

Communication Systems

project

Frequency-Modulated Continuous-Wave Joint Radar and Communications

```
% Given system parameters
fc = 62.64e9;           % Center frequency in Hz
fs = 2e9;               % Sampling frequency in Hz
Tc = 15.2e-6;          % Chirp duration in seconds
guard_time = 0.1e-6;    % Guard time at the end of each chirp

% Parameters for chirp generation
num_chirps = 256;
total_bits = 13;

% Information bits
bits_bandwidth = 7;
bits_frequency = 6;

% Generate random bit sequences for bandwidth and frequency
bandwidth_bits = randi([0, 1], num_chirps, bits_bandwidth)
```

```
bandwidth_bits = 256x7
    1     1     1     0     0     1     1
    1     0     1     0     0     1     1
    0     0     1     1     1     1     0
    1     1     1     0     0     1     1
    1     0     0     0     1     0     1
    0     1     0     1     0     0     1
    0     1     0     1     1     1     1
    1     1     0     1     0     1     0
    1     0     0     1     1     0     1
    1     0     0     1     1     1     0
    ⋮
```

```
frequency_bits = randi([0, 1], num_chirps, bits_frequency)
```

```
frequency_bits = 256x6
    1     0     1     1     1     0
    0     0     1     0     0     1
    0     0     0     0     0     1
    0     1     1     1     1     0
    0     1     0     0     0     1
    1     0     0     1     1     0
    0     1     0     1     0     0
    0     1     1     1     0     0
    0     0     1     1     1     0
    0     0     0     0     1     0
```

⋮

```
totalSignalBits = cat(2,bandwidth_bits,frequency_bits)
```

```
totalSignalBits = 256×13
```

```

1      1      1      0      0      1      1      1      0      1      1      1      0
1      0      1      0      0      1      1      0      0      1      0      0      1
0      0      1      1      1      1      0      0      0      0      0      0      1
1      1      1      0      0      1      1      0      1      1      1      1      0
1      0      0      0      1      0      1      0      1      0      0      0      1
0      1      0      1      0      0      1      1      0      0      1      1      0
0      1      0      1      1      1      1      0      1      0      1      0      0
1      1      0      1      0      1      0      0      1      1      1      0      0
1      0      0      1      1      0      1      0      0      1      1      1      0
1      0      0      1      1      1      0      0      0      0      0      1      0
⋮

```

```
% Convert binary bits to decimal values
```

```
bandwidth_values = linspace(400e6, 800e6, 2^bits_bandwidth);
```

```
frequency_values = linspace(-100e6, 100e6, 2^bits_frequency);
```

```
selected_bandwidths = bandwidth_values(bi2de(bandwidth_bits,'left-msb') + 1);
```

```
selected_frequencies = frequency_values(bi2de(frequency_bits,'left-msb') + 1);
```

```
close all ;
```

```
% Generate chirps
```

```
chirp_duration = Tc + guard_time;
```

```
t = linspace(0, Tc, fs * Tc);
```

```
time = linspace(0, chirp_duration, fs * chirp_duration);
```

```
transmitted_chirps = zeros(num_chirps, fs * chirp_duration);
```

```
stepUp_chirps = zeros(num_chirps, fs * chirp_duration);
```

```
for i = 1:num_chirps
```

```
    f0 = selected_frequencies(i);
```

```
    f1 = f0 + selected_bandwidths(i);
```

```
    transmitted_chirps(i, 1:length(t)) = chirp(t,f0,Tc,f1,"linear",0,'complex');
```

```
    stepUp_chirps(i, :) = transmitted_chirps(i, :) .* exp(1i * 2 * pi * fc * time );
```

```
end
```

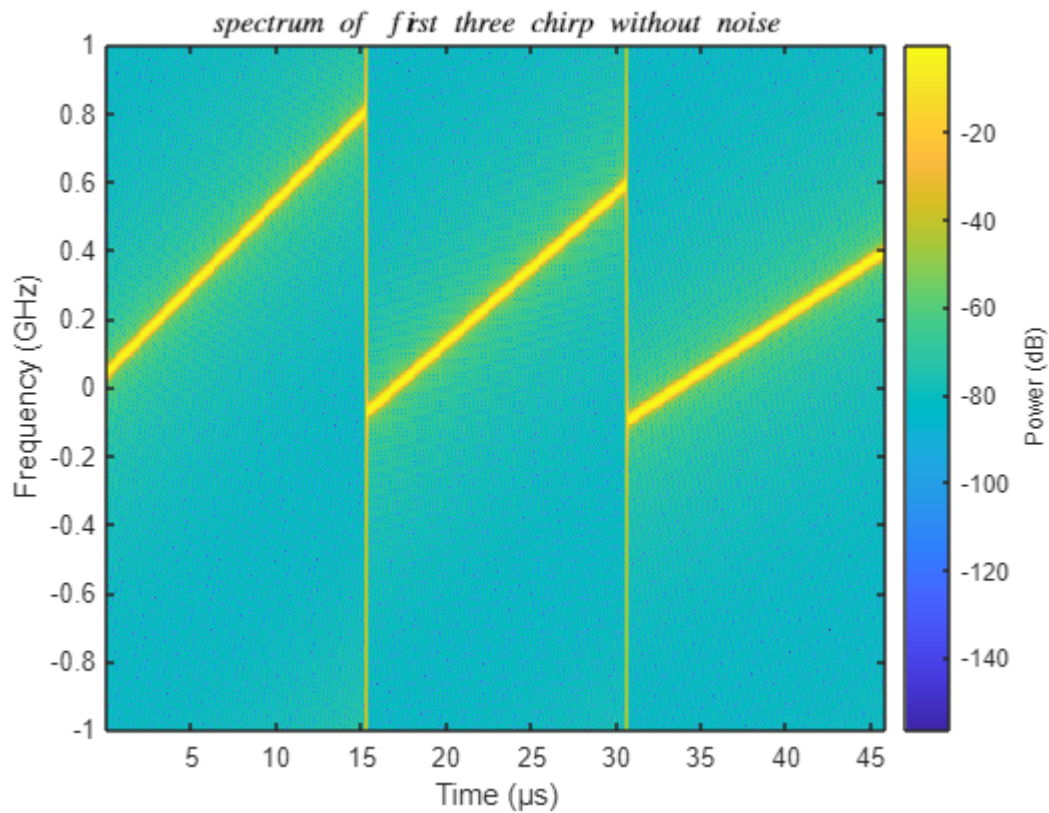
```
transmitted_chirps_fromAntenna = reshape(conj(stepUp_chirps'), 1, []);
```

```
transmitted_chirps_beforStepup = reshape(conj(transmitted_chirps'), 1, []);
```

```
pspectrum(transmitted_chirps_beforStepup(1,1:91800),fs,'spectrogram' ...
```

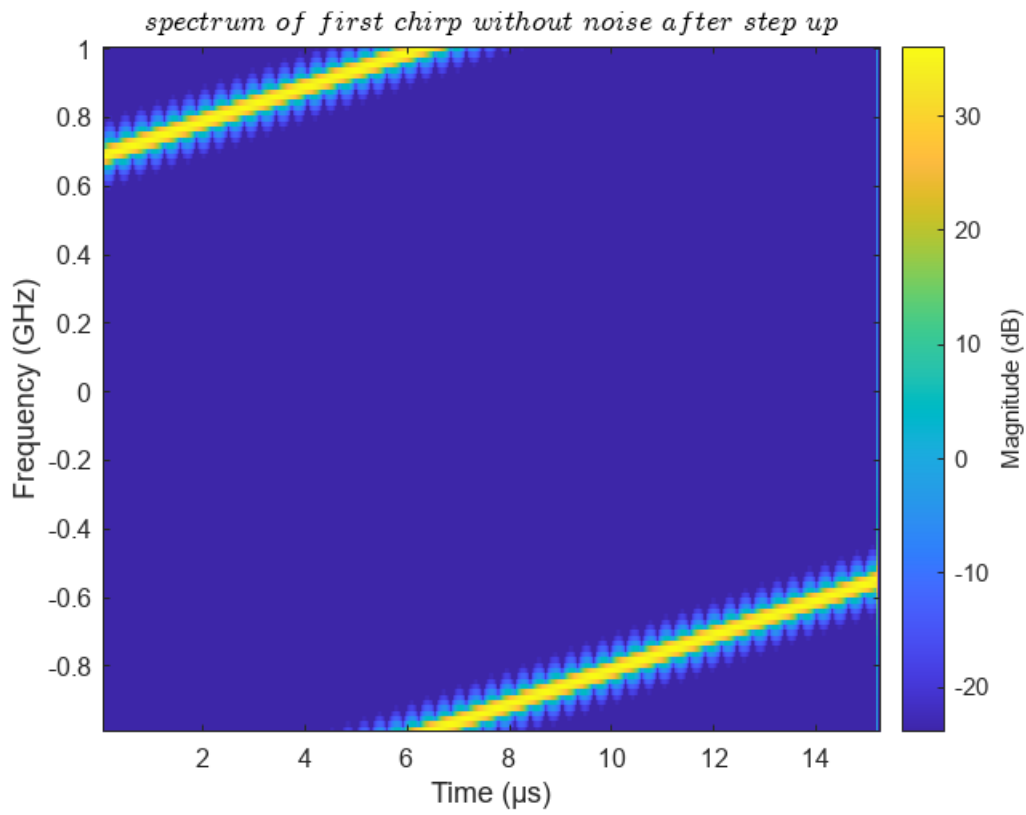
```
    , 'TimeResolution',1e-7, 'OverlapPercent',99,'Leakage',0.85)
```

```
title('$ spectrum \ of \ first \ three \ chirp \ without \ noise $' , 'Interpreter','latex')
```

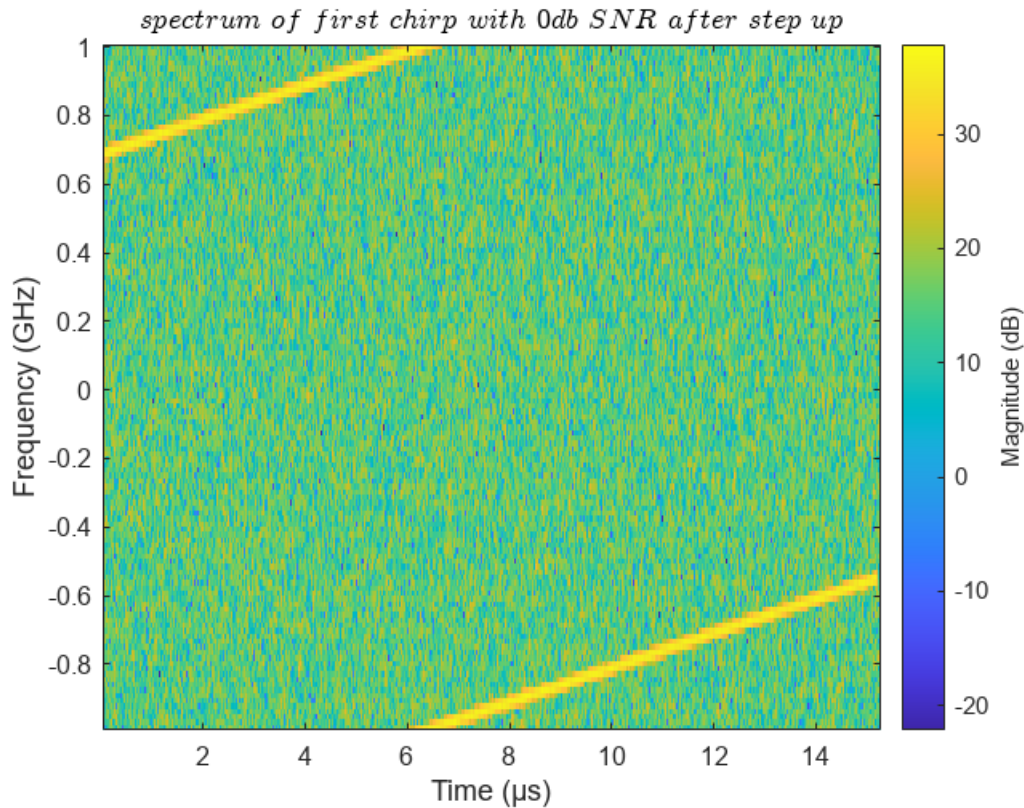


```
% Parameters for AWGN channel
received_chirps = zeros(3 , num_chirps*fs*chirp_duration);

received_chirps(1 , :) = awgn(transmitted_chirps_fromAntenna, 0, 'measured');
received_chirps(2 , :) = awgn(transmitted_chirps_fromAntenna, 10, 'measured');
received_chirps(3 , :) = awgn(transmitted_chirps_fromAntenna, 20, 'measured');
figure
stft(transmitted_chirps_fromAntenna(1,1:30600),fs)
title(['$ spectrum \ of \ first \ chirp \ without \ noise ' ...
      ' \ after \ step \ up $'] , 'Interpreter','latex')
```



```
figure
stft(received_chirps(1,1:30600),fs)
title('$ spectrum \ of \ first \ chirp \ with \ 0db \ SNR \ after \ step \ up $' , 'Interprete
```



% Receiver

```
received_chirps_fromAntenna0dB = received_chirps(1,:) ;
received_chirps_fromAntenna10dB = received_chirps(2,:) ;
received_chirps_fromAntenna20dB = received_chirps(3,:) ;

demultiplaxed_signal0db = reshape(received_chirps_fromAntenna0dB,fs*Tc+200,[]);
removed_gards0db = demultiplaxed_signal0db(1:fs*Tc, :);

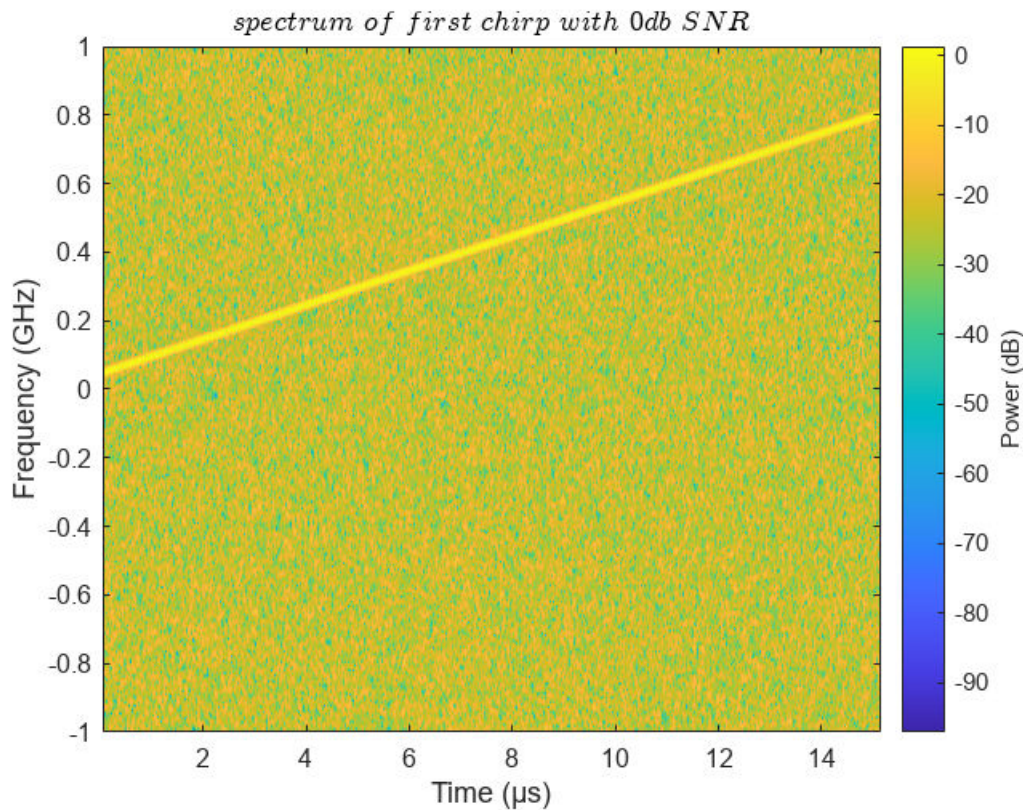
demultiplaxed_signal10db = reshape(received_chirps_fromAntenna10dB,fs*Tc+200,[]);
removed_gards10db = demultiplaxed_signal10db(1:fs*Tc, :);

demultiplaxed_signal20db = reshape(received_chirps_fromAntenna20dB,fs*Tc+200,[]);
removed_gards20db = demultiplaxed_signal20db(1:fs*Tc, :);

signal0db = zeros(256,30400);
signal10db = zeros(256,30400);
signal20db = zeros(256,30400);

for i=1:256
    signal0db(i,:) = conj(removed_gards0db(:,i))' .* exp(-1i * 2 * pi * fc * t);
    signal10db(i,:) = conj(removed_gards10db(:,i))' .* exp(-1i * 2 * pi * fc * t);
    signal20db(i,:) = conj(removed_gards20db(:,i))' .* exp(-1i * 2 * pi * fc * t);
end
```

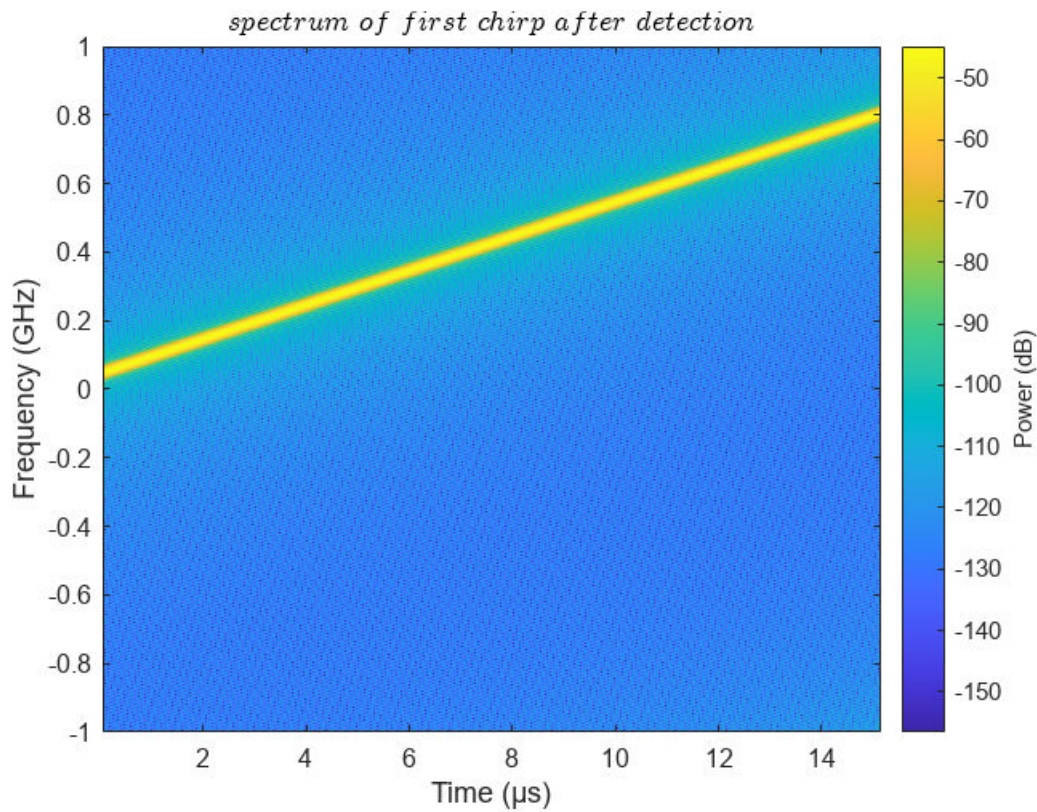
```
figure
pspectrum(signal0db(1,:),fs,'spectrogram' ...
    , 'TimeResolution',1e-7, 'OverlapPercent',99,'Leakage',0.85)
title('$ spectrum \ of \ first \ chirp \ with \ 0db \ SNR $' , 'Interpreter','latex')
```



```
output0db = receiver(signal0db,pure_chirps,5)
```

```
output0db = 256x13
    1    1    1    0    0    1    1    1    0    1    1    1    0
    1    0    1    0    0    1    1    0    0    1    0    0    1
    0    0    1    1    1    1    0    0    0    0    0    0    1
    1    1    1    0    0    1    1    0    1    1    1    1    0
    1    0    0    0    1    0    1    0    1    0    0    0    1
    0    0    0    0    0    0    0    0    0    0    0    0    0
    0    0    0    0    0    0    0    0    0    0    0    0    0
    0    0    0    0    0    0    0    0    0    0    0    0    0
    0    0    0    0    0    0    0    0    0    0    0    0    0
    0    0    0    0    0    0    0    0    0    0    0    0    0
    ⋮
```

```
figure
pspectrum(pure_chirps(bit2int(output0db(1,:))',13,true)+1,:),fs,'spectrogram' ...
    , 'TimeResolution',1e-7, 'OverlapPercent',99,'Leakage',0.85)
title('$ spectrum \ of \ first \ chirp \ after \ detection $' , 'Interpreter','latex')
```

```
output10db = receiver(signal10db,pure_chirps,5)
```

```
output10db = 256×13
```

```

1      1      1      0      0      1      1      1      0      1      1      1      0
1      0      1      0      0      1      1      0      0      1      0      0      1
0      0      1      1      1      1      0      0      0      0      0      0      1
1      1      1      0      0      1      1      0      1      1      1      1      0
1      0      0      0      1      0      1      0      1      0      0      0      1
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
⋮

```

```
output20db = receiver(signal20db,pure_chirps,5)
```

```
output20db = 256×13
```

```

1      1      1      0      0      1      1      1      0      1      1      1      0
1      0      1      0      0      1      1      0      0      1      0      0      1
0      0      1      1      1      1      0      0      0      0      0      0      1
1      1      1      0      0      1      1      0      1      1      1      1      0
1      0      0      0      1      0      1      0      1      0      0      0      1
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
0      0      0      0      0      0      0      0      0      0      0      0      0
⋮

```

Practical test

```
load('FMCW_fcBWmod_JRC.mat');

comm_rx_data = double(data_16bit_IP)+1i*double(data_16bit_QP);
comm_rx_data = interp(comm_rx_data,2);

samplesMat = (0:255).'*30600+(1:30400);
samplesVec = reshape(samplesMat.',1,256*30400);
rx_data = comm_rx_data(samplesVec);

demoultiplaxed_signal = reshape(rx_data,fs*Tc,[]);

output_practical = receiver(conj(demoultiplaxed_signal'),pure_chirps,32)
```

```
output_practical = 256x13
    0     0     1     1     1     1     0     0     1     1     1     1     0
    1     1     1     0     1     0     0     1     0     0     0     0     0
    1     1     0     0     0     1     0     1     1     1     0     1     1
    1     0     0     0     1     1     0     1     1     1     1     1     1
    0     0     0     0     1     1     1     0     0     0     0     1     1
    0     0     0     0     1     1     1     1     1     0     1     1     1
    0     0     1     0     1     0     0     1     1     1     0     0     0
    0     0     0     0     0     0     1     0     0     0     0     0     0
    0     0     0     1     0     1     1     1     1     0     0     1     1
    0     0     1     0     1     1     0     1     1     0     0     1     0
    ⋮
```

plots of practical test

we analyze the initial chirp , discerning its first 7 bits for bandwidth and the remaining 6 bits for frequency , represented as binary numbers **0011110** and **011110** and decimal numbers **30** and **30**. this reveals that our initial chirp has a bandwidth of **494.49MHz**, and a initial frequency of **-4.7619MHz**.

And we identify thirty chirp binary numbers representing bandwidth and frequency denoted as **0000000** and **000000** with corresponding decimal values **0** and **0**. Consequently, the resulting chirp exhibits bandwidth and frequency characteristics designated as **400MHz** and **-100MHz**.

```
output_practical(1,:)
```

```
ans = 1x13
    0     0     1     1     1     1     0     0     1     1     1     1     0
```

```
bandwidth = bandwidth_values(bit2int(output_practical(1,1:7)',7,true)+1)
```

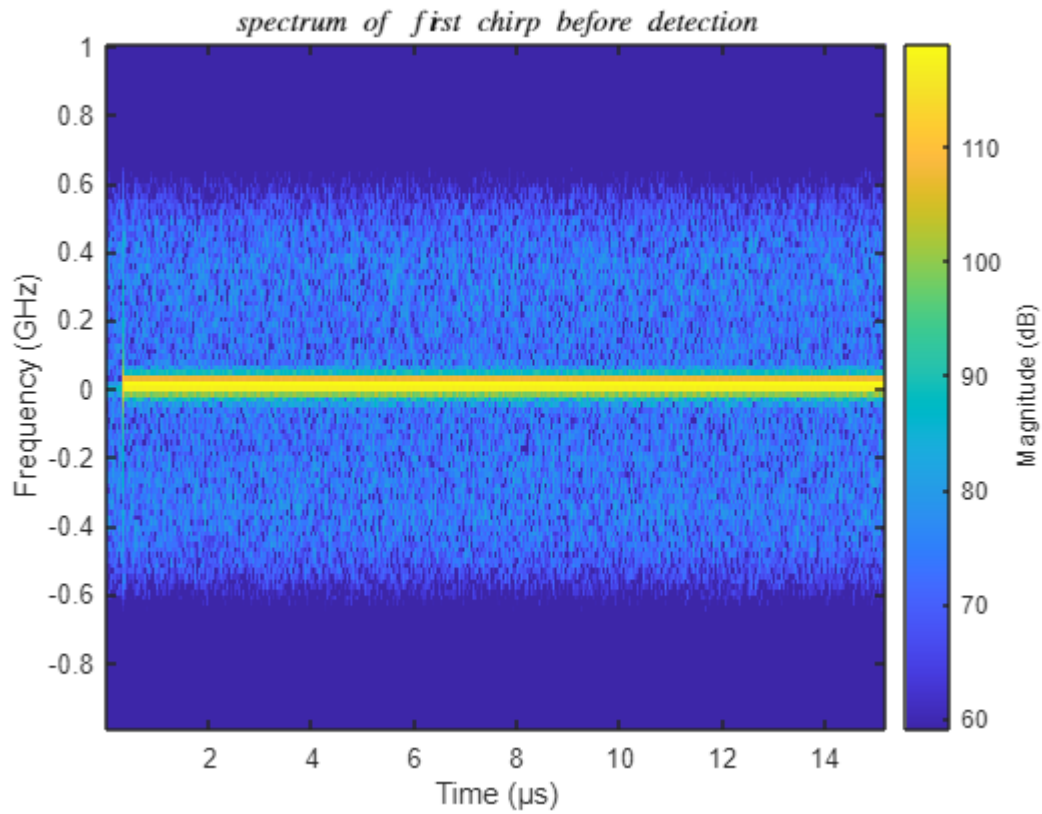
```
bandwidth = 4.9449e+08
```

```
frequency = frequency_values(bit2int(output_practical(1,8:13)',6,true)+1)
```

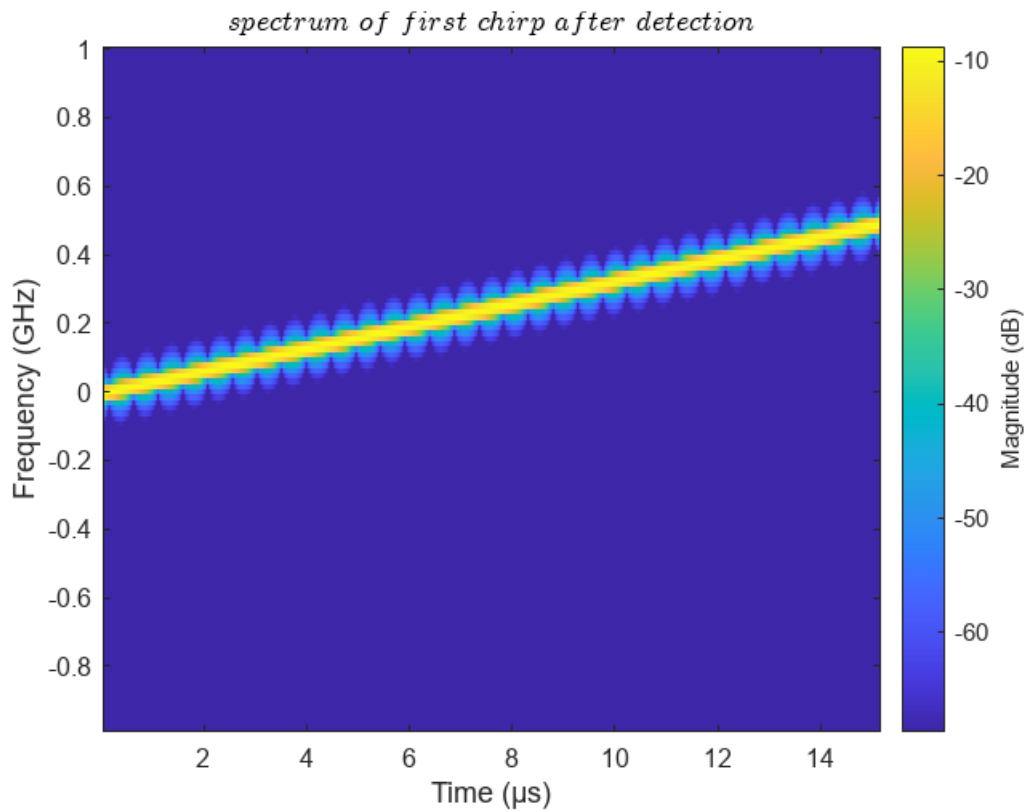
```
frequency = -4.7619e+06
```



```
figure
stft(conj(demoultiplaxed_signal(:,1)')),fs)
title('$ spectrum \ of \ first \ chirp \ before \ detection $' , 'Interpreter','latex')
```



```
figure
stft(pure_chirps(bit2int(output_practical(1,:)',13,true)+1,:),fs)
title('$ spectrum \ of \ first \ chirp \ after \ detection $' , 'Interpreter','latex')
```



```
output_practical(31,:)
```

```
ans = 1×13
      0      0      0      0      0      0      0      0      0      0      0      0      0
```

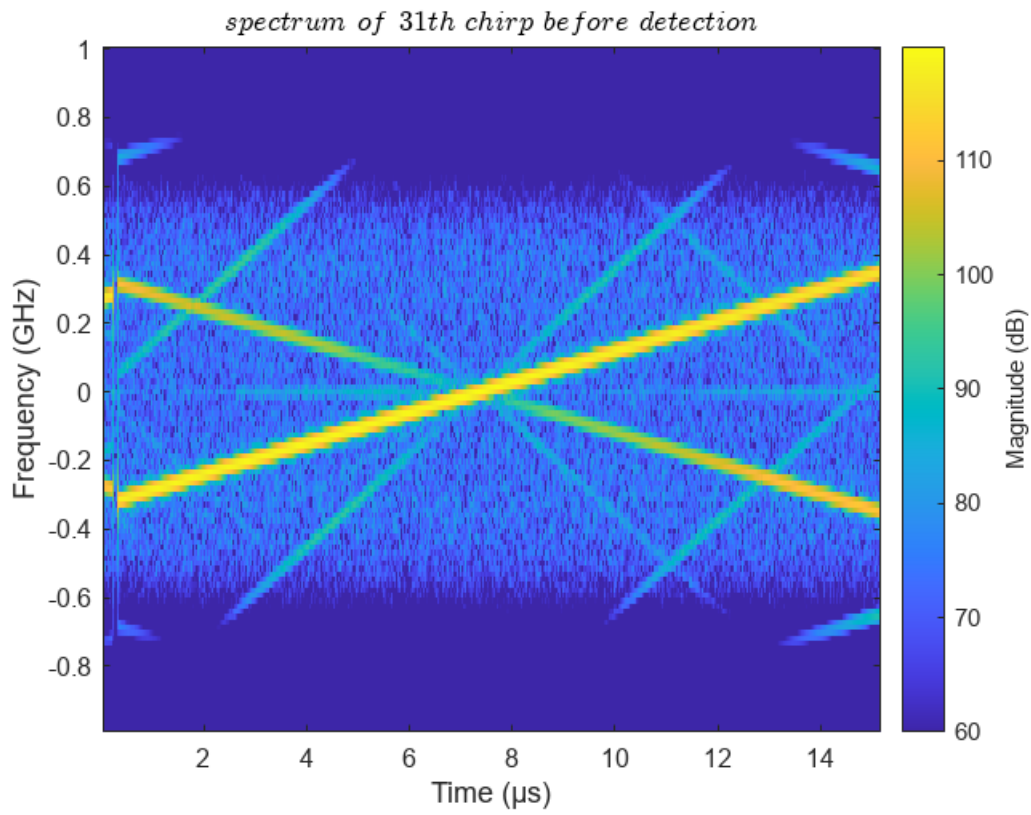
```
bandwidth = bandwidth_values(bit2int(output_practical(31,1:7)',7,true)+1)
```

```
bandwidth = 400000000
```

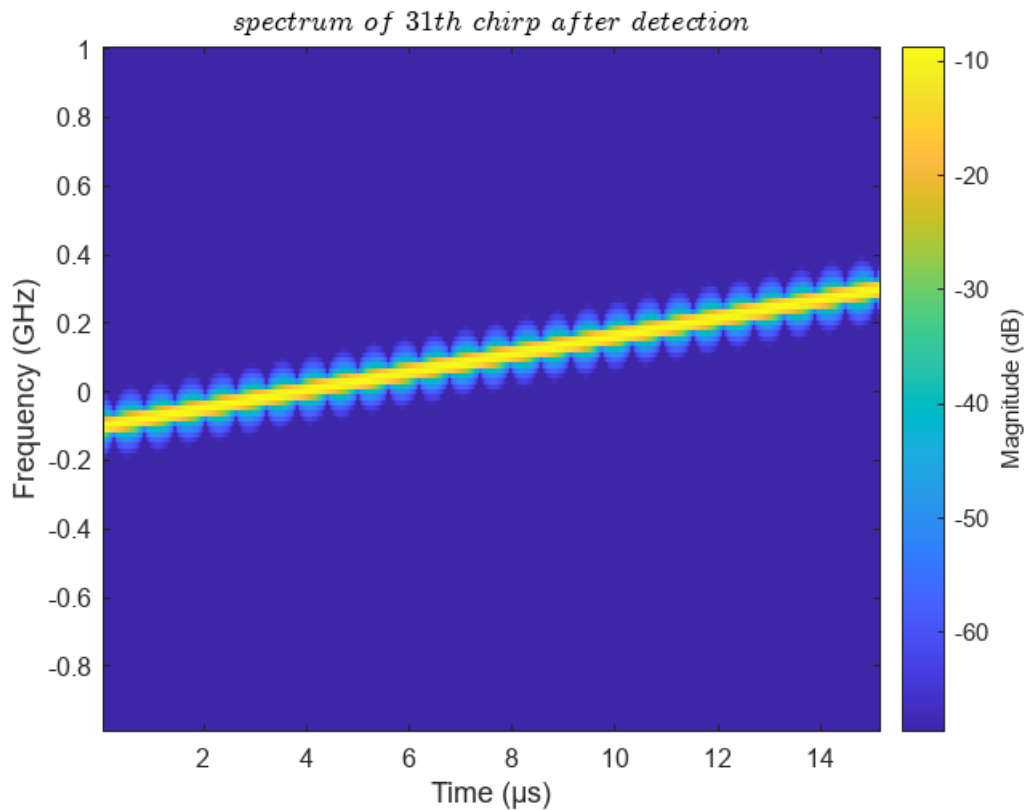
```
frequency = frequency_values(bit2int(output_practical(31,8:13)',6,true)+1)
```

```
frequency = -100000000
```

```
figure
stft(conj(demoultiplaxed_signal(:,31)'),fs)
title('$ spectrum \ of \ 31th \ chirp \ before \ detection $' , 'Interpreter','latex')
```



```
figure
stft(pure_chirps(bit2int(output_practical(31,:)',13,true)+1,:),fs)
title('$ spectrum \ of \ 31th \ chirp \ after \ detection $' , 'Interpreter','latex')
```



functions

```
function out = receiver(signal,reference,number_chirps_to_detect)

    out = zeros(256, 13);

    for i= 1:number_chirps_to_detect
        temp = signal(i,:)/norm(signal(i,:));
        out(i,:) = ml_section(temp,reference);
    end

end

function out = ml_section(signal,reference)

    distance = zeros(1,8192);

    for i = 1:8192
        distance(1,i) = abs(norm(reference(i,:) - signal));
    end
    [~, minIndex] = min(distance);
    out = int2bit(minIndex-1,13,true)';

end
```