

# NUMBER AND BRIGHTNESS

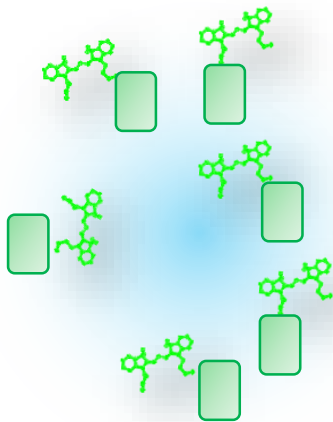
Emmanuel MARGEAT  
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Centre de Biochimie Structurale - Montpellier

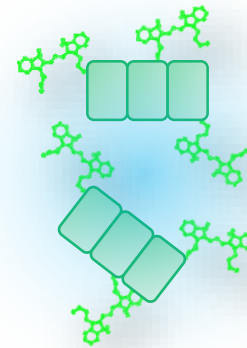
# Measuring oligomerization

In an observation volume (« a pixel »), the fluorescence signal  $I$  is proportional to the number of fluorophores

$$n = 6$$
$$\varepsilon = 1$$



$$I \sim 6$$



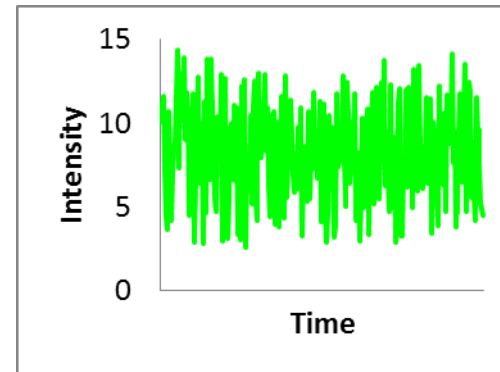
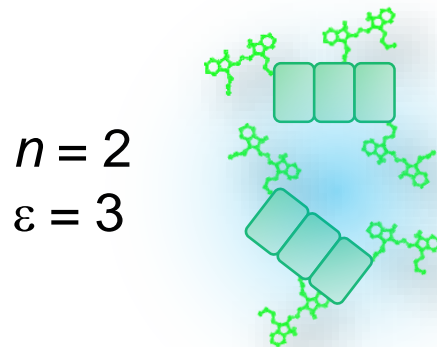
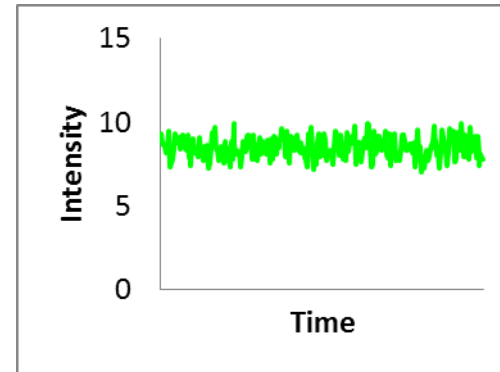
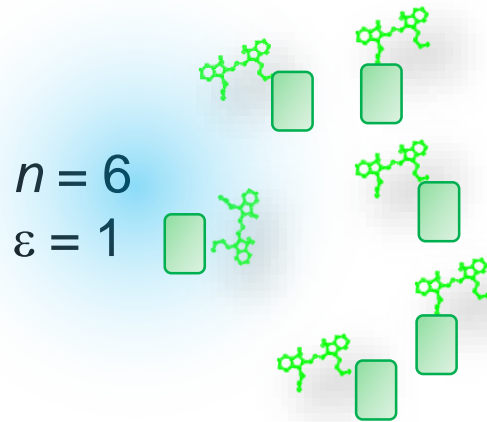
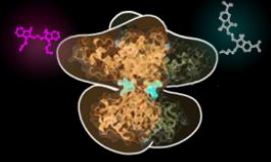
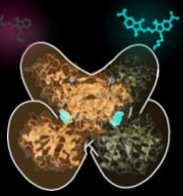
$$n = 2$$
$$\varepsilon = 3$$

We define  $n$ =number of diffusing particles in the observation volume,  
and  $\varepsilon$ =their molecular brightness

$$I = \varepsilon \cdot n$$

In the « small ensemble » regime,  $\varepsilon$  and  $n$  are extracted from the fluctuation of  $I$

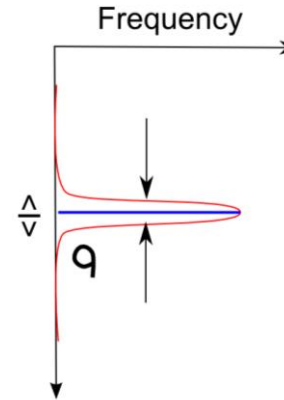
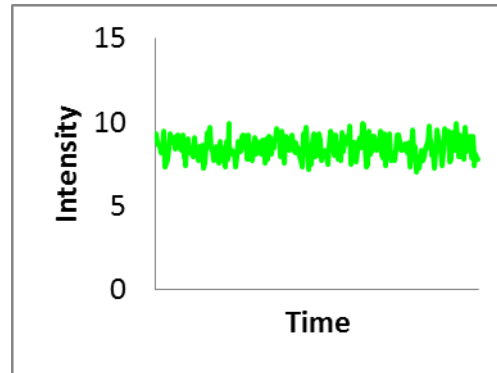
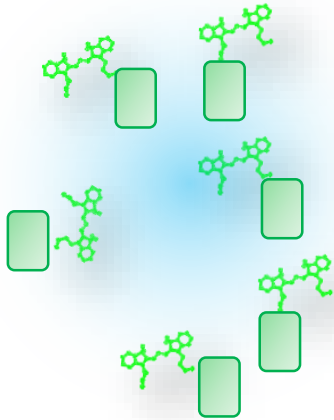
# Measuring oligomerization



# Measuring oligomerization

$$n = 6$$

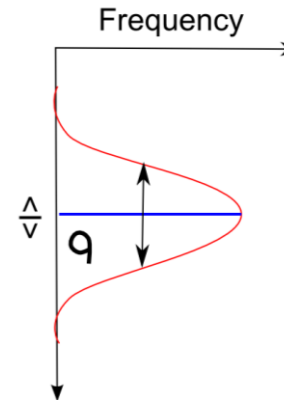
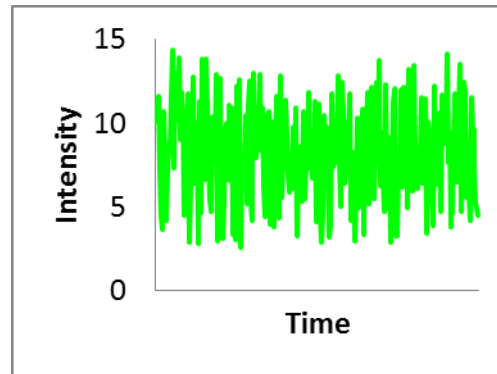
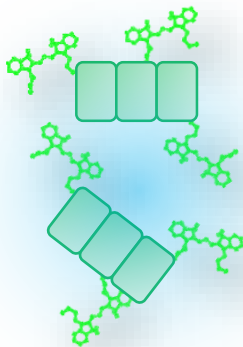
$$\varepsilon = 1$$



Same  $\langle I \rangle$   
Different  $\sigma$

$$n = 2$$

$$\varepsilon = 3$$

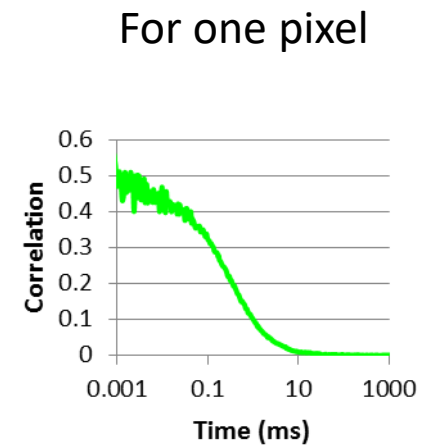
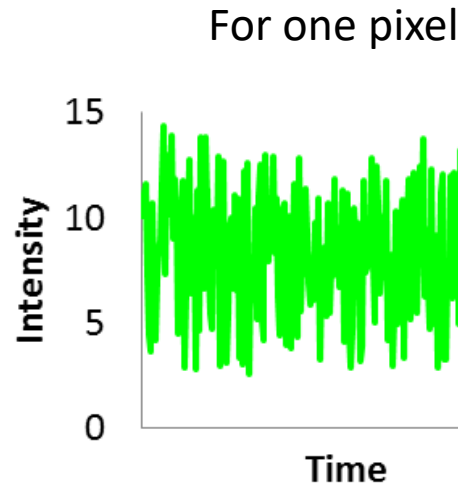
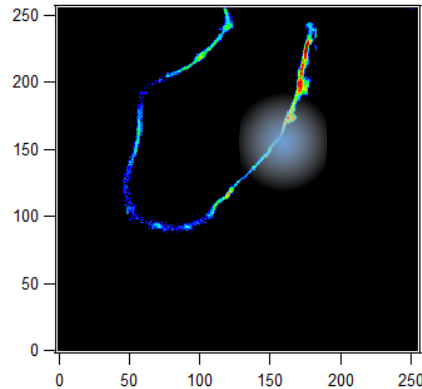
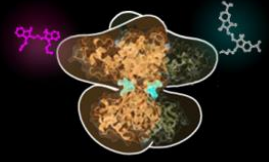
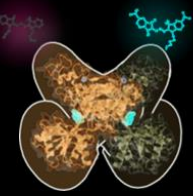


$$\varepsilon = \frac{\sigma^2 - \langle I \rangle}{\langle I \rangle}$$

$$n = \frac{\langle I \rangle^2}{\sigma^2 - \langle I \rangle}$$

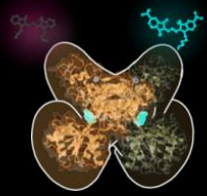
Change in the number of diffusing species ( $n$ ) and their brightness ( $\varepsilon$ )

# Data acquisition I : FCS

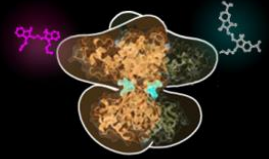


Obtain simultaneously  $n$ ,  $\varepsilon$ ,  $t_d$  with great accuracy

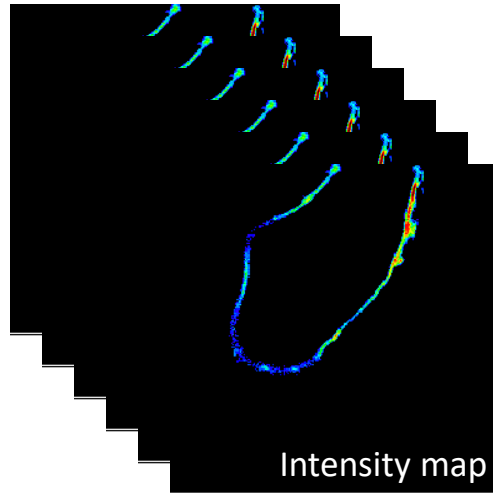
- Time consuming (several seconds / pixel)
- Photobleaching is a big issue
- Difficult to obtain an image of  $n$ ,  $\varepsilon$ ,  $t_d$  (only a few points)



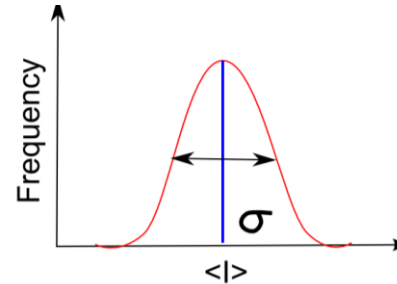
# Data acquisition II : N&B



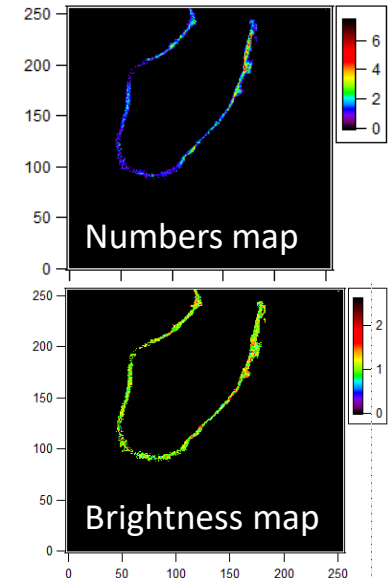
Stack of 100 images



For each pixel



*Calculation of  $n$  &  $\varepsilon$*

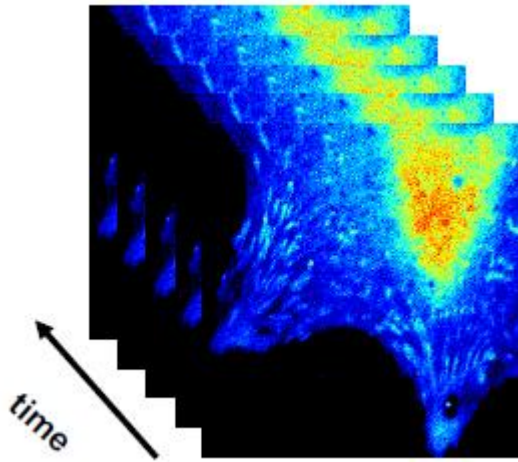


- + Obtain an image of  $n$  &  $\varepsilon$
- + Photobleaching is reduced
- + Implemented on commercial CLSM

- Timing information ( $t_D$ ) is loss
- Necessary to have high speed scanning, photon counters preferred

# Principle of the N&B analysis

For a stack of  $k$  images, we define for each pixel !



$$F = \frac{\sum F(x, y)}{K}$$

$$\sigma_F^2 = \frac{\sum (F(x, y) - F)^2}{K}$$

Therefore we calculate:

$$\frac{\sigma_F^2}{\langle F \rangle^2} = \frac{1}{\langle N \rangle} \Rightarrow \langle N \rangle = \frac{\langle F \rangle^2}{\sigma_F^2}$$

$$\langle F \rangle = B \langle N \rangle \Rightarrow B = \frac{\sigma_F^2}{\langle F \rangle}$$

# Principle of the N&B analysis

## Contributions to the variance

Fluctuations of the number of particles  $\sigma_n^2 = \varepsilon^2 n$

$n$  = true number

Fluctuations due to detector noise  $\sigma_d^2 = \varepsilon n$

$\varepsilon$  = true brightness

Total variance of the signal  $\sigma^2 = \sigma_n^2 + \sigma_d^2$

$$B = \frac{\sigma_F^2}{\langle F \rangle} = \frac{\varepsilon^2 n + \varepsilon n}{\varepsilon n} = 1 + \varepsilon$$

$$\langle N \rangle = \frac{\langle F \rangle^2}{\sigma_F^2} = \frac{\varepsilon^2 n^2}{\varepsilon^2 n + \varepsilon n} = \frac{\varepsilon n}{\varepsilon + 1}$$

$$\varepsilon = \frac{\sigma_F^2 - \langle F \rangle}{\langle F \rangle}$$

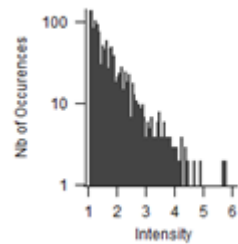
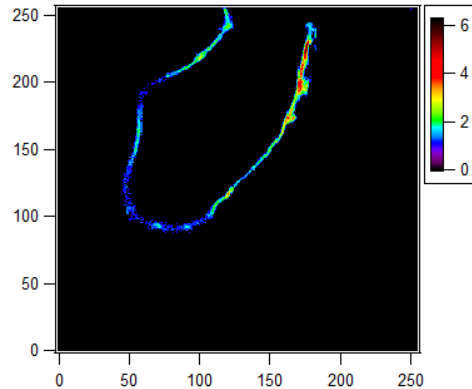
$$n = \frac{\langle F \rangle^2}{\sigma_F^2 - \langle F \rangle}$$

If the molecules are immobile, only the detector noise contributes to the variance (ie  $\sigma^2 = \varepsilon n$ ). Thus,  $n$  cannot be calculated, and  $B=1$

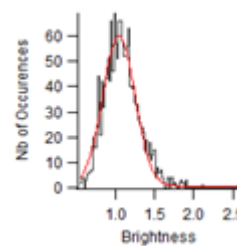
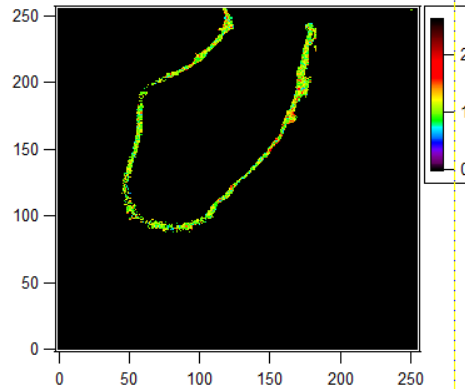


# N&B data representation

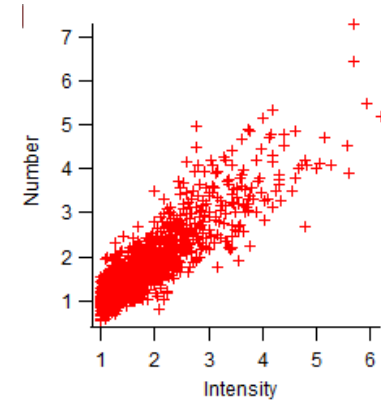
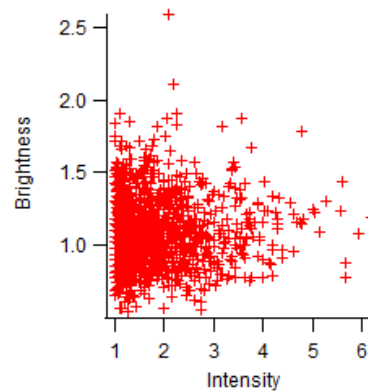
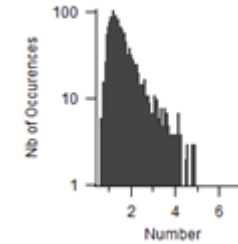
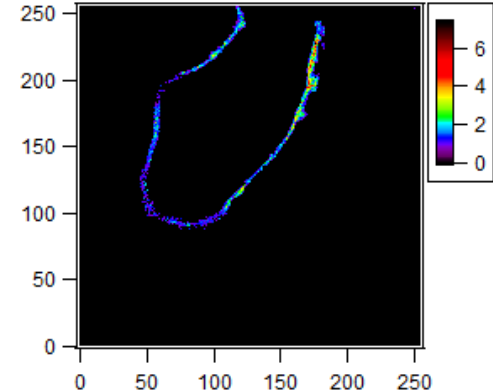
Intensity map



Brightness map



Number map



# N&B : Experimental considerations

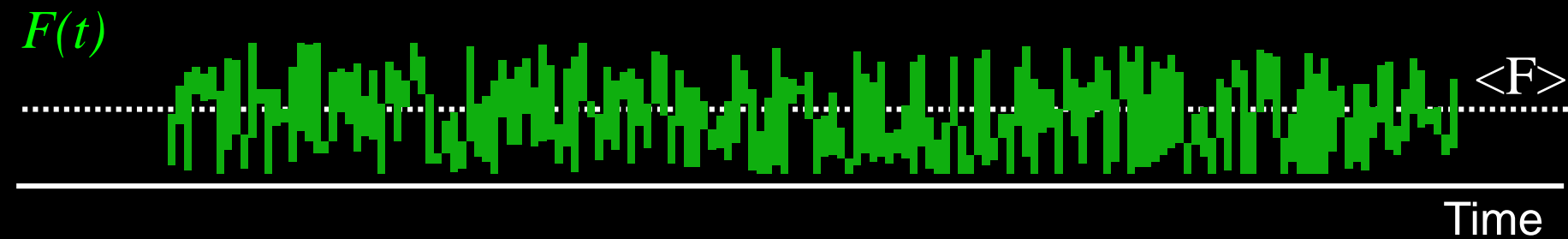
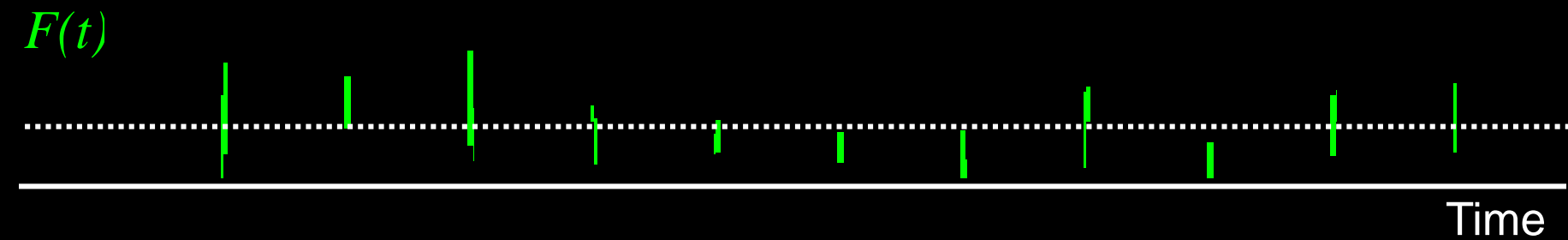
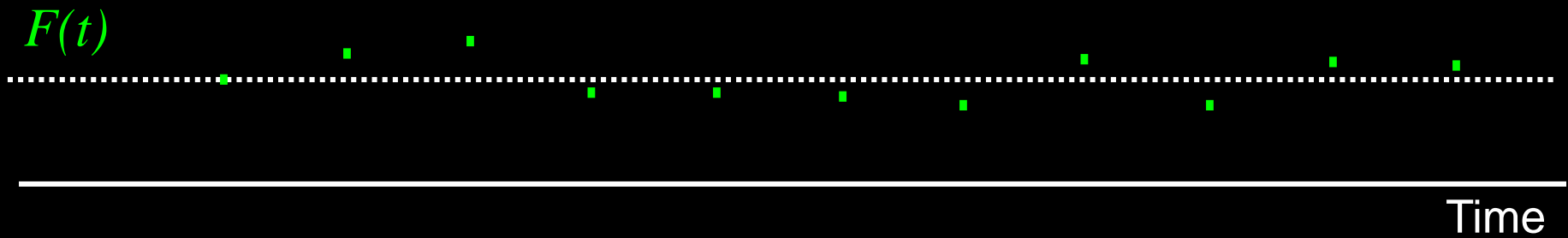
## Imaging system

- In principle, any microscope with laser scanning can be used
  - Sensitivity
  - Photon counting detectors
  - Fast scanning

## In the lab we use a semi-commercial system

- Femtosecond IR laser for 2-photon excitation
  - Low background
  - No out-of focus photobleaching
  - Small observation volume
  - Multicolor excitation (cross-correlation)
- Inverted microscope, high NA objective
- Detector ISS ALBA : scanning mirrors et 2 channel detection

# Fast Scanning



# Slow scanning

$F(t)$



Time

$F(t)$



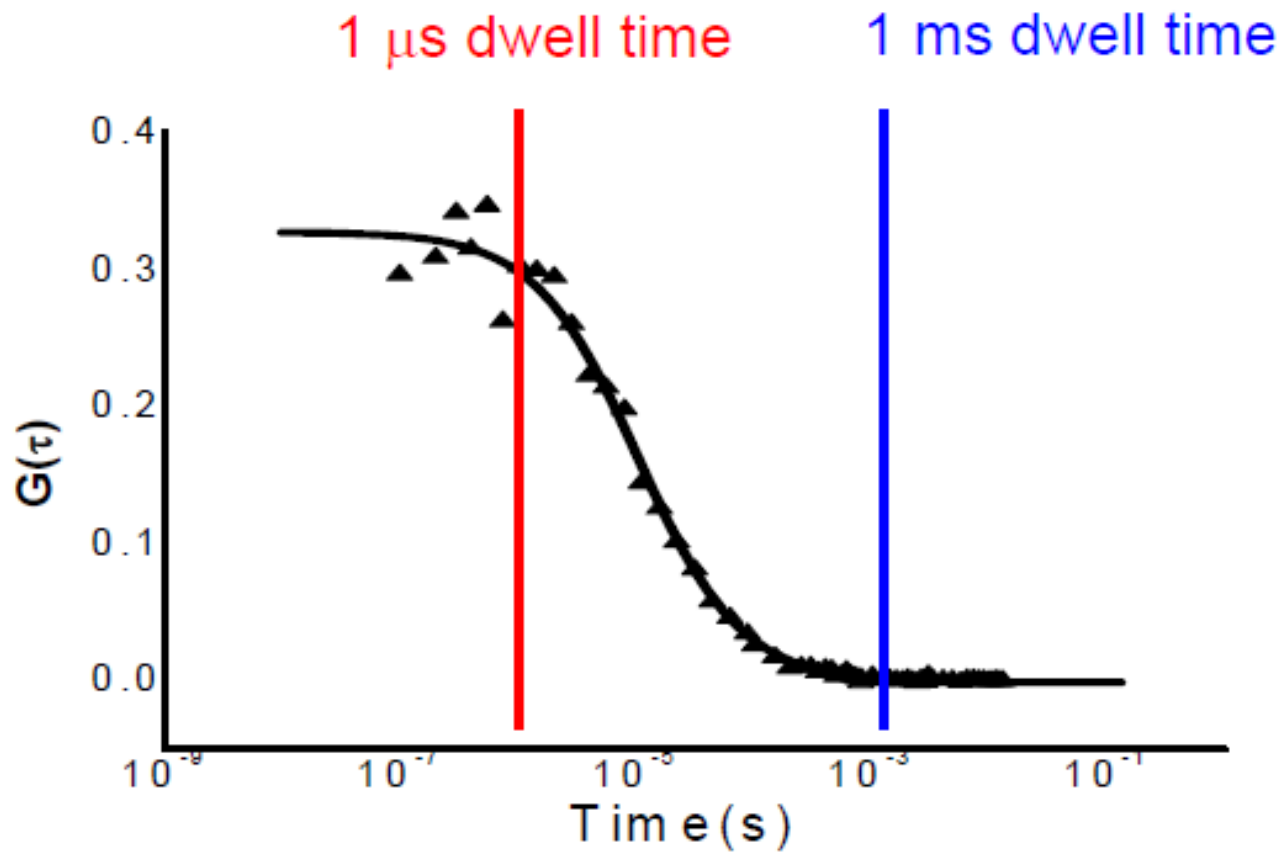
Time

$F(t)$



Time

Increasing the dwell time decreases the amplitude of the fluctuation.



# Summary of N&B

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- N&B distinguishes between number of molecules and molecular brightness in the same pixel
- The acquisition for the N&B can be done with a commercial Laser Scanning Microscope (LSM) and the same data used for RICS can be used to map N and B.
- The Immobile fraction can be separated since it has a Brightness value =1
- The N&B analysis of paxillin at adhesions shows large aggregates of protein during disassembly.

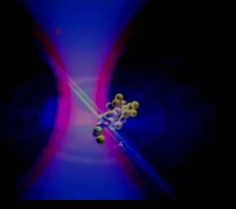
# N&B : en résumé

- N&B allows the quantification of the number of molecules, and their brightness, pixel by pixel
  - An « image » of N and B is obtained
- Aquisition can be done with a conventional LSCLM
- An immobile fraction can be detected ( $B=1$ )
- Sample photobleaching can be reduced as compared to FCS, but temporal information is lost.

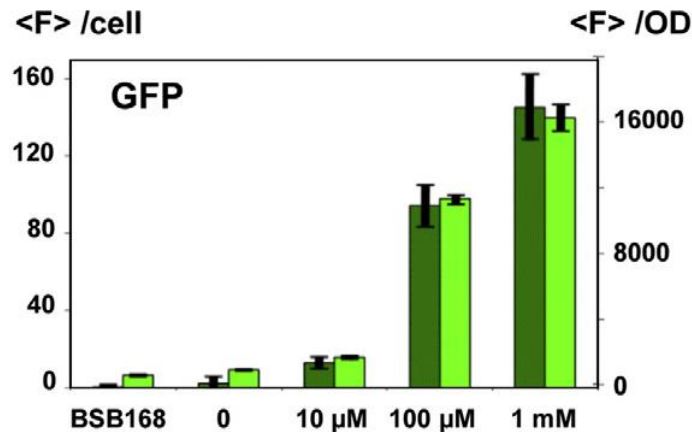
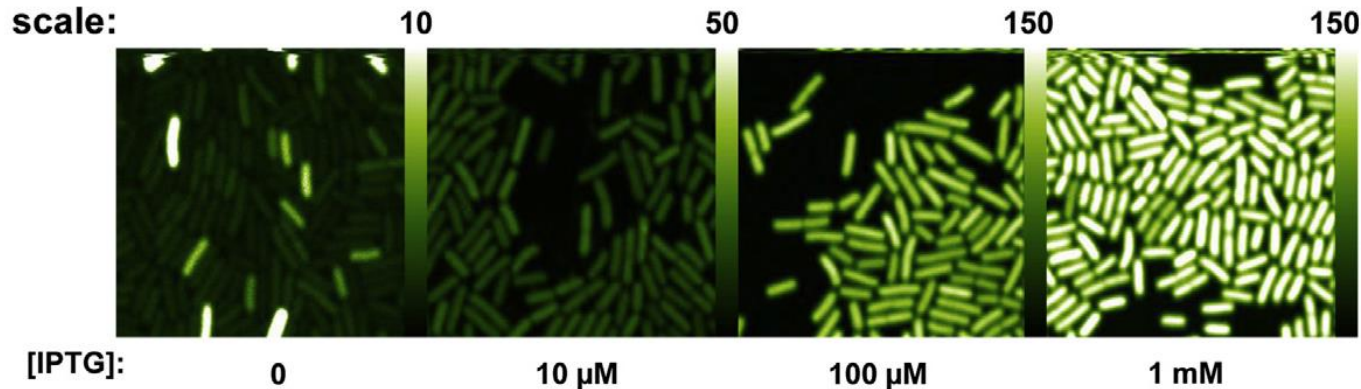


- Fluctuations in N are needed !!!
  - Low concentration ( $< \mu\text{M}$ )
  - Low background noise
  - Low photobleaching

# Quantification of noise in gene expression in bacteria



Expression of Gfpmut2 under control of an inducible promoter in *B. Subtilis*



Correlation between the expression determined by 2P-microscopy and ensemble fluorescence



# Quantification of noise in gene expression in bacteria

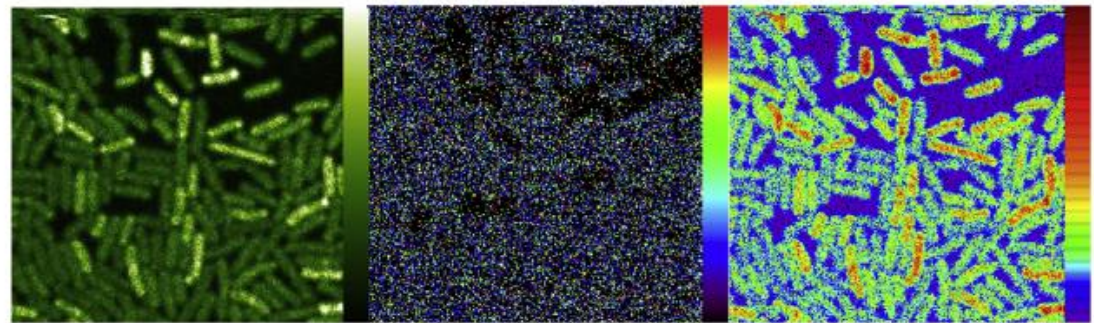
Expression of Gfpmut3 under control of *gapB* promoter in *B. Subtillis*

Glucose

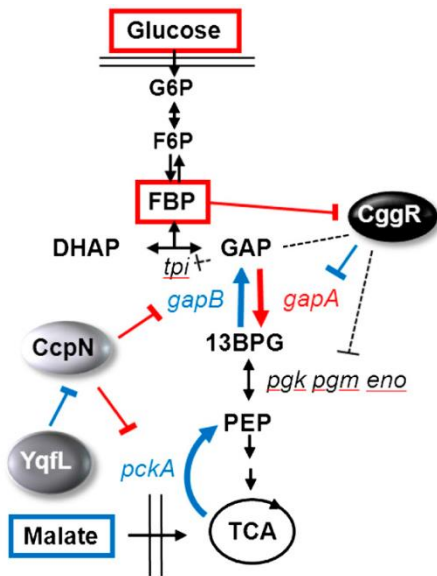
f

$\epsilon$

n

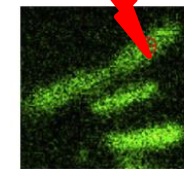
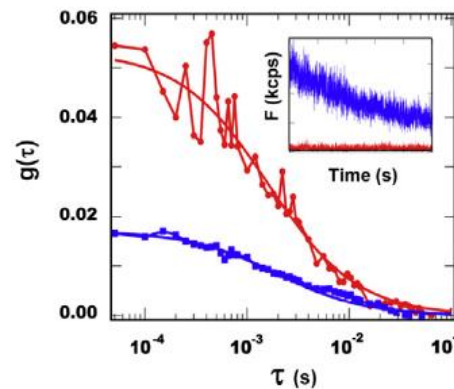


Variability in gene expression in a population

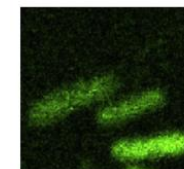


Glucose

Malate

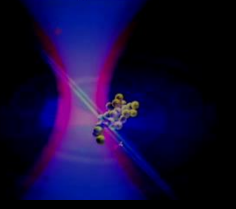


Before FCS

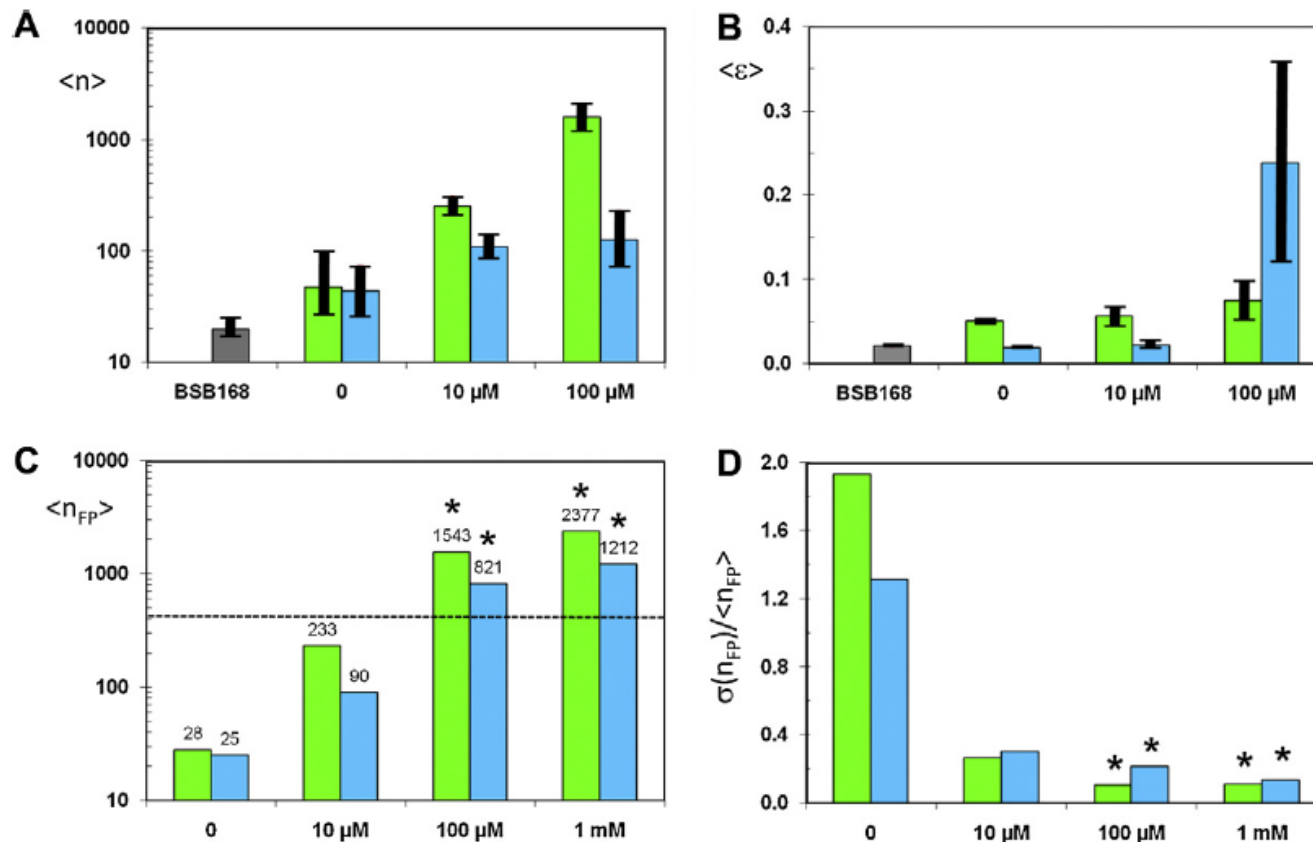


After FCS

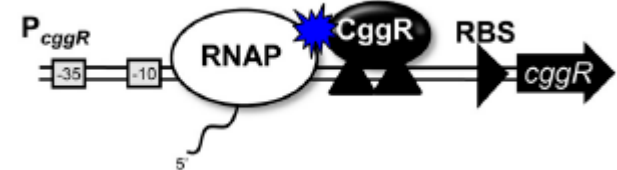
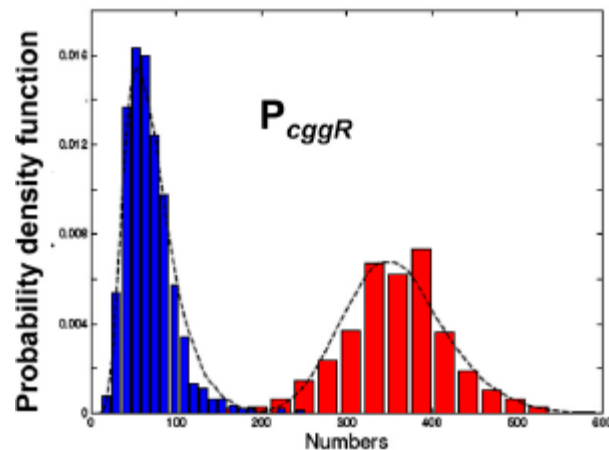
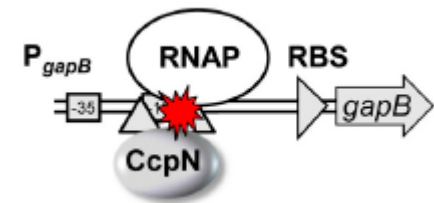
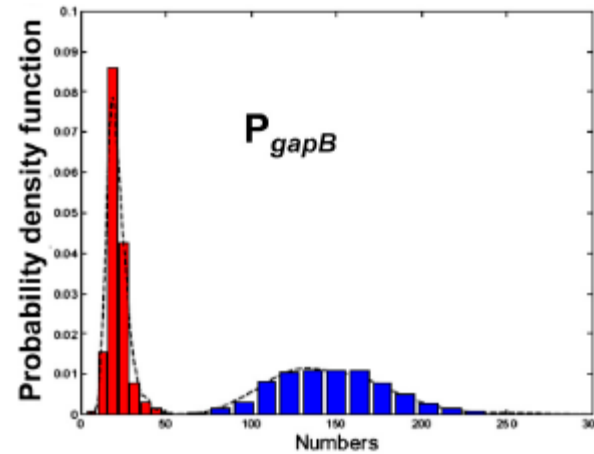
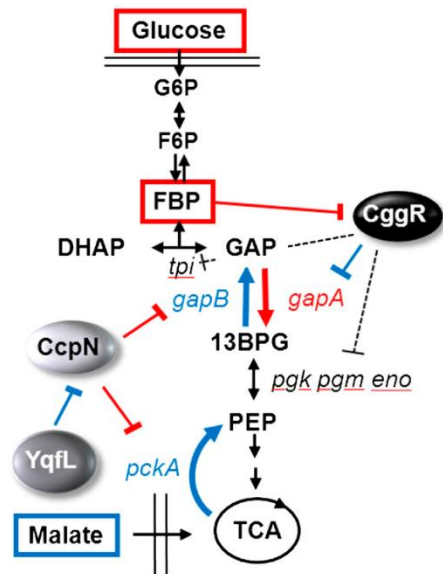
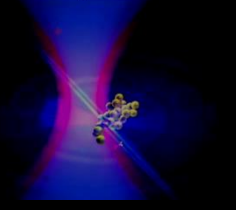
# Quantification of noise in gene expression in bacteria

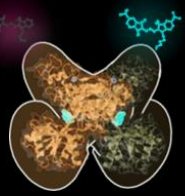


Expression of **Gfpmut3** and **CFP** under control of *gapB* promoter in *B. Subtilis*

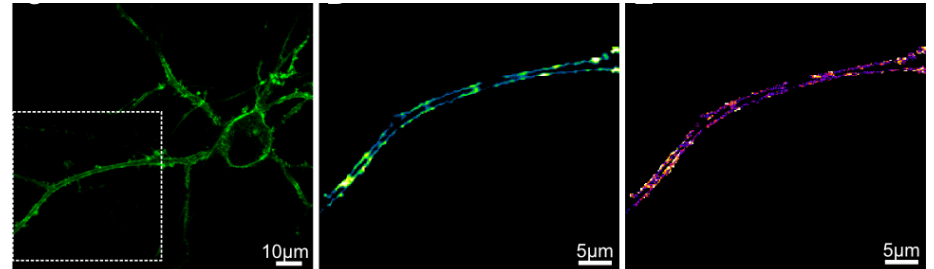
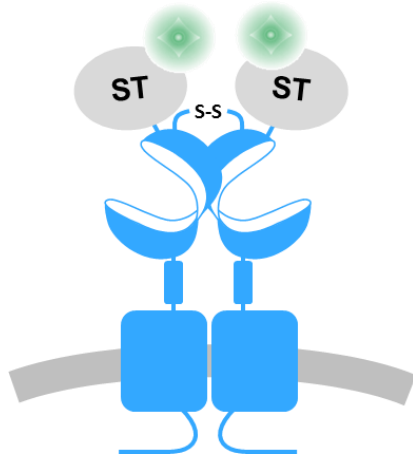
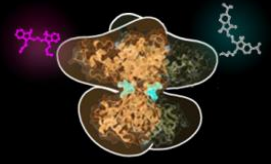


# Quantification of noise in gene expression in bacteria





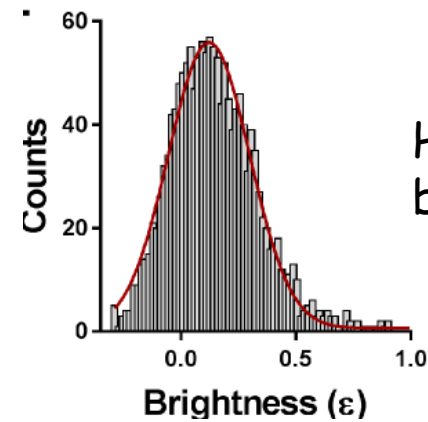
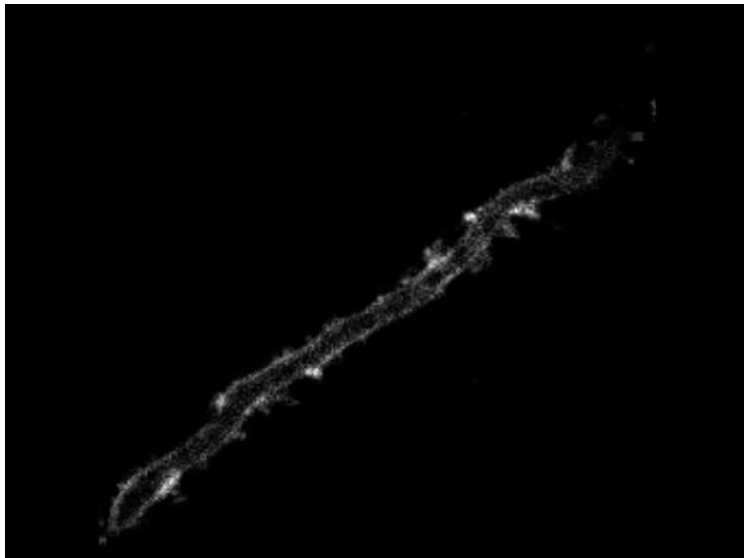
# mGluR and GABA<sub>B</sub> oligomerization



Neuron

ROI

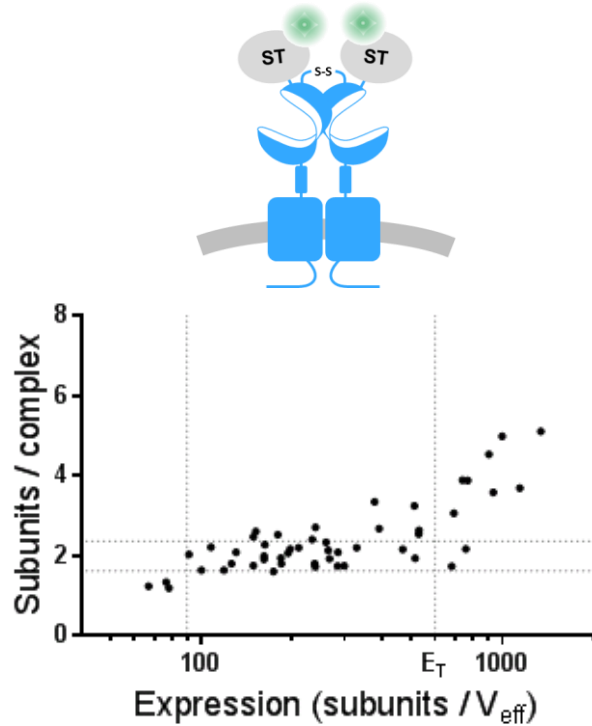
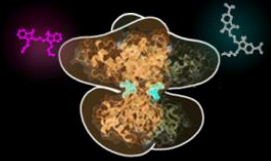
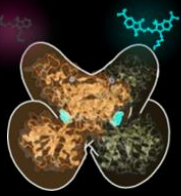
Bmap



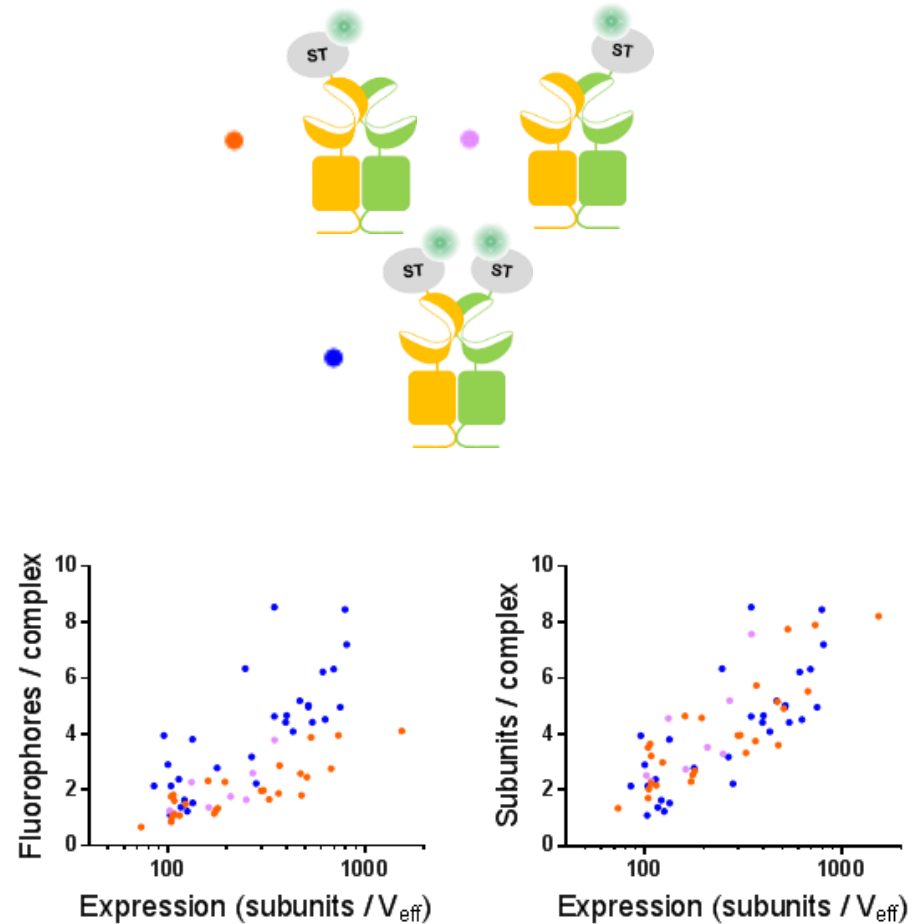
Histogram of  
brightness values

→ Compare with the value of a single Alexa488

# mGluR and GABA<sub>B</sub> oligomerization

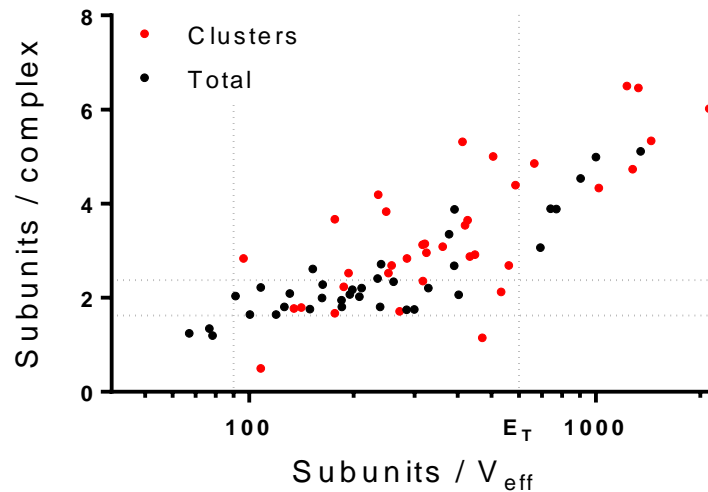
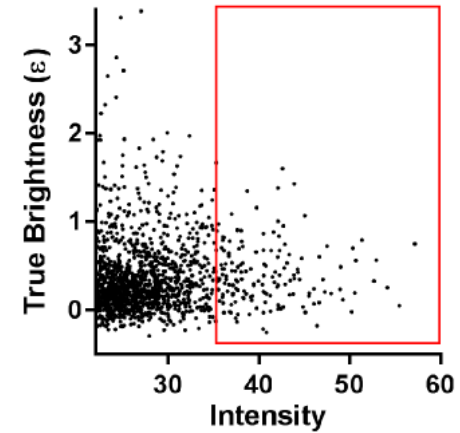
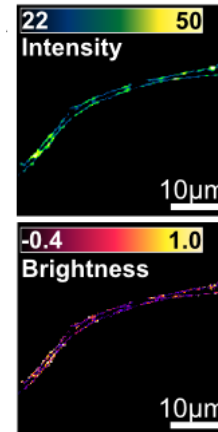
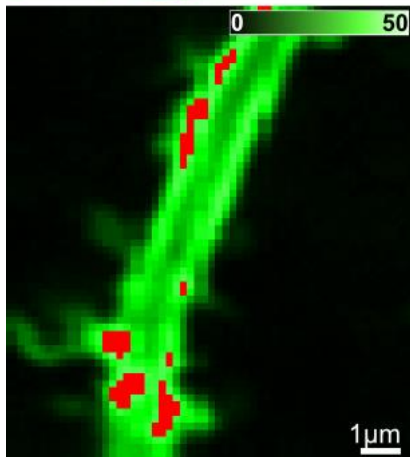
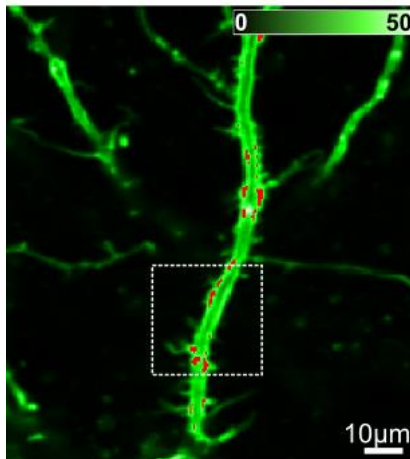
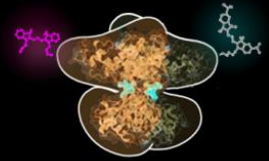
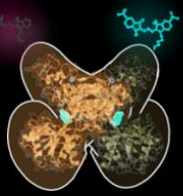


→ mGlu2 appears mainly as a dimer



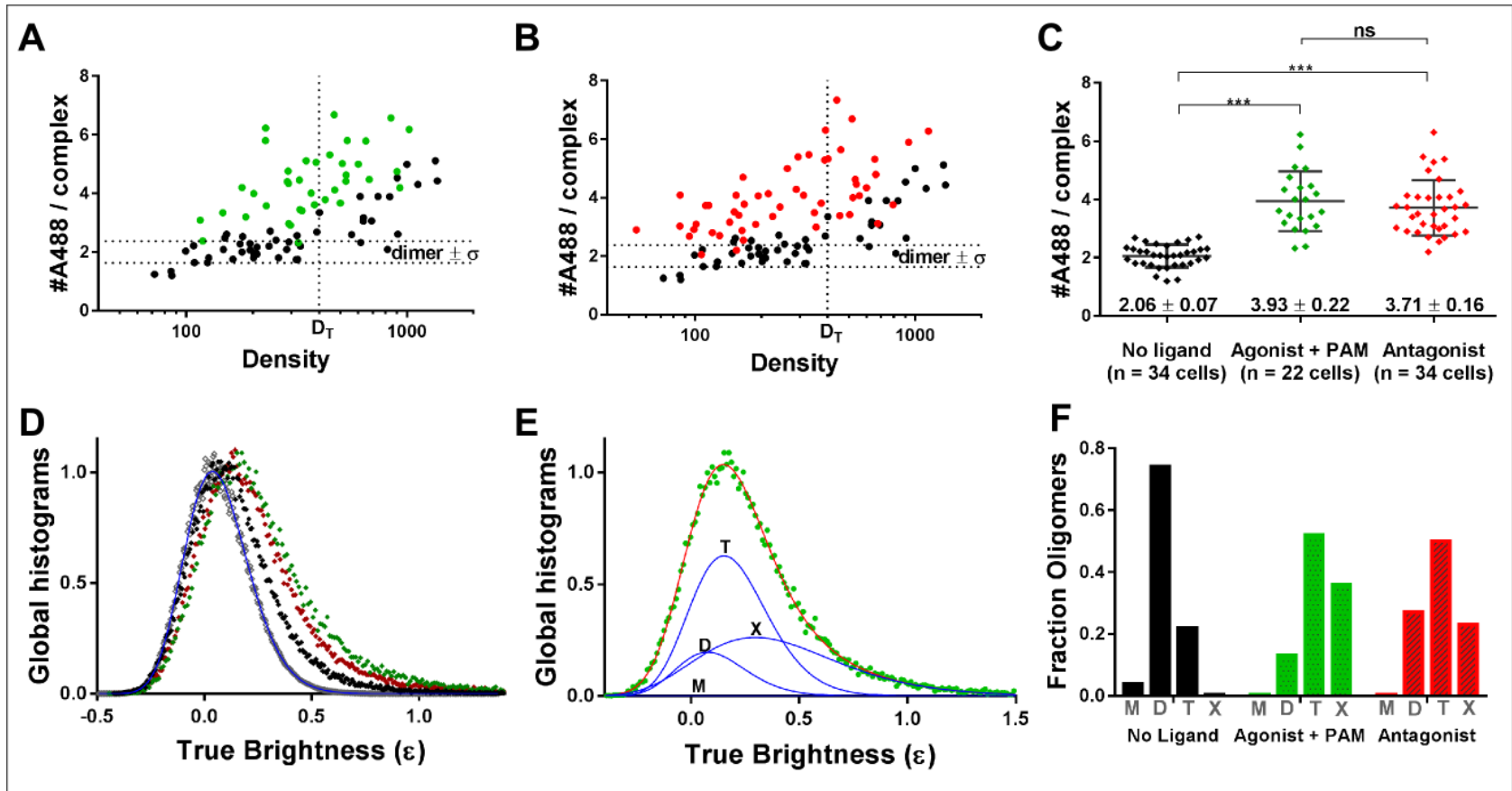
→ GABA<sub>B</sub> forms higher order oligomers

# Spatial distribution



→ regions of higher intensity represent higher expression, not clusterisation

# Ligand effects on mgluR oligomerization



→ mGlu2 makes dimers of dimers in the presence of agonists and antagonists