

# DIGITAL LOGIC & DESIGN (EE-227)

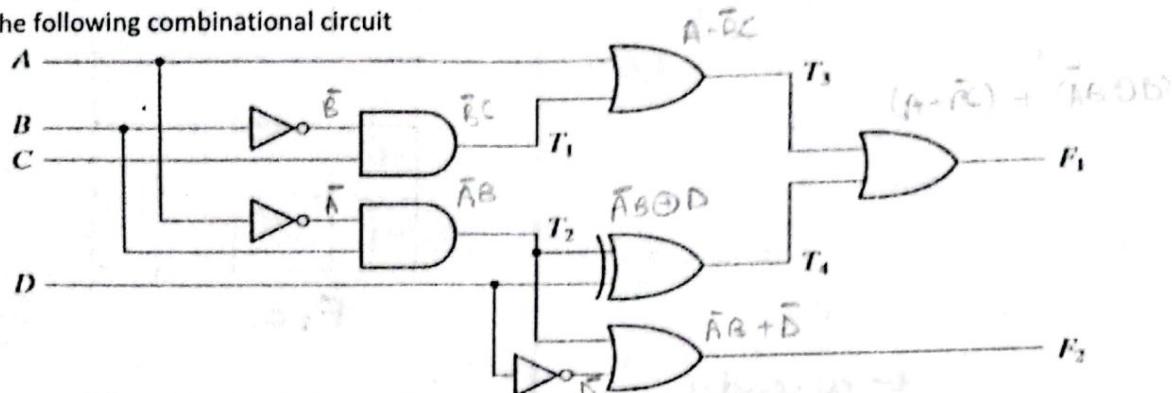
## ASSIGNMENT #3

ID: 231-0501

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SECTION: A

1. Consider the following combinational circuit



- Derive the Boolean expressions for the outputs  $F_1$  and  $F_2$  as a function of the four inputs.
- List the truth table with 16 binary combinations of the four input variables. Then list the binary values for  $T_1$  through  $T_4$  and outputs  $F_1$  and  $F_2$  in the table.
- Simplify Boolean expressions of  $F_1$  and  $F_2$  using Boolean algebra and K-maps.
- List the truth table for simplified expression  $F_1$  and  $F_2$  and compare both truth tables

EXPRESSIONS

$$F_1 = (\bar{A} + \bar{B} \cdot C) + ((\bar{A} \cdot B) \oplus D), \quad T_1 = \bar{B} \cdot C, \quad T_3 = A + \bar{B} \cdot C$$

$$F_2 = \bar{A}B + \bar{D}, \quad T_2 = \bar{A} \cdot B, \quad T_4 = \bar{A}B \oplus D$$

TRUTH TABLE

	A	B	C	D	$T_1$	$T_2$	$T_3$	$T_4$	$F_1$	$F_2$
0	0	0	0	0	0	0	0	0	0	1
1	0	0	0	1	0	0	0	1	1	0
2	0	0	1	0	1	0	1	1	1	0
3	0	0	1	1	1	0	1	0	1	1
4	0	1	0	0	0	1	0	1	1	0
5	0	1	0	1	0	1	0	1	1	1
6	0	1	1	0	0	1	0	0	0	1
7	0	1	1	1	0	1	0	1	1	1
8	1	0	0	0	0	0	0	0	0	1
9	1	0	0	1	0	0	0	0	0	1
10	1	0	1	0	1	0	1	1	1	0
11	1	0	1	1	1	0	1	0	1	1
12	1	1	0	0	0	0	0	1	1	0
13	1	1	0	1	0	0	1	0	1	1
14	1	1	1	0	0	0	1	1	1	0
15	1	1	1	1	0	0	1	1	1	1

**ASSIGNMENT # 3 [EE-227]**

**SIMPLIFICATION OF EXPRESSIONS:**

$$F_1 = A + \bar{B}C + (\bar{A}B \oplus D)$$

$$= A + \bar{B}C + \bar{A}\bar{B}\bar{D} + \bar{A}\bar{B}D$$

$$= A + \bar{B}C + \bar{A}\bar{B}\bar{D} + (A + \bar{B})D$$

$$= A + B\bar{D} + \bar{B}C + AD + \bar{B}D$$

$$= A + AD + B\bar{D} + \bar{B}C + \bar{B}D$$

$$= A(1+D) + B\bar{D} + \bar{B}D + \bar{B}C$$

$$F_1 = A + (B \oplus D) + \bar{B}C$$

$$F_2 = \bar{A}B + \bar{D}$$

← already  
in  
simplified  
form

AB	CD	00	01	11	10
00		1	1	1	
01		1			1
11		1	1	1	1
10		1	1	1	1

$$F_1 = A + CD' + B'D + BD'$$

AB	CD	00	01	11	10
00		1			1
01		1	1	1	1
11		1			1
10		1			1

$$F_2 = A'B + C'D' + CD'$$

TRUTH TABLE

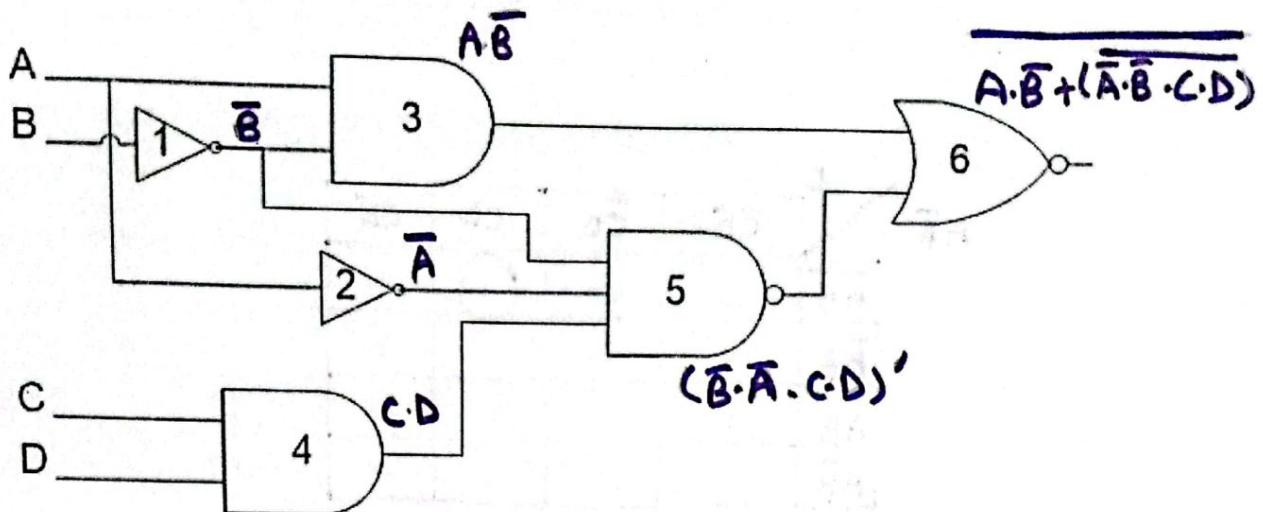
	A	B	C	D	F1	F2		A	B	C	D	F1	F2
0	0	0	0	0	0	1	8	1	0	0	0	1	1
1	0	0	0	1	1	0	9	1	0	0	1	1	0
2	0	0	1	0	1	1	10	1	0	1	0	1	1
3	0	0	1	1	1	0	11	1	0	1	1	1	0
4	0	1	0	0	1	1	12	1	1	0	0	1	1
5	0	1	0	1	0	1	13	1	1	0	1	1	0
6	0	1	1	0	1	1	14	1	1	1	0	1	1
7	0	1	1	1	0	1	15	1	1	1	1	1	0

COMPARE RESULTS:

By comparing both the truth tables, we can see that output remains same and simplified expression doesn't change the output.

**ASSIGNMENT # 3 [EE-227]**

2. Consider the following combinational circuit



- Derive the Boolean expressions for the output  $F_1$  as a function of the four inputs.
- List the truth table with 16 binary combinations of the four input variables. Then list the binary values output  $F_1$  in the table.
- Simplify Boolean expressions of  $F_1$  using Boolean algebra and K-maps,
- List the truth table for simplified expression  $F_1$  and compare both truth tables.

EXPRESSION

$$F_1 = \overline{(A \cdot \bar{B})} + (\overline{\bar{A} \cdot \bar{B}} \cdot (\bar{C} \cdot \bar{D}))$$

$$\begin{aligned} \text{Simplification: } &= (A \cdot B')' \cdot ((A' \cdot B' \cdot C \cdot D)')' \\ &= (\bar{A} + \bar{B}) \cdot (\bar{A}' \cdot \bar{B}' \cdot C \cdot D) \\ &= (\bar{A} + \bar{B}) \cdot (\bar{A} \bar{B} \bar{C} \bar{D}) = \bar{A} \bar{B} \bar{C} \bar{D} + \bar{B} \bar{A} \bar{B} \bar{C} \bar{D} = \bar{A} \bar{B} \bar{C} \bar{D} + 0 = \bar{A} \bar{B} \bar{C} \bar{D} \end{aligned}$$

TRUTH TABLE

	A	B	C	D	$F_1$	$F_1$		A	B	C	D	$F_1$	$F_1$
0	0	0	0	0	0	0	8	1	0	0	0	0	0
1	0	0	0	1	0	0	9	1	0	0	1	0	0
2	0	0	1	0	0	0	10	1	0	1	0	0	0
3	0	0	1	1	1	1	11	1	0	1	1	0	0
4	0	1	0	0	0	0	12	1	1	0	0	0	0
5	0	1	0	1	0	0	13	1	1	0	1	0	0
6	0	1	1	0	0	0	14	1	1	1	0	0	0
7	0	1	1	1	0	0	15	1	1	1	1	0	0

## SIMPLIFICATION OF EXPRESSION:

ASSIGNMENT

$AB \backslash CD$	$\bar{C}B$	$\bar{C}D$	$CD$	$C\bar{B}$
$\bar{A}B$	0	0	1	0
$\bar{A}B$	0	0	0	0
$A\bar{B}$	0	0	0	0
$A\bar{B}$	0	0	0	0

From K-Map :-  $F_1 = \bar{A}\bar{B}CD$

TRUTH TABLE

	A	B	C	D	$\bar{A}$	$\bar{B}$	$\bar{C}$	$\bar{D}$	$F_1$
0	0	0	0	0	1	1	1	1	0
1	0	0	0	1	1	1	1	0	0
2	0	0	1	0	1	1	0	1	0
3	0	0	1	1	1	1	0	1	0
4	0	1	0	0	1	0	1	0	0
5	0	1	0	1	1	0	1	0	1
6	0	1	1	0	1	0	1	1	0
7	0	1	1	1	1	0	1	1	0

COMPARE RESULTS:

Comparing both truth tables gives the same answers as simplifying an expression has no effect on output.

$\rightarrow$  K-Map

$\rightarrow$  K-Map

**ASSIGNMENT # 3 [EE-227]**

3. Design a combinational circuit that converts a three-bit Binary number to a 3-bit Gray code.  
 NOTE: Implement the circuit with exclusive-OR gates.

TABLE

$B_2$	$B_1$	$B_0$	GRAY CODE		
BINARY			$G_2$	$G_1$	$G_0$
0	A	B	0	0	0
0	0	0	0	0	0
1	0	0	0	0	1
2	0	1	0	1	1
3	0	1	0	1	0
4	1	0	1	1	0
5	1	0	1	1	1
6	1	1	0	0	0
7	1	1	1	0	0

SIMPLIFICATION:

For  $G_2$ :

$BC$	$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$A$	0	0	0	0
$\bar{A}$	1	1	1	1
$A$	1	1	1	1

$= A$

For  $G_1$ :

$BC$	$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$A$	0	0	1	1
$\bar{A}$	1	1	0	0
$A$	1	1	0	0

$= A\bar{B} + \bar{A}B$   
 $= A \oplus B$

For  $G_0$ :

$BC$	$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$A$	0	0	0	0
$\bar{A}$	1	0	1	0
$A$	0	1	0	1

$= B\bar{C} + \bar{B}C$   
 $= B \oplus C$

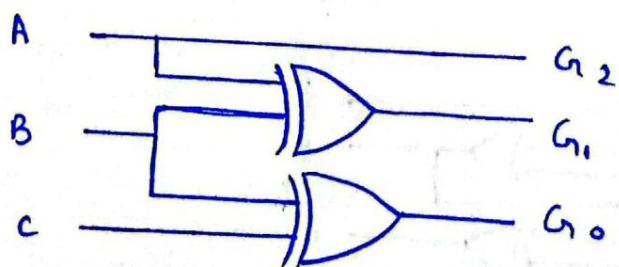
EXPRESSIONS:

$$G_2 = \sum (4, 5, 6, 7) = A$$

$$G_1 = \sum (2, 3, 4, 5) = A \oplus B$$

$$G_0 = \sum (1, 2, 5, 6) = B \oplus C$$

Circuit:



- ASSIGNMENT # 3 [EE-227]**
4. Design a combinational circuit that converts a 3-bit Gray code to a three-bit Binary number.  
**NOTE:** Implement the circuit with exclusive-OR gates.

TABLE

	GRAY CODE			A	B	C
	G2	G1	G0			
0	0	0	0	0	0	0
1	0	0	1	0	0	1
2	0	1	1	0	1	0
3	0	1	0	1	0	1
4	1	1	1	1	1	0
5	1	1	0	1	0	1
6	1	0	1	1	1	0
7	1	0	0	1	1	1

SIMPLIFICATION:

For  $B_2$ :

A	$B\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	0	0	0	0
A	1	1	1	1

$$A = G_2$$

For  $B_1$ :

A	$B\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	0	0	1	1
A	1	1	0	0

$$B = G_0 \oplus G_1$$

For  $B_0$ :

A	$B\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	0	1	0	1
A	1	0	1	0

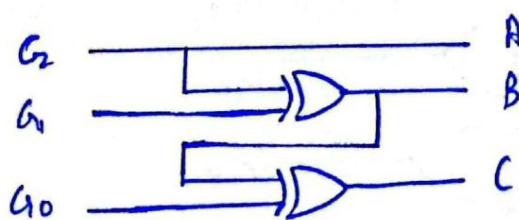
$$C = G_2 \oplus (G_0 \oplus G_1)$$

EXPRESSIONS:

$$A = B_2 = G_2$$

$$B = B_1 = G_0 \oplus G_1$$

$$C = B_0 = G_2 \oplus G_0 \oplus G_1$$



**ASSIGNMENT # 3 [EE-227]**

5. Design a combinational circuit that converts a bit four binary number to a four-bit Gray code.

	$B_3$	$B_2$	$B_1$	$B_0$	BINARY	GRAY (4-bit)			
	A	B	C	D	G3	G2	G1	G0	
0	0	0	0	0	0	0	0	0	
1	0	0	0	1	0	0	0	1	
2	0	0	1	0	0	0	1	1	
3	0	0	1	1	0	0	1	0	
4	0	1	0	0	0	-	1	0	
5	0	1	0	1	0	-	1	1	
6	0	1	1	0	0	-	0	1	
7	0	1	1	1	0	-	0	0	
8	1	0	0	0	1	-	0	1	
9	1	0	0	1	1	-	0	1	
10	1	0	1	0	1	-	1	0	
11	1	0	1	1	1	-	0	0	
12	1	1	0	0	0	-	1	1	
13	1	1	0	1	0	-	0	1	
14	1	1	1	0	1	0	0	0	
15	1	1	1	1	1	0	0	0	

SIMPLIFICATION:

For  $G_3$ :

	AB	CD	00	01	11	10
00	00	00	0	0	-	0
01	01	00	0	0	0	0
11	11	11	1	1	1	1
10	10	10	1	1	1	1

$$= A$$

For  $G_2$ :

	AB	CD	00	01	11	10
00	00	00	0	0	0	0
01	01	11	1	1	1	1
11	11	00	0	0	0	0
10	10	11	1	1	1	1

$$= \bar{A}B + A\bar{B}$$

$$= A \oplus B$$

For  $G_1$ :

	AB	CD	00	01	11	10
00	00	00	0	0	1	1
01	01	11	1	1	0	0
11	11	11	1	1	0	0
10	10	00	0	0	1	1

$$= \bar{B}C + BC$$

$$= B \oplus C$$

For  $G_0$ :

	AB	CD	00	01	11	10
00	00	00	0	1	0	1
01	01	11	0	1	0	1
11	11	11	0	1	0	1
10	10	00	1	0	0	1

$$= \bar{C}D + CD$$

$$= C \oplus D$$

EXPRESSIONS:

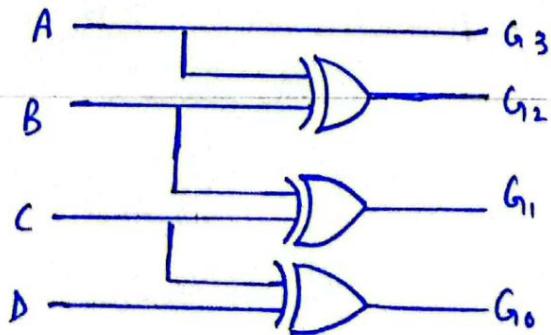
$$G_3 = B_3 = A$$

$$G_2 = B_2 \oplus B_3 = A \oplus B$$

$$G_1 = B_1 \oplus B_2 = B \oplus C$$

$$G_0 = B_1 \oplus B_0 = C \oplus D$$

Circuit:-



**ASSIGNMENT # 3 [EE-227]**

6. Design a combinational circuit that converts a BCD to an 8,4,-2,-1 code.

BCD CODE				w	x	y	z
				8	4	-2	-1
0	0	0	0	0	0	0	0
1	0	0	0	1	0	1	1
2	0	0	1	0	0	1	0
3	0	0	1	1	0	0	0
4	0	1	0	0	0	1	1
5	0	1	0	1	0	1	0
6	0	1	1	0	0	0	1
7	0	1	1	1	0	0	0
8	1	0	0	0	1	1	1
9	1	0	0	1	1	0	1
10	1	0	1	0	0	0	0
11	1	0	1	1	0	1	1
12	1	1	0	0	0	0	0
13	1	1	0	1	1	1	0
14	1	1	1	0	1	0	1
15	1	1	1	1	1	1	0

-2

SIMPLIFICATION:

AB	CD	00	01	11	10
00	00	1			1
01	01	1			1
11	X	X	X	X	X
10	1	X	X	X	X

AB	CD	00	01	11	10
00	00	1	1	1	1
01	01	1			
11	X	X	X	X	X
10	1	X	X	X	X

AB	CD	00	01	11	10
00	00				
01	01	1	1	1	1
11	X	X	X	X	X
10	1	1	X	X	X

AB	CD	00	01	11	10
00	00	1	1	1	1
01	01	1	1	1	1
11	X	X	X	X	X
10	1	1	X	X	X

$$\begin{aligned} y &= \bar{C}D + C\bar{D} \\ &= C \oplus D \end{aligned}$$

$$x = B\bar{C}\bar{D} + \bar{B}D + \bar{B}C$$

$$w = A + BD + BC$$

$$z = D$$

EXPRESSIONS:

$$8: A + BD + BC$$

$$4: B\bar{C}\bar{D} + \bar{B}D + \bar{B}C$$

$$-2: \bar{C}D + C\bar{D} = C \oplus D$$

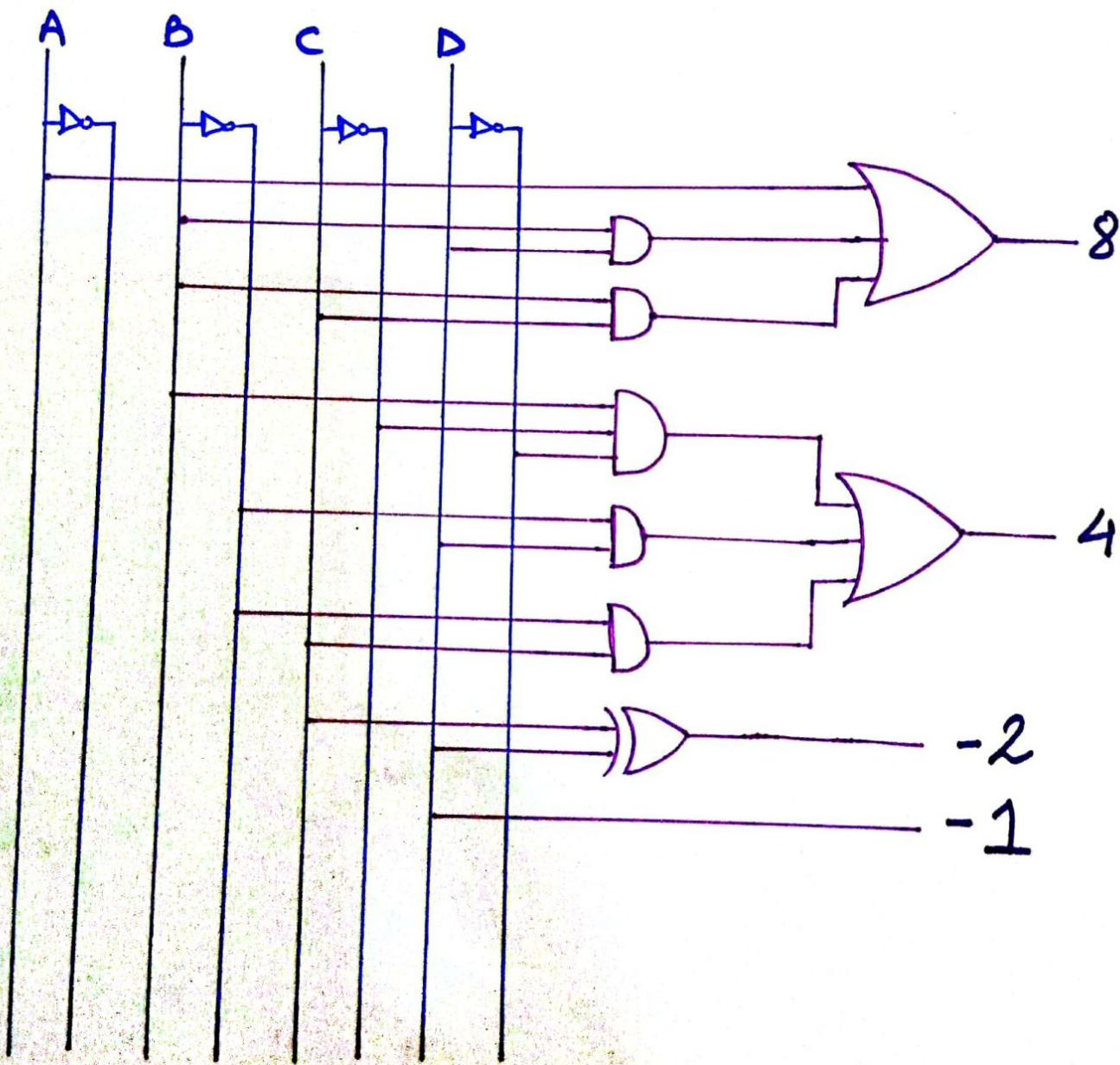
$$-1: D$$

**ASSIGNMENT # 3 [EE-227]**

Design

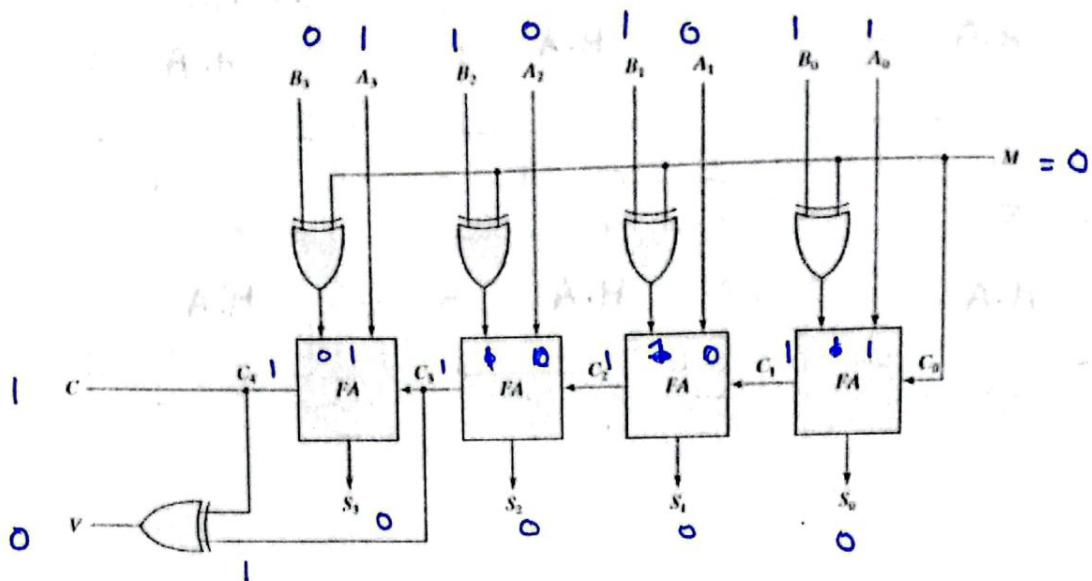
6. Design a combinational circuit that converts a BCD to an 8.4. -2. -1 code.

①  
Circuit :



**ASSIGNMENT # 3 [EE-227]**

9. Perform unsigned Addition A+B where A= 9 and B= 7 using Following is 4-adder/subtractor circuit? Also write short note on working of C and V bits for signed and unsigned addition/subtraction



$$A = 9 = 1001$$

$$B = 7 = 0111$$

$$A+B = 10000 = 16$$

There are cases:

if  $V = C_4 \oplus C_3 = 1 \oplus 1 = 0$  then it means addition has been performed

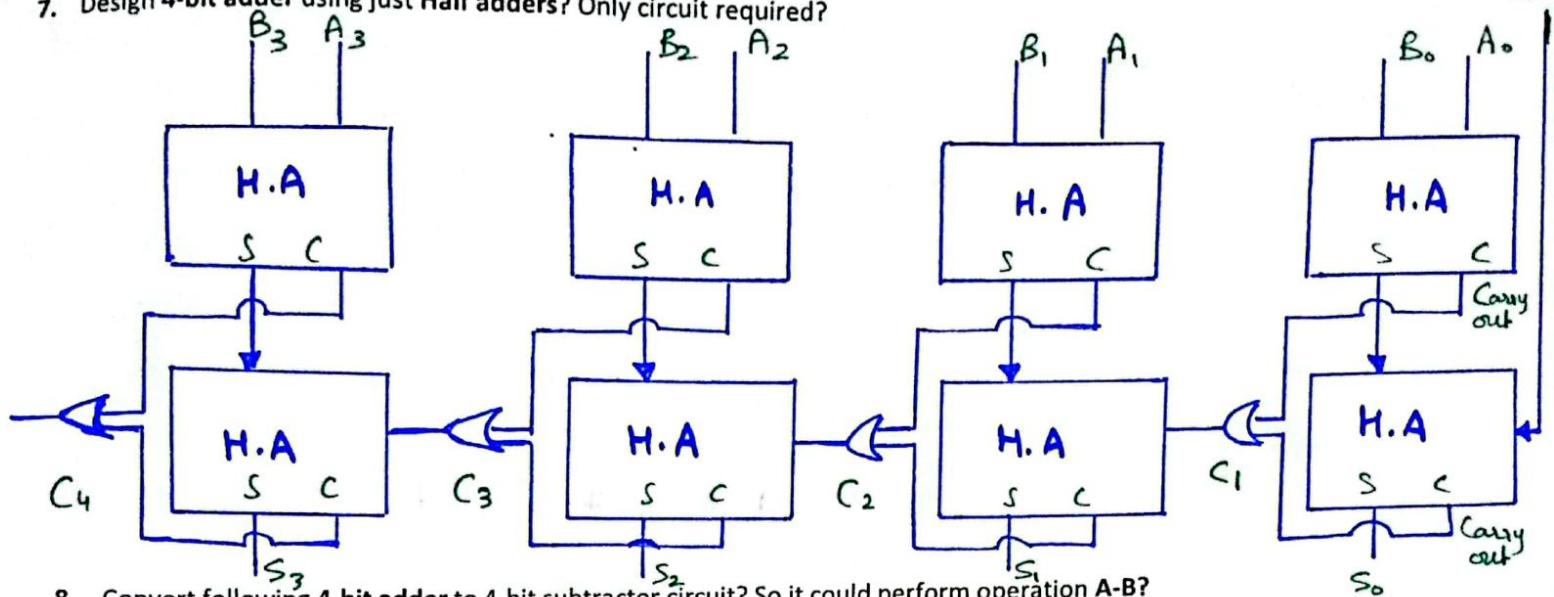
if '0' is carried in '1' carried out in most significant bit means addition of negative numbers has been performed. The result will be non-negative.

$$V = 1 \oplus 0 = 1$$

if '1' is carried in '0' carried out in most significant bit means addition of two non-negative numbers and getting  $V = 0 \oplus 0 = 1$  a negative result.

**ASSIGNMENT # 3 [EE-227]**

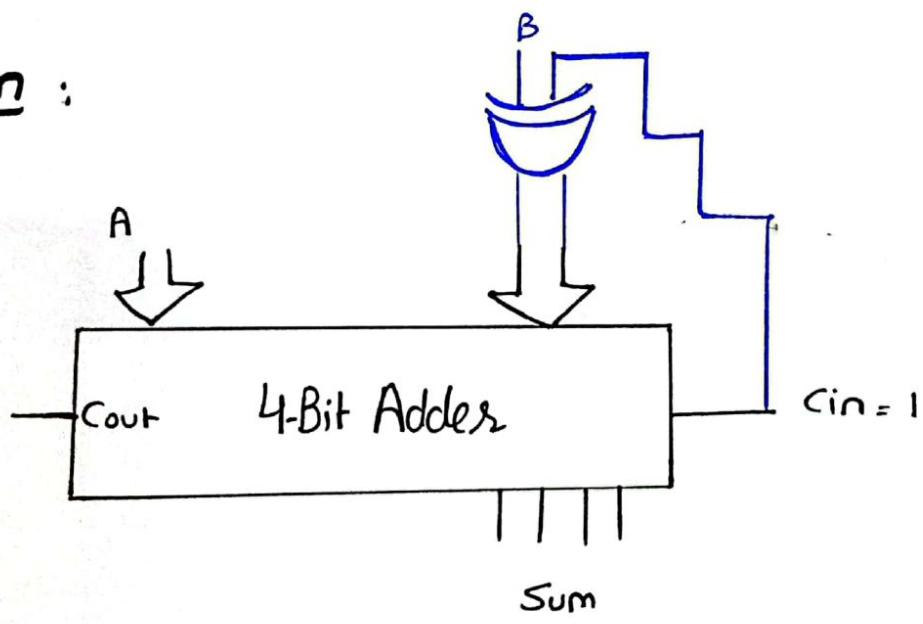
7. Design 4-bit adder using just Half adders? Only circuit required?



8. Convert following 4-bit adder to 4-bit subtractor circuit? So it could perform operation A-B?

Note: B could be represented in 2's complement

Solution :



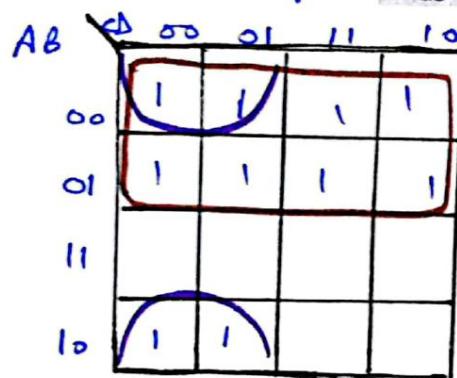
$$\begin{aligned} B \oplus 1 &= B' \\ + \text{Cin} = 1 &= 2^{\text{S}} \\ \text{Comp.} \end{aligned}$$

### ASSIGNMENT # 3 [EE-227]

10. Design Circuit that accepts 4-bit BCD number as input and Detects BCD is valid/invalid?

A	B	C	D	F	A	B	C	D	E
0	0	0	0	1	8	1	0	0	0
1	0	0	1	1	9	1	0	0	1
2	0	0	1	0	10	1	0	1	0
3	0	0	1	1	11	1	0	1	1
4	0	1	0	0	12	1	1	0	0
5	0	1	0	1	13	1	1	0	1
6	0	1	1	0	14	1	1	1	0
7	0	1	1	1	15	1	1	1	1

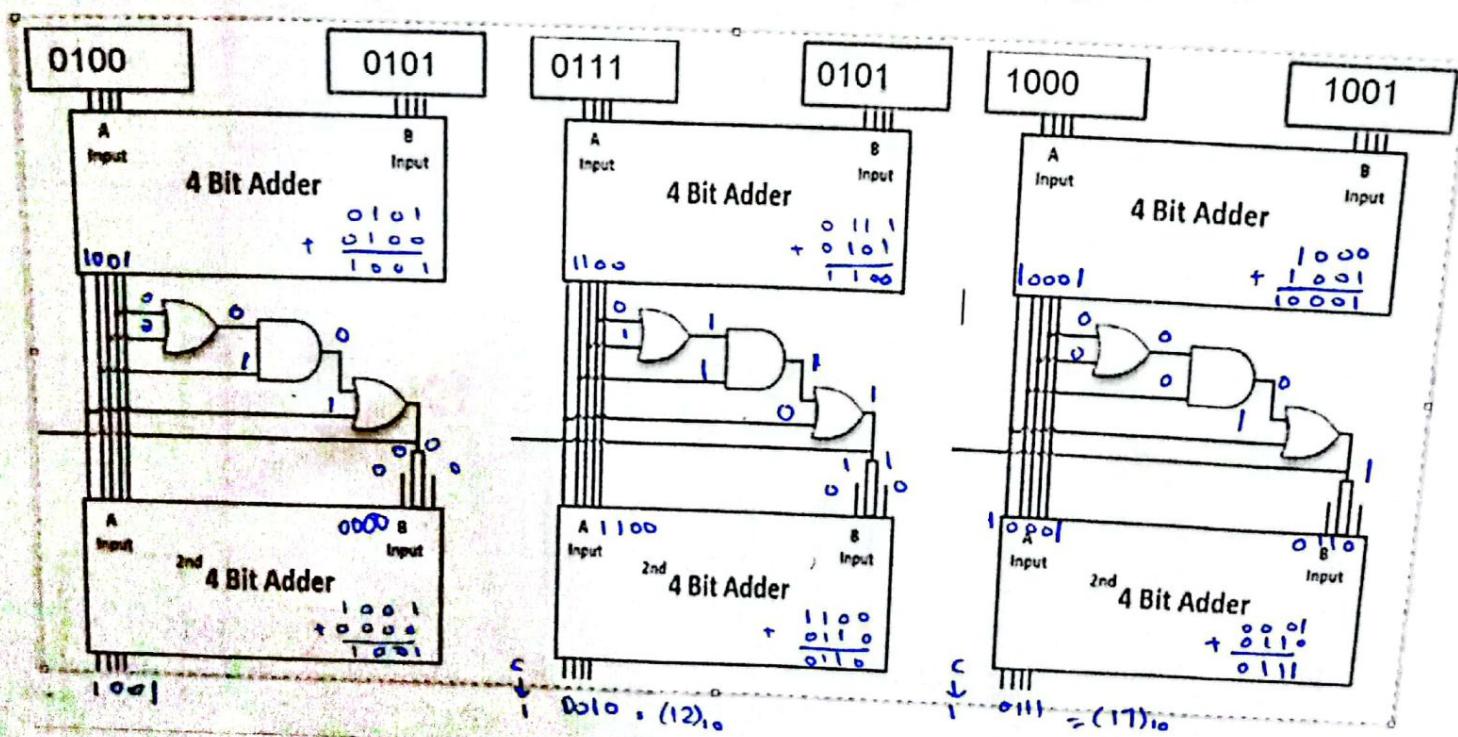
SIMPLIFICATION:



EXPRESSIONS:

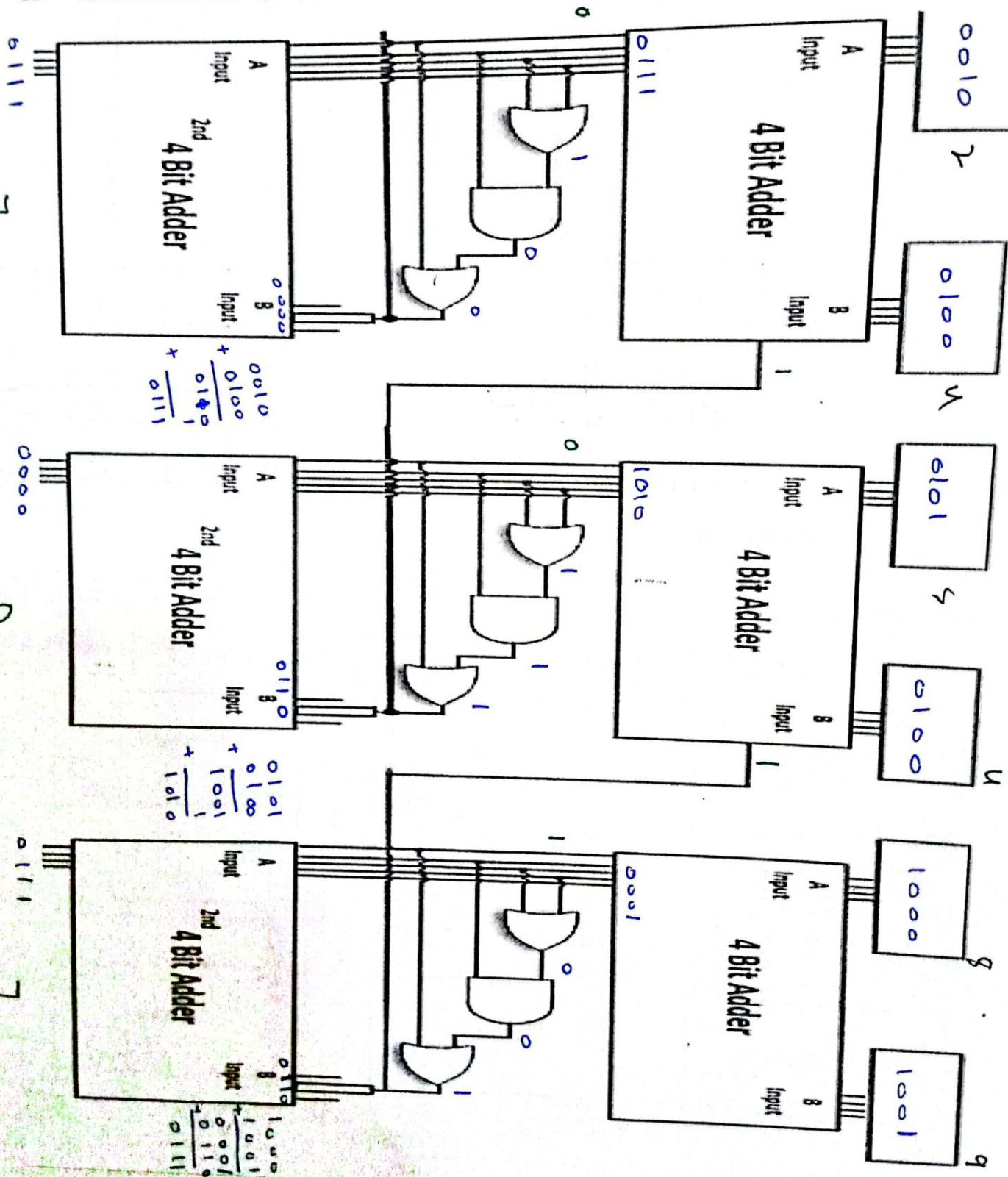
$$A' + B'C'$$

11. Perform BCD Addition using following circuit? BCD numbers are given in boxes on top?



**ASSIGNMENT # 3 [EE-227]**

12. Perform BCD addition  $(258)_{BCD} + (449)_{BCD}$  using following circuit?

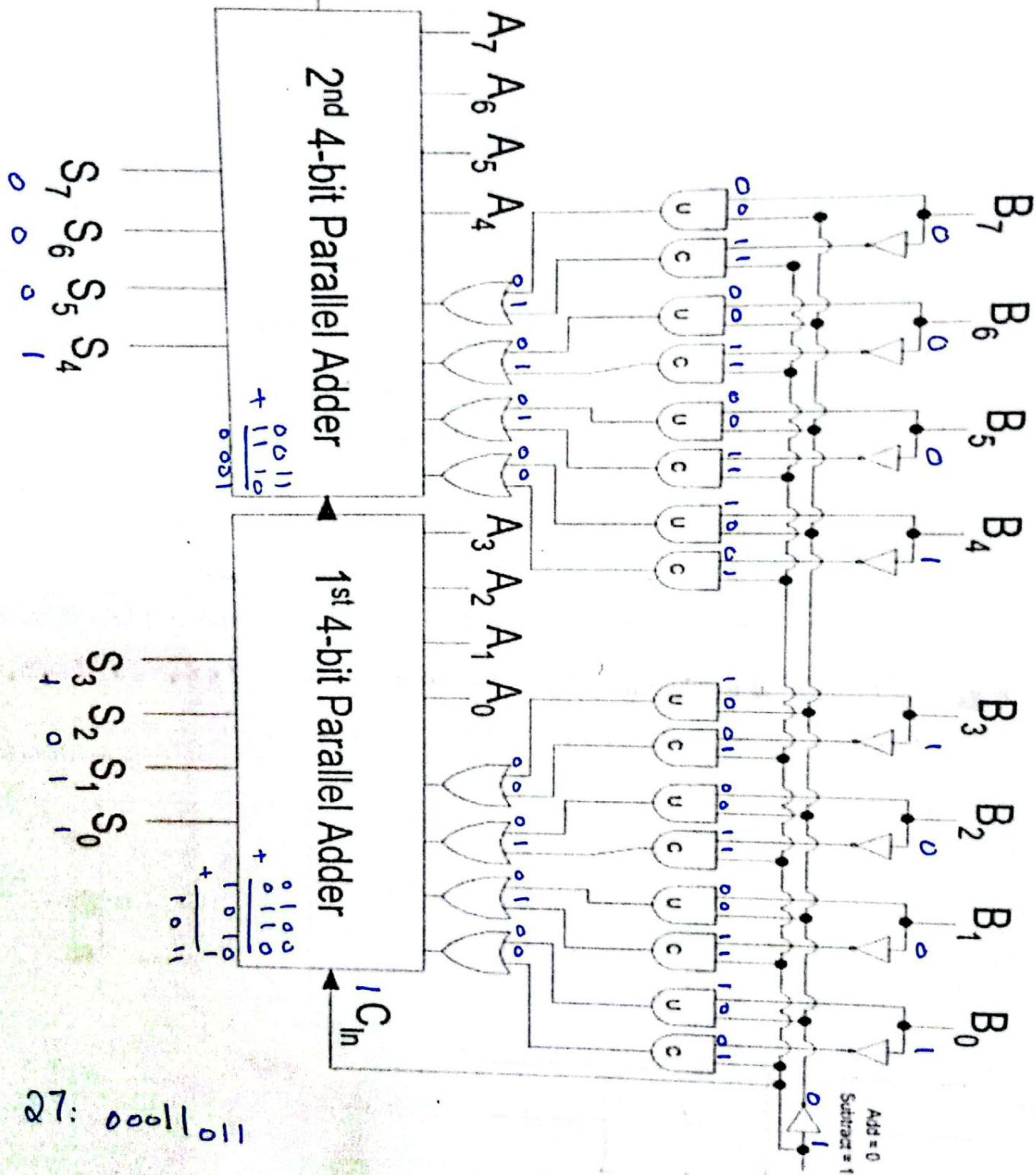


**ASSIGNMENT # 3 [EE-227]**

13. Implement the binary arithmetic operation (A-B), using the following 8-bit addition/Subtraction circuit?

$$A = (52)_{10} = (?)_2$$

$$\begin{array}{r} 00110100 \\ \text{discarded in case of subtraction} \\ \text{B} = (25)_{10} = (?)_2 \\ 00011001 \end{array}$$



$$27: 00011011$$

### ASSIGNMENT # 3 [EE-227]

14. Design a single bit comparator from the following table? Write expression for  $A=B$ ,  $A < B$  and  $A > B$ ? Design circuit from expression using logic gates?

TABLE:

INPUT		OUTPUT		
A	B	$A > B$	$A = B$	$A < B$
0	0	0	1	0
0	1	0	0	1
1	0	1	0	0
1	1	0	1	0

EXPRESSIONS

$$F_{A=B} =$$

$$AB + \bar{A}\bar{B} = \overline{A \oplus B}$$

$$\begin{array}{c} A \\ B \end{array} \rightarrow D \rightarrow A = B$$

$$F_{A > B} =$$

$$A\bar{B}$$

$$\begin{array}{c} A \\ B \end{array} \rightarrow D \rightarrow A > B$$

$$F_{A < B} =$$

$$\bar{A}B$$

$$\begin{array}{c} A \\ B \end{array} \rightarrow D \rightarrow A < B$$

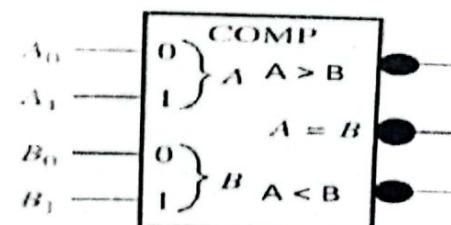
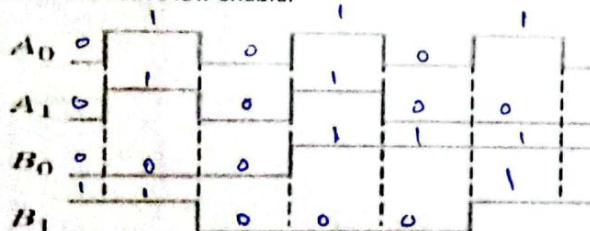
15. Write expression for 5-bit comparator? (Use section 4.6(Morris Mono) to design 5-bit comparator)

$$A = B = (A_5 \oplus B_5)' \cdot (A_4 \oplus B_4)' \cdot (A_3 \oplus B_3)' \cdot (A_2 \oplus B_2)' \cdot (A_1 \oplus B_1)' \cdot (A_0 \oplus B_0)'$$

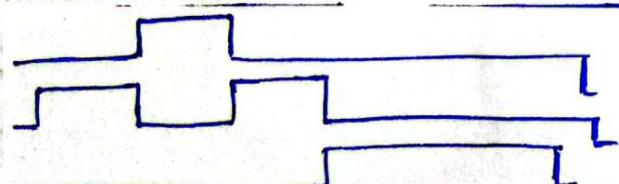
$$A > B = A_5 B_5' + x_5 A_4 B_4' + x_5 x_4 A_3 B_3' + x_5 x_4 x_3 A_2 B_2' + x_5 x_4 x_3 x_2 A_1 B_1' + x_5 x_4 x_3 x_2 x_1 A_0 B_0'$$

$$A < B = A_5' B_5 + x_5 A_4' B_4 + x_5 x_4 A_3' B_3 + x_5 x_4 x_3 A_2' B_2 + x_5 x_4 x_3 x_2 A_1' B_1 + x_5 x_4 x_3 x_2 x_1 A_0' B_0$$

16. Apply the Waveform give below to the comparator circuit. Determine the output waveforms of  $A = B$ ,  $A < B$ ,  $A > B$  which are active low enable.

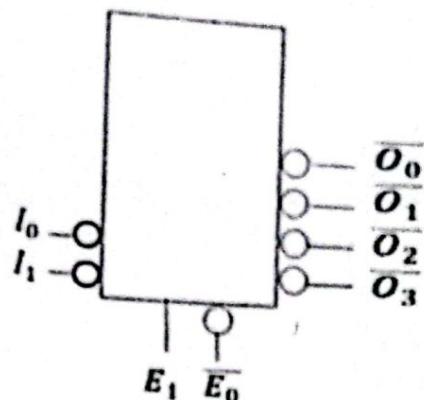


WAVEFORMS



**ASSIGNMENT # 3 [EE-227]**  
 17. Design following 2x4 Decoder? For reference see Section 4.9(figure 4.19)

BLOCK DIAGRAM



TABLE

		INPUT				OUTPUT			
$E_1$	$E_0$	$I_1$	$I_0$	$\bar{O}_0$	$\bar{O}_1$	$\bar{O}_2$	$\bar{O}_3$		
X	X	X	X	1	1	1	1		
0	X	X	X	1	1	1	1		
1	0	1	1	0	1	1	1		
1	0	1	0	1	0	1	1		
1	0	0	1	1	1	0	1		
1	0	0	0	1	1	1	0		

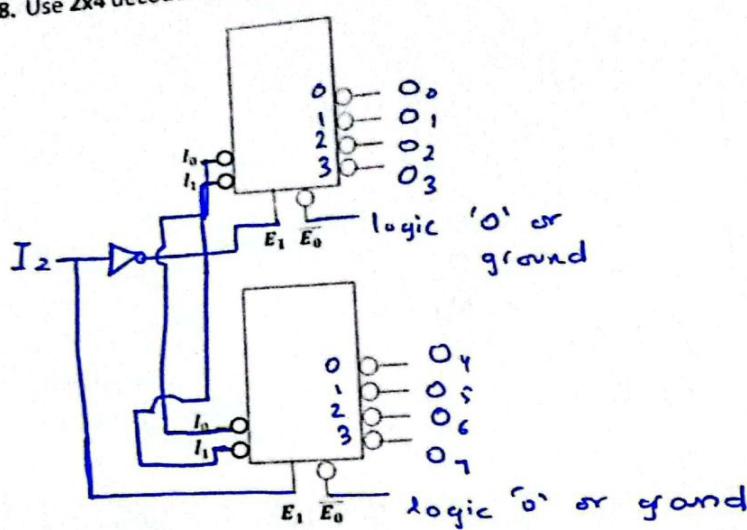
EXPRESSIONS:

$$\begin{aligned}
 \bar{O}_0 &= \overline{E_1} \overline{E_0} I_1 I_0 = \overline{E_1} + \overline{E_0} + \overline{I_1} + \overline{I_0} \\
 \bar{O}_1 &= \overline{E_1} \overline{E_0} \overline{I_1} \overline{I_0} = \overline{E_1} + \overline{E_0} + I_1 + I_0 \\
 \bar{O}_2 &= \overline{E_1} \overline{E_0} \overline{I_1} I_0 = \overline{E_1} + \overline{E_0} + I_1 + \overline{I_0} \\
 \bar{O}_3 &= \overline{E_1} \overline{E_0} I_1 \overline{I_0} = \overline{E_1} + \overline{E_0} + I_1 + I_0
 \end{aligned}$$



### ASSIGNMENT # 3 [EE-227]

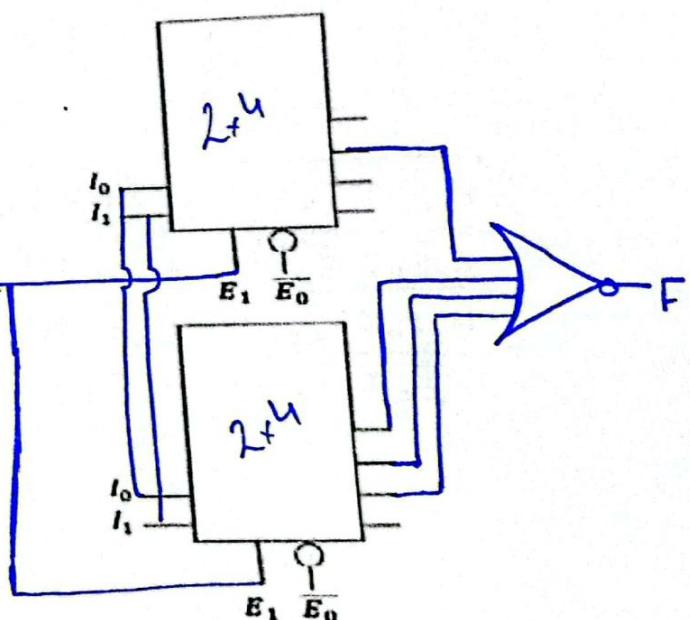
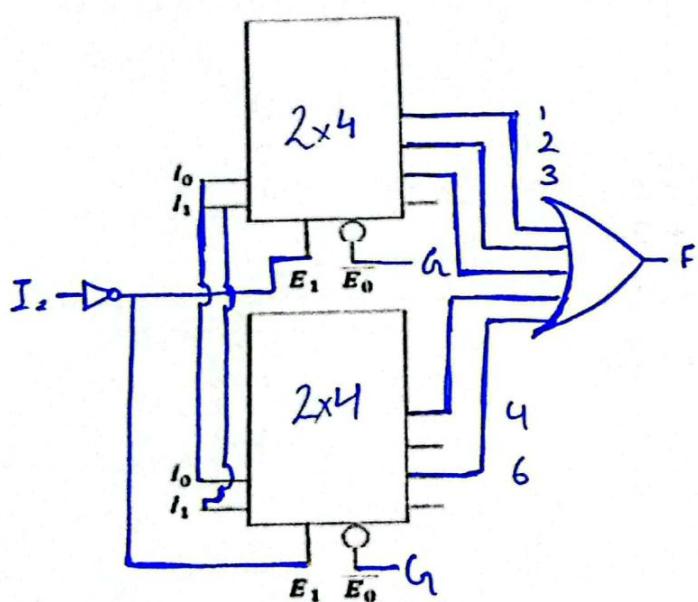
18. Use 2x4 decoder to design 3x8 decoder? Rename OUTPUTS and identify least and most decoder



19. Use following 2x4 decoders to implement given function

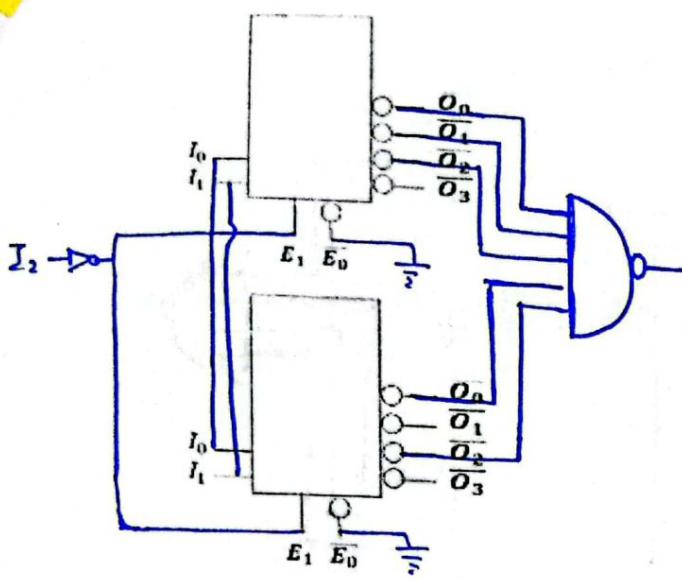
a.  $F(A, B, C) = \sum(0, 1, 2, 4, 6)$

b.  $F(A, B, C) = \prod(1, 4, 5, 6)$

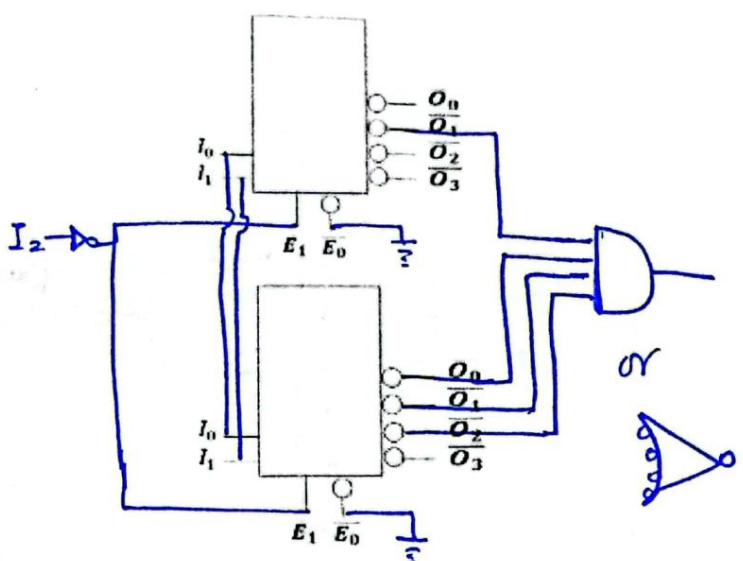


**ASSIGNMENT # 3 [EE-227]**

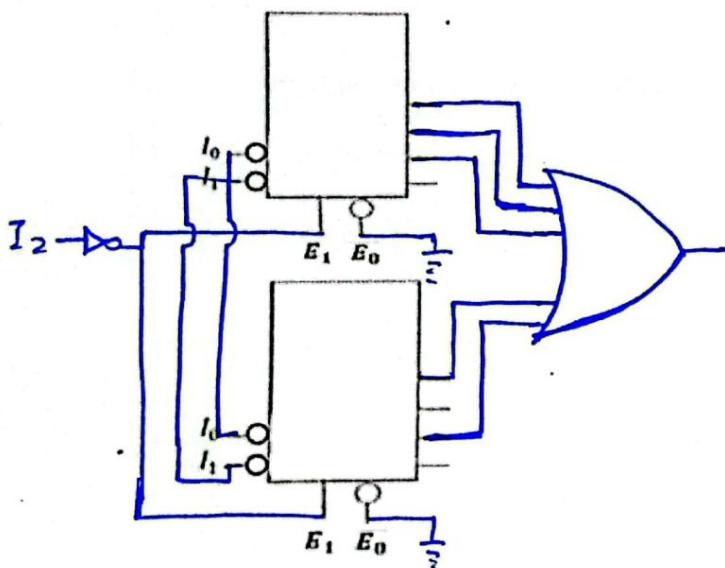
c.  $F(A, B, C) = \sum(0, 1, 2, 4, 6)$



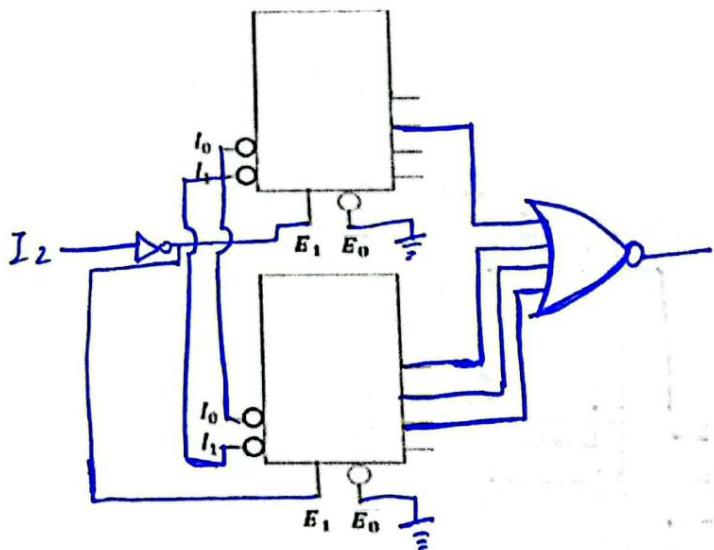
d.  $F(A, B, C) = \prod(1, 4, 5, 6)$



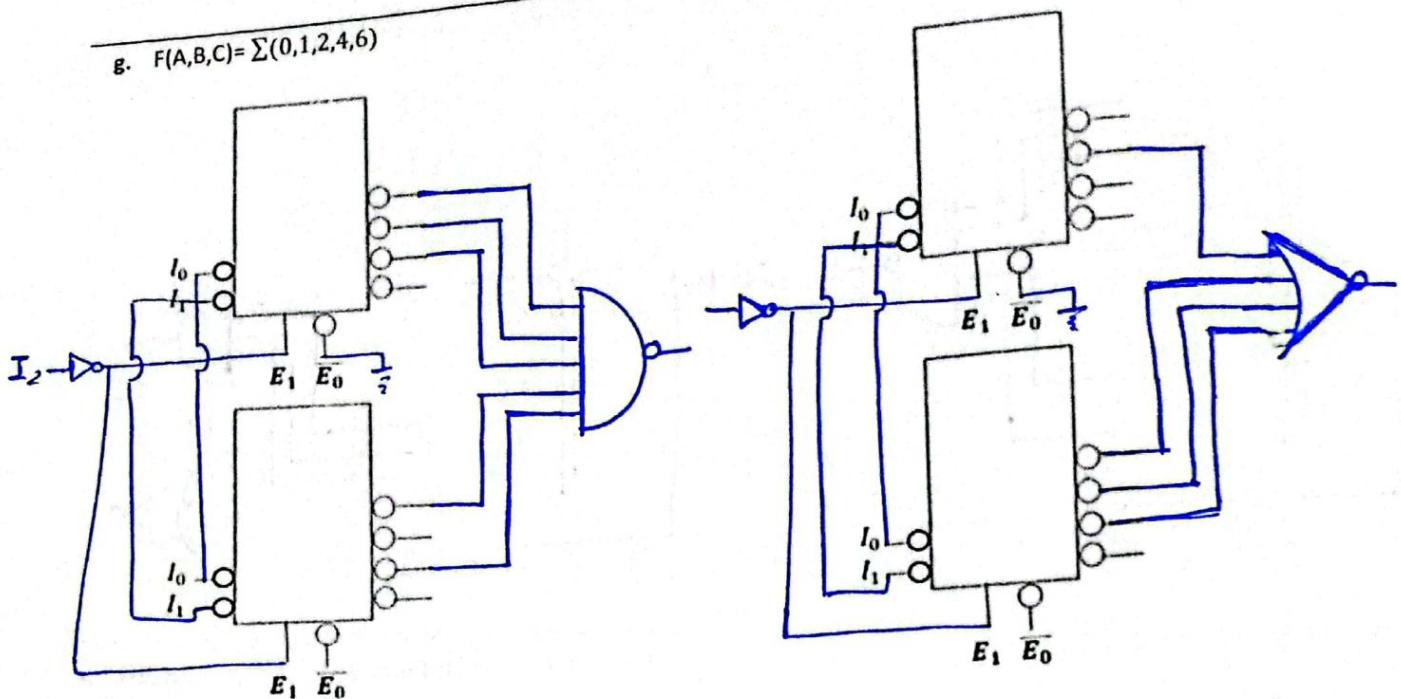
e.  $F(A, B, C) = \sum(0, 1, 2, 4, 6)$



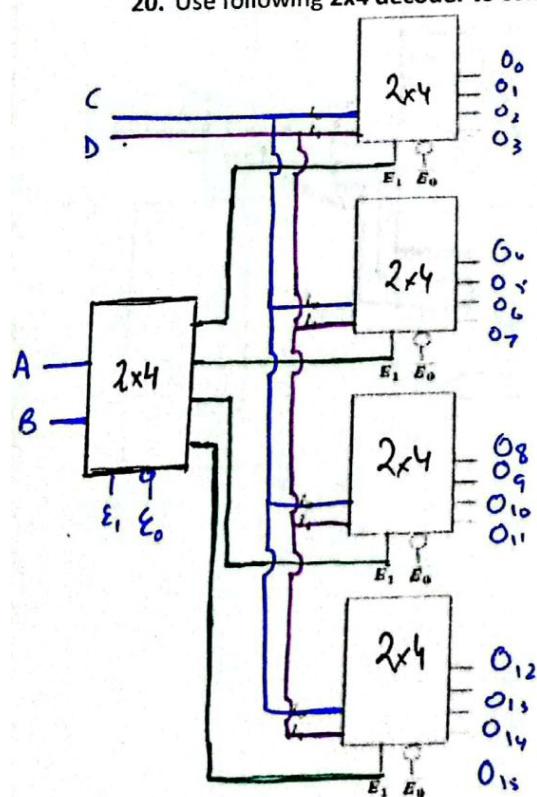
f.  $F(A, B, C) = \prod(1, 4, 5, 6)$



g.  $F(A, B, C) = \sum(0, 1, 2, 4, 6)$



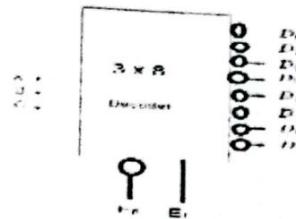
20. Use following  $2 \times 4$  decoder to construct  $4 \times 16$  decoder. You are not supposed to use any external gates?



**ASSIGNMENT # 3 [EE-227]**

21. Design following 3x8 Decoder? For reference see Section 4.9(figure 4.18, table 4.6)

**BLOCK DIAGRAM**



**TABLE**

INPUT				OUTPUT								
$\bar{E}_0$	$E_1$	A	B	C	$\bar{D}_0$	$\bar{D}_1$	$\bar{D}_2$	$\bar{D}_3$	$\bar{D}_4$	$\bar{D}_5$	$\bar{D}_6$	$\bar{D}_7$
1/0	0	X	X	X	1	1	1	1	1	1	1	1
1	0/1	X	X	X	1	1	1	1	1	1	1	1
0	1	0	0	0	0	1	1	1	1	1	1	1
0	1	0	0	1	1	0	1	1	1	1	1	1
0	1	0	1	0	1	1	0	1	1	1	1	1
0	1	0	1	1	1	1	1	0	1	1	1	1
0	1	1	0	0	1	1	1	1	0	1	1	1
0	1	1	0	1	1	1	1	1	1	0	1	1
0	1	1	1	0	1	1	1	1	1	1	0	1
0	1	1	1	1	1	1	1	1	1	1	1	0

**EXPRESSIONS**

$$\bar{D}_0 = (\bar{A}\bar{B}\bar{C})$$

$$\bar{D}_4 = \bar{A}\bar{B}\bar{C}$$

$$\bar{D}_1 = (\bar{A}\bar{B}C)$$

$$\bar{D}_5 = \bar{A}\bar{B}C$$

$$\bar{D}_2 = \bar{A}B\bar{C}$$

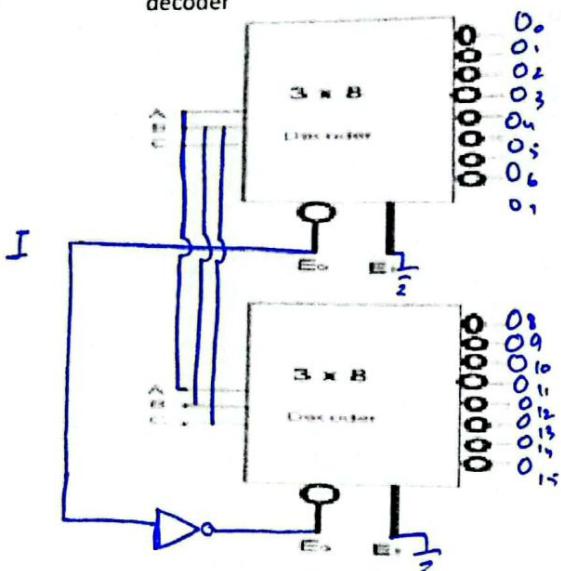
$$\bar{D}_6 = \bar{A}B\bar{C}$$

$$\bar{D}_3 = \bar{A}BC$$

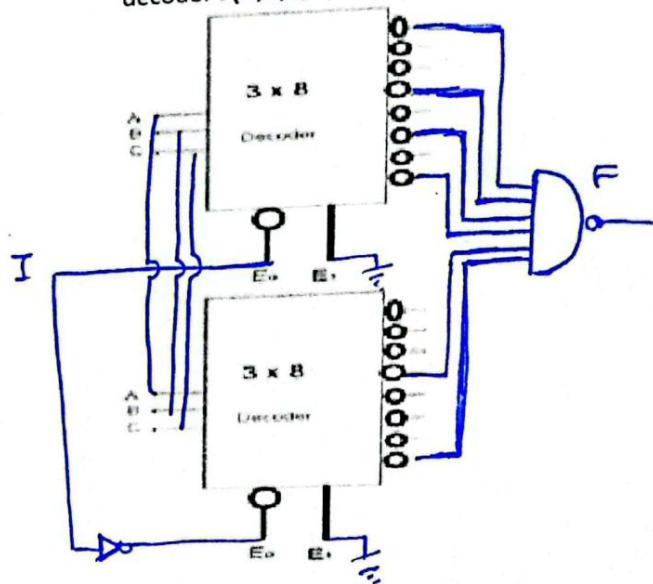
$$\bar{D}_7 = \bar{A}BC$$

### ASSIGNMENT # 3 [EE-227]

22. Use above designed  $3 \times 8$  decoder to design  $4 \times 16$  decoder



23. Implement following function using two  $3 \times 8$  decoder  $F(A, B, C, D) = \sum(0, 3, 5, 7, 11, 15)$



24. Design 4X2 Low Priority Encoder? For reference see section 4.10(table 4.8)

TABLE

INPUT				OUTPUT			Valid
D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	A	B		
0	0	0	0	X	X	0	0
1	X	X	X	0	0	1	1
0	1	X	X	0	1	1	1
0	0	1	X	1	0	1	1
0	0	0	1	1	1	1	1

SIMPLIFICATION AND EXPRESSIONS

$$A = \bar{D}_0 \bar{D}_1$$

$$B = \bar{D}_2 \bar{D}_0 + \bar{D}_0 D_1$$

$$B = \bar{D}_0 (D_1 + \bar{D}_2)$$

D <sub>2</sub> D <sub>3</sub>		00	01	11	10
D <sub>0</sub> D <sub>1</sub>		X	1	1	1
00		0	0	0	0
01		0	0	0	0
11		0	0	0	0
10		0	0	0	0

D <sub>2</sub> D <sub>3</sub>		00	01	11	10
D <sub>0</sub> D <sub>1</sub>		X	1	0	0
00		1	1	1	1
01		1	1	1	1
11		0	0	0	0
10		0	0	0	0

$$V = D_0 + D_1 + D_2 + D_3$$

### ASSIGNMENT # 3 [EE-227]

25. Design  $8 \times 3$  Low Priority Encoder? For reference see slides Lec\_17 uploaded on google classroom?

TABLE

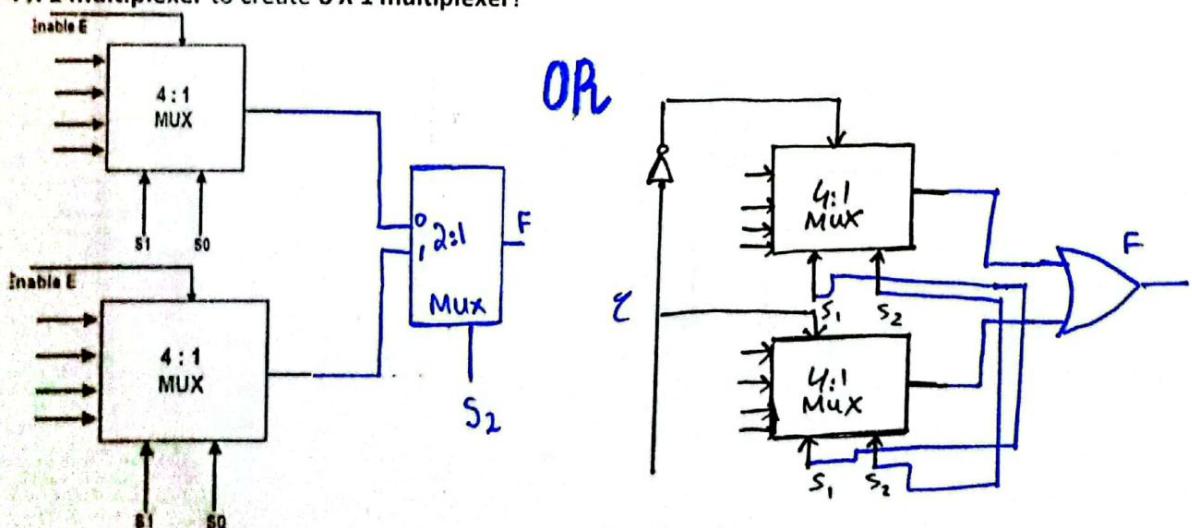
	INPUTS							OUTPUTS		
$I_0$	$I_1$	$I_2$	$I_3$	$I_4$	$I_5$	$I_6$	$I_7$	$O_0$	$O_1$	$O_2$
1	X	X	X	X	X	X	X	0	0	0
0	1	X	X	X	X	X	X	0	0	1
0	0	1	X	X	X	X	X	0	1	1
0	0	0	1	X	X	X	X	1	0	0
0	0	0	0	1	X	X	X	1	0	1
0	0	0	0	0	1	X	X	1	1	0
0	0	0	0	0	0	1	X	1	1	1

$$O_0 = I_0 \bar{I}_3 \bar{I}_4 \bar{I}_0 + I_1 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0 + I_2 \bar{I}_3 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0 + I_3 \bar{I}_6 \bar{I}_5 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0$$

$$O_1 = I_2 \bar{I}_1 \bar{I}_0 + I_3 \bar{I}_5 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0 + I_7 \bar{I}_6 \bar{I}_5 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0$$

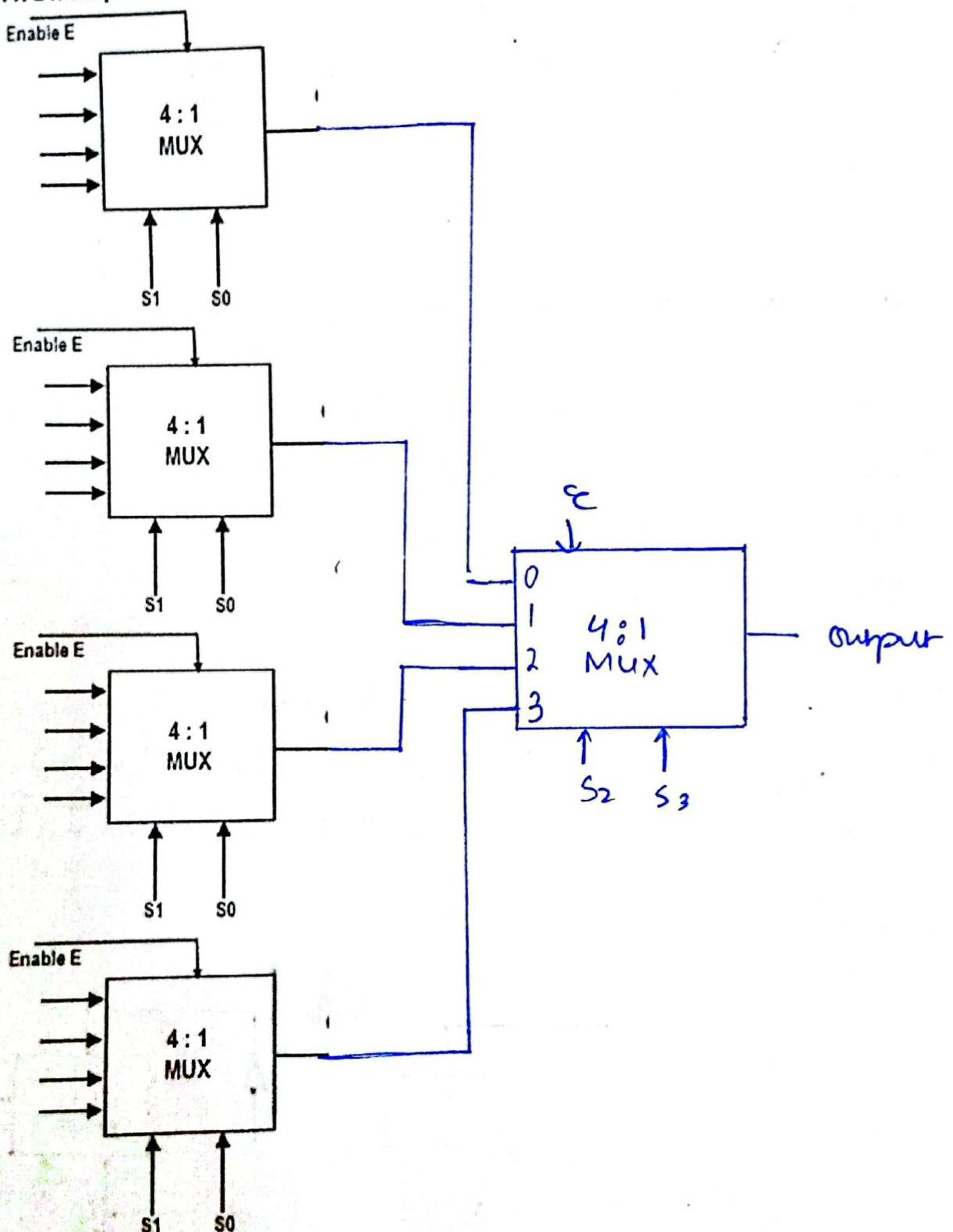
$$O_2 = I_1 \bar{I}_0 + I_2 \bar{I}_1 \bar{I}_0 + I_3 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0 + I_7 \bar{I}_6 \bar{I}_5 \bar{I}_4 \bar{I}_3 \bar{I}_1 \bar{I}_0$$

26. Use following  $4 \times 1$  multiplexer to create  $8 \times 1$  multiplexer?



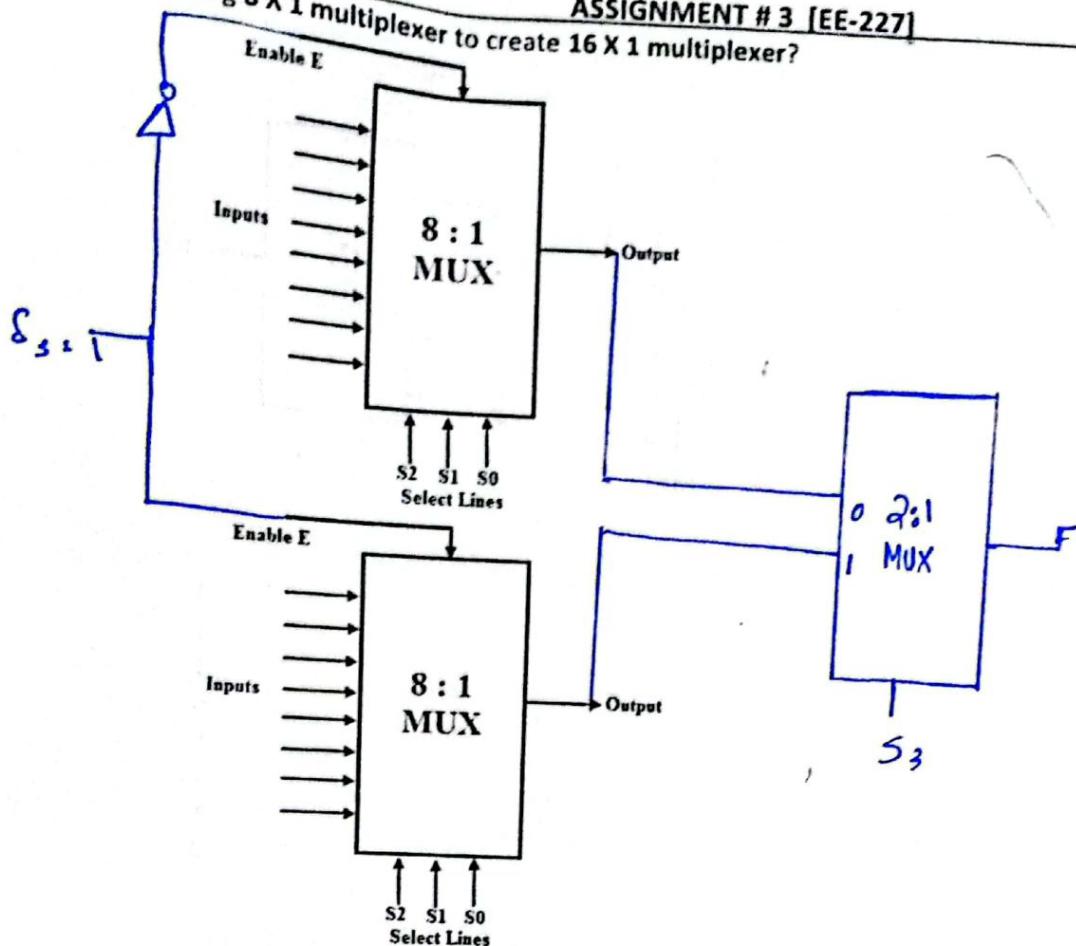
**ASSIGNMENT # 3 [EE-227]**

**27. Use following 4 X 1 multiplexer to create 16 X 1 multiplexer?**

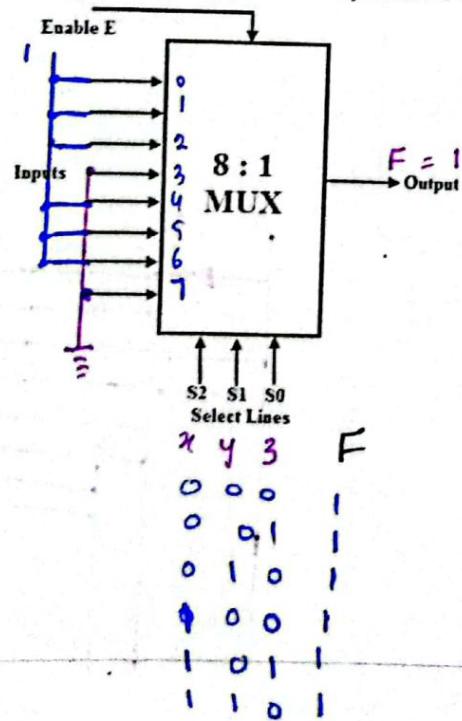


**ASSIGNMENT # 3 [EE-227]**

28. Use following  $8 \times 1$  multiplexer to create  $16 \times 1$  multiplexer?

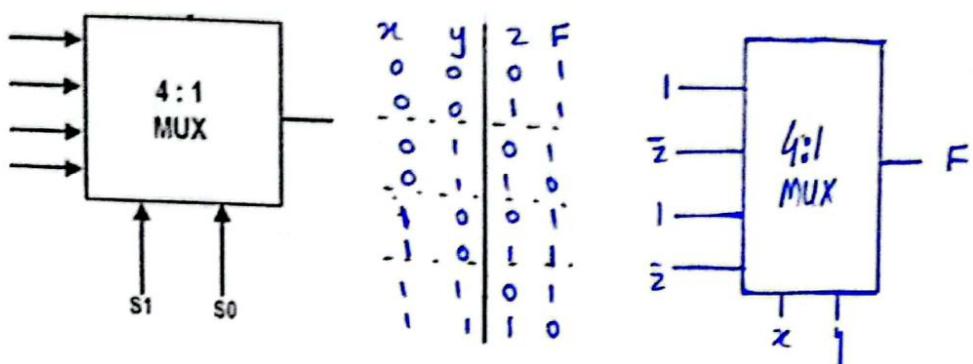


29. Implement given function using  $8 \times 1$  multiplexer?  $F(x, y, z) = \sum(0, 1, 2, 4, 5, 6)$



**ASSIGNMENT # 3 [EE-227]**

30. Implement given function using  $4 \times 1$  multiplexer?  $F(x, y, z) = \sum(0, 1, 2, 4, 5, 6)$



TABLE

x	y	z	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

31. Implement given function using  $8 \times 1$  multiplexer?  $F(w, x, y, z) = \sum(0, 2, 5, 7, 8, 10, 12, 13, 14, 15)$

