

Question 1 table (given) \Rightarrow

(a)

Experience (Year)	(\$1000) Salary
1.2	42
2.5	46
3.1	51
3.9	58
5.2	62

$$\text{We know } h_{\omega}(x) = \omega_0 + \omega_1 x$$

$$\text{Salary} = \beta_0 + \beta_1 \times \text{experience}$$

where x is experience

$\beta_0 = \omega_0$ (the intercept of line)

$\beta_1 = \omega_1$ (the slope of line)

$$h_{\omega}(x) = \text{Salary}$$

$$\bar{x} = \frac{1.2 + 2.5 + 3.1 + 3.9 + 5.2}{5} = 3.18$$

$$\bar{y} = \frac{42 + 46 + 51 + 58 + 62}{5} = 51.8$$

after that we will find

$x_i - \bar{x}$ & $y_i - \bar{y}$ (deviations)

$$\Rightarrow (x - \bar{x}) = (1.2 - 3.18), (2.5 - 3.18), (3.1 - 3.18), (3.9 - 3.18) \\ (5.2 - 3.18)$$

$$\Rightarrow = -1.98, -0.68, -0.08, 0.72, 2.02$$

$$\Rightarrow (y - \bar{y}) = (42 - 51.8), (46 - 51.8), (51 - 51.8), (58 - 51.8), (62 - 51.8)$$

$$\Rightarrow = -9.8, -5.8, -0.8, 6.2, 10.2$$

Product of deviations $(x - \bar{x})(y - \bar{y})$

$$\Rightarrow (-1.98)(-9.8), (-0.68)(-5.8), (-0.08)(-0.8), (0.72)(6.2), \\ (2.02)(10.2).$$

$$\Rightarrow (19.404) + (3.94) + (0.064) + (4.464) + (20.604) -$$

now adding all of them we get

$$\Rightarrow 48.48 //$$

now we find $(x - \bar{x})^2$

$$\Rightarrow (-1.98)^2 + (-0.68)^2 + (-0.08)^2 + (0.72)^2 + (2.02)^2$$

$$\Rightarrow 3.92 + 0.462 + 0.0064 + 0.518 + 4.08$$

$$\Rightarrow 8.988 //$$

$$\text{Calculating } \beta_1 \text{ i.e. } \beta_1 = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x_i - \bar{x})^2}$$

$$\beta_1 = \frac{48 \cdot 48}{8 \cdot 988} = \underline{\underline{5.394}}$$

$$\beta_0 = \bar{y} - \beta_1 \bar{x}$$

$$\therefore \beta_0 = 51.8 - 5.394 \times 3.18$$

$$\beta_0 = 34.6470$$

\therefore we know that

$$\text{Salary} = \beta_0 + \beta_1 \times \text{experience}$$

$$[\text{Salary} = 34.6470 + 5.394 \times \text{experience}] //$$

(b) Salary of Person with 4.5 years of experience

$$\text{Salary} = 34.6470 + 5.394 \times 4.5 //$$

$$\text{Salary} = 58.92 \times (\$1000) //$$

(c) Intercept the coefficient of my ~~best~~ $h_w(x)$

So evaluating β_0 & β_1

if employee have 0 experience

$$\text{Salary} = 34.6470 \times 5.394(0)$$

$$\text{Salary.} = 34.670 \times (\$1000)$$

will be basic salary //

& for β_1 ,

each year the salary will be increased

$$5.394 \times (\$1000) \text{ as the year increased.}$$

Question 2 \Rightarrow

House No.	Size	of bedrooms	Price
House 1	900	1	200
House 2	1600	3	330
House 3	1875	4	400

multiple linear Regression.

(a) Matrix X & vector Y //

hypothesis function of Multiple linear Regression

$$h_0(x) = \theta_0 + \theta_1 \times \text{Size} + \theta_2 \times \text{bedrooms.}$$

because we have to predict value on the basis of

in 2 things (i) No. of bedrooms (ii) the Size (sq.ft)

∴ θ_0 = intercept

θ_1 = coefficient of Size.

θ_2 = coefficient of Number of bedroom.

(a) Setting the matrices with help of table.

Matrix X defines the No. of different house
, No. of bedrooms and the size of the house.

$$X = \begin{bmatrix} 1 & 900 & 1 \\ 1 & 1600 & 3 \\ 1 & 1875 & 4 \end{bmatrix} \quad (3 \times 3) \quad Y = \begin{bmatrix} 200 \\ 330 \\ 400 \end{bmatrix} \quad (3 \times 1)$$

Y = the vector defines the prices of house.

equation

(b) Normal Equation & resulting of hypothesis

$$X = \begin{bmatrix} 1 & 900 & 1 \\ 1 & 1600 & 3 \\ 1 & 1875 & 4 \end{bmatrix}$$

$$X^T = \begin{bmatrix} 1 & 1 & 1 \\ 900 & 1600 & 1875 \\ 1 & 3 & 4 \end{bmatrix}$$

We have to find

$$\begin{aligned} X^T \cdot X &= \begin{bmatrix} 1 & 1 & 1 \\ 900 & 1600 & 1875 \\ 1 & 3 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 900 & 1 \\ 1 & 1600 & 3 \\ 1 & 1875 & 4 \end{bmatrix} \\ &= \begin{bmatrix} 3 & 4373 & 8 \\ 4373 & 6878129 & 13192 \\ 8 & 13192 & 26 \end{bmatrix} \end{aligned}$$

$$X^T \cdot Y = \begin{bmatrix} 1 & 1 & 1 \\ 900 & 1600 & 1875 \\ 1 & 3 & 4 \end{bmatrix} \cdot \begin{bmatrix} 200 \\ 330 \\ 400 \end{bmatrix}$$

$$3 \times 3 \times 3 \times 1$$

we get (3x1)

$$= \begin{bmatrix} 930 \\ 1630000 \\ 3250 \end{bmatrix} //$$

∴ Normal equation for Linear Regression

$$\Theta = (X^T X)^{-1} X^T y$$

Where Θ is the ^{Vector of} coefficient

Now finding $(X^T X)^{-1}$

for that we have to find the determinant of the

$$X^T X = \begin{bmatrix} 3 & 4373 & 8 \\ 4373 & 6878129 & 13192 \\ 8 & 13192 & 26 \end{bmatrix}$$

∴ for $\det(X) = a(ei - fh) - b(di - fg) + c(dh - eg)$

where matrix $(X) = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$

∴ $\det(X) =$

$$3((6878129 \times 26) - (13192 \times 13192)) - 4373((4373 \times 26) - (13192 \times 8)) + 8((4373 \times 13192) - (6878129 \times 8))$$

$$= 14402470 + 35698428 - 1308672$$

$$= 23718.$$

$$\cancel{23716} \times \cancel{105536} \times \cancel{8162} \times \cancel{2659884}$$
$$\therefore 3 \times (178831354 - 173830464) - 4373 \times$$

$$113698 - 105536 + 8(57684916 - 55025032)$$

$$\Rightarrow 3 \times 5000890 - 4372 \times 8162 + 8 \times 2659884$$

$$\Rightarrow 15002610 - 35693026 + 21279072$$

$$\Rightarrow 588716$$

Now we solve for adj. ($X^T X$)

$$\text{for } C_{11} = (6878129 \times 26 - 13192^2)$$
$$= 5002090$$

$$C_2 = -(4373 \times 26 - 8 \times 13192)$$
$$= -8126$$

$$C_{13} = (4373 \times 13192 - 6878129 \times 8)$$
$$= 2660484$$

$$C_{21} = -(4373 \times 26 - 8 \times 13192)$$
$$= -8162$$

$$C_{22} = (3 \times 26 - 8 \times 8) = 78 - 64$$
$$= 14$$

$$C_{23} = -(3 \times 13192 - 4373 \times 8)$$

$$= -4592$$

$$C_{31} = (4373 \times 13192 - 6878129 \times 8)$$

$$= 2660484$$

$$C_{32} = -(3 \times 13192 - 4373 \times 8)$$

$$= -4592$$

$$C_{33} = (3 \times 6878129 - 4373^2)$$

$$= 1511258.$$

∴ the matrix of cofactors is

$$\begin{bmatrix} 5002090 & -8126 & 2660484 \\ -8162 & 14 & -4592 \\ 2660484 & -4592 & 1511258 \end{bmatrix}$$

now dividing $\det(X^T X)$ by $\text{adj.}(X^T X)$

we get

$$\begin{bmatrix} 8.4 & -0.0137 & -2.56 \\ -0.0137 & 0.00002 & 0.0041 \\ -2.56 & 0.00419 & 0.78 \end{bmatrix} //$$

$$\text{the } \frac{\text{adj.}(X^T X)}{\det(X^T X)} = (X^T X)^{-1} //$$

$$\Theta = \begin{bmatrix} 930 \\ 1630000 \\ 3250 \end{bmatrix} \times \begin{bmatrix} 8.4 & -0.0137 & -2.56 \\ -0.0137 & 0.00002 & 0.0041 \\ -2.56 & 0.0041 & 0.78 \end{bmatrix}$$

① 3×1 3×3

$$\text{we get} = \begin{bmatrix} -22839 \\ 38.369 \\ 6983.9 \end{bmatrix}$$

$$\therefore \Theta = \begin{bmatrix} \Theta_0 \\ \Theta_1 \\ \Theta_2 \end{bmatrix} = \begin{bmatrix} 171.67 \\ -0.067 \\ 88.33 \end{bmatrix}$$

So now we put values of Θ_0 , Θ_1 & Θ_2 in the $h_w(\Theta)$

\therefore when Size = 0 & Room = 0

$$\text{Price} = 171.67 (\$/1000)$$

(C) 1500 Sq. ft. R 3 bedrooms

$$\text{price} = \Theta_0 + \Theta_1 \times + \Theta_2 \times$$

$$\text{Price} = 171.67 + 1500(-0.067) + 3 \times (88.33)$$

$$\text{Price} = 171.67 - 100.5 + 264.99$$

$$\text{Price} = 336.16 (\$/1000)$$

(d) Interpret coefficient of b_{10}

So. θ_0 is the base price of a room with 0 sq. ft of size

θ_1 is the change of price for each Sq. ft.

θ_2 is the change of price on basis of each room

Question no. 3 \Rightarrow Table given

Individual Number	Income (\$ 1000's)	Age (Year)	Approved (0 or 1)
1	45	25	0
2	60	35	1
3	75	40	1
4	50	28	0
5	90	50	1
6	100	60	1

~~Multivariate~~ Logistical
~~multiple~~ regression (with binary classification)

(a) Cost function for the problem will be

this is a perfect example we can execute with logistical regression therefore.
if I analyse the question.

~~the hypothesis of function of~~ Logistical Regress

is

$$h_0(x) = \frac{1}{1 + e^{-(\theta_0 + \theta_1 \text{Income} + \theta_2 \text{age})}}$$

where : θ_0 is the Intercept

θ_1 is coefficient of Income of person

θ_2 is coefficient of age,

$h_0(x)$ is probability that output is 1 (i.e.) Approved

∴

$$\rightarrow J(\theta) = -\frac{1}{m} \sum_{i=1}^m [y_i \log(h_0(x^{(i)})) + (1-y_i) \log(1-h_0(x^{(i)}))]$$

Where

m is the number of data point

We have 6 people that's why $m=6$)

y_i is actual value (0 or 1)

[Approved or not Approved]

$h_0(x^{(i)})$ is the hypothesis (Predicted Value)

(b) Coefficient we need to optimize in this feature

are basically 2, (i) Age (ii) Income

therefore we have to have 3 coefficient

θ_0 intercept

θ_1 (Income Coefficient)

θ_2 (Age coefficient)

(c) expression for the derivative of the cost function with respect each coefficient

i.e. $\theta_0, \theta_1, \theta_2$

So we move ahead with Gradient descent

$$\theta_j = \theta_j - \alpha \frac{\partial J(\theta)}{\partial \theta_j}$$

where α is learning rate.

We know derivative for Logistic regression

$$\frac{\partial J(\theta)}{\partial \theta_j} = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

where x_j is j^{th} feature for $x_0 = 1$

$$\theta_j = \theta_j - \alpha \cdot \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y_i) \cdot x_j^{(i)}$$

where,

α is learning rate

$h_\theta(x^{(i)})$ is predicted value for i -th

y_i is active value (0 or 1)

x_j is feature value for x_j (for the intercept

$x_0 = 1$).

update Rule for each coefficient ($\theta_0, \theta_1, \theta_2$)

$$\text{for } \theta_0 = \theta_0 - \alpha \cdot \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y_i)$$

$$\text{for } \theta_1 = \theta_1 - \alpha \cdot \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y_i) \cdot \text{Income}$$

$$\text{for } \theta_2 = \theta_2 - \alpha \cdot \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y_i) \cdot \text{Age}$$

(d) initial value of θ_0 for 1st, θ_1 for 2nd, θ_2 for 3rd
 θ_3 for 4th & so on.

Run one iteration of gradient descent using a learning rate of 0.01.

Hypothesis function for logistic regression

$$\theta_j := \theta_j - \alpha \cdot \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y_i) \cdot x_j^{(i)}$$

so we know $m = 6$

$h_\theta(x^{(i)})$ is probability for i^{th} example

y_i is actual outcome for i^{th} example as well.

$\theta_0 = 0, \theta_1 = 1, \theta_2 = 2, \theta_3 = 3, \theta_4 = 4$ & so on

given in question.

$h_\theta(x)$ for each with their initial value.

Individual 1

income = 45 age = 25 (from table)

$$h_\theta(x) = \frac{1}{1 + e^{(1+2\cdot45+3\cdot25)}}$$

$$h_0(x) = \frac{1}{1 + e^{(1+90+75)}} = \frac{1}{1 + e^{166}} \approx 1,$$

$$h_0(x) = \frac{1}{1 + e^{166}} \approx 1$$

for individual 2

income = 60 age = 35

$$h_0(x) = \frac{1}{1 + e^{(1+2.60+3.35)}} = \frac{1}{1 + e^{(1+120+105)}}$$

$$h_0(x) = \frac{1}{1 + e^{(226)}} \approx 1,$$

for individual 3

income = 75 age = 40

$$h_0(x) = \frac{1}{1 + e^{(1+2.75+3.40)}} = \frac{1}{1 + e^{(1+150+120)}}$$

$$h_0(x) = \frac{1}{1 + e^{(2.71)}} \approx 1,$$

for individual 4

income = 50 age = 28

$$h_0(x) = \frac{1}{1 + e^{(1+2 \cdot 50 + 3 \cdot 28)}} = \frac{1}{1 + e^{(1+100+84)}}$$

$$h_0(x) = \frac{1}{1 + e^{185}} \approx 1/4$$

for individual 5

income = 90 age = 50

$$h_0(x) = \frac{1}{1 + e^{(1+2 \cdot 90 + 3 \cdot 50)}} = \frac{1}{1 + e^{(1+180+150)}}$$

$$h_0(x) = \frac{1}{1 + e^{331}} \approx 1/11$$

for individual 6

income = 100 age = 60

$$h_0(x) = \frac{1}{1 + e^{(1+2 \cdot 100 + 60 \cdot 3)}} = \frac{1}{1 + e^{(1+200+180)}}$$

$$h_0(x) = \frac{1}{1 + e^{381}} \approx 1/11$$

Step² we will compute the gradients θ_0, θ_1

θ_0
2

θ_0 (Gradient descent)

$$\frac{\partial J(\theta)}{\partial \theta_0} \rightarrow \frac{1}{6} \sum_{i=1}^6 (h_\theta(x^{(i)}) - y_i)$$

so we use value of $h_\theta(x)$ & actual value y

for each individual \therefore

$$\text{for } 1 = h_\theta(x^{(1)}) - y_1 = 1 - 0 = 1$$

$$\text{for } 2 = h_\theta(x^{(2)}) - y_2 = 1 - 1 = 0$$

$$\text{for } 3 = h_\theta(x^{(3)}) - y_3 = 1 - 1 = 0$$

$$\text{for } 4 = h_\theta(x^{(4)}) - y_4 = 1 - 0 = 1$$

$$\text{for } 5 = h_\theta(x^{(5)}) - y_5 = 1 - 1 = 0$$

$$\text{for } 6 = h_\theta(x^{(6)}) - y_6 = 1 - 1 = 0$$

$$\text{So the total } \theta_0 : \frac{1}{6} \times (1+0+0+1+0+0)$$

$$\Rightarrow \frac{1}{6} \times 2 \Rightarrow \frac{2}{6} = \frac{1}{3} //$$

now for θ_1 (income)

$$\frac{\partial J(\theta)}{\partial \theta_1} = \frac{1}{6} \sum_{i=1}^6 (h_\theta(x^{(i)}) - y_i) \cdot \text{income.}$$

$$\frac{\partial J(\theta)}{\partial \theta_1} = \frac{1}{6} \times (1.45 + 0.60 + 0.75 + 0.90 + 1.50 + 0.100)$$

$$\Rightarrow \frac{1}{6} \times (45 + 50) \Rightarrow \frac{1}{6} \times 95 \Rightarrow \frac{95}{6} = 15.83 //$$

now for θ_2 (age)

$$\frac{\partial J(\theta)}{\partial \theta_2} = \frac{1}{6} \sum_{i=1}^6 (h_\theta(x^{(i)}) - y_i) \cdot \text{age.}$$

$$\Rightarrow \frac{1}{6} \times [1.25 + 0.35 + 0.45 + 1.28 + 0.50 + 0.60]$$

$$\Rightarrow \frac{1}{6} \times [25 + 28] \Rightarrow \frac{1}{6} \times 53 \Rightarrow \underline{8.83} //$$

Step 3 we update the coefficient's.

as given initial value of $\theta_0, \theta_1 \& \theta_2 = 1, 2, 3$,
resp.

$$\theta_0 = \theta_0 - \alpha \cdot \frac{\partial J(\theta_0)}{\partial \theta_0}$$

$$\theta_0 \text{ (new)} = 1 - 0.01 \cdot \frac{1}{3} \Rightarrow 1 - \frac{0.01}{3} = 0.9967 //$$

$$\theta_{1(\text{new})} = \theta_1 - \alpha \cdot \frac{\partial J(\theta)}{\partial \theta_1}$$

$$= 2 - 0.01 \cdot 15.83$$

$$\theta_1 = \underline{\underline{1.8417}} q$$

$$\theta_{2(\text{new})} = \theta_2 - \alpha \cdot \frac{\partial J(\theta)}{\partial \theta_2}$$

$$= \theta_2 - 0.01 \cdot 15.83$$

$$\theta_2 = \underline{\underline{2.9117}} q$$

(e) Now we calculate the accuracy using new updated coefficient.

for this we need accuracy formula

$$\text{i.e.} \Rightarrow \text{Accuracy} = \frac{\text{No. of correct prediction}}{\text{Total no. of prediction}} \times 100$$

so from the table we have y_j for each one

$$y_1 = 0$$

$$y_2 = 1 \quad \text{and} \quad \theta_0 = 0.997$$

$$y_3 = 1$$

$$\theta_1 = 1.842$$

$$y_4 = 0$$

$$\theta_2 = 2.912$$

$$y_5 = 1$$

$$y_6 = 1$$

So we calculate predicted values for each one separately.

individual = income = 45 K ; Age = 25

So we put in $h_{\theta}(x) = \frac{1}{1 + e^{(0.997 + 1.842 \times 45 + 2.912 \times 25)}}$

$$h_{\theta_1}(x_1) = \frac{1}{1 + e^{(0.997 + 1.842 \times 45 + 2.912 \times 25)}} = \frac{1}{1 + e^{156.68}} \\ = \frac{1}{1 + 0} \approx 1 \text{ y}$$

individual 2 = income = 60K ; age = 35

$$h_{\theta}(x_2) = \frac{1}{1 + e^{(0.997 + 1.842 \times 60 + 2.912 \times 35)}} = \frac{1}{1 + e^{213.43}} \\ = \frac{1}{1 + 0} \approx 1 \text{ y}$$

individual 3 = income = 75 K ; age = 40

$$h_{\theta}(x_3) = \frac{1}{1 + e^{(0.997 + 1.842 \times 75 + 40 \cdot 2.912)}} = \frac{1}{1 + e^{255.62}} \\ = \frac{1}{1 + 0} \approx 1 \text{ y}$$

Similarly we calculate for

individual 4, 5 & 6

we will have 1 for all of them
∴ everyone is having predicted outcome
"approved" //

individual	Actual Outcome (y)	Predicted outcome (x)
1	0	1
2	1	1
3	1	1
4	0	1
5	1	1
6	1	1
	= 4 //	= 6 //

∴ Accuracy will be

$$= \frac{4}{6} \times 100 = \boxed{66.7\% //}$$

Question No. 4 //



Predicted:

		No Churn (0)	Churn (1)
Actual	No Churn (0)	180	20
	Churn (1)	70	30

(a) calculate the accuracy, Precision, Recall & F₁ Score for the model.

So we write formulas for each task at (a)

$$\text{ACCURACY} = \frac{\text{True Positive} + \text{True Negative}}{\text{Total Number of Prediction}}$$

$$\text{PRECISION} = \frac{\text{True Positive}}{\text{True Positive} + \text{False Positive}}$$

$$\text{Recall} = \frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}}$$

$$F_1 \text{ Score} = 2 \times \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$$

we get values from given table

	Predicted: No churn	Predicted: Churn
Actual: No churn	180	20
Actual: Churn	70	30

∴ we have

$$TN = 180 \quad (\text{True Negative})$$

$$FP = 20 \quad (\text{False Positive})$$

$$FN = 70 \quad (\text{False Negative})$$

$$TP = 30 \quad (\text{True Positive})$$

Calculating the Metrics.

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

$$= \frac{30 + 180}{30 + 20 + 70 + 180} = \frac{210}{300} = 0.70 = 70\%$$

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{30}{30 + 20}$$

$$= \frac{30}{50} = \frac{3}{5} = 0.6 = 60\%$$

$$\text{Recall} = \frac{\text{TP}}{\text{TP} + \text{FN}} = \frac{30}{30+70} = \frac{30}{100} = 0.3$$

$$= 30\%$$

$$F_1 \text{ Score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$\therefore 2 \times \frac{0.6 \times 0.3}{0.6 + 0.3} = \frac{2 \times 0.18}{0.9} = 0.2 \times 2$$

$$= 0.4 = 40\%$$

(b) we get the 40% F_1 Score.

So F_1 Score is a measure between Product of Precision & recall using their harmonic value as mean.

it is useful when there is imbalance in data set & one class is common than other one.

only 10% of people is churned so we can say the data is very imbalanced and we can rely on F_1 Score.

as Accuracy can be deviated because of 90% of No churn data & the value will be

in Acuracy & F1 Score used the Precision & recall in which the False Negative and False Positive values is included in the product of the value.

$$(c) -0.6 \text{ Salary} = 30,000 \text{ probability} = 0.63 \text{ pay churning}$$

Recap Logistic Regression

$$h_{\theta}(x) = \frac{1}{1 + e^{-(\theta_0 + \theta_1 \cdot x_1 + \dots + \theta_n \cdot x_n)}}$$

So we are told to have coefficient for
 $\text{Salary} = -0.6$

$$\therefore h_{\theta}(\text{Salary}) = \frac{1}{1 + e^{-(\theta_0 - 0.6 \cdot \text{Salary})}}$$

given info. we have

$$\text{Salary} = 30,000 \text{ & probability} = 0.63$$

$$\therefore 0.63 = \frac{1}{1 + e^{-(\theta_0 - 0.6 \cdot 30,000)}}$$

$$0.63 = \frac{1}{1 + e^{-(\theta_0 - 18,000)}}$$

$$0.63 = \frac{1}{1 + \frac{1}{e^{(\Theta_0 - 18000)}}} \Rightarrow 1 + e^{-(\Theta_0 - 18000)} = \frac{1}{0.63}$$

∴ we have

$$1 + e^{-(\Theta_0 - 18000)} = 1.587$$

$$e^{-(\Theta_0 - 18000)} = 0.587$$

$$-(\Theta_0 - 18000) = \ln(0.587)$$

$$18000 - \Theta_0 = -0.533$$

$$18000 + 0.533 = \Theta_0$$

$$18000.533 = \Theta_0 //$$

for 31,000 Salary. Now

We know value $\Theta_0 = 18000.533$.

∴ putting eq.

$$h_\theta(31000) = \frac{1}{1 + e^{-(18000.533 - 0.6 \cdot 31000)}}$$

$$= \frac{1}{1 + e^{-(18000.533 - 18600)}} \text{ AlSAOUD}$$

$$\text{Now } h_0 (\text{£}31000) = \frac{1}{1 + e^{-599.48}}$$

∴ Since $e^{-599.48}$ is large no.

making $P \approx 0\%$

∴ the probability of churning will be decreases //

Question No. 5 \Rightarrow

outlook	Temp.	Humidity	Play Tennis
Sunny	Hot	High	No
Sunny	Hot	Normal	Yes
Overcast	Hot	High	Yes
Overcast	Mild	High	Yes
Sunny	Mild	Normal	No

a) We have entropy formulae

$$H(p) = - \sum_{i=1}^n p_i \log_2 (p_i)$$

So we know from the table for play tennis

So. (i) calculate the initial entropy

\Rightarrow for Playing Tennis we have

\Rightarrow 2 NO & 3 Yes.

\Rightarrow total cases = 5 $\therefore N=5$

\Rightarrow Probability (Yes) = $\frac{3}{5}$ Probability (NO) = $\frac{2}{5}$

$$\therefore H(P_i) = - \frac{3}{5} \log_2 \left(\frac{3}{5} \right) + \frac{2}{5} \log_2 \left(\frac{2}{5} \right)$$

Solving via calculator.

$$= -(-0.4421) + (+0.5287)$$

$$H(P_i) = 0.9714$$

(ii) Calculate entropy for each attribute

outlook, temperature, humidity.

Sunny = 1 Yes, 2 No
 out look → overcast = 2 Yes.

$$H(\text{Sunny}) = -\left(\frac{1}{3} \log_2 \left(\frac{1}{3}\right) + \frac{2}{3} \log_2 \left(\frac{2}{3}\right)\right)$$

$$= 0.918 //$$

$$H(\text{overcast}) = 0$$

$$H(\text{outlook}) = 0 + 0.918$$

$$= 0.918 //$$

Temperature

Hot (2 Yes, 1 No)
 Mild (1 Yes, 1 No)

$$H(\text{Hot}) = -\left(\frac{2}{3} \log_2 \left(\frac{2}{3}\right) + \frac{1}{3} \log_2 \left(\frac{1}{3}\right)\right)$$

$$= 0.918 //$$

$$H(\text{Mild}) = -\left(\frac{1}{2} \log_2 \left(\frac{1}{2}\right) + \frac{1}{2} \log_2 \left(\frac{1}{2}\right)\right)$$

$$= 1 //$$

$$H(\text{Temp.}) = 0.918 + 1$$

$$= 1.918 //$$

Humidity → High (2 yes, 1 no)
 Humidity → Normal (1 yes, 1 no)

$$H(\text{High}) = - \left(\frac{2}{3} \log_2 (2/3) + \frac{1}{3} \log_2 (1/3) \right)$$

$$= 0.918$$

$$H(\text{Normal}) = - \left(\frac{1}{2} \log_2 (1/2) + \frac{1}{2} \log_2 (1/2) \right)$$

$$= 1$$

$$H(\text{Humidity}) = 1 + 0.918$$

$$= 1.918$$

(iii) Calculating each info. gain:

$$IG(\text{outlook}) = 0.917 - 0.918 = 0.053$$

$$IG(\text{Temperature}) = 0.971 - 1.918 = -0.947$$

$$IG(\text{Humidity}) = 0.971 - 1.918 = -0.947$$

(6) outlook : overcast

Temperature: hot

Humidity: Normal

after evaluating everything

we split the outlook we know

outlook = overcast & all records
labelled as yes, therefore model
predicted would be a good day to play
Tennis