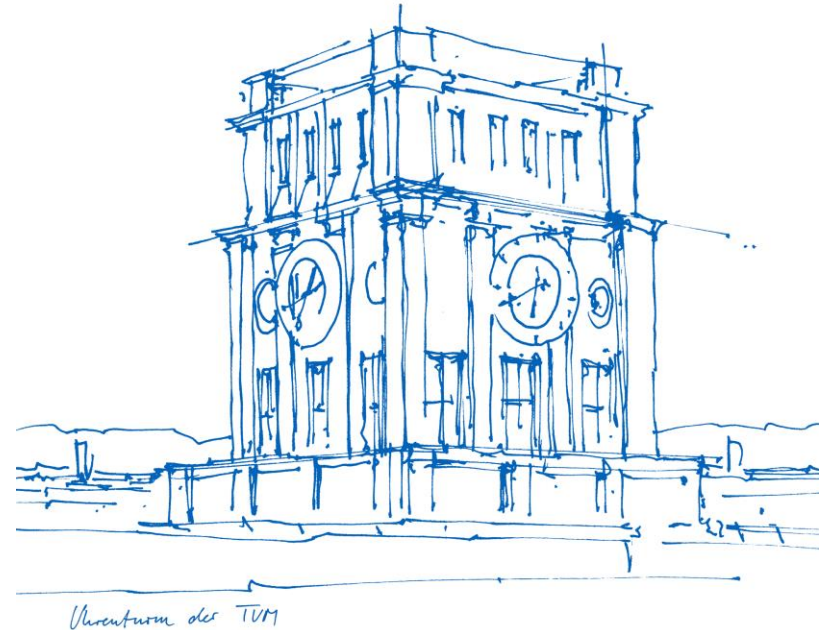


A Tutorial on Using the SSO Toolbox

Eduardo Rodrigues Della Noce

Garching, 02.09.2024



General Content

1. Defining a System Response Function
2. Finding an Optimal Box-shaped Solution Space (and visualization – 3D plot; selective design space projection)
3. Using Surrogate Modeling (with Active Learning)
4. Stacking Evaluators (Multi-fidelity simulation, Solution-Compensation Spaces)
5. Interlude: Finding an Optimal Design
6. Interlude: Using Python Bottom-up Mappings
7. Interlude: Performing Batch Analysis
8. Interlude: Requirement Spaces
9. Using Component Solution Space Optimization – Simple Example
10. Using Component Solution Space Optimization – Advanced Example

Getting Started

Code is available on both GitLab and the OneDrive

GitLab Instructions:

- Clone the tutorial project into your PC in a folder of your choosing (Project: Tutorial SSO Toolbox)
 - `git clone https://gitlab.lrz.de/lpl-tum/sso-toolbox-lpl/tutorial-sso-toolbox.git`

OneDrive Instructions:

- Copy the tutorial folder, and create a copy of the sso-toolbox inside of that

Open this folder in MATLAB (or VScode) and run 'setup_sso_toolbox.m'

- `run('sso-toolbox/setup_sso_toolbox')`

1. Defining a System Response Function

File: tutorial_01_euclidean_distance_3d

A system response function must look like this:

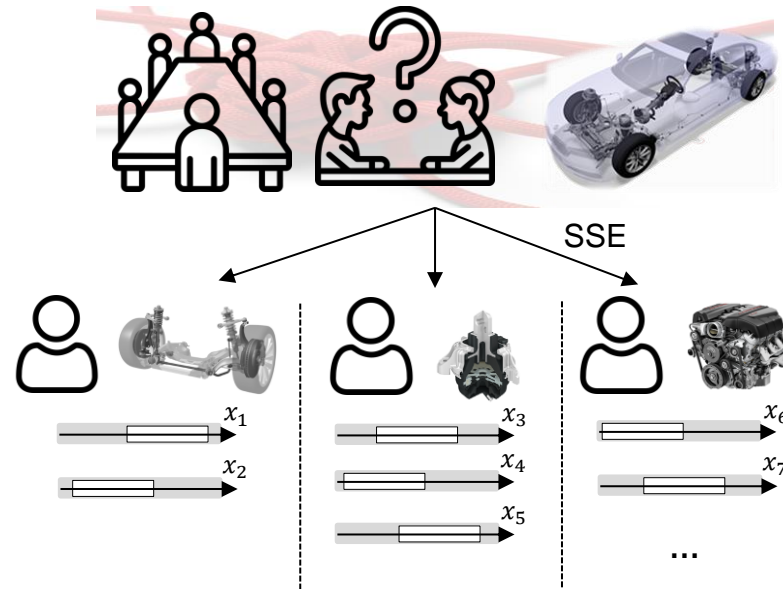
`[performanceMeasure, physicalFeasibilityMeasure, systemOutput] = f(designSample, systemParameter)`

- **designSample** : array with all design sample points; each column is a design variable, each row is a different point
- **performanceMeasure** : system response (in terms of performance); each column is a performance measure, each row is a different point
- **systemParameter** : constant system parameter (doesn't change with the samples), when applicable
- **physicalFeasibilityMeasure** : physical feasibility of the designs, when applicable
- **systemOutput** : any extra information, when applicable

Task:

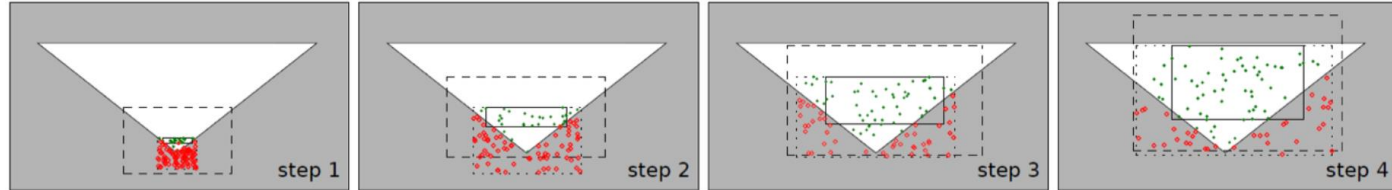
Write a function that computes the distances of all given sample points to a center (constant parameter)

2. Finding an Optimal Box-shaped Solution Space

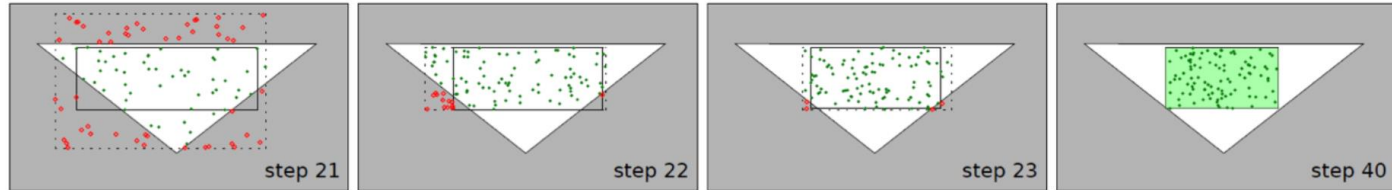


2. Finding an Optimal Box-shaped Solution Space

Phase I:
Exploration



Phase II:
Consolidation



Classical optimization on Ω_{ds} . Identify one good design \mathbf{x}_0 .
The first candidate box Ω is constructed at \mathbf{x}_0 with zero volume.
Phase I. While $\mu(\Omega)$ is changing:
Modification Step B: Extend candidate box.
Compute Monte Carlo sample in Ω .
Modification Step A: Remove bad sample designs.
Compute Monte Carlo sample in Ω .
Phase II. While $m/N < a_c$:
Modification Step A. Remove bad sample designs.
Compute Monte Carlo sample in Ω .

2. Finding an Optimal Box-shaped Solution Space

File: `tutorial_02_sso_box_sphere`

First, the problem must be setup correctly. For that, a Design Evaluator is needed.

- First setup a Bottom-up Mapping (`BottomUpMappingFunction`).
- Then, use it to create a design evaluator (`DesignEvaluatorBottomUpMapping`).
- Finally, call the box SSO function (`sso_box_stochastic`)

Tip: for more information on functions/classes, you can always use “`help <NAME>`” or “`doc <NAME>`”

Task 1:

Run the box-shaped solution space optimization function and obtain the optimal solution space with the following:

- System response: `tutorial_01_euclidean_distance_3d`
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $distance \leq 5$ (center: $[0,0,0]$)
- Initial Design: $[x_1, x_2, x_3] = [3,0,0]$

2. Finding an Optimal Box-shaped Solution Space

File: `tutorial_02_sso_box_sphere`

Visualization tools:

- Boxes in 2D and 3D can be easily plotted using the functions: `plot_design_box_2d`, `plot_design_box_3d`
- Selective Design Space Projection: `plot_selective_design_space_projection`

Common performance metrics can also be automatically plotted: `postprocess_sso_box_stochastic` → `plot_sso_box_stochastic_metrics`

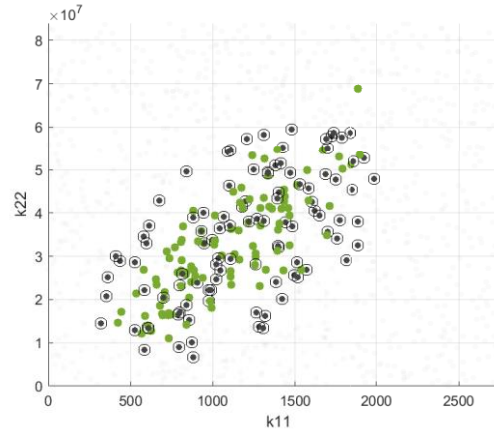
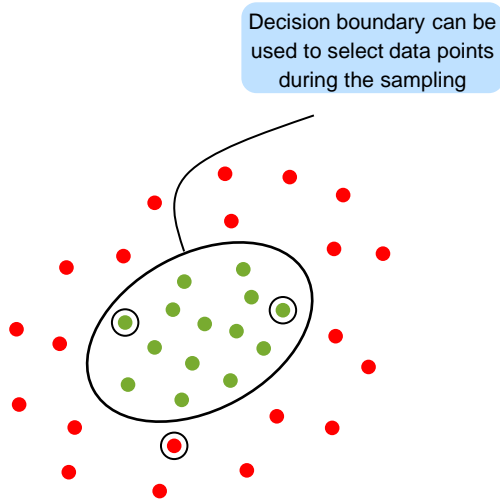
Task 2:

Visualize the solution space box in 3D, and then also use selective design space projection

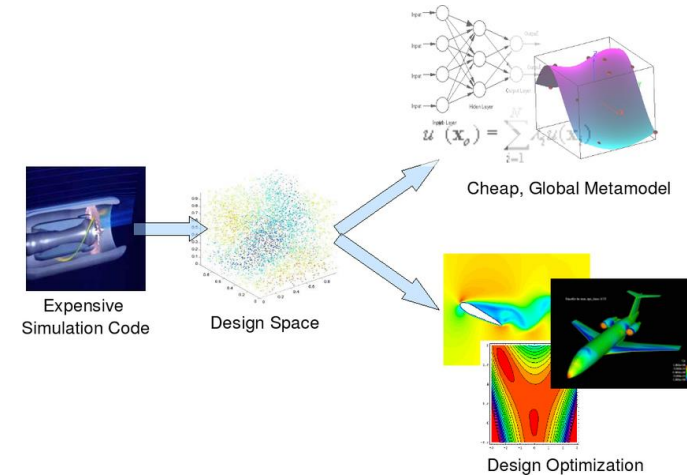
Task 3:

Plot the algorithm performance metrics for this solution

3. Using Surrogate Modeling (with Active Learning)



From: Lukas Krischer, DokSem #7



Source: <https://www.researchgate.net/profile/Tom-Dhaene/publication/265152921/figure/fig1/AS:335678228451328@1457043334234/Surrogate-modeling-versus-Design-Optimization.png>

3. Using Surrogate Modeling (with Active Learning)

File: `tutorial_03_surrogate_modeling`

Special class of surrogate modeling for top-down systems design: `DesignFastForwardBase`

Active learning method: `active_learning_model_training`

Visualization of performance metrics: `postprocess_active_learning_model_training` → `plot_active_learning_model_training_metrics`

Task 1:

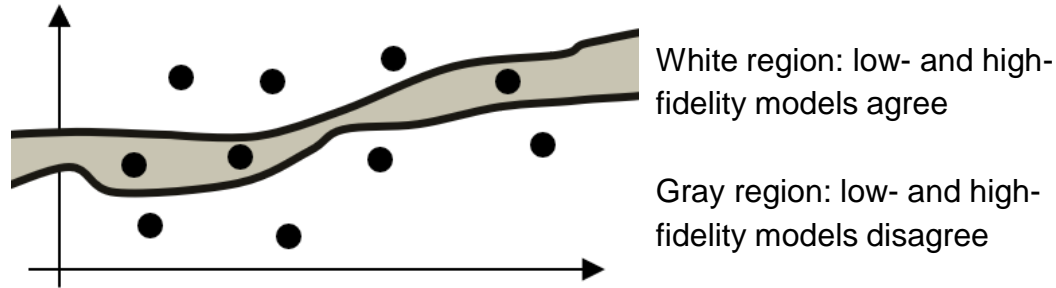
Train a surrogate model for the following problem:

- System response: `tutorial_01_euclidean_distance_3d`
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $2 \leq \text{distance} \leq 5$ (center: $[0,0,0]$)

Task 2:

Visualize how the algorithm performance metrics evolved at each iteration.

4.1 Stacking Evaluators – Multifidelity Evaluation



4.1 Stacking Evaluators – Multifidelity Evaluation

File: `tutorial_04_1_multifidelity`

Transforming a `DesignFastForwardBase` object to a `DesignEvaluatorBase` object: `DesignEvaluatorFastForward`
Estimating region of uncertainty: `design_fast_forward_find_uncertainty_score`

Task 1:

Train a surrogate model for the following problem:

- System response: `tutorial_01_euclidean_distance_3d`
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $distance \leq 5$ (center: $[0,0,0]$)
- Maximum number of iterations: 1
- Number of samples to be evaluated per iteration: 20

Task 2:

Estimate the region of uncertainty.

4.1 Stacking Evaluators – Multifidelity Evaluation

File: `tutorial_04_1_multifidelity`

Setting up a multi-fidelity evaluator: `DesignEvaluatorMultiFidelity`

Task 3:

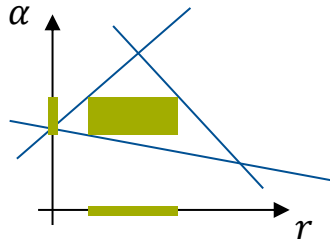
Solve a box SSO problem using the Multifidelity evaluator with the following additional considerations:

- Initial Design: $[x_1, x_2, x_3] = [3, 0, 0]$

4.2 Stacking Evaluators – Solution-compensation Spaces

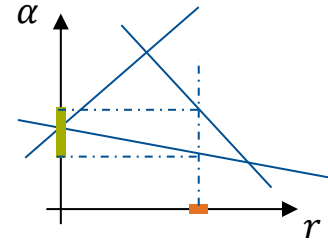
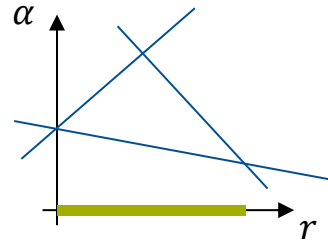
Solution Spaces:

$$\begin{aligned} \min_{[\alpha_l, \alpha_u, r_l, r_u]} & -\mu(\Omega) \\ \text{s.t. } & g(r, \alpha) \leq 0 \end{aligned}$$



Solution Compensation Spaces:

$$\begin{aligned} \min_{[r_l, r_u]} & -\mu(\Omega_a) \\ \text{s.t. } & \forall x_a \in \Omega_a \exists x_b \in \Omega_b \end{aligned}$$



early decision variables (limited controllability, PFD): sensor characteristics, $x_a = r$
late decision variables (controllable): sensor positionings, $x_b = \alpha$

From: Nicola Barthelmes, DokSem #5

4.2 Stacking Evaluators – Solution-compensation Spaces

File: tutorial_04_2_compensation

Setting up an evaluator for solution-compensation spaces: `DesignEvaluatorCompensation`

Task:

Solve a box SCSO problem with the following considerations:

- System response: `tutorial_01_euclidean_distance_3d`
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $distance \leq 5$ (center: $[0,0,0]$)
- Initial Design: $[x_1, x_2, x_3] = [3,0,0]$
- A-space: $[x_1, x_2]$; B-space: x_3

5. Interlude: Finding an Optimal Design

File: tutorial_05_point_based_optimal_design

Special optimization functions:

- `design_optimize_quantities_of_interest`
- `design_optimize_performance_score`

Task:

Find optimal designs for the 2D car crash problem: one with the best acceleration, another with the best score.

6. Interlude: Using Python Bottom-up Mappings

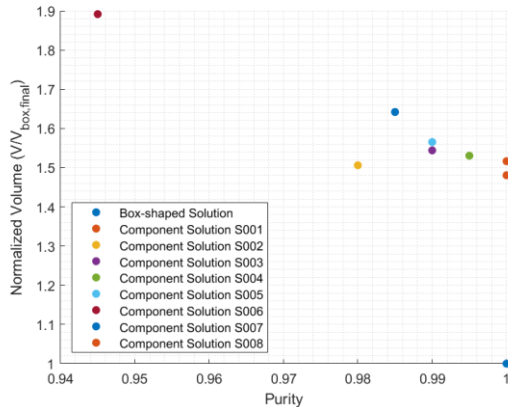
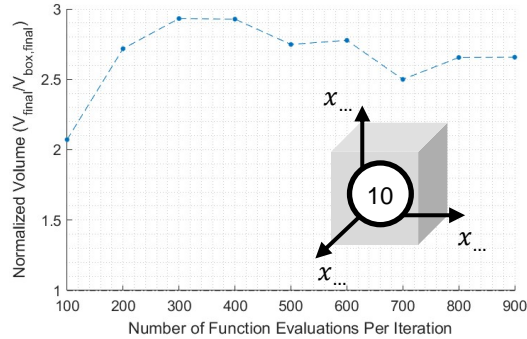
File: `tutorial_06_python_bottom_up_mapping`

Setting up a bottom-up mapping that uses Python code for its system response: `BottomUpMappingPython`

Task:

- Find the optimal box for the 2D car crash problem using the MATLAB function `car_crash_2d`
- Find the optimal box for the 2D car crash problem using the Python function `car_crash_2d_python.py`

7. Interlude: Performing Batch Analysis



ID	ReferenceID	Number Samples Per Iteration	Growth Rate	Tolerance Purity Consolidation
S001	-	200	0.2	1
S002	S001	100	0.2	1
S003	S001	300	0.2	1
S004	S001	200	0.1	1
S005	S001	200	0.3	1
S006	S001	200	0.2	0.85
S007	S001	200	0.2	1
S008	S001	200	0.2	1

7. Interlude: Performing Batch Analysis

File: tutorial_07_batch_analysis

Reading a table: batch_analysis_read_table

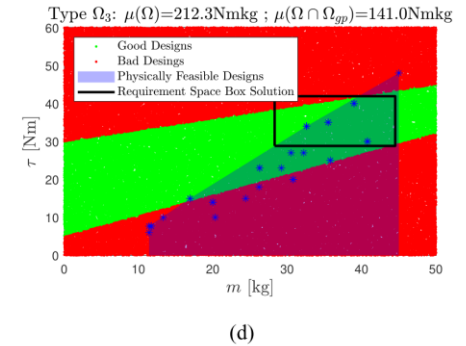
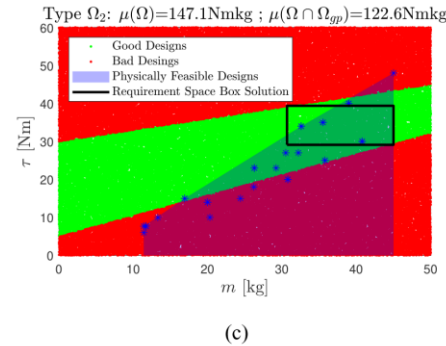
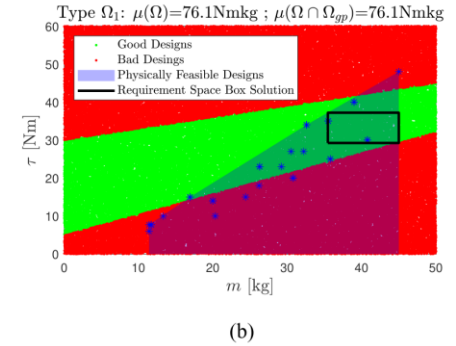
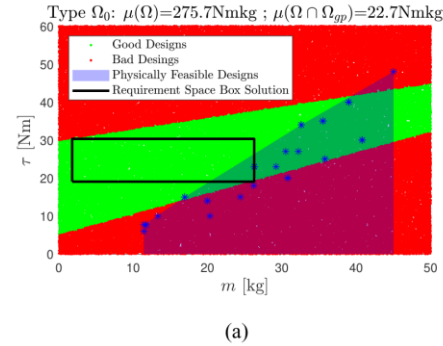
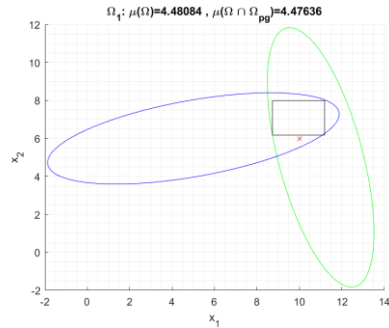
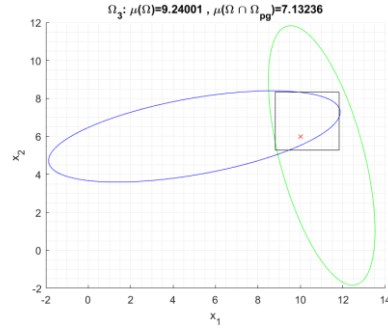
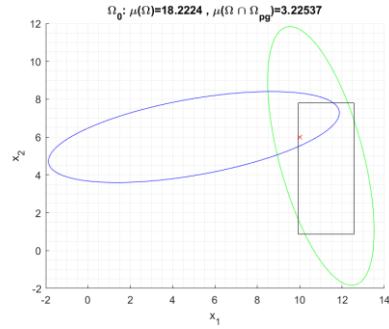
Batch SSO analysis: batch_sso_stochastic_analysis

Task:

Perform a batch analysis for the following problem:

- System response: tutorial_01_euclidean_distance_3d
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $distance \leq 5$ (center: $[0,0,0]$)
- Initial Design: $[x_1, x_2, x_3] = [3,0,0]$
- Batch options: 'BatchTestHollowSphere.xlsx'

8. Interlude: Requirement Spaces



8. Interlude: Requirement Spaces

File: tutorial_08_requirement_spaces

Important option:

- 'RequirementSpacesType' (in `sso_stochastic_options`)
- 'PhysicalFeasibilityUpperLimit' (in `DesignEvaluatorBottomUpMapping`)

Task:

Solve the following requirement spaces problem:

- System response: `two_ellipses_requirement_space`
- Design Space: $-2 \leq x_1 \leq 14$; $-2 \leq x_2 \leq 12$
- Performance Limit: $\text{ellipsenorm} \leq 1$
- Physical Feasibility Limit: $\text{ellipsenorm} \leq 1$
- Initial Design: $[x_1, x_2] = [10, 6]$
- Number of evaluations per iteration: 200
- Apply leanness condition only at the end

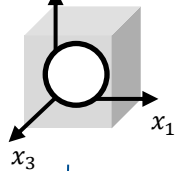
9. Component Solution Space Optimization – Simple Example

Example: Sphere

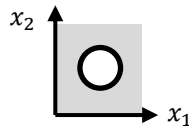
Components:

$$\mathbf{x}_{(1)} = [x_1, x_2]$$

$$\mathbf{x}_{(2)} = [x_3]$$



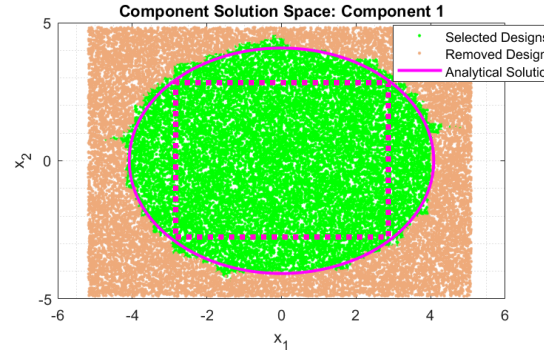
Analytical Solution



$$l = \frac{2R}{\sqrt{3}}$$

$$r = R \sqrt{\frac{2}{3}}$$

Stochastic Algorithm
Corner Box Removal



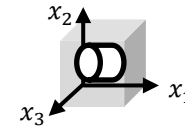
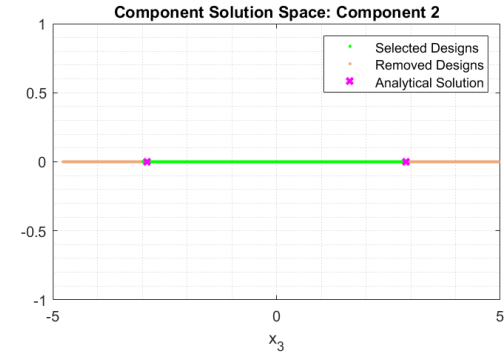
Solution Box Area:

$$A_b = l_b^2 = \left(\frac{2R}{\sqrt{3}}\right)^2 = R^2 \frac{4}{3}$$

Component Solution Space Area:

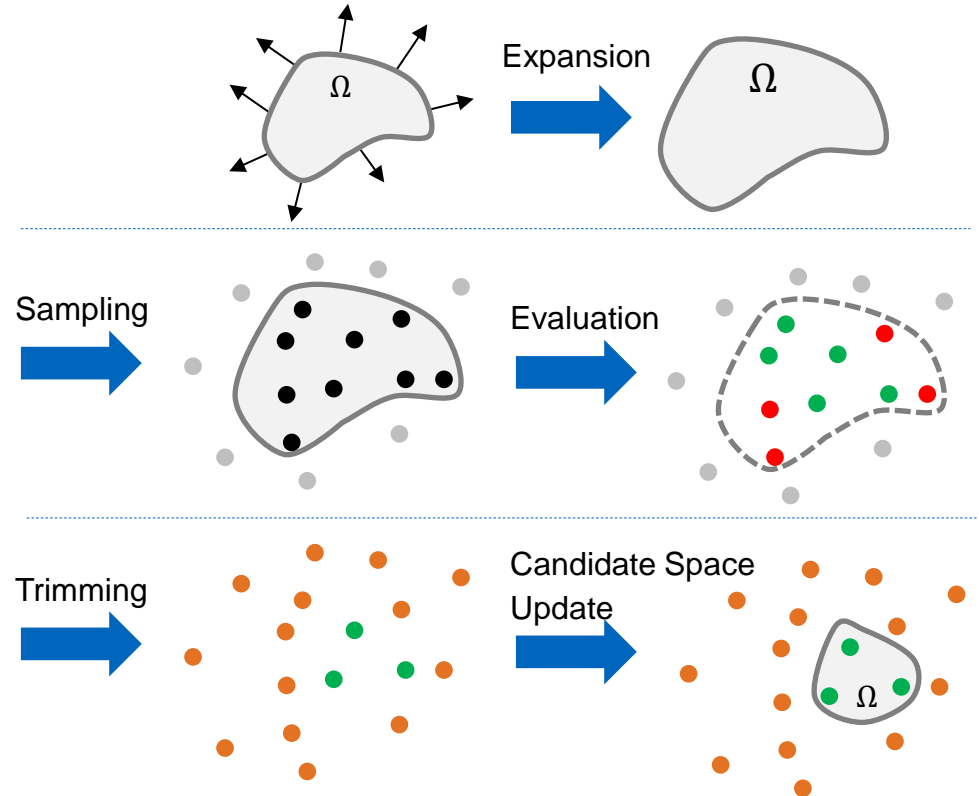
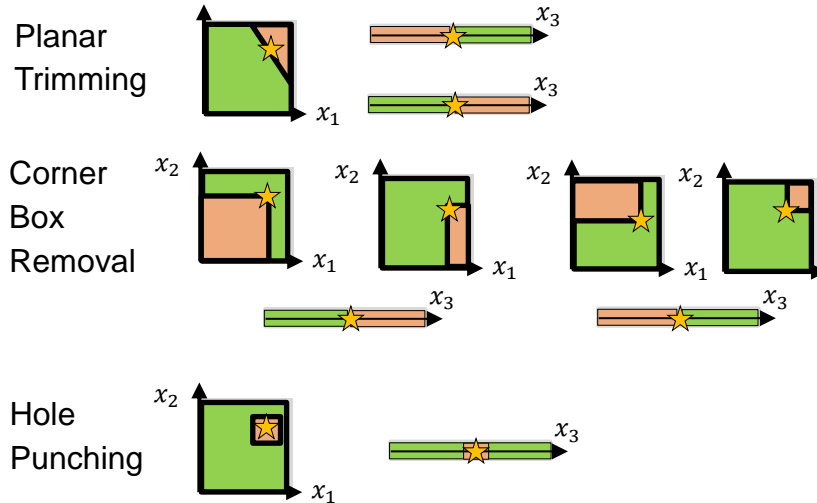
$$A_c = \pi r_c^2 = \pi \left(R \sqrt{\frac{2}{3}}\right)^2 = R^2 \frac{2\pi}{3}$$

~57% increase in area



9. Component Solution Space Optimization – Simple Example

- Candidate space operations:
 - Expand (given a growth rate g)
 - Identify x_{sample} as inside or outside
 - Be updated given samples x_{in}, x_{out}



9. Component Solution Space Optimization – Simple Example

File: `tutorial_09_component_solution_space_simple`

Candidate Space Definition: `CandidateSpaceBase`

Trimming Methods: `component_trimming_method_<NAME>`

Component SSO function: `sso_component_stochastic`

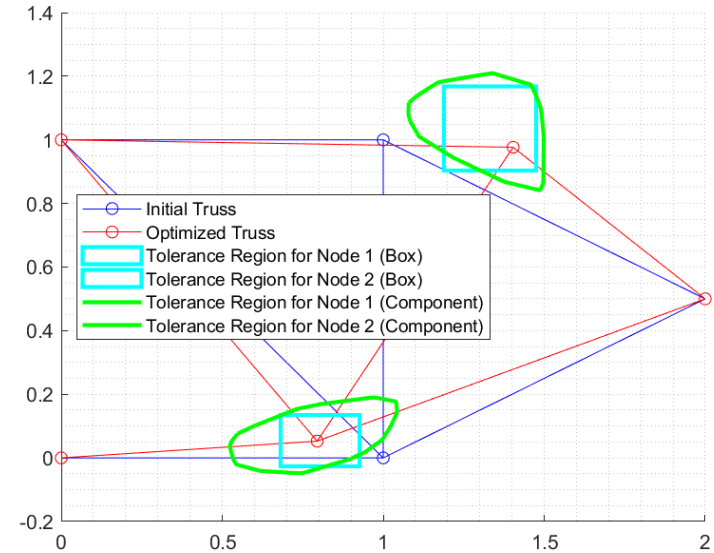
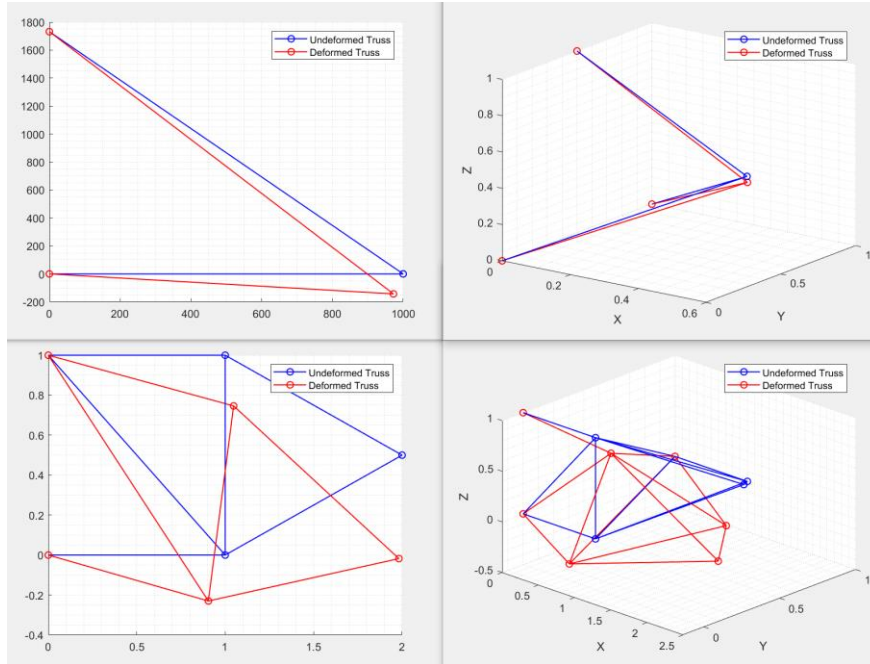
Performance metrics: `postprocess_sso_component_stochastic` →
`plot_sso_component_stochastic_metrics`

Task:

Solve the following requirement spaces problem:

- System response: `tutorial_01_euclidean_distance_3d`
- Design Space: $-6 \leq x_1, x_2, x_3 \leq 6$
- Performance Limits: $distance \leq 5$ (center: $[0,0,0]$)
- Initial Design: $[x_1, x_2, x_3] = [3,0,0]$
- Number of samples per iteration: 300

10. Component Solution Space Optimization – Advanced



10. Component Solution Space Optimization – Advanced

File: tutorial_10_component_solution_space_advanced

Options to use:

- Growth rate: 0.1
- Number of exploration/consolidation iterations: 30
- Number of evaluations per iteration: 300

Tasks:

- Setup the bottom-up mapping
- Find the optimum design with minimum displacement
- Find the optimum solution space box starting from the optimum design and having as performance limit a 10% tolerance from the optimum displacement
- Find the optimum component solution space under the same conditions
- Visualize both box and component solution space in the same plot to compare
- Plot performance metrics for each

Thank you for your attention!



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