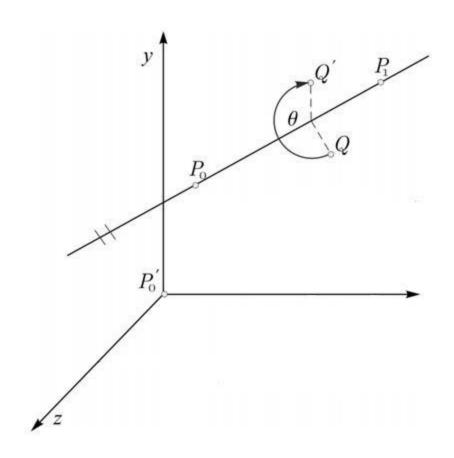
CSE4203: Computer Graphics Lecture – 4 (part - C) Transformation Matrices

Outline

- 3D Transformation
- Rotation about an arbitrary line

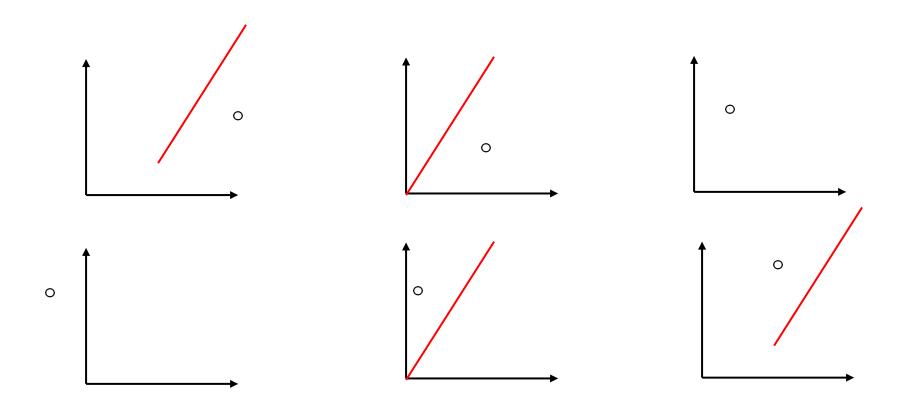
Rotation about an arbitrary line (1/1)



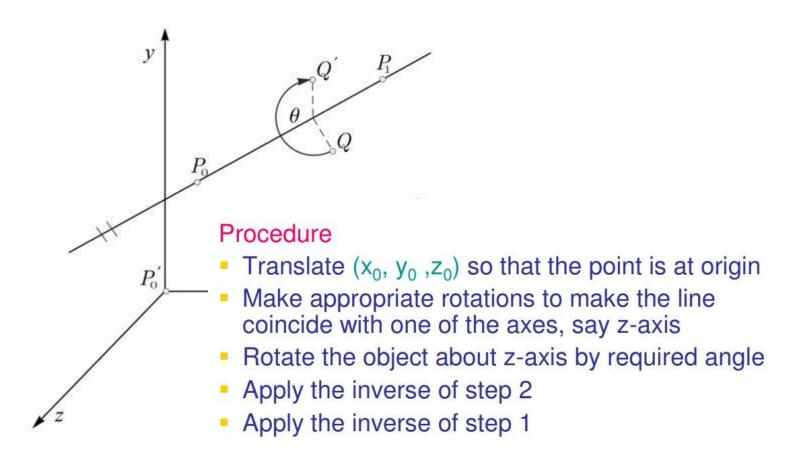
The basic idea is to make the arbitrary rotation axis coincide with one of the principle axis. Assume an arbitrary axis in space passing through the point PO (x0, y0, z0) and P1 (x1, y1, z1).

In 2D case (1/1)

Reflecting about an arbitrary line

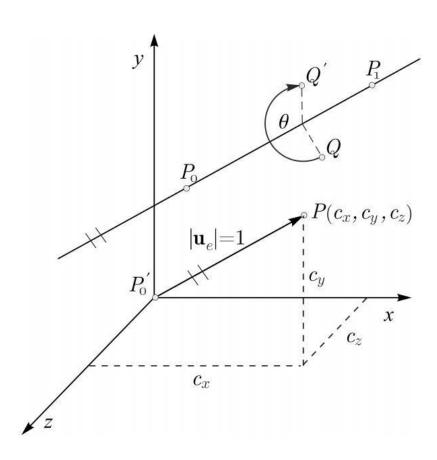


Steps (1/1)



Credit: http://ami.ektf.hu/uploads/papers/finalpdf/AMI 40 from175to186.pdf | http://web.iitd.ac.in/~hegde/cad/lecture/L6 3dtrans.pdf

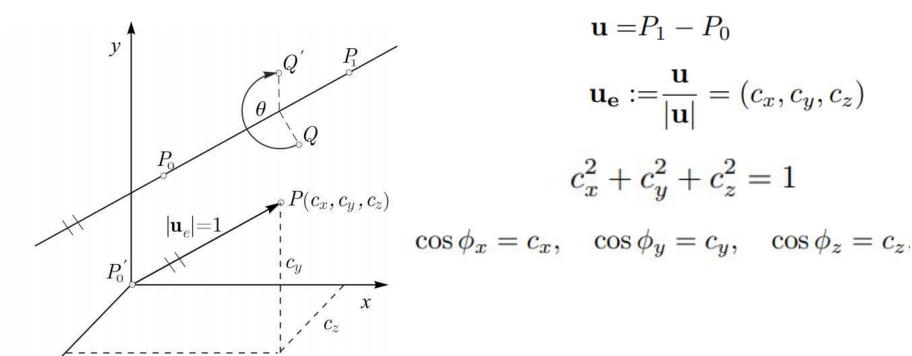
Direction Cosine (1/2)



vector are the cosines of a vector are the cosines of the angles between the vector and the three coordinate axes.

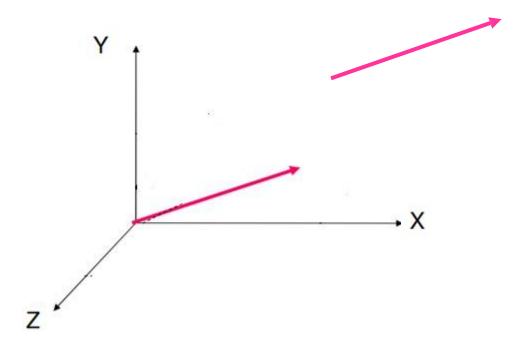
Direction Cosine (2/2)

Equivalently, they are the contributions of each component of the basis to a unit vector in that direction.



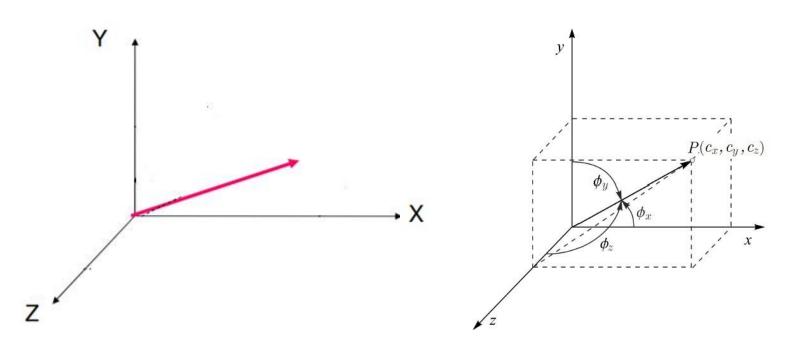
 c_x

Coinciding the line with Principal axis (1/5)



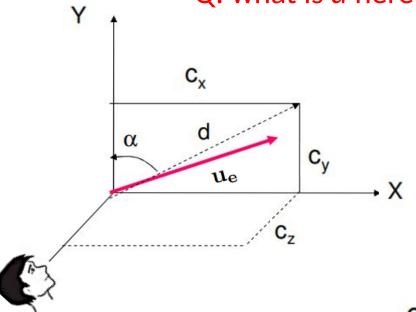
Coinciding the line with Principal axis (2/5)

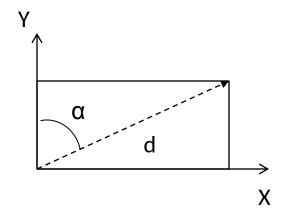
Coinciding the arbitrary axis with any axis the rotations are needed about other two axes



Coinciding the line with Principal axis (3/5)



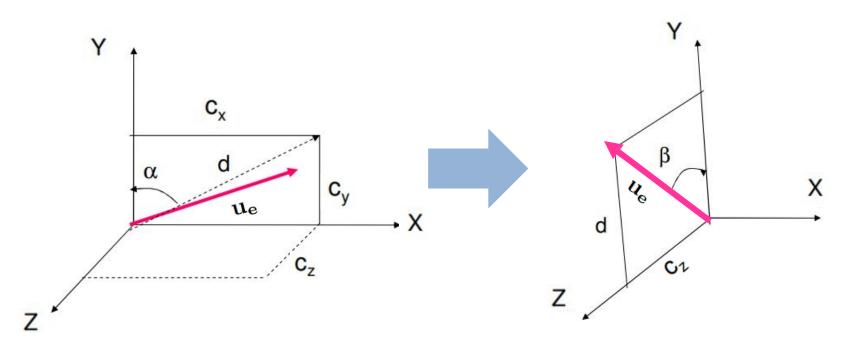




$$d = \sqrt{c_x^2 + c_y^2}$$
 $\cos \alpha = \frac{c_y}{d}$ $\sin \alpha = \frac{?}{d}$

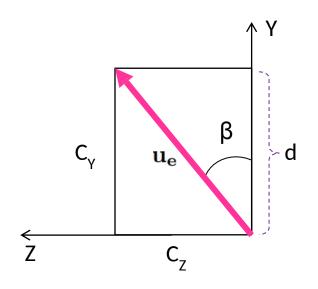
$$\sin \alpha = \frac{?}{d}$$

Coinciding the line with Principal axis (4/5)

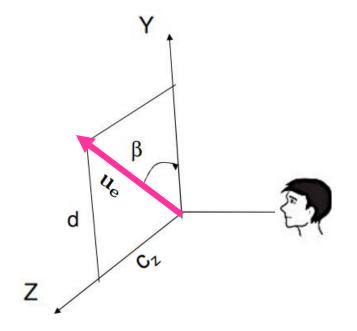


What is the rotation matrix?

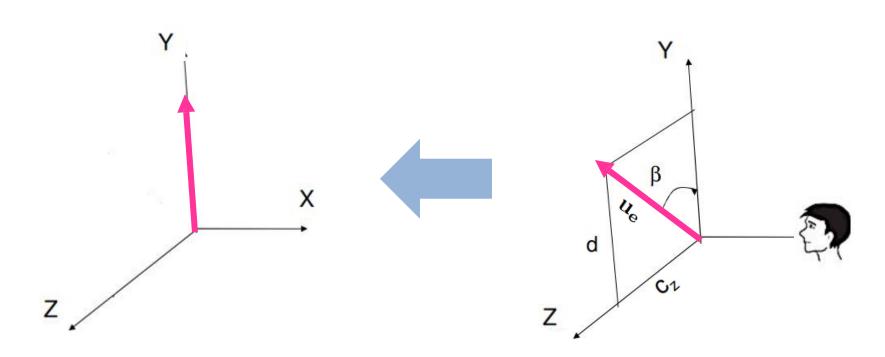
Coinciding the line with Principal axis (5/5)



$$\cos \beta = d$$
 $\sin \beta = ?$

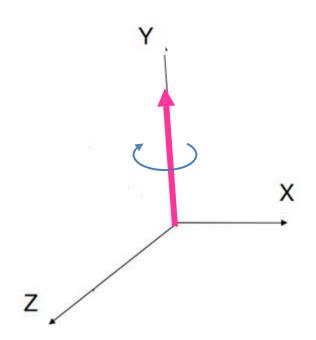


Rotating about the principal axis (1/2)



What is the rotation matrix?

Rotating about the principal axis (2/2)



What is the rotation matrix?

Undoing the steps (1/1)

Q: What are the undoing steps?

Composite Transformation (1/1)

•
$$M = T^{-1} * R_z^{-1}(\alpha) *$$
 ?

Practice Problem

• AB is a line and P is a point in 3D space; where the points A,B and P are (1,1,1), (3,3,4) and (2,2,4) respectively. We want to rotate P along AB by +90 degree. Determine the composite transformation matrix to do the task and calculate the rotated point P'.

References

- http://ami.ektf.hu/uploads/papers/finalpdf/AMI 40 from175 to186.pdf
- http://web.iitd.ac.in/~hegde/cad/lecture/L6 3dtrans.pdf