

Feature Model composition assisted by Formal Concept Analysis

Keywords: Software Product Line, Feature Model, Feature Model Composition, Formal Concept Analysis

Abstract: In the domain of software product lines, Feature Models (FM) play a central role in variability modeling, completed by configuration collections (from concrete software product lines), logical representations, constraint programming or conceptual structures, coming from the field of Formal Concept Analysis (FCA). The development of feature models may take several forms, including their synthesis from configuration collections or their design in several steps (by several teams or with different concerns). FM composition (merge) operators are part of that design activity as they assist their iterative building. In this paper, we describe an approach, based on two main merging semantics (intersection and union), which assists designers in merging several FMs. This approach benefits from the help of FCA to represent all the FMs with the same configuration set through a canonical form. We describe the implementation of our approach and present a set of concrete examples.

1 INTRODUCTION

Software Product Lines have been introduced to reduce the cost and the time needed for producing software systems, while increasing their quality and diversity (Pohl et al., 2005). The design of a software product line can be achieved in different ways, depending on the context. It has two main phases, *domain engineering*, where commonality and variability are captured and *application engineering*, which focuses on the software product derivation. In Domain engineering requirement models are defined, including more specifically *feature models* that are widely used. *Feature models* (FM) describe the commonalities and the variability of a software product line based on a hierarchical decomposition of the system features, provided with annotations and logical formulas. An FM defines the acceptable set of configurations, a configuration being a set of features. As any design process, defining a FM is not straightforward, as several concerns have to be taken into account, several actors can participate and different sources of information can be used, depending if the FM is defined using real-world product lines (a set of concrete products already exists and the FM has to synthesize their configurations) or is defined during requirement analysis.

Merging several FMs or simply analyzing their differences takes part in this design activity and has been studied thoroughly in the literature (Acher et al., 2010a). These activities require in particular to compute intersection and union of FMs. However, there is an inherent divergence between structural intersection/union and the intersection/union of the configuration sets. Indeed, one main semantics of a feature

model is its *configuration-semantics*, given by the set of configurations defined by the feature model. An issue which has to be addressed is the fact that FMs are not canonical forms, in the sense that a set of configurations (sets of features) often can be represented by several FMs. This is the same for alternative representations as propositional formulas and constraints (in Constraint Problem solving approaches).

In the domain of software product lines, when the configuration set of a product collection was the primary artifact, other approaches have been tried, that rely on Formal Concept Analysis and several of its associated representations. The conceptual structures mix features and configurations. They have limits related to the need of enumerating the configurations and to the loss of ontological knowledge (as propositional formulas). As a counterpart, they are canonical and have graphical representations, that show relations between configurations, between features, and between features and configurations.

In this paper, we propose an approach, based on FCA, for understanding and assisting the feature model composition (intersection and union), also known as feature model merging, and provide assistance to designers during this activity.

Section 2 explains how the FCA framework allows us to build canonical forms for variability in a configuration set, in the sense that they encode all the feature models that have the same configuration set. Section 3 recalls the definition of main merge operators by (Acher et al., 2010a) and describes the way conceptual structures may be used to understand and to guide the merge operations (intersection and union). Section 4 describes a process that implements

the approach, gives some illustrations of its application and investigates the scope of applicability. Section 5 details the related work. Section 6 concludes the document with some perspectives.

2 FCA FOR VARIABILITY REPRESENTATION

There are several means for representing feature-based variability, from configuration set, propositional logic, set of constraints (in Constraint Satisfaction Problem paradigm), to graph-based, or Feature Models (FMs) that can be considered a standard representation. Here we consider the FODA model (Kang et al., 1990). To illustrate the rest of the paper, we use the example of grid-based medical imaging services proposed in (Acher et al., 2010a). The original feature model is denoted FM1 and we also introduce a variation of this feature model denoted FM1v, both feature models are presented in Figure 1. Let us consider the FM1. It represents a service for medical imaging. The set of features is organized in a tree where the features are the nodes and the edges indicate various dependencies between features. The medical imaging service (MI) requires a modality (Mo) and a format (F). This mandatory relation is indicated through an edge ending with a black disk. The format (F) optionally needs a header (H), indicated by an edge ending with a black circle. The children of a feature may also be grouped into *xor groups* (if the parent feature belongs to a configuration, exactly one child feature of the group is also present) or into *or groups* (if the parent feature belongs to a configuration, one or more child features of the group are also present). An *xor group* is indicated by a black line connecting the edges going from the parent to the children. An *or group* (not present in this example) is indicated by a black filled zone connecting the edges going from the parent to the children. In this FM, the modality (Mo) imposes to choose exactly one image acquisition technique (*xor group*) among magnetic resonance imaging (MRI) or X-ray computed tomography (CT). In another FM that appears later in the paper, another image acquisition technique, namely positron emission tomography (PET), will be proposed. The format (F) requires the anonymizing service and optionally a service for header addition (H). The header may be written using exactly one (*xor group*) of the medical image exchange standards: Digital Imaging and Communication in Medicine (DICOM) or Neuroimaging Informatics Technology Initiative (Nifti).

The two feature models of Figure 1 admit the same

set of configurations, which is denoted by $\llbracket FM1 \rrbracket = \llbracket FM1v \rrbracket$. This configuration set is shown in Table 1 in which we have a column per feature and a line per configuration and in which a cross for column c and line l means that configuration l owns the feature c . In the FCA framework, such a table is called a Formal Context.

Table 1: Formal context of the configuration set associated with FM1 and FM1v.

MI1	A	CT	D	F	H	MI	MRI	Mo	Z
MI1c0	×	×	×	×	×	×		×	
MI1c1	×		×	×	×	×	×	×	
MI1c2	×	×		×		×		×	
MI1c3	×			×		×	×	×	
MI1c4	×	×		×	×	×		×	×
MI1c5	×			×	×	×	×	×	×

Definition 1 (Formal context). A formal context K is a 3-tuple (G, M, I) , where G is an objet (configuration) set, M an attribute (feature) set, and $I \subseteq G \times M$ is a binary relation which associates objects (configurations) with attributes (features) they own. For a context $K = (G, M, I)$, for $g \in G$ we will denote by $I(g)$ the set of features of g , i.e. the set $\{m \in M \mid (g, m) \in I\}$.

From the formal context, specialized algorithms from FCA framework extract *formal concepts*. A formal concept is a maximal group of objects associated with the maximal group of attributes they share. It can be read in the table of the context as a maximal rectangle of crosses (modulo permutations of rows and columns).

Definition 2 (Formal concept). Given a formal context $K = (G, M, I)$, a formal concept associates a maximal set of objects with the maximal set of attributes they share, yielding a set pair $C = (Extent(C), Intent(C))$ such that:

- $Extent(C) = \{g \in G \mid \forall m \in Intent(C), (g, m) \in I\}$ is the extent of the concept (objects covered by the concept).
- $Intent(C) = \{m \in M \mid \forall g \in Extent(C), (g, m) \in I\}$ is the intent of the concept (shared attributes).

For example, $(\{MI1c1, MI1c5\}, \{MI, Mo, F, A, MRI, H\})$ is the concept that groups configurations MI1c1 and MI1c5 (concept extent) that share the features MI, Mo, F, A, MRI and H (concept intent).

The formal concepts are ordered using including of their extent. Given two formal concepts $C_1 = (E_1, I_1)$ and $C_2 = (E_2, I_2)$ of K , the concept specialization/generalization order \preceq_C is defined by $C_2 \preceq_C C_1$ if and only if $E_2 \subseteq E_1$ (and equivalently $I_1 \subseteq I_2$). C_1 is

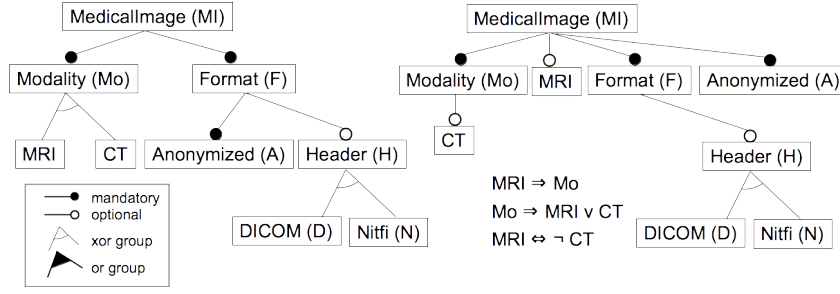


Figure 1: Right-hand-side: Feature Model FM1 from (Acher et al., 2010a) (for a medical imaging service); Left-hand-side: one equivalent variation FM1v (with same set of configurations).

a specialization (a subconcept) of C_2 . C_2 is a generalization (a superconcept) of C_1 . Due to these definitions, C_2 intent inherits (contains) the attributes from C_1 intent, while C_1 extent inherits the objects from C_2 extent.

Definition 3 (Concept lattice). *If we denote by C_K the set of all concepts of K , $\mathcal{L}_K = (C_K, \preceq_C)$, is the concept lattice associated with K .*

The graphical representation of the concept lattice exploits the inclusion property (see Figure 2) to avoid representing in the concepts the top-down inherited features and the bottom-up inherited configurations. A concept is represented in this document in a three-part box. The top part contains the concept identifier (e.g. `Concept_MI1_10`), the middle part contains the features of the intent that are introduced by this concept (e.g. `CT`), the bottom part contains the configurations of the extent that are introduced by this concept (e.g. `MI1c2`). With inherited features, and configurations the whole concept is $Concept_MI1_10 = (\{MI1c2, MI1c0, MI1c4\}, \{MI, Mo, F, A, CT\})$.

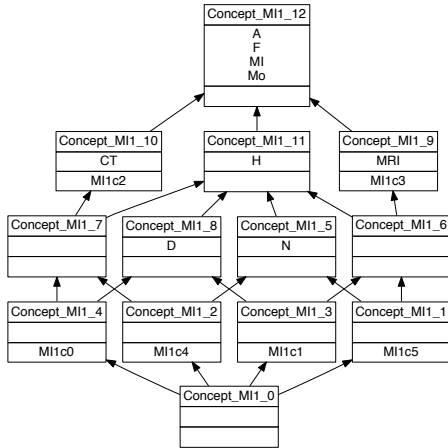


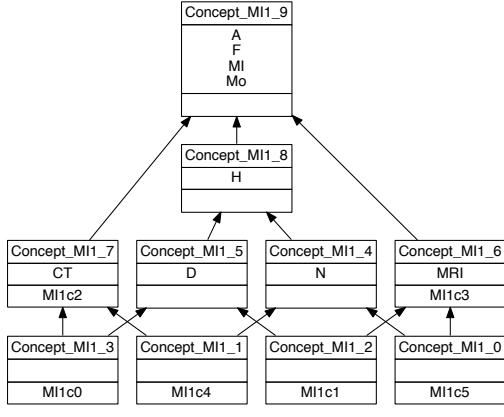
Figure 2: Concept lattice associated with Table 1

Specific suborders can be isolated in the concept lattice, as the AOC-poset which contains only the concepts introducing at least one object (configuration),

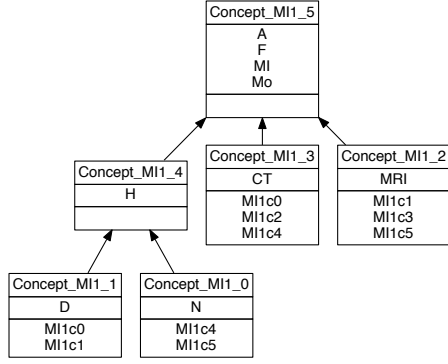
or at least one attribute (feature) (or both, see Figure 3 (a)), or the AC-poset which contains only the concepts introducing at least one attribute (feature) (see Figure 3 (b)). In the AOC-poset (as in the concept lattice) a configuration (resp. a feature) appears only once, thus we have a maximal factorization of configurations and features. In the AC-poset, one configuration (e.g. `MI1c4`) may appear several times, but features remain maximally factorized revealing a simplified structure.

Furthermore, if the formal context is exactly the set of valid configurations of a FM, conceptual structures represent, in a unique way, this configuration set: there is a unique concept lattice, a unique AOC-poset, a unique AC-poset representing the FM. Therefore, any FM with the same configuration set has the same associated conceptual structures. Thus if we consider the AOC-poset (which is a good compromise in size and in information presentation (no redundancy)) corresponding to FM1, FM1v and any other feature model with the same configuration set, all these FMs *conform* to it. This means that each dependency expressed in these feature models matches a dependency expressed in the corresponding AOC-poset. For instance, if there is a child-parent (f_c, f_p) in a FM, it belongs to the AOC-poset in this way: let C_c the concept introducing f_c and C_p the concept introducing f_p , $C_c \preceq_C C_p$.

However, the posets are hardly readable and far from feature models. That is why we introduce another equivalent structure (the equivalence class feature diagram —ECFD), which is graphically closer to the feature models. An example of ECFD is shown in Figure 4, and the constructs and the semantics of the ECFD are given in Table 2. Firstly, part of the information of the ECFD comes from the concepts that introduce the features. In our example, `MI`, `Mo`, `F` and `A` are always together in configurations, thus a FM can contain any relation set between these without changing the semantics. `MRI`, `CT` and `H` can be connected to any feature among `MI`, `Mo`, `F` or `A` (edges going to the entire box). `D` (resp. `N`) can be a child of `H`. Sec-



(a) AOC-poset



(b) AC-poset presented with leaves labeled by the configurations

Figure 3: AOC-poset and AC-poset associated with formal context of Table 1.

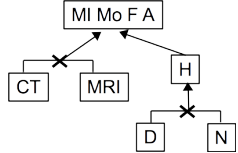


Figure 4: Equivalence class feature diagram (ECFD), alternative representation of the posets of Figure 3.

only, other information comes from the concepts that introduce the configurations and their subconcepts, as highlighted in (Ryssel et al., 2011). As the introducers of MRI and CT (resp. D and N) have no lower bound in the AOC-poset (or their lower bound is the bottom in the lattice), we deduce the mutual exclusion between them. We also observe in valid configurations (concepts introducing at least one configuration) the fact that one of both has to be present. Thus (MRI, CT) and (D, N) are *xor-groups* in the ECFD.

Both FM1 and FM1v are conform to the ECFD of Figure 4 in the sense that their dependencies match the information extracted from it. Note that for FM1v, three constraints have to be added to the graphical rep-

construct	semantics	ex. of conform FM
$A = \{a_1, \dots, a_{n_A}\}$	features a_i are always present together (or absent)	
$A = \{a_1, \dots, a_{n_A}\}$ $B = \{b_1, \dots, b_{n_B}\}$	When b_i features are present, all a_i features are present as well	
	or-group: when a_i features are present, either the b_i are present, or the c_i are present, or the b_i and the c_i are present	
	xor-group: when a_i features are present, either the b_i are present, or the c_i are present (not both)	
	mutex: features a_i and features b_i are never present together	

Table 2: Equivalence class feature diagram (ECFD): constructs and semantics. The third column gives an example of conform feature model with $n_A = n_B = 3$ and $n_C = 2$

resentation in order to express the *xor* information.

The ECFD describes the equivalence class of FMs that have the same set of configurations, provides a graphical view and is pretty interesting to guide an expert from a configuration set to a satisfying FM.

3 CONCEPTUAL STRUCTURES AND MERGE OPERATIONS

In this section, we detail how FCA can be used to assist merge (composition) operations on FMs.

3.1 Overview of merge operations

Several design situations may require FM composition, for example several experts work on designing variability and independently develop their FMs with

different concerns, or when several products have to be merged. To focus the study, we consider the two merge operations that are defined in (Acher et al., 2010a): merge-intersection and merge-union. In this work, the semantics of the merge operations is given using the configuration semantics.

Definition 4 (Merge operations (Acher et al., 2010a)).

- The merge intersection operation, denoted by \cap , builds a feature model FM_3 from two feature models FM_1 and FM_2 such that $\llbracket FM_3 \rrbracket = \llbracket FM_1 \rrbracket \cap \llbracket FM_2 \rrbracket$.
- The merge union operation, denoted by \cup , builds a feature model FM_3 from two feature models FM_1 and FM_2 such that $\llbracket FM_3 \rrbracket = \llbracket FM_1 \rrbracket \cup \llbracket FM_2 \rrbracket$.

Figure 5 illustrates these two merge operations on the medical imaging services presented in (Acher et al., 2010a). We consider again the service whose variability is described by $FM1v$ (Figure 1). The variability of another service of medical imaging is described by $FM2$ (on the right-hand-side of Figure 5). The set of configurations of $FM2$ is given in Table 3.

Table 3: $FM2$ configuration set (and formal context).

MI2	A	CT	D	F	H	MI	MRI	Mo	PET
MI2c0	x		x	x	x	x		x	x
MI2c1		x	x	x	x	x		x	
MI2c2				x		x		x	x
MI2c3	x	x	x	x	x	x		x	
MI2c4	x		x	x	x	x	x	x	
MI2c5	x			x		x		x	x
MI2c6			x	x	x	x	x	x	
MI2c7		x		x		x		x	
MI2c8	x	x		x		x		x	
MI2c9	x			x		x	x	x	
MI2c10				x		x	x	x	
MI2c11			x	x	x	x		x	x

Such operations are complex to perform based on the structure of FM since two feature models representing two close sets of configurations can be very different, as can be shown in Figure 5.

3.2 Definition of merge operations based on conceptual structures

Based on the definitions, our approach for building the intersection (resp. the union) of two feature models can be decomposed in three steps: 1) building the

table representing the configurations that appear in the two initial feature models (resp. in at least one), 2) building the AC-poset associated with the obtained table, which describes the equivalence class of possible intersection (resp. union) feature models, and 3) extracting the ECFD from the AC-poset. The ECFD will be presented to the expert to guide him/her in choosing a FM representation. This approach absorbs, during the merge operation, the differences in the structure and the representation choices of the feature models and their cross-tree constraints. We consider in the definitions of the rest of this section two formal contexts $K_1 = (G_1, M_1, I_1)$ and $K_2 = (G_2, M_2, I_2)$. K_1 and K_2 are supposed to be cleaned so that there do not exist two identical configurations (rows) in them.

3.2.1 Intersection formal context (merge-intersection)

We first introduce the notion of equality of objects (configurations), denoted \triangleq , as objects having the same set of attributes.

Definition 5 (Equality of objects).

$$g_1 \triangleq g_2 \Leftrightarrow g_1 \in G_1, g_2 \in G_2 \text{ and } I_1(g_1) = I_2(g_2)$$

In tables and figures, which are generated by tools, $MI1c0 \triangleq MI2c3$ is denoted by "MI1c0=MI2c3".

We then define the formal context associated with merge-intersection as the rows that are present in the two initial formal contexts. A labeling of rows is added to indicate their origin.

Definition 6 (Merge-intersection formal context). The formal context of merge intersection $Inter(K_1, K_2)$ is $K_{Inter(K_1, K_2)} = (G_{Inter(K_1, K_2)}, M_{Inter(K_1, K_2)}, I_{Inter(K_1, K_2)})$ such that:

- $G_{Inter(K_1, K_2)} = \{g_{g_1 \triangleq g_2} \mid \exists (g_1, g_2) \in G_1 \times G_2, g_1 \triangleq g_2\}$
- $M_{Inter(K_1, K_2)} = M_1 \cap M_2$
- $I_{Inter(K_1, K_2)} = \{(g_{g_1 \triangleq g_2}, m) \mid m \in M_{Inter(K_1, K_2)}, g_{g_1 \triangleq g_2} \in G_{Inter(K_1, K_2)}, (g_1, m) \in I_1 \text{ (or equiv. } (g_2, m) \in I_2)\}$

Table 4 shows the merge-intersection formal context for the example. The corresponding AC-poset is presented in Figure 6. The extracted ECFD is presented in the l.h.s of Figure 7. From this ECFD, an expert can extract several FMs representing the intersection. In fact, to guide the designer in his/her choices, decorations can be added on the ECFD, like ontological relation of the initial feature models, or similar groups from the same parent or mandatory information. By choosing an ontological semantics to the ECFD, one derives a feature model description which conforms with this ECFD. Such a derivation is shown in the r.h.s of Figure 7, and the corresponding FM is represented in Figure 5 (top).

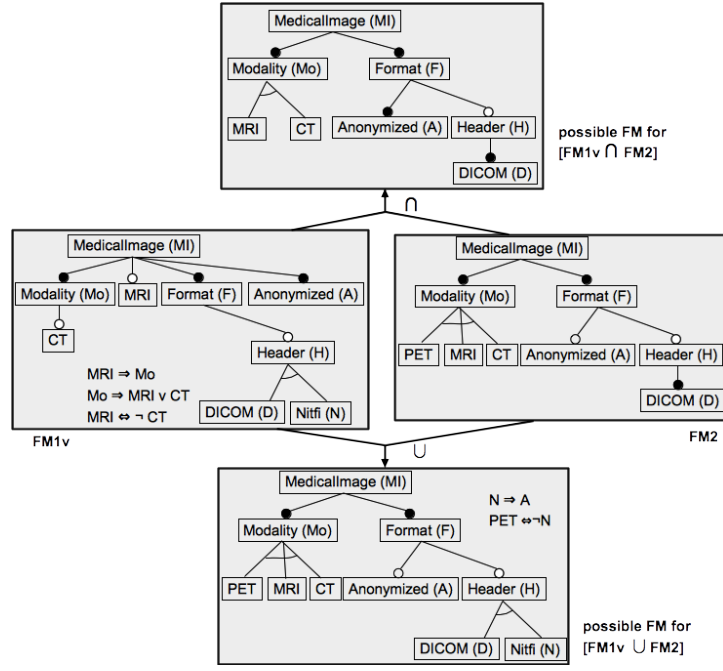


Figure 5: FM1v and FM2, with possible intersection and union Feature models. Figure adapted from (Acher et al., 2010a)

Table 4: Merge-intersection formal context.

Int12	A	CT	D	F	H	MI	MRI	Mo
MI1c0=MI2c3	×	×	×	×	×	×	×	×
MI1c1=MI2c4	×		×	×	×	×	×	×
MI1c2=MI2c8	×	×		×		×		×
MI1c3=MI2c9	×			×		×	×	×

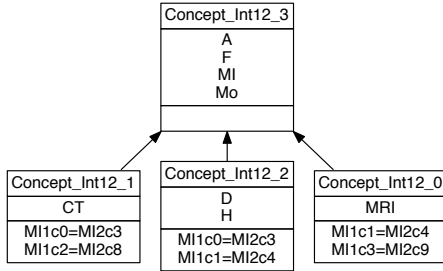


Figure 6: AC-poset associated with merge-intersection formal context of Table 4.

3.2.2 Union formal context (merge-union)

Let us now define the formal context associated with merge-union.

Definition 7 (Merge-union formal context). *Let us consider:*

- the set of common configurations (from Def. 6) $G_{Inter(K_1, K_2)}$ and the corresponding relation $I_{Inter(K_1, K_2)}$
- the set of configurations specific to G_1 : $SPE(G_1) =$

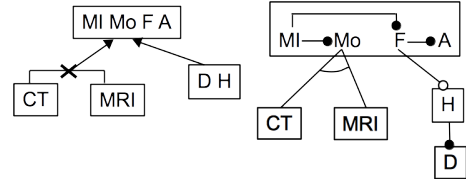


Figure 7: ECFD of AC-poset from Figure 6, and derivation of intersection FM from Figure 5 on ECFD.

$$\{g_1 \mid g_1 \in G_1 \text{ and } \nexists g_2 \in G_2, \text{ with } g_{g_1 \triangle g_2} \in G_{Inter(K_1, K_2)}\}$$

- the set of configurations specific to G_2 : $SPE(G_2) = \{g_2 \mid g_2 \in G_2 \text{ and } \nexists g_1 \in G_1, \text{ with } g_{g_1 \triangle g_2} \in G_{Inter(K_1, K_2)}\}$

The formal context of merge-union $Union(K_1, K_2)$ is: $K_{Union(K_1, K_2)} = (G_{Union(K_1, K_2)}, M_{Union(K_1, K_2)}, I_{Union(K_1, K_2)})$ such that:

- $G_{Union(K_1, K_2)} = G_{Inter(K_1, K_2)} \cup SPE(G_1) \cup SPE(G_2)$
- $M_{Union(K_1, K_2)} = M_1 \cup M_2$
- $I_{Union(K_1, K_2)} = I_{Inter(K_1, K_2)} \cup \{(g, m) \mid g \in SPE(G_1), m \in M_{Union(K_1, K_2)}, (g, m) \in I_1\} \cup \{(g, m) \mid g \in SPE(G_2), m \in M_{Union(K_1, K_2)}, (g, m) \in I_2\}$

Table 5 shows the merge-union formal context for the example. The corresponding AC-poset is presented in Figure 8. The ECFD associated with the AC-poset is presented in the l.h.s of Figure 9. An expert can choose the union FM of Figure 5 (bottom) that can be derived from the ECFD as shown in the r.h.s of Figure 9.

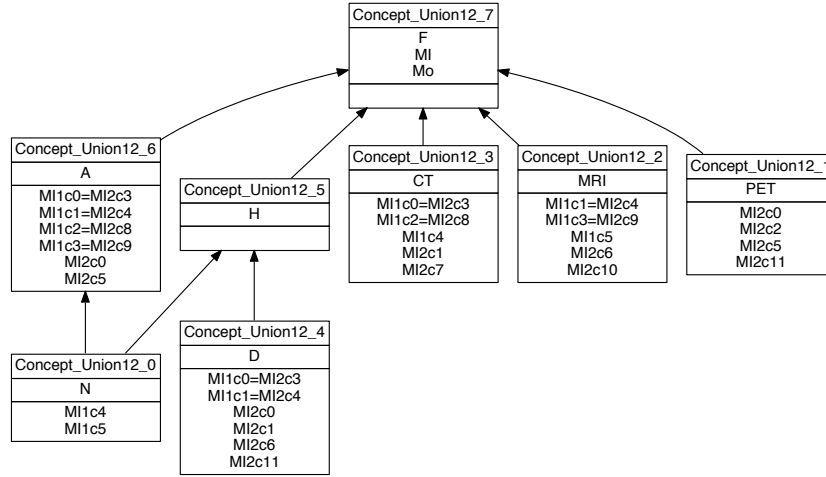


Figure 8: AC-poset associated with merge-union formal context of Table 5.

Table 5: Merge-union formal context.

Union12	A	CT	D	F	H	MI	MRI	Mo	N	PET
MI1c0=MI2c3	×	×	×	×	×	×		×		
MI1c1=MI2c4	×		×	×	×	×	×	×		
MI1c2=MI2c8	×	×		×		×		×		
MI1c3=MI2c9	×			×		×	×	×		
MI1c4	×	×		×	×	×		×	×	
MI1c5	×			×	×	×	×	×	×	
MI2c0	×		×	×	×	×		×		×
MI2c1		×	×	×	×	×		×		
MI2c2				×		×		×		×
MI2c5	×			×		×		×		×
MI2c6			×	×	×	×	×	×		
MI2c7		×		×		×		×		
MI2c10				×		×	×	×		
MI2c11			×	×	×	×		×		×

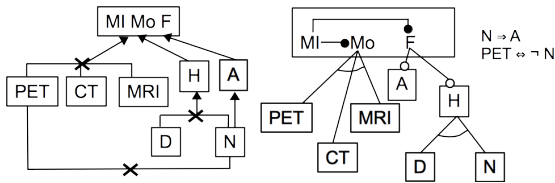


Figure 9: ECFD for AC-poset from Figure 8, and derivation of union FM from Figure 5 on ECFD.

4 IMPLEMENTATION

The approach has been implemented and tested with several feature models or variations of them, taken from the SPLOT repository¹, from the Fa-

miliar² website, or from the literature. The process is presented in Figure 10 and uses Familiar for building the configuration set of an FM and rcaexplore³ to build the AC-poset from which the ECFD structure (nodes and edges) is extracted. We also developed additional tools specific to this project: a first tool (ConfigSet2FormalContext) builds a formal context (within input format of rcaexplore) from a configuration set extracted from Familiar, a second tool (ComputeInterAndUnion) builds the intersection and union formal contexts, and a third tool (ComputeGroupsAndMutex) computes the groups Xor, Or and the mutex of the ECFD.

Table 6 shows the feature models on which we have tested our approach. For each feature model, we give the number of features, configurations, Xor groups, Or groups and constraints. We also compute the ECFD and indicate the number of Xor groups, Or groups, mutex and situations where a box in the ECFD has several direct parents in the AC-poset (*multi-par.*). The number of groups, e.g. Xor groups, may vary between the FM and the ECFD. For example, one Xor group of the ECFD may combine several Xor groups of the FM when there are additional constraints, or the ECFD may reveal more possible Xor groups than initially indicated in the FM.

Table 7 shows the information about ECFDs of the intersection (when it is not empty) and the union of the initial FMs that we obtain with our approach. As these ECFDs are intended to guide a designer towards a FM, it is important to notice that their size remains reasonable compared to the input FMs. The number of groups is not very high, and the number of mutex,

¹<http://www.splot-research.org/>

²<http://familiar.variability.io/>

³<http://dolques.free.fr/rcaexplore/>

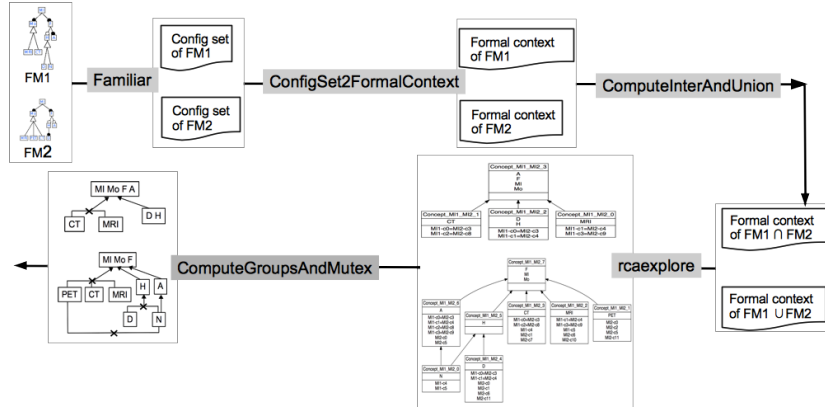


Figure 10: The implemented process.

except in three cases is also low. Multi-parent situations mainly offer two representation choices: implication or child-parent edge in the FM and they are very few.

Concept lattices, and thus, a fortiori, AOC-posets and AC-posets can be built for large datasets, e.g. in (Wray et al., 2016), the authors mention a large dataset, the Rijksmuseum collection which contains 100,000 objects and 1,716 attributes, giving 994,967 concepts computed in 68ms in average with FCbO update algorithm. The computation of the groups can be a hard task, as pointed out in (Ryssel et al., 2011). Many FMs have a very large configuration set, as Video player FM from SPLOT, with 71 features and more than 1 billion configurations. We do not address these cases, as we more specifically address the contexts where the FMs have a reasonable number of configurations, which corresponds in particular to FMs coming from real-world product lines. Product comparison matrices (PCMs) studied in (Bécan et al., 2014) give an overview of this type of dataset where many datasets could be investigated using our method: 75 PCMs, corresponding to 211 matrices that have 2 to 241 rows, and 3 to 51 possibly valued columns, with about 43% of the cells have boolean value (and the others should be translated into boolean feature via FCA scaling (Ganter and Wille, 1999)).

5 RELATED WORK

Previous research work has used FCA for Software Product Line Engineering (SPLE), mainly in the context of reengineering concrete product lines. Feature model analysis or synthesis have been done in (Loesch and Ploedereder, 2007), (Ryssel et al., 2011), (Anonymous, 2014), (Shatnawi et al., 2015). In (Niu and Easterbrook, 2009), the authors present an ap-

Table 7: Intersection and union ECFDs.

FM	Formal context		ECFD			
	#feat	#conf.	#Xor	#Or	#mutex	#multi-par.
MI1∩MI2	8	4	1	0	0	0
MI1∪MI2	10	14	2	0	1	1
Martini∪Tang	12	21	1	2	3	1
Martini∪Toacy	14	56	1	1	4	0
Tang∩Toacy	8	5	1	2	0	0
Tang∪Toacy	13	56	1	1	4	1
WikiV1∪WikiV2	20	60	5	9	26	0
WikiV1∪WikiV3	23	130	3	4	42	0
WikiV2∩WikiV3	14	50	0	6	0	0
WikiV2∪WikiV3	21	120	0	16	8	1
Bicycle1∩Bicycle2	14	8	1	0	0	0
Bicycle1∪Bicycle2	26	248	6	1	32	2
Bicycle3∩Bicycle4	23	288	5	1	8	0
Bicycle3∪Bicycle4	27	1152	6	1	8	0

proach based on aspect-oriented SPLE where they classify scenarios by functional requirements. Using FCA for feature location has been studied by (Xue et al., 2012), (Salman et al., 2013), and (Anonymous, 2013). Traceability links between features and code have been established by (Salman et al., 2013). Another available tool in the framework of FCA is the notion of implicative systems, already used in (Ryssel et al., 2011). This is another logical encoding of the formula underlying in (and equivalent to) a concept lattice (or a feature model), which can be rather compact. The paper (Anonymous, 2016) gives a procedure to derive (in a polynomial time) an implicative system directly from a feature model, thus without using the configuration set which may be an obstacle in some cases as noticed by (Ryssel et al., 2011).

Acher et al. compare various approaches for FM model merging in (Acher et al., 2010a) and (Acher et al., 2013). Some approaches, such as (Schobbens et al., 2007) and (Heymans et al., 2008) maintain separately the input feature models and establish links

Table 6: Features models (and the corresponding ECFD) used for testing the approach. *var.* stands for *variant*. *Cst* stands for *Constraint*.

FM	Feature Model					ECFD			
	#feat	#conf.	#Xor	#Or	# Cst	#Xor	#Or	#mutex	#multi-par.
MI1 (Acher et al.)	9	6	2	0	0	2	0	0	0
MI2 (Acher et al.)	9	12	1	0	0	1	0	0	0
Martini Eshop (SPLOT)	11	8	1	1	1	1	2	1	1
Tang Eshop (SPLOT)	10	13	1	1	2	1	2	1	1
Toacy Eshop (SPLOT)	12	48	1	2	0	1	2	0	0
Wiki V1 (Familiar example)	14	10	4	0	4	3	2	5	2
Wiki V2 (Wiki V1 var.)	17	50	4	1	4	6	13	1	1
Wiki V3 (Wiki V1 var.)	18	120	3	2	6	2	2	1	0
Bicycle1 (Mendonca SPLOT var.)	19	64	2	0	2	1	0	0	0
Bicycle2 (Mendonca SPLOT var.)	22	192	5	0	1	6	1	6	0
Bicycle3 (Mendonca SPLOT var.)	25	576	4	0	2	5	1	8	0
Bicycle4 (Mendonca SPLOT var.)	26	864	5	0	2	6	1	8	0

between them through constraints. The approach of (Acher et al., 2010b) establishes, in a first phase, the matching between similar elements, then an algorithm recursively merges the feature models. Catalogs of local transformation rules are proposed in (Segura et al., 2007), (Alves et al., 2006). Other approaches encode the FMs into propositional formula (Batory, 2005), then compute the formula representing the intersection (resp. the union), then synthesize a FM from the boolean formula (Czarnecki and Wasowski, 2007).

Our proposal can be analyzed with the criteria of (Acher et al., 2010a). Concerning *quality of the result*: The configuration-semantics is preserved. The non-contradictory ontological child-parent edges are preserved. We do not reduce the set of features, except if some of them are not used, they will appear in the bottom concept and they can be eliminated. The result is not final in our case, an FM has to be chosen based on the ECFD. About criterion *Error handling*: errors like empty intersection are detected. When intersection is empty, the designer should conclude to an error or an incompatibility that he/she may want to fix. But in spite of empty intersection, feature models may have common part in their structure, leading to incomplete configurations. The union, in this case, can be read to highlight such common parts. We do not make *Assumption on input FMs*: There is no specific assumption in our method. Cross-tree constraints are taken into account in the conceptual structures (implicitly, thanks to the position of the features or to the position of the configurations in subconcepts). When there are hierarchy mismatches, the AC-poset manages this information (see FM1 and its variant) but the vocabulary (feature names) has to be the same (it can be aligned before the merge operations). Then about *aspects of the implementation*: The ap-

proach needs to know the list of configurations, thus as such, the proposed solution is restricted to some contexts: FMs that have limited number of configurations; real-world product lines given with configuration sets. There is no "testing" effort since the logical semantics is guaranteed by the FCA theory. The computational complexity is polynomial for AC-posets, in the size of the number of configurations and the number of features. As detailed by (Ryssel et al., 2011), group and *mutex* computation might be exponential in the number of configurations or features but remains reasonable in typical situations, with an optimized implementation.

6 CONCLUSION

In some design situations, combining various real-world product lines, or various FMs, given through their configuration set is a useful step in the design of a variability model. In this paper, we propose an approach, based on Formal Concept Analysis (FCA), that aims to assist a designer during this task. We exploit the properties of the AC-poset to build a canonical structure, the ECFD, which represents all the FMs with the same configuration semantics. The merge-intersection and merge-union operators are encoded in the framework of FCA, that allows us to compute the ECFD for intersection and union. These ECFDs may be used to guide the expert in deriving a representative feature model conform to the ECFD.

As a current work, we are designing the process for guiding the expert while building the feature model, in choosing the child-parent edges, the groups and the constraints among those that are included in the ECFD. Besides, the approach is currently based on a configuration set, but FCA offers other struc-

tures, such as the implicative systems. We are currently investigating the transformation of an FM into such an implicative system (without computing the configuration set), then the computation of the AC-poset and the groups and mutex of the ECFD from the implicative system. This will enlarge the scope of applicability of the approach to cases where the configuration set can hardly be computed. As a future work, we also would like to apply our method to other FMs, and to PCMs, which involves a substantial work to translates the many-valued cells into FCA framework and to synthesize associated FMs.

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