i.e. MSE).
- `resample_particles()` : Returns a list of particles resampled based on their weights.
- `process(frame)` : Process a frame (image) of video and update filter state.  
\* Hint: You should call `resample_particles()` and `get_error_metrics()` here.
- `render(frame_out)` : Visualize current particle filter state.

Finally, modify the variables `num_particles`, `sigma_mse`, `sigma_dyn` in the `part_2a()` function to appropriate values.

A helper function, `run_particle_filter()`, has been provided to run your particle filter on a video. You can also display every video frame to verify that your particle filter is working properly.

Note: The helper function `run_particle_filter()` can save the template image patch and outputs generated by your `render()` method for desired frames. See template code for details.

Input directory: `circle/0000.jpg` to `circle/0099.jpg`

Code: `ParticleFilter()` and `part_2a()` in `ps5.py`

**b.**

Now use the particle filter with a noisy video sequence of images in the 'pres\_debate\_noisy' directory.

Input directory: `pres_debate_noisy/000.jpg` to `pres_debate_noisy/099.jpg`

Code: `part_2b()` in `ps5.py`

### 3 CHANGES IN APPEARANCE

In the last section you were working with a static template assuming that the target will not change in shape. This can be addressed by updating the model's appearance over time.

Modify your existing tracker to include a step which uses the history to update the tracking window model. We can accomplish this using what's called an Infinite Impulse Response (IIR) filter. The concept is simple: we first find the best tracking window for the current particle distribution as displayed in the visualizations. Then we just update the current window model to

be a weighted sum of the last model and the current best estimate.

$$Template(t) = \alpha Best(t) + (1 - \alpha) Template(t - 1)$$

where  $Best(t)$  is the patch of the best estimate or mean estimate. It's easy to see that by recursively updating this sum, the window implements an exponentially decaying weighted sum of (all) the past windows. For this assignment, you may assume  $t$  to be the frame number, in lieu of a time measure.

**a.**

Implement the appearance model update feature. Run the tracker on the presidential debate images and adjust parameters until you can track the person's hand (the one not holding the microphone). Your tracker's bounding box should only contain the hand at all times. Run the tracker. You can save the video frames with the visualizations overlaid for reference.

Classes, methods: Derive a class `AppearanceModelPF` from `ParticleFilter`, retaining the same interface - i.e., with methods `process()` and `render()`, as defined above. The constructor and `process()` method should transparently handle model updates. You can supply additional keyword arguments to the constructor, if needed.

Finally, modify the variables `num_particles`, `sigma_mse`, `sigma_dyn` in the `part_3()` function to appropriate values

Input directory: `pres_debate/000.jpg` to `pres_debate/165.jpg`

Code: `AppearanceModelPF()` and `part_3()` in `ps5.py`

## 4 PARTICLE FILTERS AND OCCLUSIONS

For this part we will work with a much more difficult video to perform tracking with, `pedestrians.mp4`. We'd like to be able to track the blond-haired woman (the one with the white jacket) as she crosses the road. If you try applying your adaptive tracker to this video, you will probably find that you will have difficulty dealing simultaneously with occlusion and the perspective shift as the woman walks away from the camera. Thus, we need some way of relying less on updating our appearance model from previous frames and more on a more sophisticated model of the dynamics of the figure we want to track.

Expand your appearance model to include window size as another parameter. This will change the representation of your particles. You are highly recommended to use `cv2.resize` for your implementation to resize the template to track.

**a.**

Run the tracker and save the video frames described below with the visualizations overlaid. You will receive full credit if you can reliably track (illustrate this with the rectangle outline) all the way to the end of the street and deal gracefully with the occlusions (reasonable tracking at frame 300). The tracking box must track the person's position and size. The bounding box is expected to contain more than 50% of the tracked person and should be within 0.5 times to 2 times the size of the person.



Classes, methods: Derive a class `MDParticleFilter` from `AppearanceModelPF`, retaining the same interface - i.e., with methods `process()` and `render()`, as defined above. The constructor and `process()` method should transparently handle model updates in appearance and dynamics. You can supply additional keyword arguments to the constructor and other methods, if needed.

Finally, modify the variables `num_particles`, `sigma_mse`, `sigma_dyn` in the `part_4()` function to appropriate values.

Code: `MDParticleFilter()` and `part_4()` in `ps5.py`

Report: Frames to record 40, 100, 240, 300.

-Input: `pedestrians/000.jpg` to `pedestrians/319.jpg`.

-Output: `ps5-4-a-1.png`, `ps5-4-a-2.png`, `ps5-4-a-3.png`, and `ps5-4-a-4.png`

-Text Answer: Describe what you did. How did you modify the Particle Filter class to continue tracking after occlusions?

## 5 TRACKING MULTIPLE TARGETS

Now use either a kalman or particle filter to track multiple targets as they move through the given video. Use the sequence of images in the TUD-Campus directory to detect the people shown below. The bounding box is expect to contain more than 50% of the tracked person and should be within 0.5 times to 2 times the size of the person.



Input directory: `TUD-Campus/01.jpg` to `TUD-Campus/71.jpg`

Code: `part_5()` in `experiment.py`

Report:

- Frames to record: 29, 56, 71

- Output: `ps5-5-a-1.png`, `ps5-5-a-2.png`, `ps5-5-a-3.png`

- Text Answer: Describe what you did. How different it was to use a KF vs PF? Which one worked best and why? Include details about any modifications you had to apply to handle multiple targets.

## 6 DETECT PEDESTRIANS FROM A MOVING CAMERA

Finally, detect pedestrians from the given video of a moving camera. Use the images in the directory 'follow' to track the man with the hat holding a white plastic bag. Similar to earlier tasks, the bounding box is expected to contain more than 50% of the tracked person and should be within 0.5 times to 2 times the size of the person.

Input directory: follow/001.jpg to follow/186.jpg

Code: part\_6() in experiment.py

Report:

- Frames to record: 60, 160, 186
- Output: ps5-6-a-1.png, ps5-6-a-2.png, ps5-6-a-3.png
- Text Answer: Describe what you did. Did this task present any additional challenges compared to the previous sections? Include details about any modifications you had to apply.