

Assignment # 1

Q1 In figure, ^{particle} 1 of charge $+1.0 \mu\text{C}$ and particle 2 of charge $-3.0 \mu\text{C}$ are held at separation $L = 10.0 \text{ cm}$ on an x-axis. If particle 3 of unknown charge q_3 is to be located such that the net electrostatic force on it from particles 1 and 2 is zero, what must be the (a) x and (b) y coordinates of particle 3?

$$1 \text{ charge} = q_1 = +1.0 \mu\text{C}$$

$$2 \text{ charge} = q_2 = -3 \mu\text{C}$$

$$\text{Distance} = L = 10.0 \text{ cm}$$

$$\text{Net electrostatic force} = \vec{F}_{\text{net}} = 0$$

The forces \vec{F}_{13} and \vec{F}_{23} are equal but in opposite direction

$$\begin{aligned} \vec{F}_{13} &= -\vec{F}_{23} \\ \frac{k q_1 q_3}{(10+x)^2} &= - \left[\frac{k q_2 q_3}{x^2} \right] \\ \frac{q_1}{(10+x)^2} &= - \frac{q_2}{x^2} \\ \frac{x^2}{(10+x)^2} &= - \frac{(-3 \times 10^{-6})}{1 \times 10^{-6}} \\ \left[\frac{x}{(10+x)} \right]^2 &= 3 \end{aligned}$$

$$x = \sqrt{3} (10+x)$$

$$\begin{aligned} x &= (10)(1.7320) + 1.7320 x \\ -17.320 &= 1.7320 x - x \end{aligned}$$

$$0.7320 x = -17.3205$$

$$x = -17.320$$

$$\boxed{x = -23.6602 \text{ cm}}$$

Total distance from origin

$$d = 10 - 23.6602 = \boxed{-13.6602 \text{ cm}}$$

$$x\text{-coordinate} = -13.660 \quad y\text{-coordinate of } q_3 = 0$$

Q2 How many electrons would have to be removed from a coin to leave it with a charge of $+1.0 \times 10^{-7} \text{ C}$?

$$q = 1 \times 10^{-7} \text{ C}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$n = ?$$

$$q = ne$$

$$n = \frac{q}{e}$$

$$e$$

$$n = \frac{1 \times 10^{-7}}{1.6 \times 10^{-19}}$$

$$n = 6.25 \times 10^{11}$$

Q3 At each point on the surface of the cube shown in fig, the electric field is parallel to the z axis. The length of each edge of the cube is 3.0 m. On the top face of the cube the field is $E = -34 \text{ k N/C}$ and on the bottom face it is $E = +20 \text{ k N/C}$. Determine the net charge contained within the cube.

Length of each edge of cube = $L = 3.0 \text{ m}$

$$\vec{E} \text{ on Top face} = \vec{E}_T = -34 \text{ k N/C}$$

$$\vec{E} \text{ on bottom face} = \vec{E}_b = +20 \text{ k N/C}$$

Net charge within cube = $q = ?$

Flux at Top face:-

$$\Phi = \vec{E} \cdot \vec{A} = EA \cos \theta$$

$$\Phi_T = (-34)(3)^2 \cos 0^\circ$$

$$\Phi_T = -306 \text{ Nm}^2/\text{C}$$

Flux at bottom face:-

$$\Phi_b = \vec{E} \cdot \vec{A} = EA \cos \theta$$

$$\Phi_b = (20)(3)^2 \cos 180^\circ$$

$$\Phi_b = -180 \text{ Nm}^2/\text{C}$$

Total flux:

$$\Phi = \Phi_T + \Phi_b$$

$$\Phi = -306 - 180$$

$$\Phi = -486 \text{ Nm}^2/\text{C}$$

By Gauss's law

$$\Phi = \frac{q_{\text{enc}}}{\epsilon_0}$$

$$\begin{aligned} q_{\text{enc}} &= \epsilon_0 \Phi \\ &= (8.85 \times 10^{-12}) (-486) \\ &= -4301.1 \times 10^{-12} \text{ C} \end{aligned}$$

$$q = -4.3 \times 10^{-9} \text{ C}$$

Q4 A long, straight wire ————
——— electric field zero. Calculate —

Linear charge density = $\lambda = 3.6 \text{ n C/m}$

Radius = $r = 1.5 \text{ cm}$

Surface charge density = ?

Net electric field is sum of all electric fields.

$$\vec{E}_{\text{net}} = \vec{E}_{\text{wire}} + \vec{E}_{\text{cylin}}$$
$$0 = \frac{\lambda}{4\pi r \epsilon_0} + \frac{\lambda'}{4\pi r \epsilon_0}$$

$$0 = \lambda + \lambda'$$

$$\lambda' = -\lambda \quad \sim \text{ii}$$

For wire:-

$$\lambda = q/l$$

$$q = \lambda l$$

For cylinder:-

$$\lambda' = q/V$$

$$q = \lambda' V$$

Volume of cylinder = $\pi r^2 l$

$$q = \lambda' \pi r^2 l \quad \sim \text{iii}$$

comparing eq ii, and iii

$$\lambda L = \lambda' \pi r^2 L$$

$$\lambda = \lambda' \pi r^2$$

$$\lambda' = \frac{\lambda}{\pi r^2}$$

$$\lambda' = \frac{(3.6 \times 10^{-9} \text{ C/m})}{\pi (1.5 \times 10^{-2} \text{ cm})^2}$$

$$\lambda' = \frac{3.6 \times 10^{-9}}{7.068 \times 10^{-4}}$$

$$\lambda' = 0.5093 \times 10^{-5}$$

$$\lambda' = 5.093 \times 10^{-6} \text{ C/m}^2$$

Q5 Two charged concentric spherical shells have radii 10.0 cm (a) at $r = 20.0 \text{ cm}$

Outer Radius = $R = 15 \text{ cm}$

Inner Radius = $r = 10 \text{ cm}$

Charge on inner shell = $q_1 = 4 \times 10^{-8} \text{ C}$

Charge on outer shell = $q_2 = 2 \times 10^{-8} \text{ C}$

\vec{E} at $r = 12 \text{ cm} = ?$

\vec{E} at $r = 20 \text{ cm} = ?$

Electric field through inner shell.

$$\Phi = \oint \vec{E} \cdot d\vec{A}$$

$$= \oint E ds = E \oint ds$$

$$\Phi = 4 E \pi r^2 \text{ --- ii}$$

$$\Phi = \frac{q}{\epsilon_0}$$

$$E 4 \pi r^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{4 \pi \epsilon_0 r^2}$$

$$\vec{E} = \frac{k q}{r^2}$$

$$\vec{E} = \frac{(9 \times 10^9) (4 \times 10^{-8})}{(12 \times 10^{-2})^2} = \frac{36 \times 10}{14.4 \times 10^{-4}}$$

$$\vec{E} = 0.25 \times 10 \times 10^4$$

$$\vec{E} = 2.5 \times 10^4 \text{ N/C}$$

• Electric field through outer shell.

$$\Phi = \vec{E} \cdot \vec{A} = \oint E ds$$

$$\Phi = E \oint ds = 4\pi r^2 E = \Phi$$

$$\Phi = \frac{Q}{\epsilon_0}$$

$$\vec{E} = \frac{kq}{r^2}$$

$$= \frac{(9 \times 10^9)(2 \times 10^{-8})}{(20 \times 10^{-2})^2}$$

$$\boxed{\vec{E} = 4.5 \times 10^3 \text{ N/C}}$$