

Name: Key

ID #: _____

As always you need to show your work. Fill in the appropriate blanks

1. The char eqn of A is $\begin{pmatrix} 6 & 2 & 0 \\ 0 & 1 & 2 \\ 0 & -2 & 1 \end{pmatrix}$ is $(6-\lambda)[(1-\lambda)(1-\lambda)+4] = 0$ with evals

$$6, 1 \pm 2i$$

$$\begin{aligned} (1-\lambda)^2 &= -4 \\ \lambda - 1 &= \pm 2i \\ \lambda &= 1 \pm 2i \end{aligned}$$

2. The char eqn of A is $\begin{pmatrix} 6 & 2 \\ -3 & 1 \end{pmatrix}$ is $(6-\lambda)(1-\lambda)+6 = 0$ with evals

$$3, 4$$

$$\begin{aligned} \lambda^2 - 6\lambda - 1\lambda + 6 + 6 &= 0 \\ \lambda^2 - 7\lambda + 12 &= 0 \\ \lambda &= \frac{7 \pm \sqrt{49 - 48}}{2} = \frac{7 \pm 1}{2} = 3 \text{ or } 4 \end{aligned}$$

3. Matrices A and B have the same eigenvalues if they are similar.

Matrices A and B are similar if

$$A = P B P^{-1}$$

for some

invertible P