

$\frac{\partial f}{\partial x}$

$\frac{\partial f}{\partial y}$

$$(e^{2y} - y \cos xy) dx + (2xe^{2y} - x \cos xy + 2y) dy = 0$$

Step #1: $M = e^{2y} - y \cos xy$

$N = 2xe^{2y} - x \cos xy + 2y$

$$\frac{\partial M}{\partial y} = 2(e^{2y}) - [y(-\sin xy(x) + \cos xy(1))]$$

$$\frac{\partial N}{\partial x} = 2e^{2y}(1) - [x(-\sin xy(y)) + \cos xy(1)] + 0$$

$$\frac{\partial M}{\partial y} = 2e^{2y} + x y \sin xy - \cos xy$$

$$\frac{\partial N}{\partial x} = 2e^{2y} + x y \sin xy - \cos xy$$

As it holds the property of differential Equation

Step #2: $M = e^{2y} - y \cos xy$

$$\frac{\partial f}{\partial x} = e^{2y} - y \cos xy$$

$$\int \frac{\partial f}{\partial x} = \int (e^{2y} - y \cos xy) dx$$

$$f = \int e^{2y} dx - \int y \cos xy dx$$

$$f = e^{2y} \int 1 dx - y \int \cos xy dx$$

$$f = x \cdot e^{2y} - y \cdot \frac{\sin xy}{y} + C$$

$$f = x \cdot e^{2y} - y \cdot \frac{\sin xy}{y} + g(y)$$

$$f = x e^{2y} - \sin xy + g(y) \rightarrow \text{eq. (A)}$$

$$\frac{\partial f}{\partial y} = x e^{2y}(2) - \cos(xy)(x) + g'(y)$$

Step #3:

$$\frac{\partial f}{\partial y} = (2xe^{2y} - x \cos xy + g'(y))$$

$$2xe^{2y} - x \cos xy + 2y = 2xe^{2y} - x \cos xy + g'(y)$$

$$g'(y) = 2y$$

Step #4: $\int (g'(y)) dy = \int (2y) dy$

$$g(y) = 2 \int y dy$$

$$g(y) = 2 \left(\frac{y^2}{2} \right)$$

$$g(y) = y^2 \rightarrow \text{eqv}(B)$$

Put eqv(B) in eqv(A)

$$f = x e^{2y} - \sin xy + g(y)$$

$$f(x, y) = x e^{2y} - \sin xy + y^2$$

$$C = x e^{2y} - \sin xy + y^2 \quad \therefore C = f(x, y)$$