

Name: SCL

ID #: \_\_\_\_\_

Show your work. Fill in the appropriate blanks

A set of 4 vectors ( $a_1$   $a_2$   $a_3$   $a_4$ ) row reduces to

$$\begin{pmatrix} 1 & 2 & 0 & 1 \\ 0 & 0 & 1 & 5 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$x_1 + 2x_2 + x_4 = 0$$

$$x_3 + 5x_4 = 0$$

Q1) Circle pivot columns and put a box around pivot entries.

Q2) Are the vectors LI?

NO

Q3) The pivot variables are

 $x_1$   $x_3$ 

Q4) The free variables are

 $x_2$   $x_4$ Q5) Write down a formula for all solutions to  $Ax = 0$ .

$$x = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \boxed{x_2} \begin{pmatrix} -2 \\ 1 \\ 0 \\ -1 \end{pmatrix} + \boxed{x_4} \begin{pmatrix} 0 \\ 0 \\ -5 \\ 1 \end{pmatrix} + \boxed{\phantom{x_2}} \begin{pmatrix} \phantom{-2} \\ \phantom{1} \\ \phantom{0} \\ \phantom{-1} \end{pmatrix} + \boxed{\phantom{x_4}} \begin{pmatrix} \phantom{-2} \\ \phantom{1} \\ \phantom{0} \\ \phantom{-1} \end{pmatrix}$$

Q6) Fill in any pivot columns.  $\begin{pmatrix} a_1 \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}, \begin{pmatrix} a_3 \\ \phantom{a_3} \\ \phantom{a_3} \\ \phantom{a_3} \end{pmatrix}, \begin{pmatrix} \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}, \begin{pmatrix} \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}, \begin{pmatrix} \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}$

Q7) Write down two different non-trivial solutions to  $Ax = 0$ .  $\begin{pmatrix} -2 \\ 1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ -5 \\ 1 \end{pmatrix}$

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The AM of  $(a_1 \ a_2 \ a_3 \ a_4 \ b)$  for  $Ax = b$  row reduces to

$$\begin{pmatrix} 1 & 2 & 0 & 1 & 1 \\ 0 & 0 & 1 & 5 & 2 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

*Inconsistent*

$$x_1 + 2x_2 + x_4 = 0$$

$$x_3 + 5x_4 = 0$$

Q1) Circle pivot columns and put a box around pivot entries.

Q2) Are the vectors  $(a_1 \ a_2 \ a_3 \ a_4)$  LI?NO

Q3) The pivot variables are

 $x_1 \ x_3$ 

Q4) The free variables are

 $x_2 \ x_4$ Q5) Write down a formula for all solutions to  $Ax = b$ .

$$x = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} = \begin{pmatrix} \text{No Soln} \end{pmatrix} + \boxed{\phantom{0}} \begin{pmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{pmatrix} + \boxed{\phantom{0}} \begin{pmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{pmatrix} + \boxed{\phantom{0}} \begin{pmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{pmatrix} + \boxed{\phantom{0}} \begin{pmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{pmatrix}$$

Q6) Fill in any pivot columns.  $\begin{pmatrix} a_1 \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}, \begin{pmatrix} a_3 \\ \phantom{a_3} \\ \phantom{a_3} \\ \phantom{a_3} \end{pmatrix}, \begin{pmatrix} \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \\ \phantom{a_1} \end{pmatrix}$

Q7) Write down two different non-trivial solutions to  $Ax = 0$ .  $\begin{pmatrix} -2 \\ 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} -1 \\ 0 \\ -5 \\ 1 \end{pmatrix}$

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Q1) Explain how to invert a square matrix A.

Now Reduce  $(A | I) \sim (I | A^{-1})$   
 if A is invertible. Recd of  $A^{-1}$

Q2) If the matrix  $\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 2 \\ 2 & 4 & 8 \end{pmatrix}$  is invertible complete

$$A^{-1} = \begin{pmatrix} 0 & -2 & \frac{1}{2} \\ -2 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

write DNE in the ~~splace~~ for the matrix in the inverse does Not Exist!

In[2]:= **Inverse** $\left[\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 2 \\ 2 & 4 & 8 \end{pmatrix}\right]$  // **MatrixForm**

Out[2]//MatrixForm=

$$\begin{pmatrix} 0 & -2 & \frac{1}{2} \\ -2 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

$$\begin{aligned} & \begin{pmatrix} 0 & 0 & 1 & | & 1 & 0 & 0 \\ 0 & 1 & 2 & | & 0 & 1 & 0 \\ 2 & 4 & 8 & | & 0 & 0 & 1 \end{pmatrix} \sim \begin{pmatrix} 2 & 4 & 8 & | & 0 & 0 & 1 \\ 0 & 1 & 2 & | & 0 & 1 & 0 \\ 0 & 0 & 1 & | & 1 & 0 & 0 \end{pmatrix} \\ & \sim \begin{pmatrix} 2 & 4 & 8 & | & 0 & 0 & 1 \\ 0 & 1 & 0 & | & -2 & 1 & 0 \\ 0 & 0 & 1 & | & 1 & 0 & 0 \end{pmatrix} \sim \begin{pmatrix} 2 & 4 & 0 & | & -8 & 0 & 1 \\ 0 & 1 & 0 & | & -2 & 1 & 0 \\ 0 & 0 & 1 & | & 1 & 0 & 0 \end{pmatrix} \\ & \sim \begin{pmatrix} 2 & 0 & 0 & | & 0 & -4 & 1 \\ 0 & 1 & 0 & | & -2 & 1 & 0 \\ 0 & 0 & 1 & | & 1 & 0 & 0 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & 0 & | & 0 & -2 & \frac{1}{2} \\ 0 & 1 & 0 & | & -2 & 1 & 0 \\ 0 & 0 & 1 & | & 1 & 0 & 0 \end{pmatrix} \end{aligned}$$