

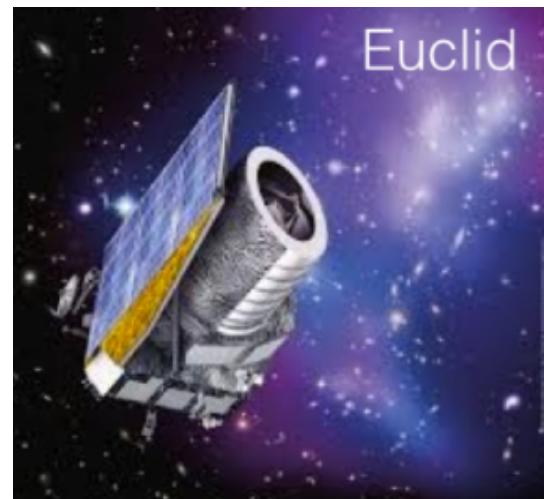
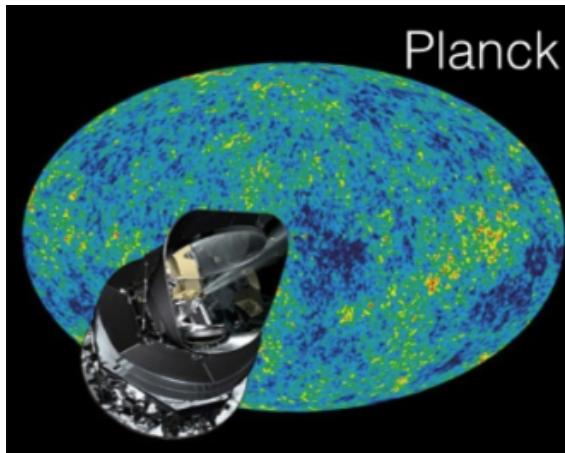
# LECTURE I: THE UNIFORM UNIVERSE

**Alkistis Pourtsidou**

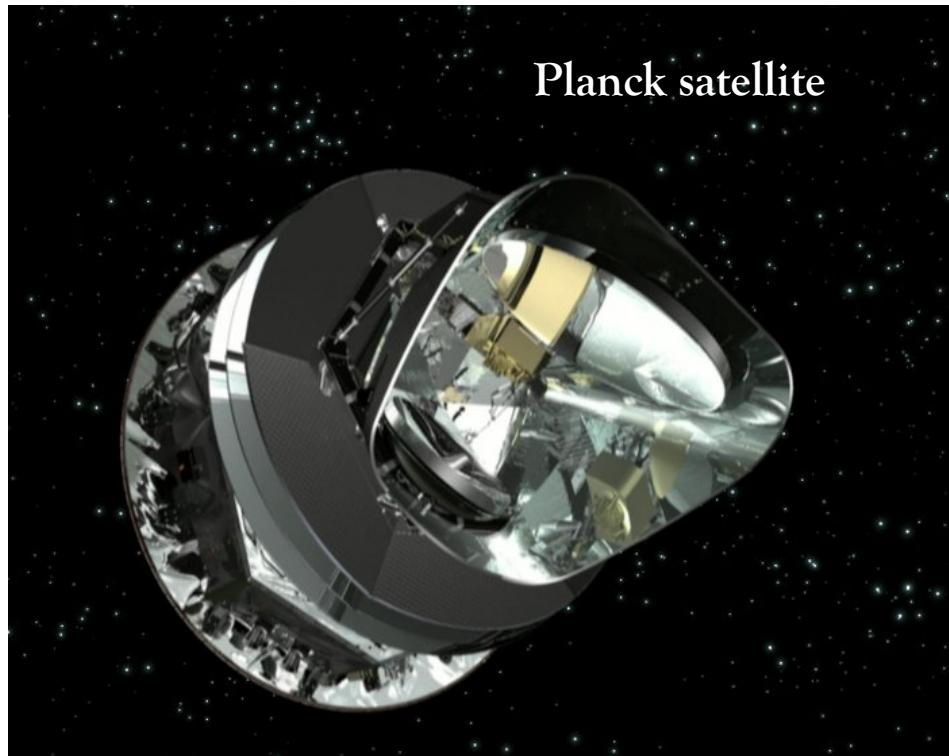
*Queen Mary University of London*

# OUR UNIVERSE

- What does the Universe look like? How has it evolved throughout cosmic time? We need a map!
- Our Universe evolves in time, so we need a 3D map, to capture all the information: across the sky and along time
- We utilise ground based telescopes as well as satellites.



# THE PLANCK SATELLITE



Planck satellite

Scanned the sky for 4 years  
(2009-2013).

Detected the Cosmic  
Microwave Background with  
unprecedented precision.

But also stellar cradles in the  
Milky Way, a multitude of  
other galaxies, galaxy clusters.

# THE COSMIC MICROWAVE BACKGROUND (CMB)

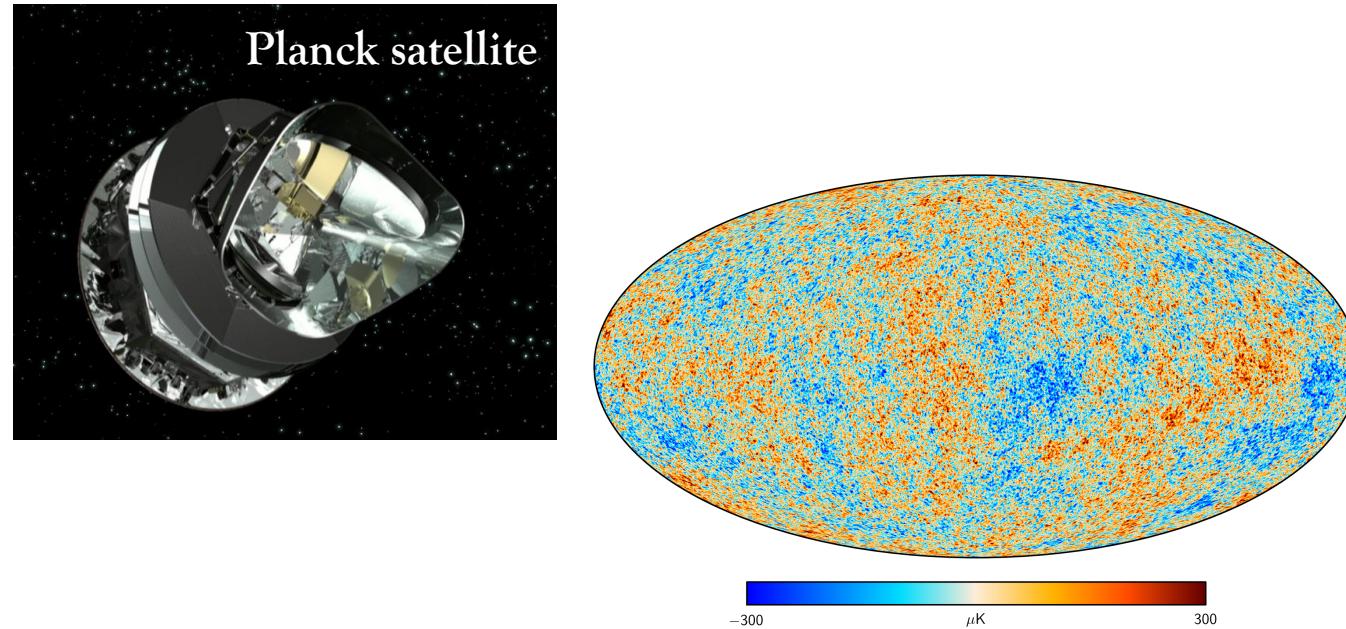


Figure 1: CMB map from the Planck satellite 2015 data.

Figure 1 is a snapshot of the Universe 400,000 years after the Big Bang! Our Universe is 14 billion years old. So the CMB is the “baby” Universe. The CMB map shows very small temperature fluctuations that correspond to (slightly) different densities in the early Universe. These are the seeds of all structure we see today (galaxies etc.).

# EXAMPLE: THE COSMIC MICROWAVE BACKGROUND (CMB)

$$\bar{T} = 2.73 \text{ K}$$

$$\frac{\delta T}{\bar{T}} \sim 10^{-5}$$

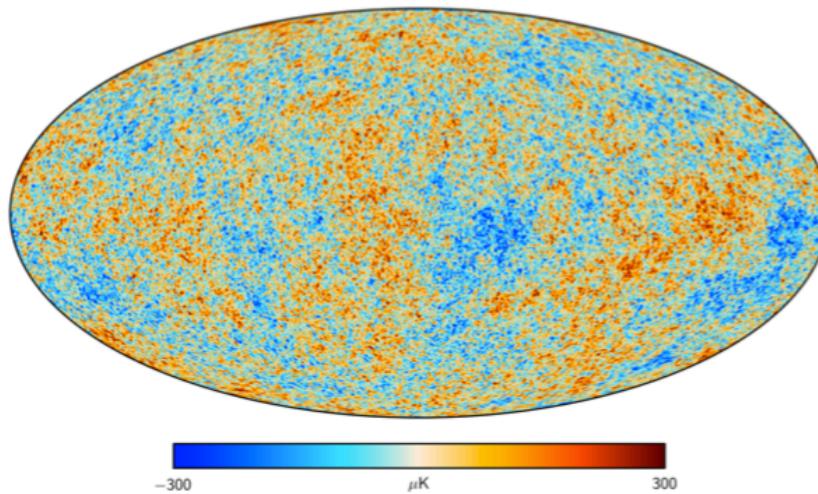
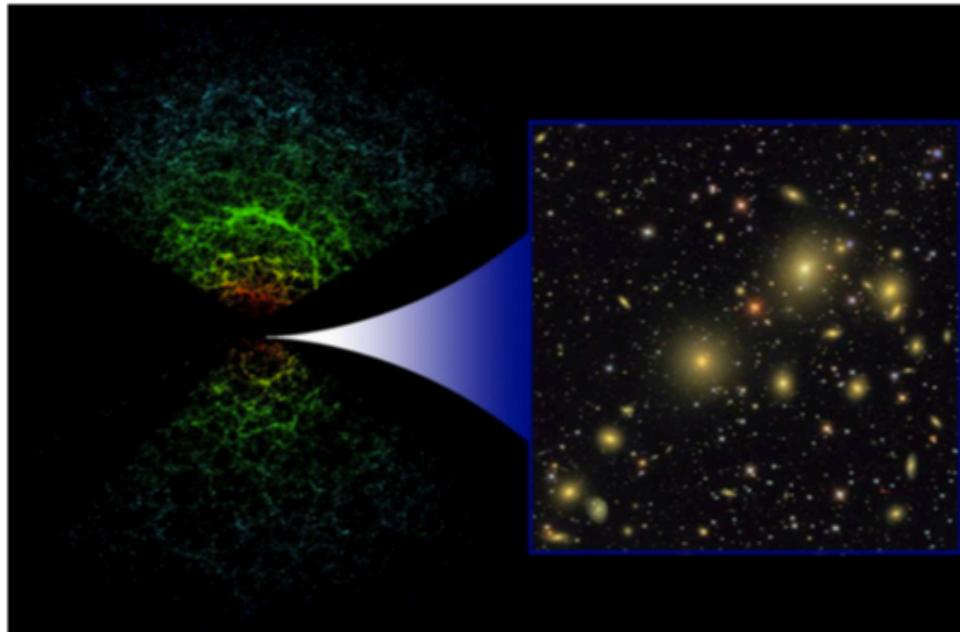


Figure: Temperature data from the Planck satellite, 2015.

- Early Universe photons scatter off electrons - the process of multiple scattering produced a thermal (blackbody) spectrum
- Eventually, the Universe cooled down enough, e and p formed neutral atoms and CMB photons could travel freely

## EXAMPLE: LARGE SCALE STRUCTURE (LSS)

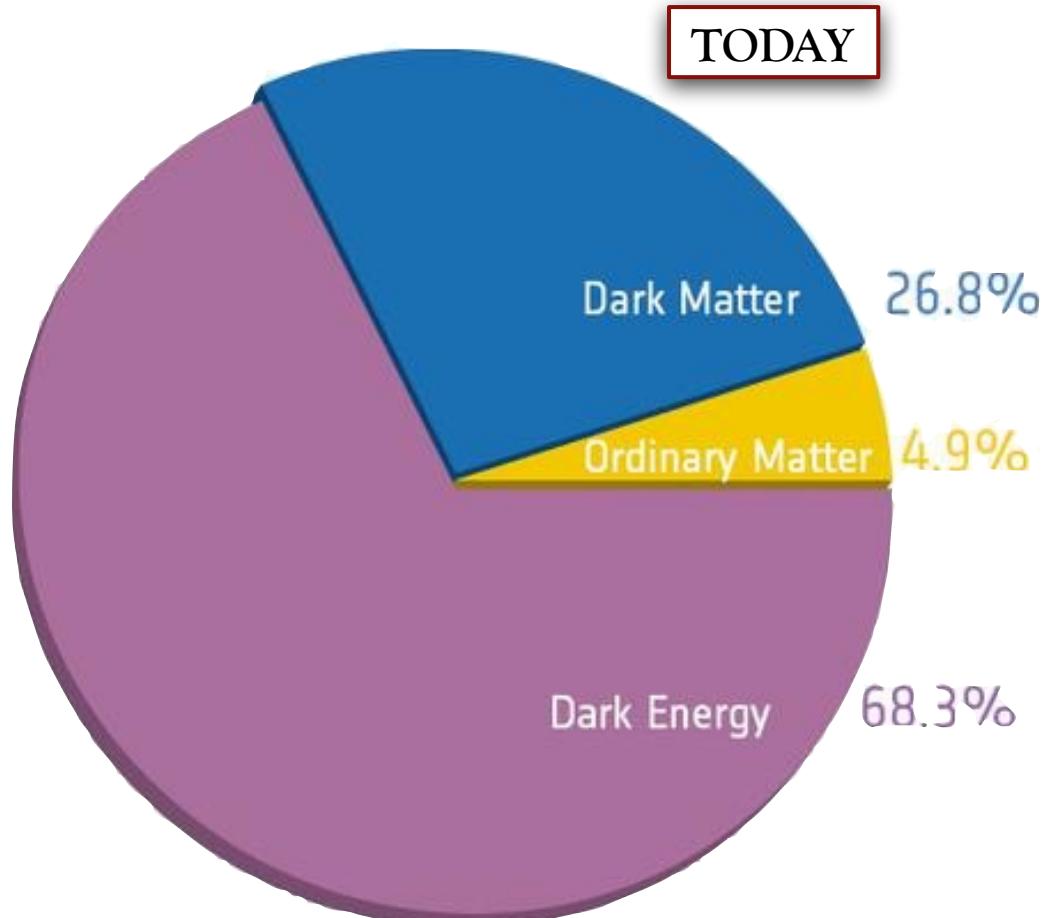
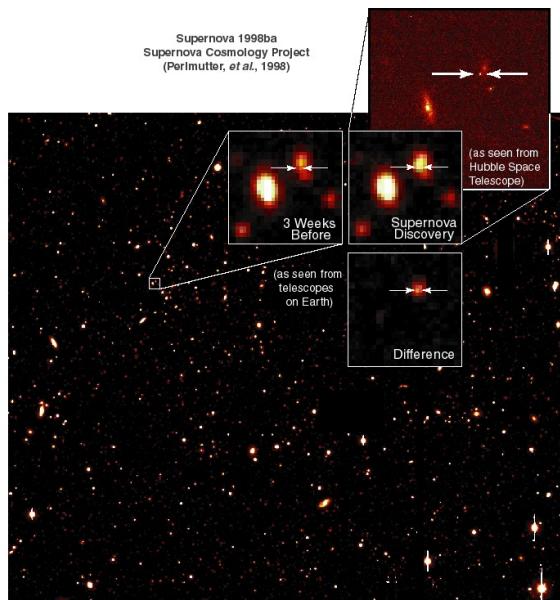
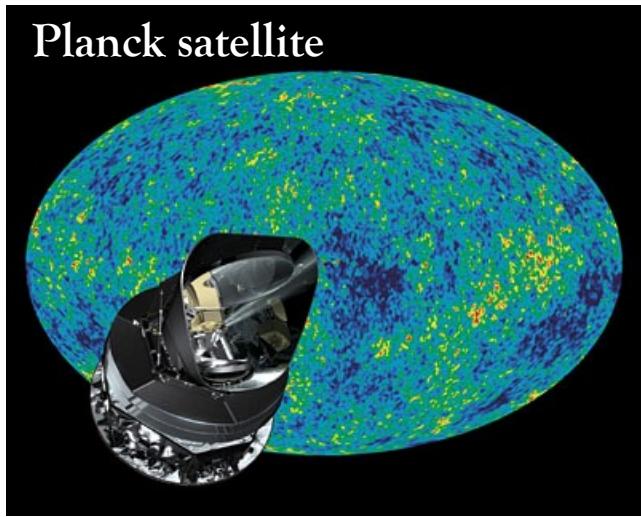


**Figure:** A map of the observed distribution of galaxies on large scales, from the Sloan Digital Sky Survey (SDSS).

This is the Universe “today! On large scales, we see galaxies and clusters of galaxies, and voids (empty space between clusters of galaxies).

# WHAT IS OUR UNIVERSE MADE OFF?

Planck satellite



# NORMAL MATTER IS JUST 5%!

# THE PERIODIC TABLE OF THE ELEMENTS

Alkali Metal

## Alkaline Earth

## transition Metal

Basic Metal

### Semimetal

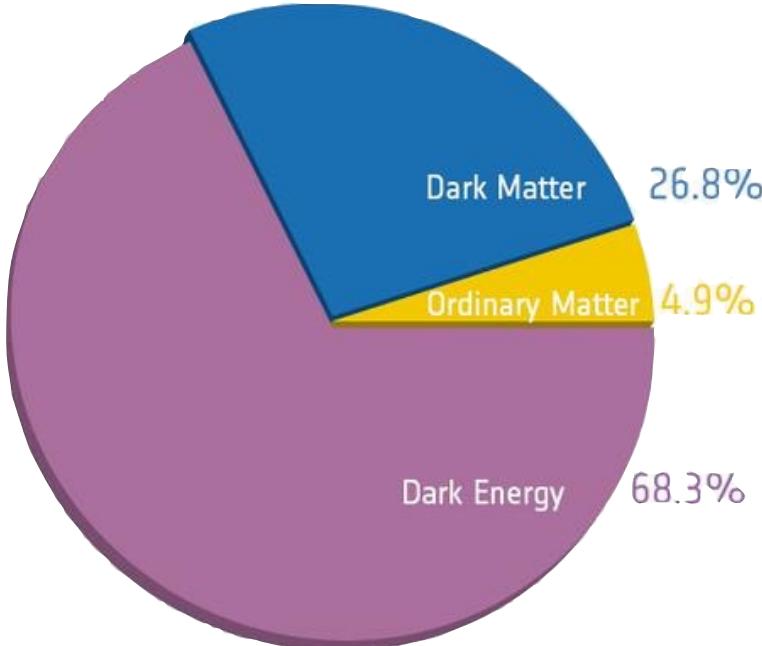
### Nonmetal

### **halogen**

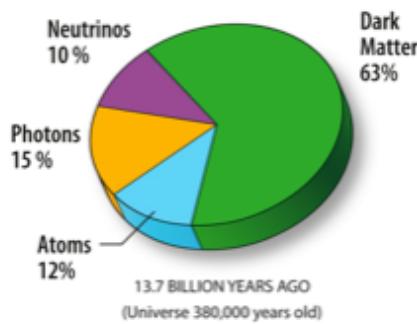
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# DARK MATTER AND DARK ENERGY



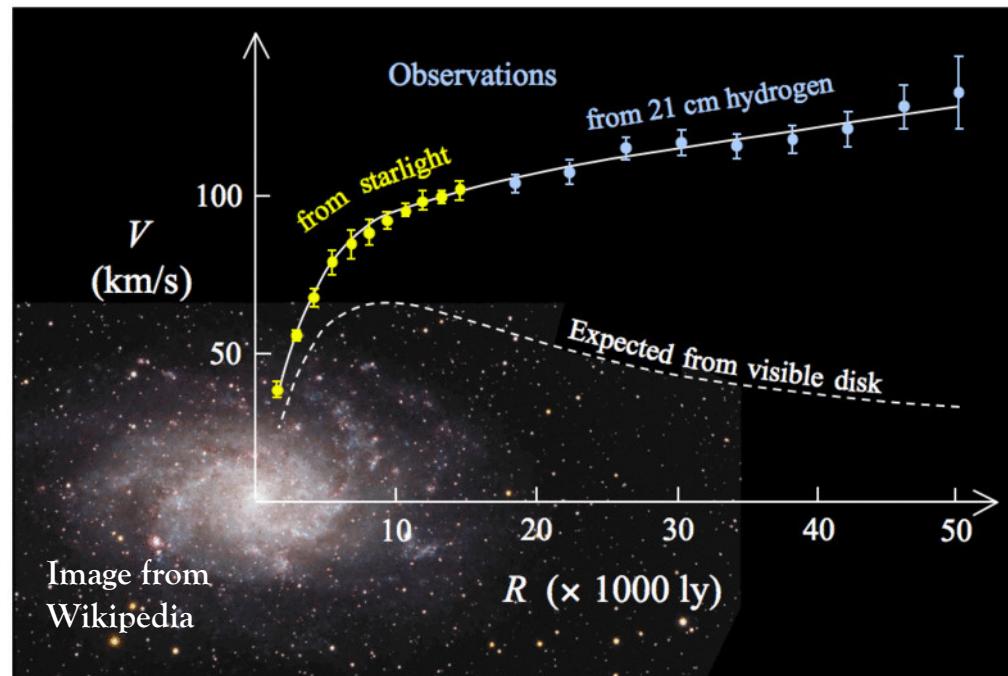
- Note things were very different in the past...



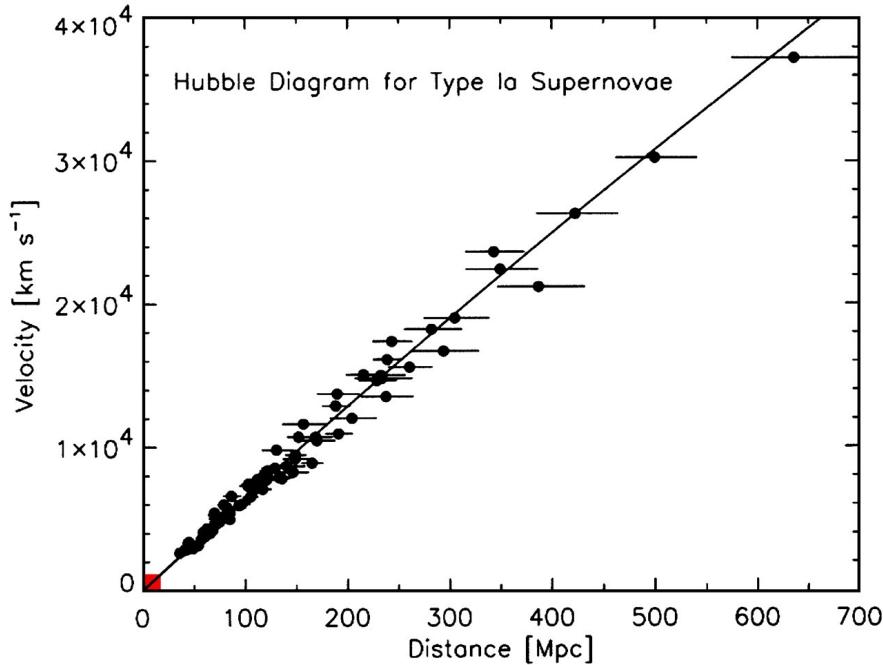
- Most of our Universe is made of dark matter and dark energy.
- **Dark matter** accounts for the missing mass in the Universe. It doesn't interact with light.
- Effects of DM can be seen gravitationally.
- Popular DM candidate: **WIMP** (Weakly Interacting Massive Particle)
- Back in fashion: **Primordial Black Holes**
- My personal favourite: **Neutrinos** (but it's hard...)

# EVIDENCE FOR DARK MATTER: GALAXY ROTATION CURVES

- Newtonian expectation for the orbital velocity:  
$$v = 1/\sqrt{R}$$
- The discrepancy between the two curves can be accounted for by adding a dark matter halo surrounding the galaxy



# THE UNIVERSE IS EXPANDING

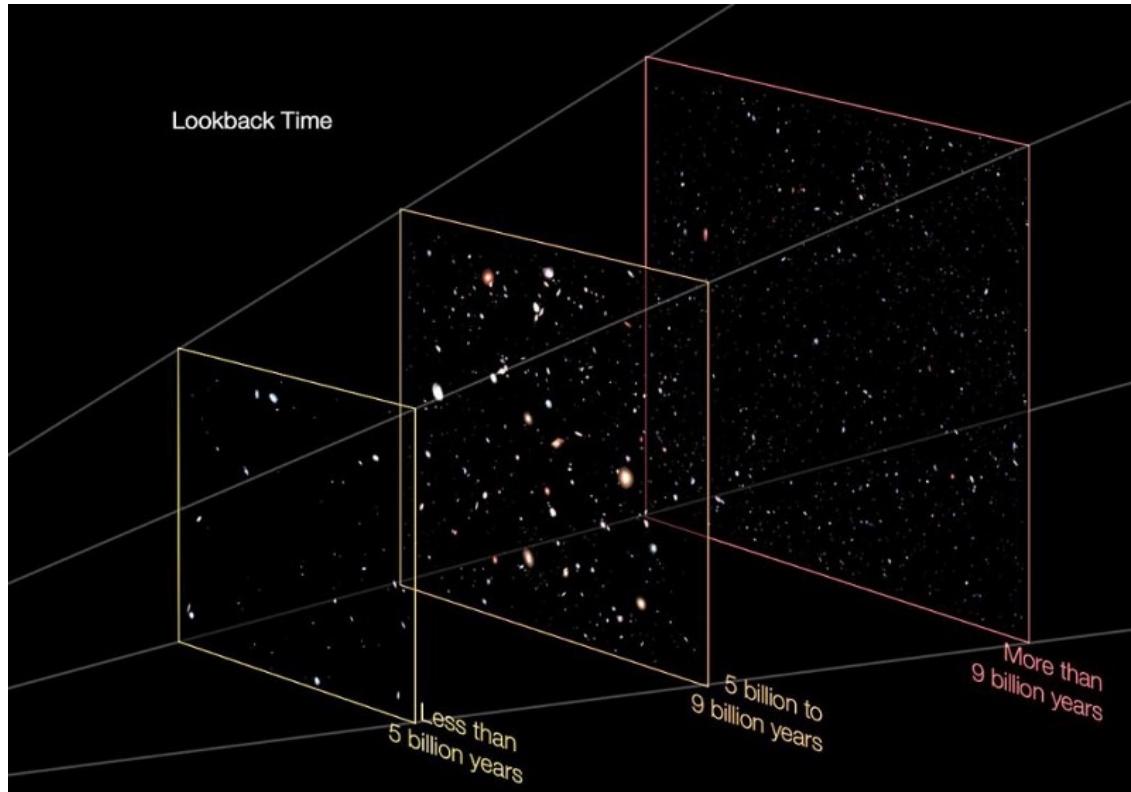


- In the 1920's, Hubble discovered that the Universe is expanding.
- Galaxies move away from us, their velocities are proportional to their distance from us.

$$v = H_0 d$$

$$H_0 = 100h \text{ km/sec/Mpc}$$

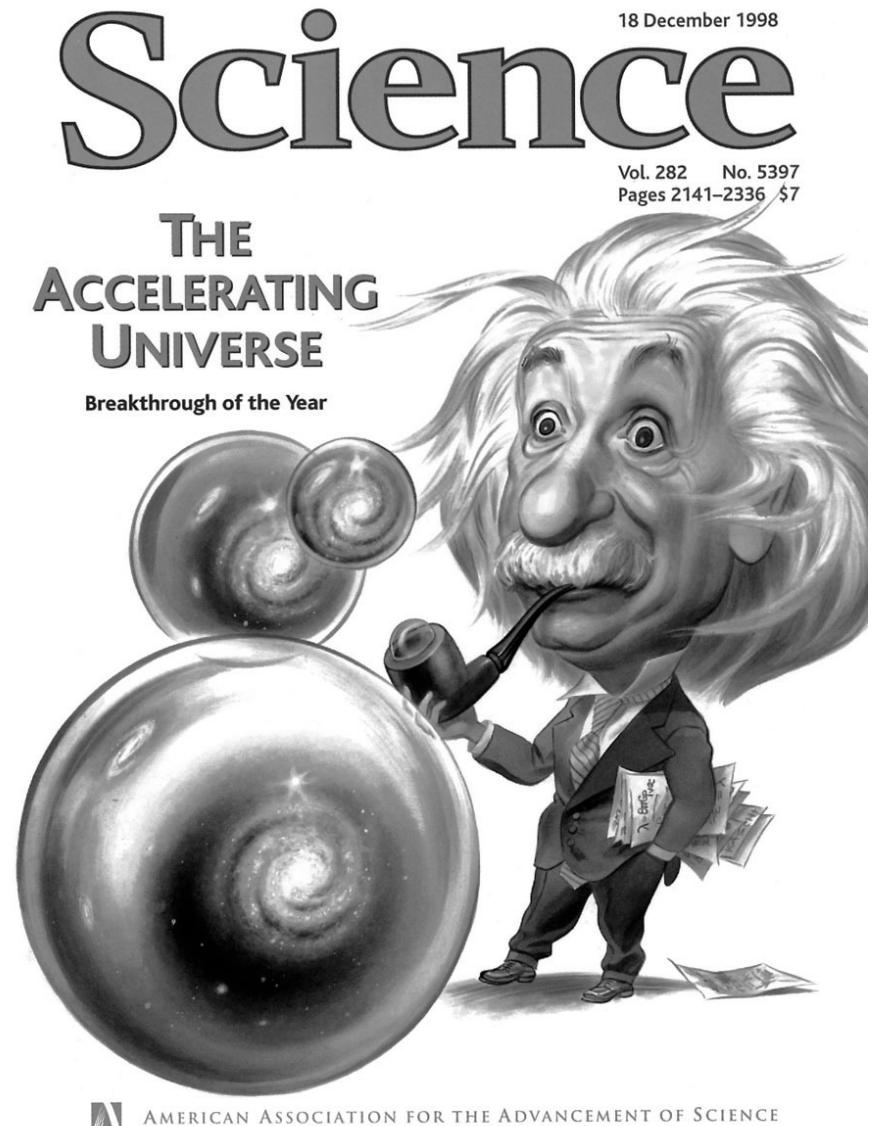
# THE UNIVERSE IS EXPANDING



- The Universe is expanding, but matter will slow the expansion down.
- The more matter, the more rapidly the expansion slows down

# THE DARK ENERGY BREAKTHROUGH

- 1998: Two teams measured the expansion of the Universe and discovered that the Universe's expansion is currently speeding up!
- Galaxies are **accelerating** away from us! This means something other than matter is present in the Universe...
  - Dark energy!



AMERICAN ASSOCIATION FOR THE ADVANCEMENT OF SCIENCE

# DARK ENERGY IS STRANGE

I find  
**DARK ENERGY**  
Repulsive

- Dark Energy is repulsive, not attractive: pulls things apart
- Smoothly filling space
- Constant energy per unit volume
- **More energy as space expands!**

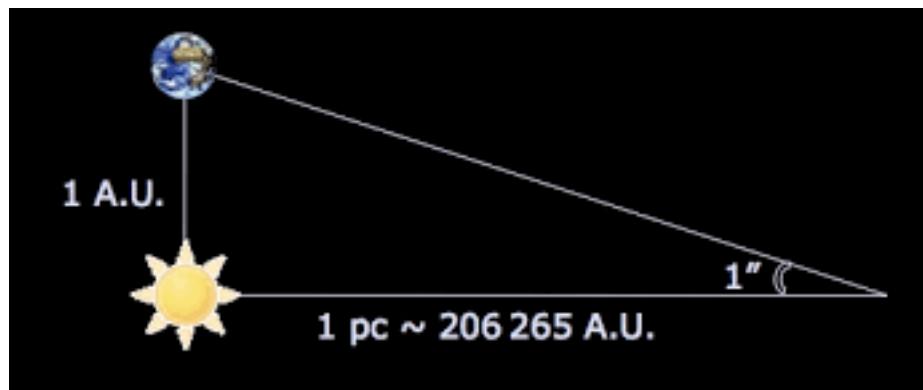
# WHAT COULD DARK ENERGY BE?

- Cosmological constant ( $\Lambda$ )
- Energy of the vacuum. Quantum fluctuations in the vacuum have energy.
- In terms of a mass scale:  $\rho_V = M_V^4$
- This leads to a discrepancy of 30 orders of magnitude between theory (Quantum Field Theory) and observations for  $M_V$
- We need **extreme fine tuning** to get the final, observed, **tiny value**
- Alternatives: evolving scalar field (e.g. quintessence - has the same problem), modified gravity - often has the same problem or doesn't manage to do the job!

# COSMIC LENGTH SCALES

## Cosmological length units reminder:

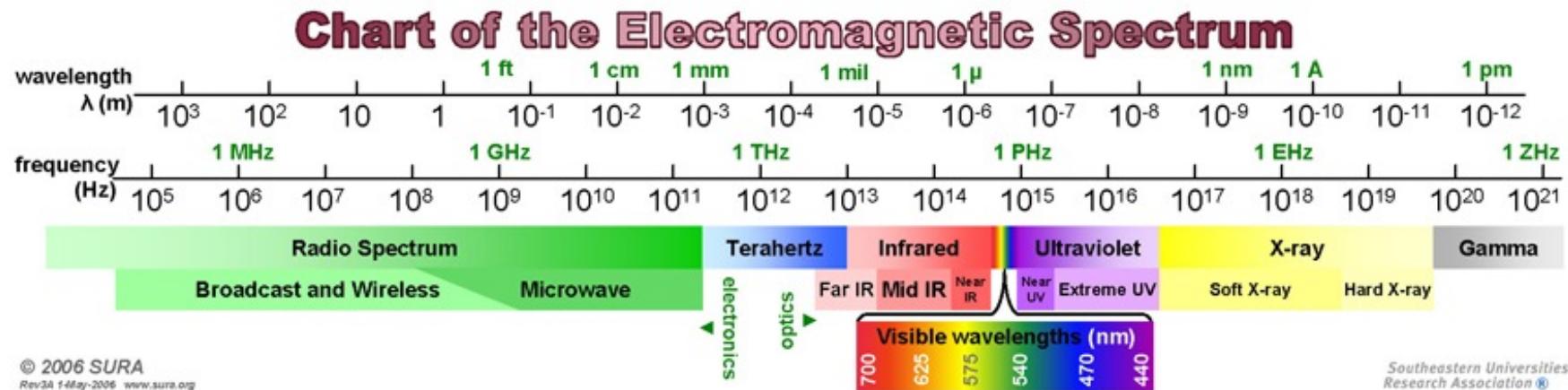
- ◆ The astronomical unit (AU): The mean distance from the Sun to the Earth.  $1 \text{ AU} = 149.6 \times 10^6 \text{ km}$
- ◆ The parsec (pc): the distance at which 1 AU subtends 1 arc sec (1 arcsec =  $1/3600$  degrees). In cosmology we usually encounter Mpc.
- ◆ Lightyear (LY): the distance light travels in a year in vacuum. This is equal to  $9.46 \times 10^{15} \text{ m}$ .



# BUT WHAT DO WE MEAN BY "LIGHT"?

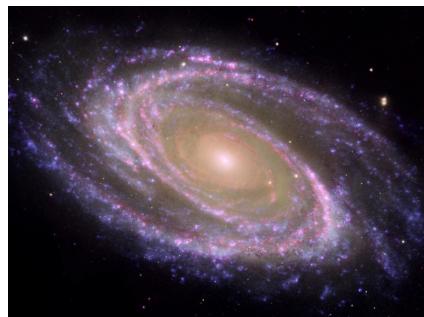
We observe in many different wavelengths (frequencies):

- ◆ Radio waves
- ◆ Infrared light
- ◆ Visible light
- ◆ Ultraviolet light
- ◆ X-rays
- ◆ Gamma rays



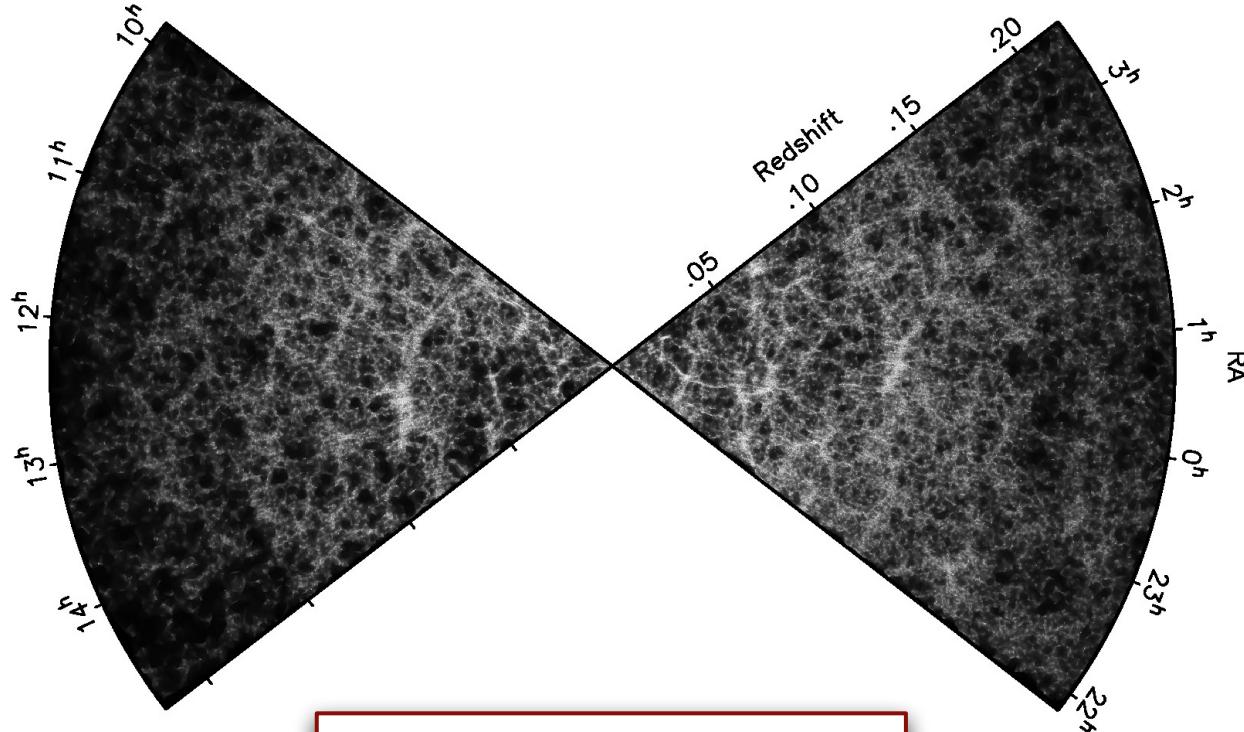
# VISIBLE LIGHT: STARS AND GALAXIES

- ◆ Visible light from nuclear fusion within stars.
- ◆ The Sun is an average star ( $2 \times 10^{30}$  kilograms = 1 solar mass). The nearest stars to us are a few lightyears away.
- ◆ In cosmology, we rarely talk about individual stars. We work with the collection of stars called **galaxies**.
- ◆ Galaxies are beautiful and complicated objects, but in cosmology we just treat them as point-like objects emitting light.



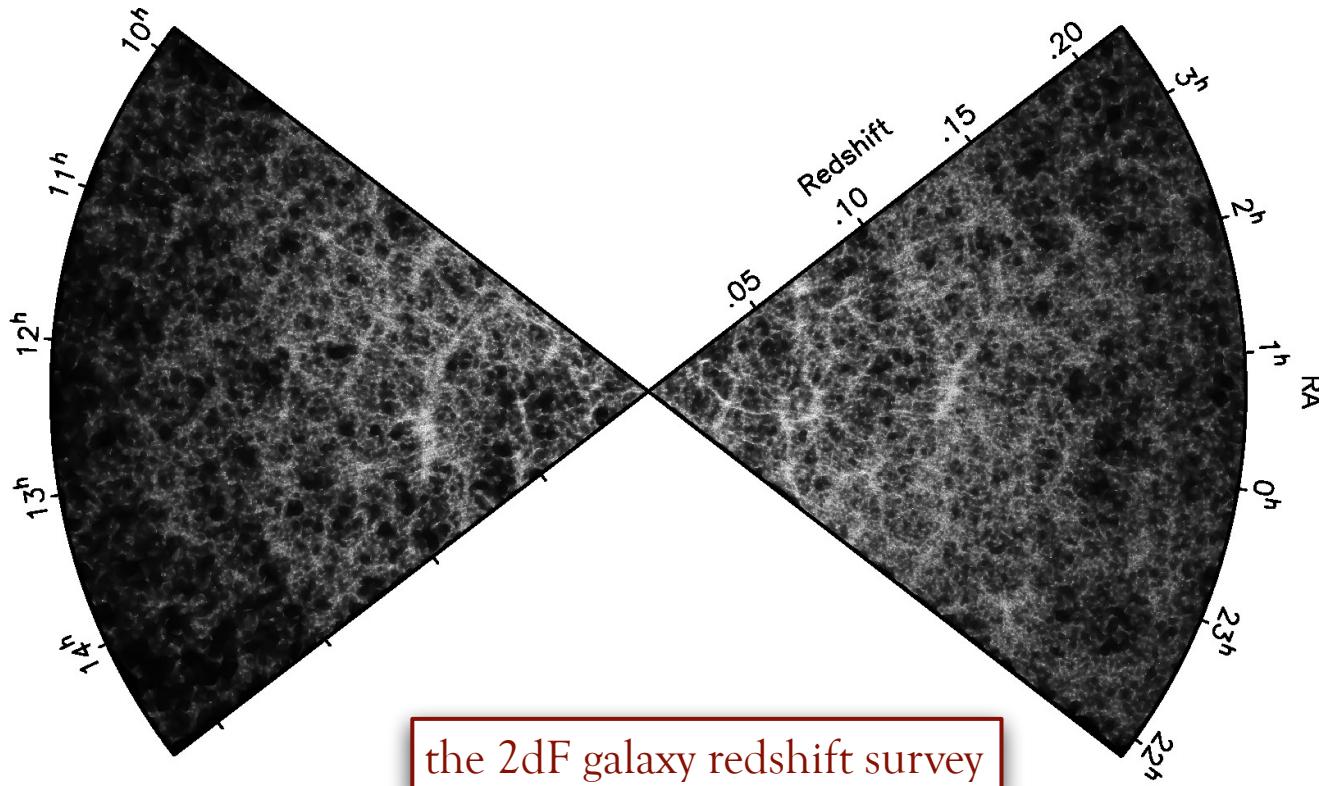
# CLUSTERS OF GALAXIES, SUPERCLUSTERS, AND VOIDS

- ◆ Surveying larger regions of the Universe, say on a scale of hundreds of Mpc, one sees a variety of large-scale structures.



# CLUSTERS OF GALAXIES, SUPERCLUSTERS, AND VOIDS

- ◆ The Figure is a carefully reconstructed map of the nearby region of our Universe (scale 1:10<sup>27</sup>)
- ◆ In some places galaxies are **clearly grouped into clusters of galaxies.**

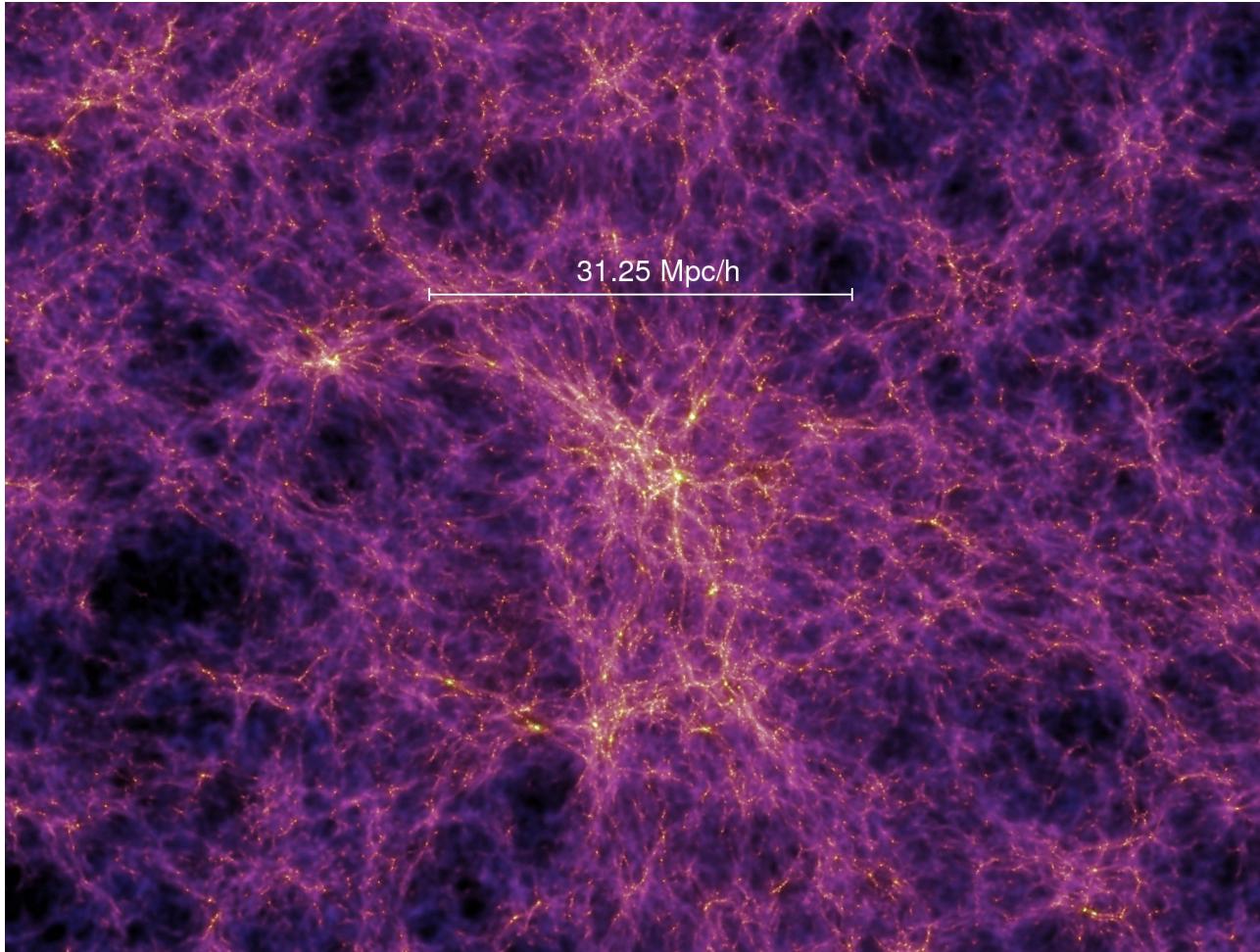


# CLUSTERS OF GALAXIES, SUPERCLUSTERS, AND VOIDS

- ◆ Galaxy clusters are themselves grouped into superclusters, joined by “filaments” and “walls” of galaxies.
- ◆ In between this “foamlike” structure lie large voids, some as large as 50 Mpc across.
- ◆ **Large-scale smoothness:** Only once we get to scales of 100 Mpc or more does the Universe begin to appear smooth. This means that we cannot find any large structures on scales greater than about 100 Mpc.
- ◆ The galaxy superclusters and voids are believed to be the biggest structures in the Universe.

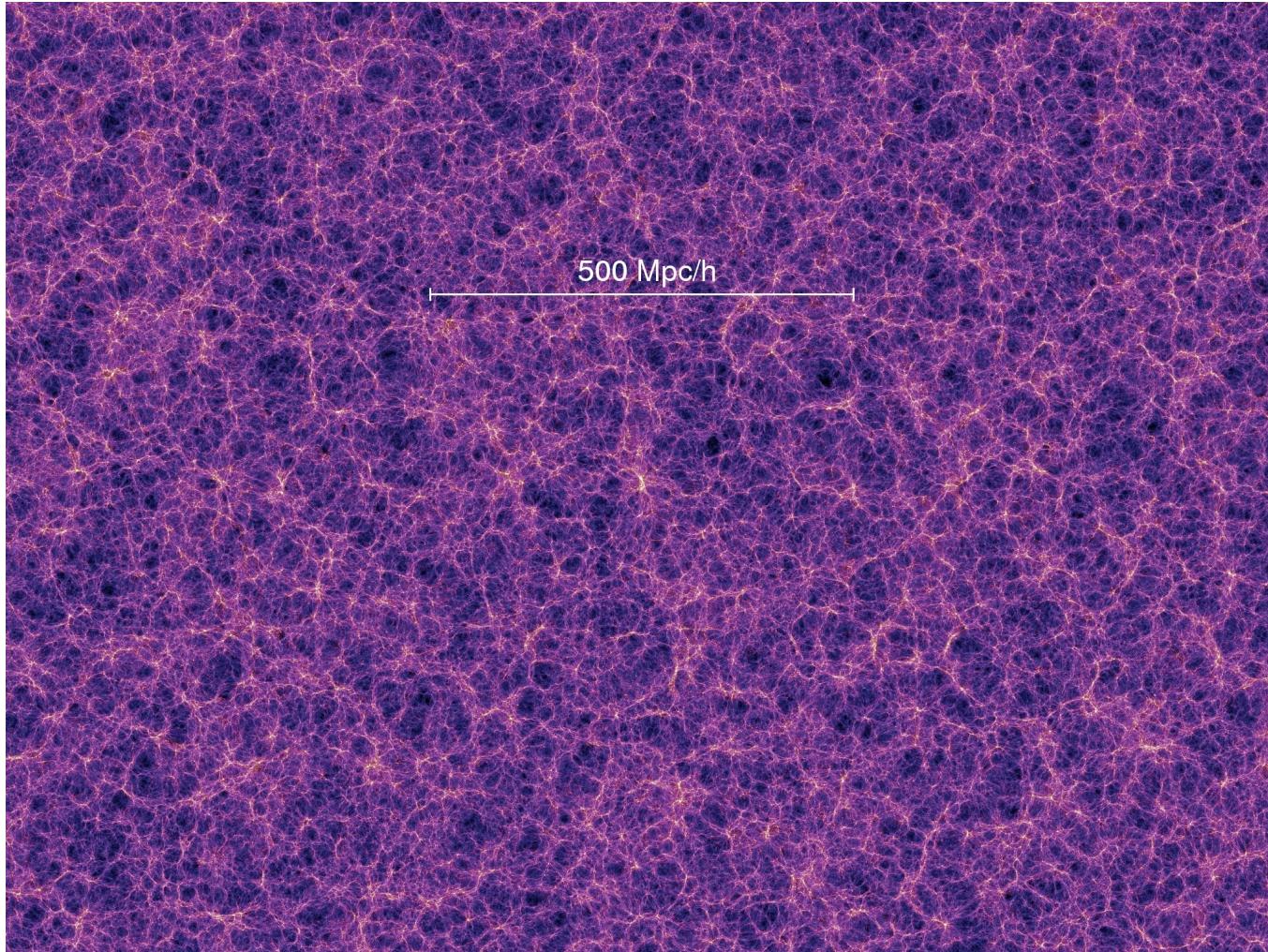
# MATTER DISTRIBUTION ON LARGE SCALES

[Image from the Millennium Simulation]



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[Image from the Millennium Simulation]

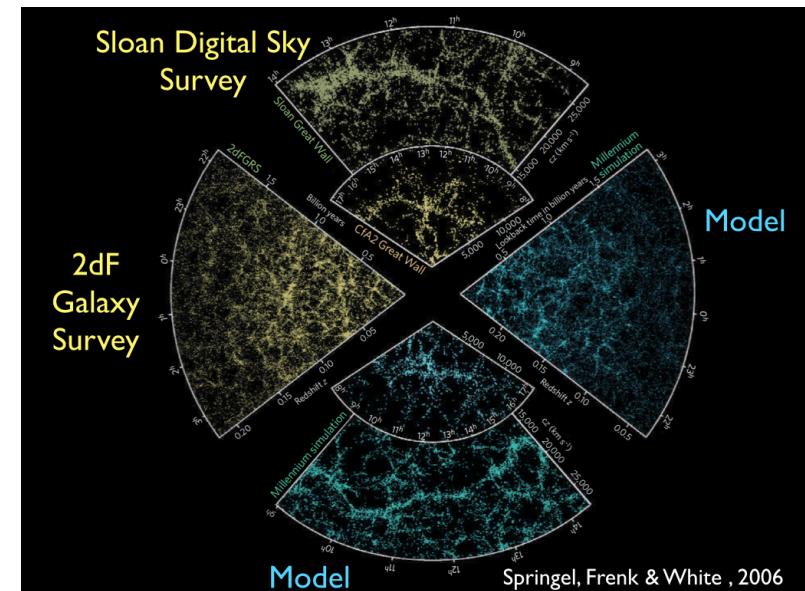
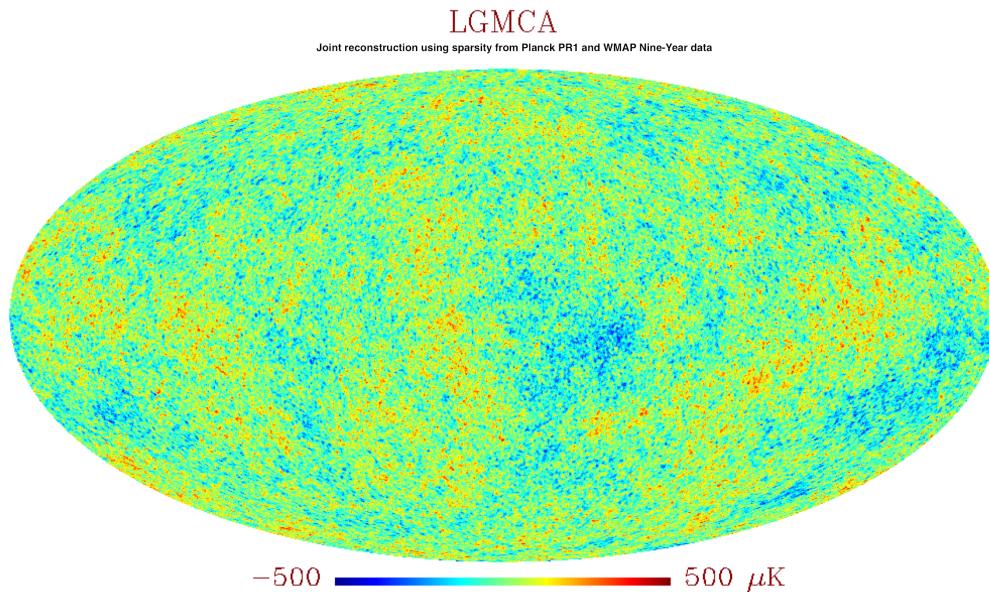


# HOMOGENEITY AND ISOTROPY

- ◆ The largest structures have a size of the order of 100 Mpc
  - ◆ Beyond this the Universe appears to be smooth, i.e. no larger structures on larger scales
  - ◆ We therefore say that the Universe on the largest scales is **homogeneous** (uniform) and **isotropic** (no preferred direction)
  - ◆ This is called **the cosmological principle**, and it is the underpinning of modern cosmology.

# OBSERVATIONS THAT SUPPORT THE COSMOLOGICAL PRINCIPLE

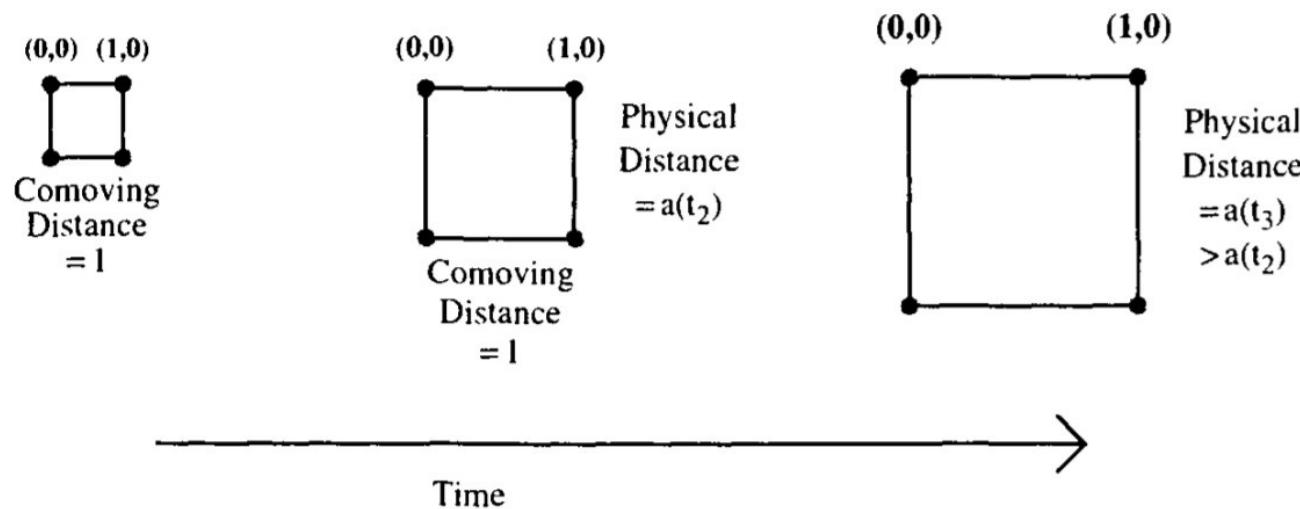
- ◆ The cosmic microwave background is smooth (fluctuations are only 1/100,000 at large scales).
- ◆ Large scale structure observations from galaxy surveys.
- ◆ Simulations of the Universe only in agreement with observations if the cosmological principle is assumed!



# EXPANSION OF THE UNIVERSE

- ◆ What does expansion mean?
- ◆ It **does not** mean that the Earth's orbit is going to get further from the Sun (gravity wins!).
- ◆ It **does not** mean that the stars within our galaxy are going to be more widely separated with time (gravity wins!).
- ◆ But it **does mean** that distant galaxies are getting further apart. There we do not have excess density (pretty much homogeneous/isotropic), and galaxies are flying apart from one another.
- ◆ **Hence:** the expansion of the Universe is felt on large scales, on which the cosmological principle applies.

# THE EXPANDING UNIVERSE: COMOVING COORDINATES



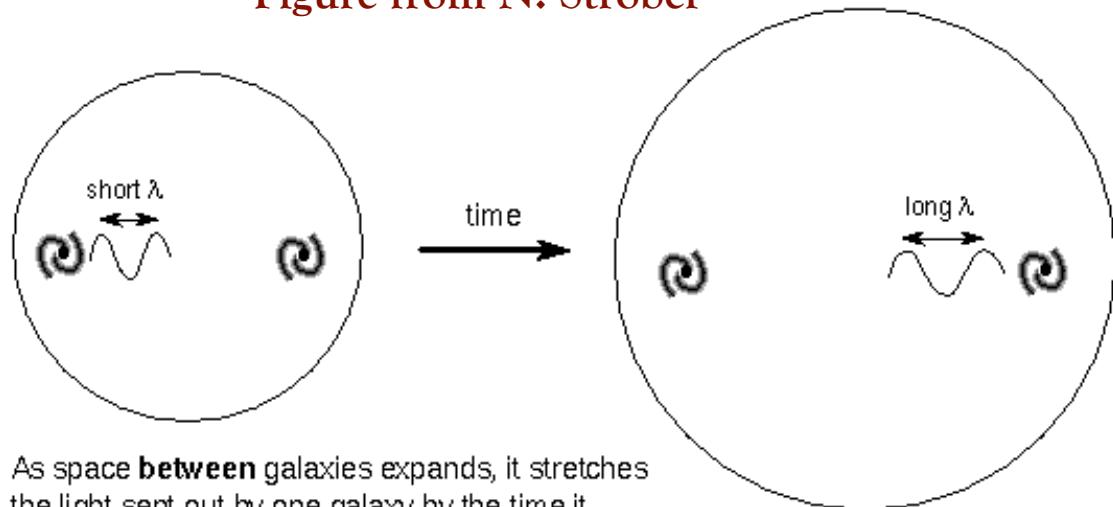
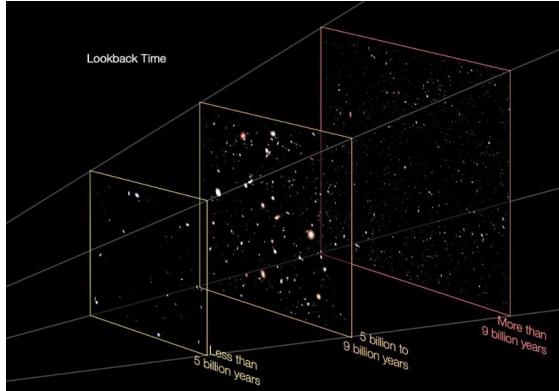
Expansion of the universe. The comoving distance between points on a hypothetical grid remains constant as the universe expands. The physical distance is proportional to the comoving distance times the scale factor, so it gets larger as time evolves.

$$d_{\text{phys}} = ad_{\text{com}}$$

Figure from S. Dodelson

# REDSHIFT

Figure from N. Strobel



- ◆ Redshift ( $z$ ) is related to the expansion (the scale factor,  $a$ )

$$1 + z = \frac{1}{a}$$

## Calculation of redshift, $z$

Based on wavelength	Based on frequency
$z = \frac{\lambda_{\text{obsv}} - \lambda_{\text{emit}}}{\lambda_{\text{emit}}}$	$z = \frac{f_{\text{emit}} - f_{\text{obsv}}}{f_{\text{obsv}}}$
$1 + z = \frac{\lambda_{\text{obsv}}}{\lambda_{\text{emit}}}$	$1 + z = \frac{f_{\text{emit}}}{f_{\text{obsv}}}$

# THEORY

What underlying theory or theories govern the evolution of the Universe?

- on small scales *Quantum Field Theory* (sets the initial conditions)
- on large scales *Einstein's General Relativity*
- to understand the “details” – what drives inflation, what is the nature of dark matter and dark energy – need to confront theory with observations, make sense of observations
- However, “details” – what is the dark stuff (dark energy, dark matter), what are the initial conditions, etc. – still unclear: cosmology is a very active area of research!

# SIMULATIONS

- ◆ Put initial conditions in a numerical simulation and solve the evolution equations
- ◆ It works! We get the structure we observe (clusters, voids, ...)

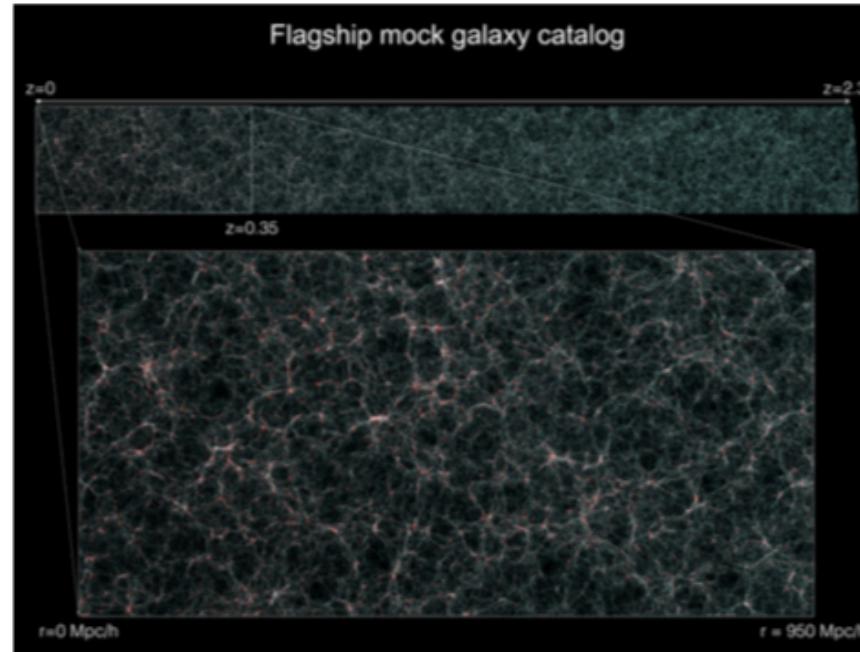
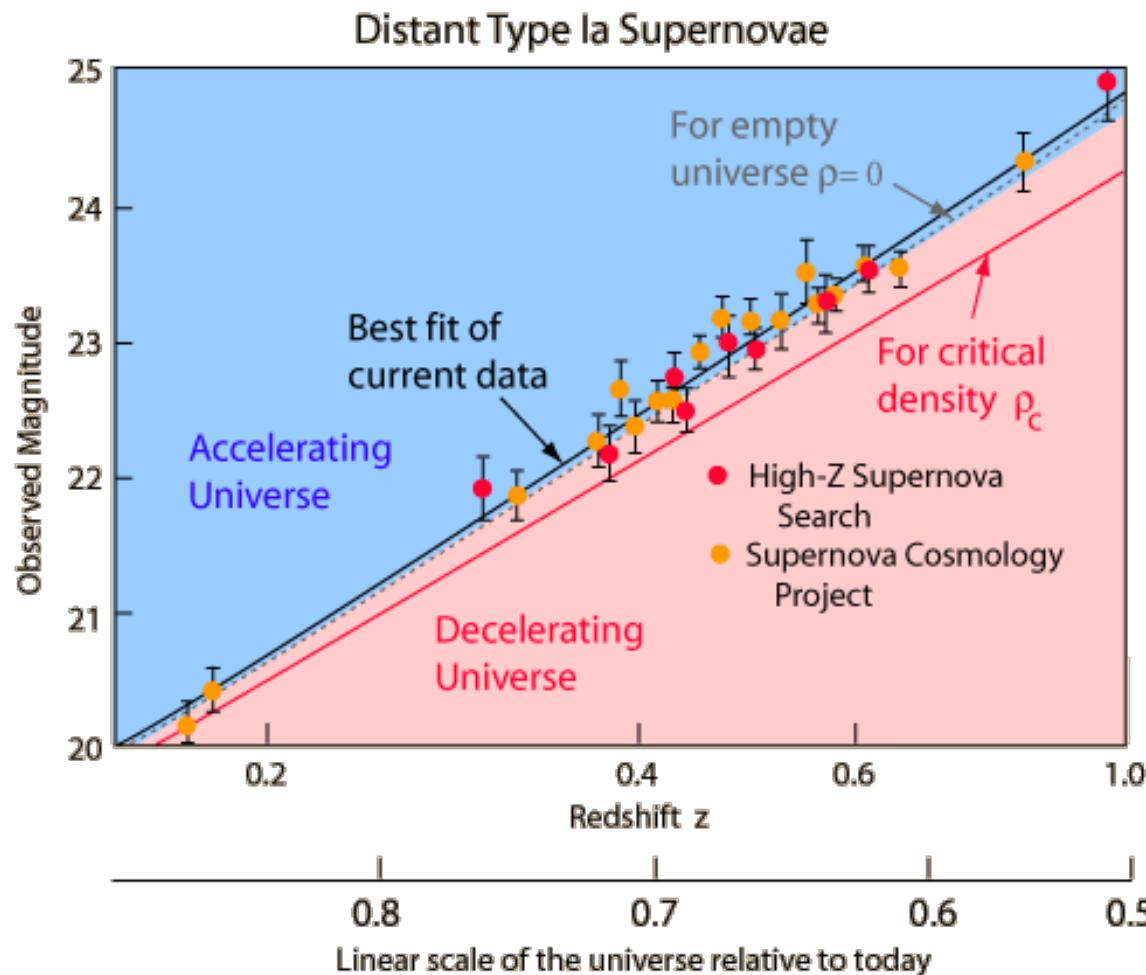


Figure: Euclid Consortium Cosmological Simulations Science Working Group.

# OBSERVATIONS / DATA ANALYSIS

Get the data, analyse them, and compare them with the predictions of your favourite model (informed by simulations). Statistics crucial for cosmology!



# OBSERVATIONS / DATA ANALYSIS

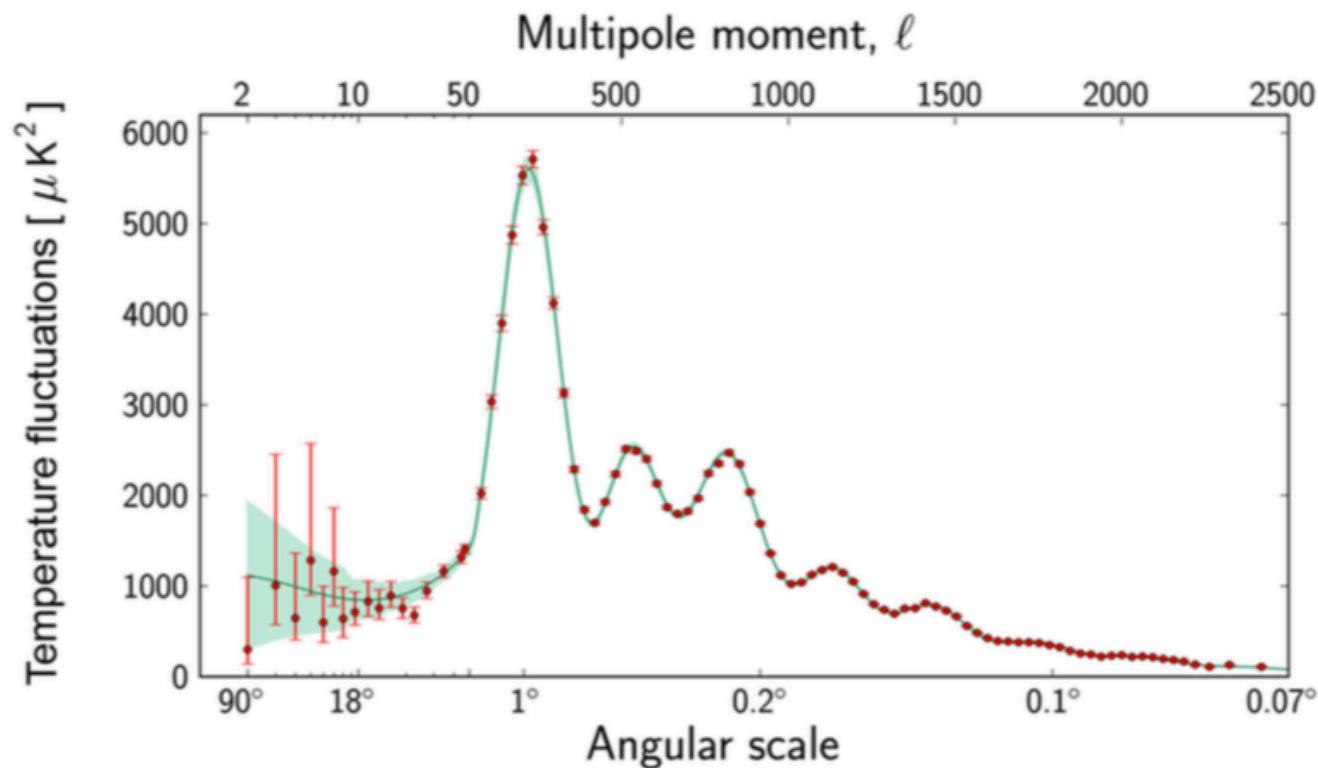
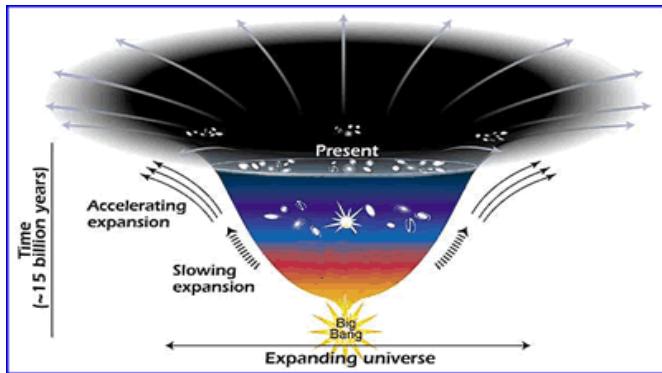


Figure: Planck 2015 data and best fit model. The agreement is near-perfect!

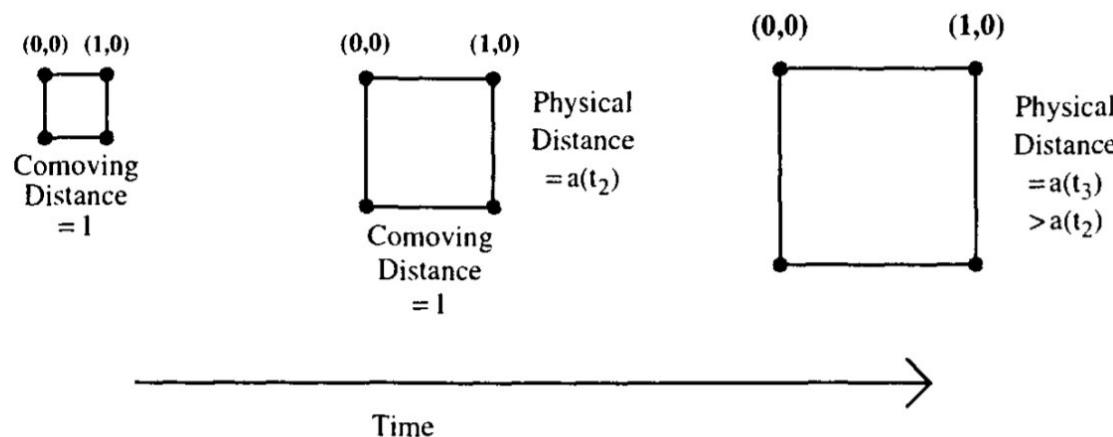
# THE SCALE FACTOR

- ◆ We already saw that the scale factor quantifies the expansion



- ◆ We set  $a=1$  today and it gets smaller as  $1/(1+z)$
- ◆ E.g.  $a=0.001$  for  $z=999$

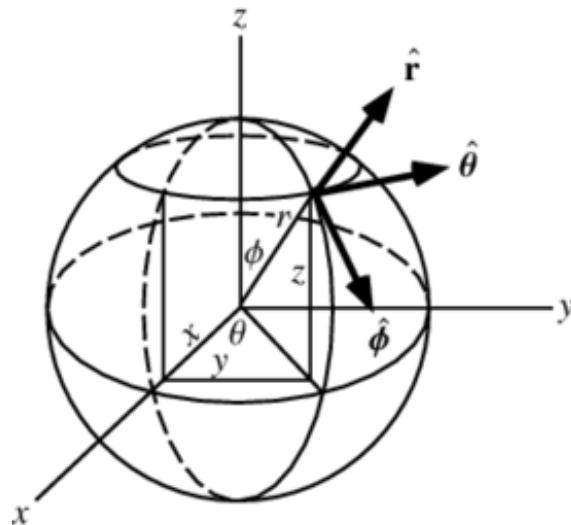
For low redshifts,  $z \approx v/c$ , so redshift directly measures recession velocity



**Figure 1.1.** Expansion of the universe. The comoving distance between points on a hypothetical grid remains constant as the universe expands. The physical distance is proportional to the comoving distance times the scale factor, so it gets larger as time evolves.

# THE METRIC

- ◆ We saw that coordinate differences on expanding grid are comoving distances
- ◆ To get a physical distance  $dl$ , from a set of coordinate differences, we need to use a metric.
- ◆ The metric for distances on the surface of a sphere is:



$$dl^2 = g_{ij} dx^i dx^j$$

$$dl^2 = R^2(d\theta^2 + \sin^2 \theta d\phi^2)$$

$$g_{\theta\theta} = R^2$$

$$g_{\phi\phi} = R^2 \sin^2 \theta$$

Adapted slide from Will Percival

## THE FRIEDMANN-ROBERTSON-WALKER METRIC

- ◆ A homogeneous, isotropic, expanding Universe is described by the FRW metric
- ◆ It contains the scale factor, which is a function of time

$$ds^2 = dt^2 - a(t)^2 \left( \frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right)$$

- ◆ The geometry of the Universe is parametrised by  $k$
- ◆ Spatially flat Universe:  $k=0$

$$ds^2 = -dt^2 + g_{ij}dx^i dx^j$$

$$g_{00} = -1 \quad g_{ij} = \delta_{ij} a(t)^2$$

# GENERAL RELATIVITY

## ◆ Einstein's Equations

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi GT_{\mu\nu}$$

Christoffel Symbol       $\Gamma^\alpha_{\mu\nu} = \frac{1}{2}g^{\alpha\beta} \left[ \frac{\partial g_{\beta\mu}}{\partial x^\nu} + \frac{\partial g_{\beta\nu}}{\partial x^\mu} - \frac{\partial g_{\mu\nu}}{\partial x^\beta} \right]$

Ricci (Curvature) Tensor

$$R_{\mu\nu} = \partial_\alpha \Gamma^\alpha_{\mu\nu} - \partial_\nu \Gamma^\alpha_{\mu\alpha} + \Gamma^\alpha_{\beta\alpha} \Gamma^\beta_{\mu\nu} - \Gamma^\alpha_{\beta\nu} \Gamma^\beta_{\mu\alpha}$$

Ricci Scalar       $R = g^{\mu\nu} R_{\mu\nu}$

Energy Momentum Tensor       $T_{\mu\nu}$

“Matter tells space how to curve, and space tells matter how to move”

## APPLICATION TO THE FRW METRIC

FRW metric for flat space has:

$$g_{00} = -1 \quad g_{ij} = \delta_{ij} a(t)^2$$

So (for example) the Christoffel symbol reduces to:

$$\begin{aligned}\Gamma^0_{ij} &= \frac{1}{2} g^{0\alpha} \left[ \frac{\partial g_{\alpha i}}{\partial x^j} + \frac{\partial g_{\alpha j}}{\partial x^i} - \frac{\partial g_{ij}}{\partial x^\alpha} \right] \\ &= \frac{1}{2} g^{00} \left[ \frac{\partial g_{0i}}{\partial x^j} + \frac{\partial g_{0j}}{\partial x^i} - \frac{\partial g_{ij}}{\partial x^0} \right] \\ &= \delta_{ij} \frac{1}{2} \frac{d}{dt} a^2 = \delta_{ij} \dot{a}a\end{aligned}$$

## THE TIME-TIME COMPONENT OF EINSTEIN'S EQUATIONS

$$R_{00} = -3 \frac{\ddot{a}}{a} \quad R = 6 \left[ \frac{\ddot{a}}{a} + \left( \frac{\dot{a}}{a} \right)^2 \right]$$

$$R_{00} + \frac{1}{2}R = 8\pi G T_{00} = 8\pi G \rho$$

### THE FRIEDMANN EQUATION FOR COSMOLOGICAL EVOLUTION

$$\left( \frac{\dot{a}}{a} \right)^2 \equiv H^2 = \frac{8\pi G}{3} \rho$$

# THE SPACE-SPACE COMPONENT OF EINSTEIN'S EQUATIONS

$$\frac{\ddot{a}}{a} + \frac{1}{2} \left( \frac{\dot{a}}{a} \right)^2 = -4\pi G P$$

P is the diagonal space-space component of the energy momentum tensor

Combine with Friedmann to get the acceleration equation:

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} (\rho + 3P)$$

Deceleration, unless  $\rho+3P < 0$

Energy conservation equation:

$$\dot{\rho} + 3 \left( \frac{\dot{a}}{a} \right) (\rho + P) = 0$$

# Friedman equation

- Einstein equations

$$H(t)^2 \equiv \left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi G}{3} \rho - \frac{K}{a^2}$$

*if not flat*

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} (\rho + 3P)$$

- Energy-momentum conservation

$$\dot{\rho} + 3H(\rho + P) = 0, \quad \rho = \sum_i \rho_i$$

- Two of these equations are independent

Three unknown quantities  $a, \rho, P$

→ we need to specify the equation of state  $w = P / \rho$

# EQUATION OF STATE PARAMETER

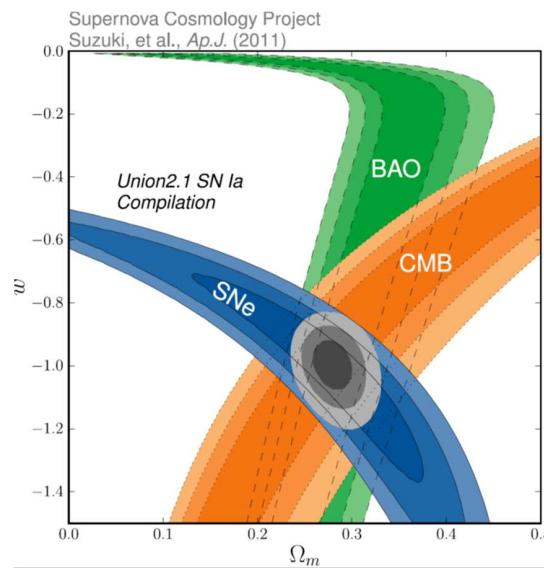
$$w = \frac{P}{\rho}$$

Non-Relativistic matter is pressureless  $w = 0$

Radiation is relativistic  $w = 1/3$

Dark energy? Cosmological constant has  $w = -1$

Quintessence has  $w = w(a)$



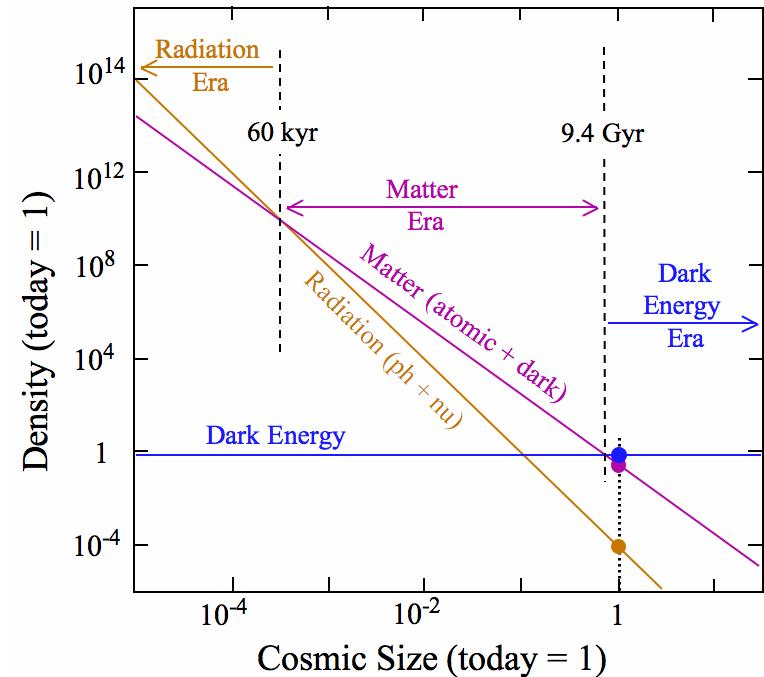
# EVOLUTION OF MATTER, RADIATION, DARK ENERGY

Pressureless matter:  $w=0$

$$\rho_m(a) = \rho_{m,0} a^{-3}$$

Radiation (relativistic):  $w=1/3$

$$\rho_\gamma(a) = \rho_{\gamma,0} a^{-4}$$



Dark energy with  $w=w(a)$ :

$$\rho(a) = \rho_0 \exp \left\{ 3 \int_a^1 \frac{da'}{a'} [1 + w(a')] \right\}$$

Cosmological constant:  $w=-1$        $\rho_{de} = \rho_{de,0}$

## DENSITY COMPONENTS

Radiation, matter (CDM and baryonic), dark energy + flat geometry

$$\left(\frac{\dot{a}}{a}\right)^2 \equiv H^2 = \frac{8\pi G}{3} \rho$$

For the Hubble rate H, we can write:

$$H^2 = \frac{8\pi G \rho}{3} = H_0^2 \{ \Omega_{\text{de}}(a) + [\Omega_b(a) + \Omega_{\text{cdm}}(a)] + \Omega_\gamma(a) \}$$

Where  $\Omega_i = \rho_i / \rho_{\text{crit}}$      $H_0 = 100h \text{ km sec}^{-1} \text{Mpc}^{-1}$

$$\rho_{\text{crit}} = 1.88h^2 \times 10^{-29} \text{ gcm}^{-3}$$

# THE SCALES OF OUR UNIVERSE

Hubble time:  $t_H = \frac{1}{H_0} = 9.78 \times 10^9 / h \text{ yr}$

Hubble distance:  $D_H = \frac{c}{H_0} = 3000 / h \text{ Mpc}$

## THE E(z) FUNCTION

We often express the Hubble rate via:  $H(z) = H_0 E(z) = 100hE(z)$

$$E(z) = \sqrt{\Omega_m(1+z)^3 + \Omega_r(1+z)^4 + \Omega_k(1+z)^2 + \Omega_\Lambda}$$

# COMOVING DISTANCE AND CONFORMAL TIME

Light travelling on a comoving grid:  $dx = cdt/a$

Total line of sight comoving distance (i.e.  
comoving distance from us to a distant galaxy):

$$d_{\text{comov}}(a) = \int_{t(a)}^{t_0} \frac{cdt'}{a(t')} = \int_a^1 \frac{cda'}{a'^2 H(a')}$$

Example if matter dominates:  $d_{\text{comov}}(a) = \frac{2c}{H_0} \left[ 1 - a^{1/2} \right]$

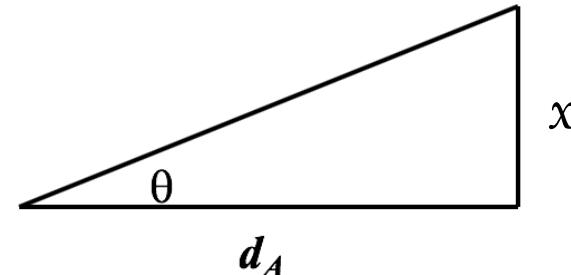
Conformal time: the comoving distance  
light has travelled since the big bang:

$$\eta \equiv \int_0^t \frac{cdt'}{a(t')}$$

# ANGULAR DIAMETER DISTANCE

Given an object perpendicular to the line of sight with physical size  $x$  and angular size  $\theta \ll 1$  as viewed from Earth, what is its distance?  
(assuming flat space  $k=0$ )

$$d_A = \frac{x}{\theta}$$



$$x = ad_{\text{com}}\theta$$

$$d_A = ad_{\text{com}} = d_{\text{com}}/(1+z)$$

Generalisation for non-flat cosmologies:

$$d_A(a) = \frac{a}{H_0 \sqrt{|\Omega_k|}} \left\{ \begin{array}{ll} \sinh[\sqrt{\Omega_k} H_0 d_{\text{comov}}] & \Omega_k > 0 \\ \sin[\sqrt{-\Omega_k} H_0 d_{\text{comov}}] & \Omega_k < 0 \end{array} \right.$$

# THE THERMAL HISTORY OF THE UNIVERSE: THE HIGHLIGHTS

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Event	time $t$	redshift $z$	temperature $T$
Inflation	$10^{-34}$ s (?)	—	—
Baryogenesis	?	?	?
EW phase transition	20 ps	$10^{15}$	100 GeV
QCD phase transition	20 $\mu$ s	$10^{12}$	150 MeV
Dark matter freeze-out	?	?	?
Neutrino decoupling	1 s	$6 \times 10^9$	1 MeV
Electron-positron annihilation	6 s	$2 \times 10^9$	500 keV
Big Bang nucleosynthesis	3 min	$4 \times 10^8$	100 keV

# THERMAL HISTORY OF THE UNIVERSE: THE HIGHLIGHTS

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Event	time $t$	redshift $z$	temperature $T$
Matter-radiation equality	60 kyr	3400	0.75 eV
Recombination	260–380 kyr	1100–1400	0.26–0.33 eV
Photon decoupling	380 kyr	1000–1200	0.23–0.28 eV
Reionization	100–400 Myr	11–30	2.6–7.0 meV
Dark energy-matter equality	9 Gyr	0.4	0.33 meV
Present	13.8 Gyr	0	0.24 meV

# THERMAL HISTORY OF THE UNIVERSE: THE HIGHLIGHTS

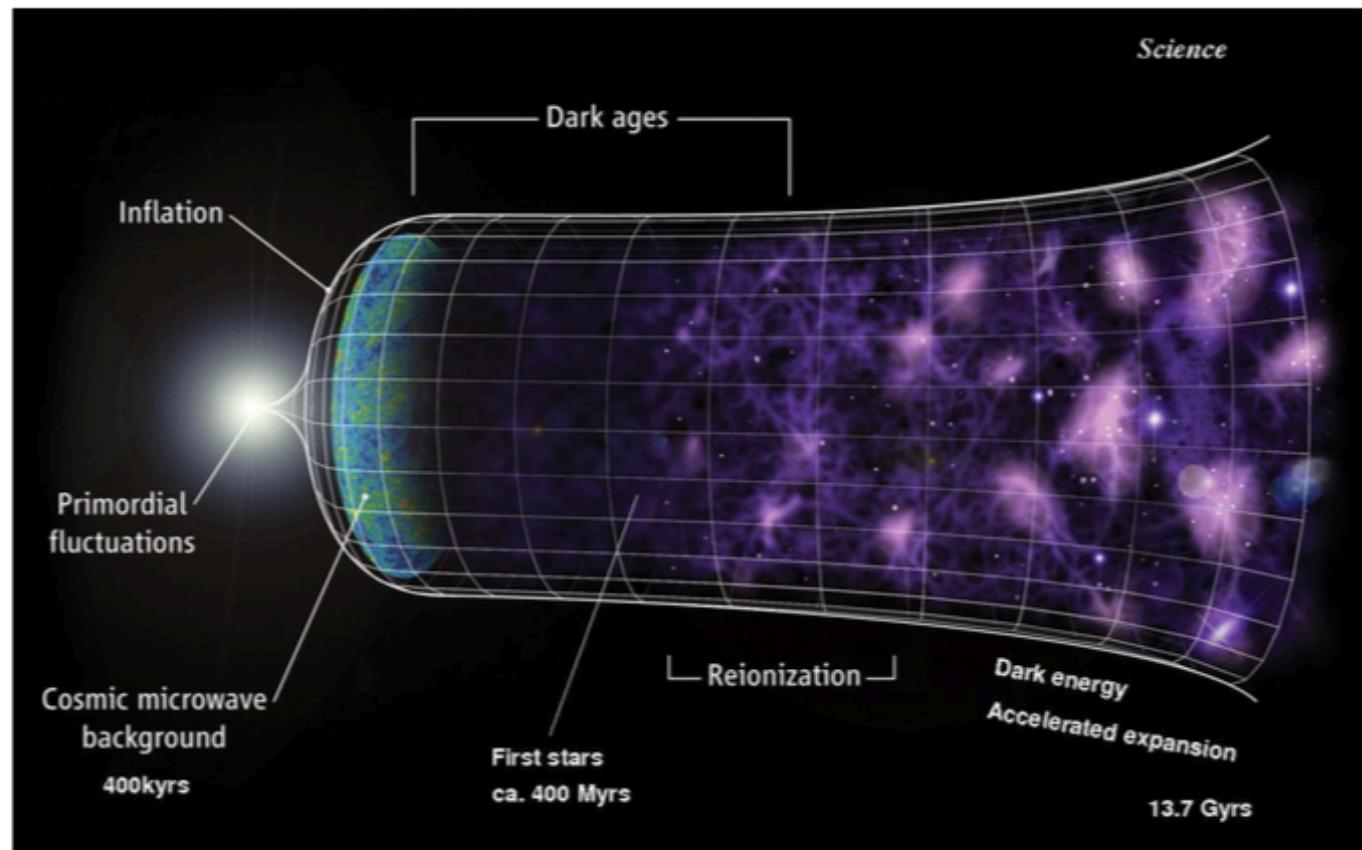
- ◆ The beginning - Hot Big Bang: note that **temperature evolves as  $1/a$**
- ◆ **Inflation** and end of inflation
- ◆ **Baryogenesis:** QFT requires the existence of antiparticles. We do observe an overabundance of matter (baryons) over anti-matter.
- ◆ **Electroweak phase transition:** At 100 GeV particles get masses via Higgs mechanism. This leads to a change in the strength of the weak interaction.
- ◆ **QCD phase transition:** Below 100 MeV strong interactions between quarks and gluons dominate. Baryons (such as  $n$  and  $p$ ) are formed.
- ◆ **Nucleosynthesis:** the lightest nuclei are formed 3 mins after the Big Bang / Radiation domination

# THERMAL HISTORY OF THE UNIVERSE: THE HIGHLIGHTS

- ◆ **Matter-Radiation equality**
- ◆ **Recombination:** Electrons and protons form neutral hydrogen atoms.  $e^- + p^+ \rightarrow H + \gamma$
- ◆ **Photon decoupling:** Before recombination the strongest coupling between the photons and the rest of the plasma is through Thomson scattering. But recombination results in sharp drop in electron density. Photons decouple. They have since streemed freely through the Universe  $\rightarrow$  CMB
- ◆ **Reionization:** First stars start ionising the neutral hydrogen around them “Cosmic Dawn”. By the end of this process, Universe completely ionised (but HI still found within galaxies).
- ◆ **Galaxy formation - dark energy domination - now and the future!**

# A BRIEF OVERVIEW OF THE UNIVERSE

The cosmological standard model: the evolution of the Universe.



# REFERENCES / FURTHER READING

