

# Software Requirements Specification for 2D Localizer

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## Revision History

Date	Version	Notes
2025/02/05	1.0	Initial Draft
Date 2	1.1	Notes

# 1 Reference Material

This section records information for easy reference.

## 1.1 Table of Units

Throughout this document SI (Système International d’Unités) is employed as the unit system. In addition to the basic units, several derived units are used as described below. For each unit, the symbol is given followed by a description of the unit and the SI name.

symbol	unit	SI
m	length	metre
rad	angle	radians

## 1.2 Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The symbols are listed in alphabetical order.

[Remeber to organize them in order —TPLT]

symbol	unit	description
$i$	—	Index for robot’s poses
$j$	—	Index for number of beacons
$\eta_j$	—	Sensor noise
$m$	—	Index for number of FMs
$n$	—	Total number of beacons used
$S$	—	Set of beacon coordinates
$g_j(x_i)$	m	Noisy range measurement of the robot’s $i$ th taken from $j$ th beacon
$F$	—	Coordinates of FMs
$\sigma_j^2$	m <sup>2</sup>	Noise variance for $j$ th beacon
$\tilde{d}_j$	m	Measured distance with noise
$C(x_i)$	m	Cost Function
$I$	m <sup>-2</sup>	Total Fisher Information Matrix
$\theta$	rad	Robot angle
$T_{robot}$	m <sup>2</sup>	surface area over which heat is transferred in
$\tilde{D}$	m <sup>2</sup>	coil surface area
$d_j$	m <sup>2</sup>	surface area over which heat is transferred in

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$T_{env}$	$m^2$	coil surface area
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### 1.3 Abbreviations and Acronyms

[Double check if you need Likely Changes —TPLT]

Abbreviation/Acronym	Definition
2D	Two-Dimensional
2D Localizer	2D Localization Solution
A	Assumption
CRLB	Cramér-Rao Lower Bound
DD	Data Definition
FIM	Fisher Information Matrix
FM	Fiducial Marker
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
MLE	Maximum Likelihood Estimation
PDF	Probability Density Function
PS	Physical System Description
R	Requirement
SE(2)	Special Euclidean Group in 2D
SRS	Software Requirements Specification
TM	Theoretical Model
UC	Unlikely Change

### 1.4 Mathematical Notation

Throughout this document, there will be typographic conventions as well as mathematical operators that are used to distinguish different variables and operations.

Variable	Definition	Description
<b>A</b>	Matrix	Bold capital letter
<b>a</b>	Vector	Bold lowercase letter

$a/A$	Scalar	Italicized uppercase/lowercase symbol
$\  \ \ $	Euclidean (2) Norm	Vertical brackets

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## 2 Introduction

Mobile robots have been used to traverse areas with various hazards, help collect data whether through its sensors or obtaining samples, and overall complete challenging tasks. Due to their autonomy, there is no need to constantly monitor them as they have their own means with interacting with the environment. However, it could raise some concern when there is no reliable method to track their movements, especially if they are placed in a vastly large area or places that may be difficult to access once they are operational. Risks such as having difficulty retrieving them if there is a malfunction keeping them from returning or possible collisions in the area or with other robots are reasons one would want to find a way to locate them as they carry out their tasks. The program being documented, 2D Localizer, proposes to solve this problem by developing a 2D localization solution that can implement various sensors to accurately localize the robots as they traverse the map provided.

The following section provides an overview of the Software Requirement Specification (SRS) for 2D Localizer. This section explains the purpose of this document, the scope of the requirements, the characteristics of the intended reader, and the organization of the document.

### 2.1 Purpose of Document

The main purpose of this document is to describe the requirements needed to run the localizer. Information such as the constraints, assumptions and theoretical models used will be provided to help readers get a better understanding of the purpose and computations of 2D Localizer. Therefore, it can be used as a reference guide on how to plan and set up the requirements needed by the user to get the desired and accurate results.

### 2.2 Scope of Requirements

The scope of the requirements includes the robot analyzed being in a controlled environment to help with potential lighting problems for vision sensors used. The sensors used on the robot and environment are specified for modelling purposes. Some models can include a sum through sensors having independent measurements. The noise from the sensors will be considered zero-mean Gaussian for simplicity in calculations.

### 2.3 Characteristics of Intended Reader

Reviewers of this documentation should have taken a graduate course on linear algebra, estimation theory or matrix computation. They should also have some knowledge in undergraduate statistics and probability.



## 2.4 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [Smith and Lai \(2005\)](#), [Smith et al. \(2007\)](#), and [Smith and Koothoor \(2016\)](#). The presentation follows the standard pattern of presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the data definitions and trace back to find any additional information they require.

The goal statements are refined to the theoretical models and the theoretical models to the instance models. The data definitions are used to support the definitions of the different models.

## 3 General System Description

This section provides general information about the system. It identifies the interfaces between the system and its environment, describes the user characteristics and lists the system constraints.

### 3.1 System Context

The system context is displayed in [Figure 1](#) below. The circles represent the external aspects related to the software which are the users. The rectangle represents the software system being used (2D Localizer) and the arrows explain what information is being passed between the user and the software.

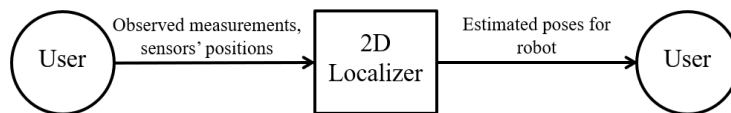


Figure 1: System Context

- User Responsibilities:
  - Provide inputs including the coordinates of each environmental sensor and the measurements taken from them.
  - Evaluate the inputs to ensure all are their respective types
- 2D Localizer Responsibilities:
  - Detect data type mismatch, such as a string of characters instead of a floating point number
  - Estimate the position and orientation of the robot

## 3.2 User Characteristics

The end user of 2D Localizer should have some familiarity with types of range sensors along with how to read and collect their data. They should also have basic experience with programming.

## 3.3 System Constraints

There are no system constraints.

# 4 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, definitions and finally the instance models.

## 4.1 Problem Description

2D Localizer is intended to help keep track of mobile robots while carrying out their tasks.

### 4.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements:

- **Pose:** Position and orientation of the robot.
- **Localization:** Determining where an object is with respect to its environment.
- **Fiducial Markers:** Markers placed around the environment for the robot to determine its location.
- **Beacon:** A range sensor

### 4.1.2 Physical System Description

The physical system of the localizer includes the following elements:

PS1: The mobile robot

PS2: The beacons placed in the environment

PS3: The camera sensors on the mobile robot

PS4: The fiducial markers in the environment

### 4.1.3 Goal Statements

Given the imported 2D map, coordinates of all sensors and fiducial markers in the environment, and the noisy measurements of the sensors, the goal statements are:

GS1: Calculate the estimated pose and error of the robot throughout its trajectory from both sensors (environment and robot).

GS2: Display a visual representation of the robot traversing the 2-D map with the sensors placed.

## 4.2 Solution Characteristics Specification

The instance models that govern 2D Localizer are presented in Subsection 4.2.6. The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

### 4.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical model by filling in the missing information for the physical system. The numbers given in the square brackets refer to the theoretical model [TM], general definition [GD], data definition [DD], instance model [IM], or likely change [LC], in which the respective assumption is used.

A1 : Robot uses camera sensors while the environment uses beacons and fiducial markers (FMs)

A2 : Localizer is used in a controlled environment (i.e., indoors)

A1 : Each sensor has independent measurements

A1 : Sensor noise is zero-mean Gaussian

### 4.2.2 Theoretical Models

This section focuses on the general equations and laws that 2D Localizer is based on.

Number	TM1
Label	<b>Noisy Range Measurement</b>
Equation	$g_j(x) = \ \mathbf{x}_i - \mathbf{a}_j\  + \eta_j$
Description	<p>The equation above gives the noisy range measurement <math>g_j</math> (m) of the beacons placed in the environment (A1) where</p> <p><math>\mathbf{x}_i</math> is the position of the robot (m),</p> <p><math>\mathbf{a}_j</math> is the position of the jth beacon placed (m), and</p> <p><math>\eta_j</math> is the noise from the jth beacon (m) (A4).</p>
Source	<a href="#">Sequeira et al. (2024)</a>
Ref. By	DD1
Preconditions	A4
Derivation	None

Number	TM2
Label	<b>Fisher Information Matrix</b>
Equation	$\mathbf{I} \cong \sum_{j=1}^N \frac{1}{\sigma_j^2} \frac{(\hat{x} - a_j)(\hat{x} - a_j)^T}{\ \hat{x} - a_j\ ^2}$
Description	<p>This equation gives the Fisher Information Matrix which shows how much information the data provides about the robot's position</p> <p><math>\sigma_j^2</math> is the sensor variance used in the noise factor</p> <p><math>\hat{x}</math> is the estimated position in IM2</p>
Source	Citation here
Ref. By	TM3
Preconditions	A4, IM2
Derivation	

Number	TM3
Label	<b>Cramér-Rao Lower Bound (CRLB)</b>
Equation	$Var(\hat{x}) \geq \frac{1}{I(\hat{x})}$
Description	<p>This equation gives the CRLB which shows how accurate an estimate of a parameter is given the noise in the measurements by providing a lower bound to the estimate's variance. We are able to use <a href="#">TM2</a> to get this lower bound</p> <p><math>Var(\hat{x})</math> is the variance of the unbiased estimator in <a href="#">IM2</a></p>
Source	<a href="#">Barfoot (2017)</a>
Ref. By	None
Preconditions	<a href="#">TM2</a> , <a href="#">IM2</a>
Derivation	None

Number	TM4
Label	<b>Special Euclidean (SE) 2 Transformation</b>
Equation	$T_{robot} = \begin{bmatrix} \mathbf{R}(\theta) & \mathbf{t} \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & x \\ \sin \theta & \cos \theta & y \\ 0 & 0 & 1 \end{bmatrix}$
Description	<p>This equation shows SE(2) which represents all possible 2D transformations of the robot. Since the robot has cameras placed on it (A1), SE(2) can be used to get the position and orientation through the FMs.</p> <p><math>\mathbf{R}(\theta)</math> is the rotation represented as a <math>2 \times 2</math> matrix</p> <p><math>\mathbf{t}</math> is the translation represented as a <math>2 \times 1</math> matrix</p> <p><math>[0 \ 1]</math> makes sure that the matrix is homogenous</p>
Source	<a href="#">Barfoot (2017)</a>
Ref. By	DD??, DD??
Preconditions	
Derivation	

### 4.2.3 General Definitions

This section collects the laws and equations that will be used in building the instance models.

Number	GD1
Label	<b>Probability Density Function (PDF)</b>
SI Units	$\text{m}^{-1}$
Equation	$p_j \left( \tilde{d}_j   \mathbf{x} \right) = \mathcal{N} \left( \ \mathbf{x} - \mathbf{a}_j\ , \sigma_j^2 \right)$
Description	<p>This definition is about the Gaussian PDF (A4) being used in IM1. This provides the PDF of the actual noisy range measurement <math>\tilde{d}_j</math> of beacon <math>j</math> (DD1) that is conditioned on the robot’s position <math>\mathbf{x}</math>.</p> <p><math>\mathcal{N}</math> is the normal distribution with <math>\ \mathbf{x} - \mathbf{a}_j\ </math> as the mean (predicted range) and <math>\sigma_j^2</math> as the variance (sensor noise/uncertainty).</p>
Source	<a href="#">Sequeira et al. (2024)</a>
Ref. By	IM1

#### 4.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models. The dimension of each quantity is also given.

Number	DD1
Label	<b>Actual Range Measurement</b>
Symbol	$\tilde{d}_j$
SI Units	m
Equation	$\tilde{d}_j = \ \mathbf{x}_i - \mathbf{a}_j\  + \eta_j$
Description	<p><math>\tilde{d}_j</math> is the actual beacon measurement that will be used compared to TM1 which is just a model. Although it would return a scalar from the sensor, the formulation the equation above.</p> <p><math>\mathbf{x}_i</math> is the position of the robot (m),</p> <p><math>\mathbf{a}_j</math> is the position of the jth beacon placed (m), and</p> <p><math>\eta_j</math> is the noise from beacon j(m) (A4).</p>
Sources	<a href="#">Sequeira et al. (2024)</a>
Ref. By	GD1

#### 4.2.5 Data Types

[This section is optional. In many scientific computing programs it isn't necessary, since the inputs and output are straightforward types, like reals, integers, and sequences of reals and integers. However, for some problems it is very helpful to capture the type information. —TPLT]

[The data types are not derived; they are simply stated and used by other models. —TPLT]

[All data types must be used by at least one of the models. —TPLT]

[For the mathematical notation for expressing types, the recommendation is to use the notation of ?. —TPLT]

This section collects and defines all the data types needed to document the models. [Modify the examples below for your problem, and add additional definitions as appropriate. —TPLT]



Type Name	Name for Type
Type Def	mathematical definition of the type
Description	description here
Sources	Citation here, if the type is borrowed from another source

#### 4.2.6 Instance Models

This section transforms the problem defined in Section 4.1 into one which is expressed in mathematical terms. It uses concrete symbols defined in Section 4.2.4 to replace the abstract symbols in the models identified in Sections 4.2.2 and 4.2.3.

The goal GS1 is solved by IM1 and IM2.

Number	IM1
Label	<b>Joint Likelihood Function</b>
Input	$\tilde{\mathbf{d}}, N$
Output	$p(\tilde{\mathbf{d}} \mathbf{x})$
Equation	$p(\tilde{\mathbf{d}} \mathbf{x}) = \prod_{j=1}^N p(\tilde{d}_j \mathbf{x})$
Description	<p>This equation uses the measurements gotten from each beacon (A3) to calculate the product of how likely <math>\mathbf{x}</math> is the best position to reflect the inputs where</p> <p><math>\tilde{\mathbf{d}} = [\tilde{d}_1, \tilde{d}_2, \dots, \tilde{d}_N]</math>,</p> <p><math>N</math> is the number of beacons, and</p> <p><math>p(\tilde{d}_j \mathbf{x})</math> is the Gaussian PDF from GD1</p>
Sources	<a href="#">Sequeira et al. (2024)</a>
Ref. By	IM2

Number	IM2
Label	<b>Maximum Likelihood Estimation (MLE)</b>
Input	$p(\tilde{\mathbf{d}} \mathbf{x})$
Output	$\hat{\mathbf{x}}$
Equation	$\hat{\mathbf{x}} = \arg \max_x p(\tilde{\mathbf{d}} \mathbf{x})$
Description	Continuing from IM1, the MLE equation gives an estimate based on the maximum probability calculated from the joint likelihood function. $p(\tilde{\mathbf{d}} \mathbf{x})$ is the joint likelihood function from IM1
Sources	<a href="#">Sequeira et al. (2024)</a>
Ref. By	TM2, TM3

### Derivation of ...

[The derivation shows how the IM is derived from the TMs/GDs. In cases where the derivation cannot be described under the Description field, it will be necessary to include this subsection. —TPLT]

#### 4.2.7 Input Data Constraints

Table 5 shows the data constraints on the input output variables. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable. The column for software constraints restricts the range of inputs to reasonable values. The software constraints will be helpful in the design stage for picking suitable algorithms. The constraints are conservative, to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise.

The specification parameters in Table 5 are listed in Table 7.

(\*) [you might need to add some notes or clarifications —TPLT]

Table 5: Input Variables

Var	Physical Constraints	Software Constraints	Typical Value	Uncertainty
$L$	$L > 0$	$L_{\min} \leq L \leq L_{\max}$	1.5 m	10%

Table 7: Specification Parameter Values

Var	Value
$L_{\min}$	0.1 m

#### 4.2.8 Properties of a Correct Solution

A correct solution must exhibit [fill in the details —TPLT]. [These properties are in addition to the stated requirements. There is no need to repeat the requirements here. These additional properties may not exist for every problem. Examples include conservation laws (like conservation of energy or mass) and known constraints on outputs, which are usually summarized in tabular form. A sample table is shown in Table 9 —TPLT]

Table 9: Output Variables

Var	Physical Constraints
$T_W$	$T_{\text{init}} \leq T_W \leq T_C$ (by A??)

[This section is not for test cases or techniques for verification and validation. Those topics will be addressed in the Verification and Validation plan. —TPLT]

## 5 Requirements

This section provides the functional requirements, the business tasks that the software is expected to complete, and the nonfunctional requirements, the qualities that the software is expected to exhibit.

## 5.1 Functional Requirements

- R1: Provide the inputs for 2D Localizer which include the 2D map, the coordinates of all sensors and markers located in the environment, and the measurements taken from the sensors.
- R2: 2D Localizer will acquire  $\hat{x}$  from the inputs in R1.
- R3: 2D Localizer will calculate the estimated pose from the measurements provided for IM2.
- R4: 2D Localizer will verify that inputs provided are within their constraints.
- R5: 2D Localizer will show a visual animated graph that tracks the mobile robots work while also displaying the sensors' coordinates.

## 5.2 Nonfunctional Requirements

This problem prioritizes the accuracy of the estimations along with its performance when it comes to keeping up with the robot's movements. That being said, the nonfunctional requirements are:

- NFR1: **Accuracy:** The accuracy of the computed estimations should meet the threshold when comparing to the predicted measurements.
- NFR2: **Understandability:** The software should be simple to understand and implement.
- NFR3: **Maintainability:** The software should be simple to modify some components when needed.
- NFR4: **Usability:** The software should be easy to run and have minimal troubleshooting.

## 5.3 Rationale

This program has rationale for the assumptions mentioned in 4.2.1:

- A1: Assuming the type of sensors assisted in setting up the type of output variables that is needed for each set of estimates.
- A2: Referring to A1, vision sensors will be used on the robot and lighting could affect the way they detect FMs. Another main reason for this assumption is so that the coordinates of each beacon and FM can be structured around the area the user provides.
- A3: To find the sum and products of variables that need data from each beacon and FM places (TM2, IM1), having each sensor collect independent data from different positions would help with the overall accuracy the program wants to achieve.

- A4: Having a Gaussian noise assumption simplifies computations in the program especially when some sensors used in robotics follow a Gaussian distribution.

## 6 Unlikely Changes

UC1: A4 There are various models that are derived based on the Gaussian noise meaning that it would be detrimental to change.

## 7 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an “X” may have to be modified as well. Table 11 shows the dependencies of theoretical models, general definitions, data definitions, and instance models with each other. Table 12 shows the dependencies of instance models, requirements, and data constraints on each other. Table 13 shows the dependencies of theoretical models, general definitions, data definitions, instance models, and likely changes on the assumptions.

	TM1	TM2	TM3	TM4	GD1	DD1	IM1	IM2
TM1								
TM2								X
TM3		X						X
TM4								
GD1								
DD1	X							
IM1					X	X		
IM2							X	

Table 11: Traceability Matrix Showing the Connections Between Items of Different Sections

## 8 Values of Auxiliary Constants

[Show the values of the symbolic parameters introduced in the report. —TPLT]

[The definition of the requirements will likely call for SYMBOLIC\_CONSTANTS. Their values are defined in this section for easy maintenance. —TPLT]

[The value of FRACTION, for the Maintainability NFR would be given here. —TPLT]

	IM1	IM2	R1	R2	R3	R4	R5
IM1							
IM2	X						
R1							
R2			X				
R3		X					
R4							
R5							

Table 12: Traceability Matrix Showing the Connections Between Requirements and Instance Models

	A1	A2	A3	A4
TM1	X			X
TM2			X	X
TM3				
TM4	X	X		
GD1				X
DD1				X
IM1			X	
IM2				
UC1				X

Table 13: Traceability Matrix Showing the Connections Between Assumptions and Other Items

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