

Slide Examples Solutions

Lecture 1,2,3

Lecture 1

Example 1:

- Lets consider the spectrum of a channel is between 3 MHz and 4 MHz and $\text{SNR}_{\text{db}} = 24 \text{ dB}$. Then find the maximum capacity achieved by channel. If it is possible to achieved the limit then how many signal level is required?

Solution: by Younus-131

$$\text{Bandwidth, } B = 4 - 3 = 1 \text{ MHz}$$

$$\text{SNR} = 10^{(\text{SNR}_{\text{db}}/10)} = 10^{(24/10)} = 251.1886$$

$$\begin{aligned} \text{Maximum capacity, } C &= B \log_2(1 + \text{SNR}) \\ &= 1 \times \log_2(1 + 251.1886) \\ &= 7.978 \text{ Mbps} \approx 8 \text{ Mbps} \end{aligned}$$

$$\text{Nyquist Formula, } C = 2B \log_2 M$$

$$\Rightarrow \frac{C}{2B} = \log_2 M$$

$$\Rightarrow M = 2^{\frac{C}{2B}} = 2^{\frac{8}{2 \times 1}} = 16$$

Example 2:

- What are the propagation time and the transmission time for a 2.5-kbyte message if the bandwidth of the network is 1 Gbps? Assume that the distance between the sender and the receiver is 12,000 km and that light travels at 2.4×10^8 m/s.

Solution: by Younus-131

$$\begin{aligned} \text{Propagation time} &= \frac{d}{s} \\ &= \frac{12 \times 10^6}{2.4 \times 10^8} \\ &= 5.357 \times 10^{-3} \text{ s} \\ &= 5357 \mu\text{s} \end{aligned} \quad \left| \begin{array}{l} \text{Given,} \\ d = 12000 \text{ km} \\ = 12 \times 10^6 \text{ m} \\ s = 2.4 \times 10^8 \text{ m/s} \end{array} \right.$$

Here,

$$\begin{aligned} \text{Size of the message} &= 2.5 \text{ Kbyte} \\ &= 2.5 \times 10^3 \text{ byte} \\ &= 2.5 \times 10^3 \times 8 \text{ bit} \end{aligned}$$

$$\text{bandwidth} = 1 \text{ Gbps} = 1 \times 10^9 \text{ bps}$$

$$\begin{aligned} \text{Transmission time} &= \frac{\text{size of the message}}{\text{bandwidth}} \\ &= \frac{2.5 \times 10^3 \times 8}{1 \times 10^9} \text{ s} \\ &= 2 \times 10^{-5} \text{ s} = 20 \mu\text{s} \end{aligned}$$

Lecture 3

Example: Multistage Switch

Design a three-stage, 200×200 switch ($N = 200$) with $k = 4$ and $n = 20$.

Solution: Added from the Lecture Slide

In the *first stage* we have N/n or 10 crossbars,
each of size 20×4 .

In the *second stage*, we have 4 crossbars,
each of size 10×10 .

In the *third stage*, we have 10 crossbars,
each of size 4×20 .

The total number of crosspoints is $2kN + k(N/n)^2$, or 2000 crosspoints.

This is 5 percent of the number of crosspoints in a single-stage switch ($200 \times 200 = 40,000$).

Example- Non-blocking

Redesign the previous three-stage, 200×200 switch, using the Clos criteria with a minimum number of crosspoints.

Solution: Added from the Lecture Slide

We let $n = (200/2)^{1/2}$, or $n = 10$.

We calculate $k = 2n - 1 = 19$.

In the *first stage*, we have $200/10$, or 20, crossbars,
each with 10×19 crosspoints.

In the *second stage*, we have 19 crossbars,
each with 20×20 crosspoints.

In the *third stage*, we have 20 crossbars
each with 19×10 crosspoints.

The total number of crosspoints is

$$20(10 \times 19) + 19(20 \times 20) + 20(19 \times 10) = 15200.$$