Name:

Show an appropriate amount of work. You can (and probably should) check your work with a computer.

- 1. Compute the magnitude and argument for
- **1.1.**  $Z = \left(\frac{i}{1+i}\right)^3$

abs(z) =	

- arg(z) =
- **1.2.**  $Z = \left(\frac{1+\hat{i}}{\sqrt{1+3}\,\hat{i}}\right)^3$ 
  - abs(z) =
  - arg(z) =
- **1.3.** The roots of  $z^4 = -64$ 
  - abs(z) =
  - arg(z) =
- **1.4.** The roots of  $z^2 + 2iz + 5 = 0$ 
  - abs(z) =
  - arg(z) =
- **1.5.**  $Z = \bar{l}^{\bar{l}}$ 
  - abs(z) =
  - arg(z) =

- $\mathbf{2.1.} \ Z = \left(\frac{\bar{l}}{1+\bar{l}}\right)^3$   $Z = \boxed{ + \bar{l}}$
- 2.2.  $Z = \left(\frac{1+\bar{i}}{\sqrt{1+3\,\bar{i}}}\right)^3$   $Z = \boxed{ + \bar{i}}$
- **2.3.** The roots of  $z^3 = -64$

$$Z_{1} = \boxed{ + i }$$

$$Z_{2} = \boxed{ + i }$$

$$Z_{3} = \boxed{ + i }$$

**2.4.** The roots of  $z^2 + 2iz + 5 = 0$ 

$$Z_1 = \boxed{ + i }$$

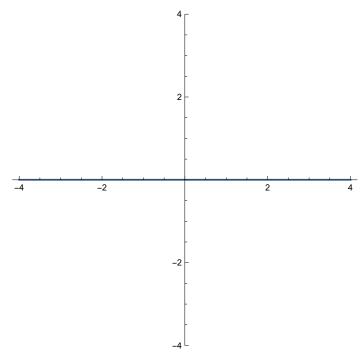
$$Z_2 = \boxed{ + i }$$

 $Z = \bar{l}^{\bar{l}}$   $Z = + \bar{l}$ 

## 3. Sketch Points

- **3.1.** Sketch the set of points  $C_1$  that satisfy |z-2| < 1. Make sure you label the set.
- **3.2.** Sketch the set of points  $C_2$  that satisfy  $\operatorname{im}(z-2)=1$ . Make sure you label the set.
- **3.3.** Sketch the set of points  $C_3$  that satisfy  $arg(z-2) = \pi/4$ . Make sure you label the set.





**4.1.** For cos(z) complete the

following  $u(x, y) = \boxed{ and v(x, y) = }$ 

 $\partial_X u =$  and  $\partial_X v =$ 

 $\partial_y u =$  and  $\partial_y v =$ 

Analytic Yes or No

**4.2.** For  $i x^2 - 2xy - i y^2$  complete the following

u(x, y) = and v(x, y) =

 $\partial_X u =$  and  $\partial_X v =$ 

 $\partial_y u =$  and  $\partial_y v =$ 

Analytic Yes or No .

If yes f(z) =

**4.3.** For  $i x^2 - 2xy - y^2$  complete the following

u(x, y) = and v(x, y) =

 $\partial_X u = \boxed{ }$  and  $\partial_X v = \boxed{ }$ 

 $\partial_y u =$  and  $\partial_y v =$ 

Analytic Yes or No

If yes f(z) =

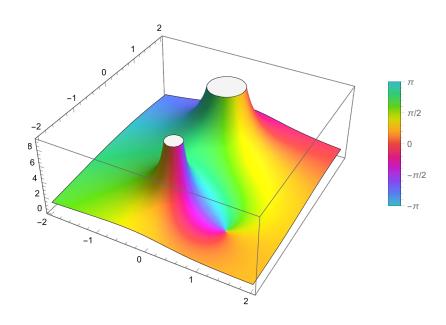
**5.** Is  $e^{x-iy}$  analytic? Yes or No . Show your work below.

**6.** Label poles with  $P_1, P_2, \dots$  Label zeros with  $Z_1, Z_2, \dots$ 

$$f[z] := 3 \frac{z - 1 + i}{(1 + z^2)}$$

ComplexPlot3D[f[z],

{z, 2}, PlotLegends → Automatic]



7. Complete the following. The TS

$\arctan(z) = \sum_{k=0}^{\infty} z_{k}$	$a_k z$	whe	ere
$a_k =$			
converges for			Justify your

convergence statement using a Calculus II theorem. Give a simpler complex analytic justification below.

8. Complete the following. The TS

 $log(2 + z) = \sum_{k=0}^{\infty} a_k z^k$  where  $a_k =$ converges for . Justify your

convergence statement using a Calculus II theorem. Give a simpler complex analytic justification below.

9. Label and explain the singularity and color discontinuity visible in the plot below using appropriate language. The TS

$$f(z) = \sum_{k=0}^{\infty} a_k (z - z_0)^k \text{ with } z_0 = -2 + 2i \text{ has}$$

$$a_k = \boxed{\qquad} \text{and converges for}$$

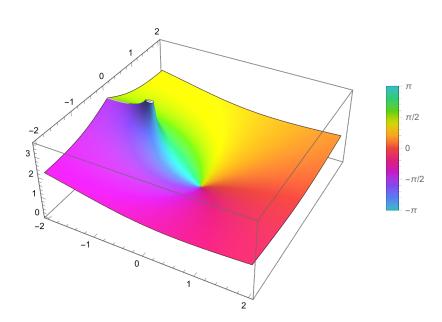
$$\begin{vmatrix} z - z_0 \end{vmatrix} < \boxed{\qquad} \text{. Explain what the TS}$$

converges to around the color discontinuity.

$$In[*]:= f[z_] := Log[1 + z]$$

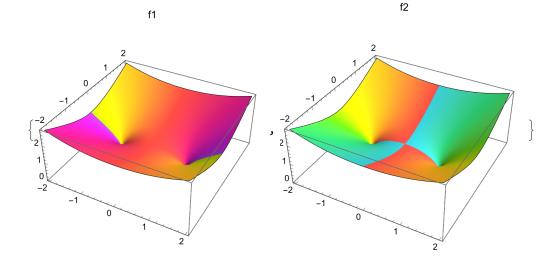
ComplexPlot3D[f[z],

{z, 2}, PlotLegends → Automatic]

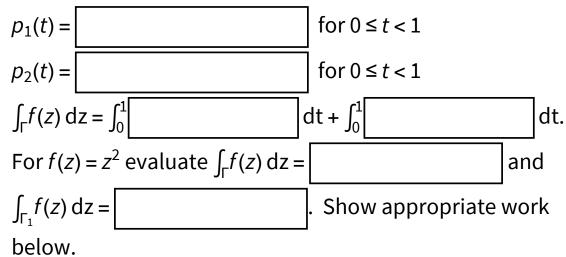


10. Label and explain the singularity and color discontinuity visible in the plots below using appropriate language. Explain why you might expect  $f_1$  to match  $f_2$ . Explain why they do not match using appropriate language.

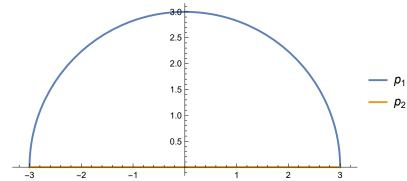
f1[z]:= 
$$\sqrt{1-z^2}$$
  
f2[z]:=  $i \sqrt{z^2-1}$   
{ComplexPlot3D[f1[z], {z, 2}, PlotLabel  $\rightarrow$  "f1"],  
ComplexPlot3D[f2[z], {z, 2}, PlotLabel  $\rightarrow$  "f2"]}



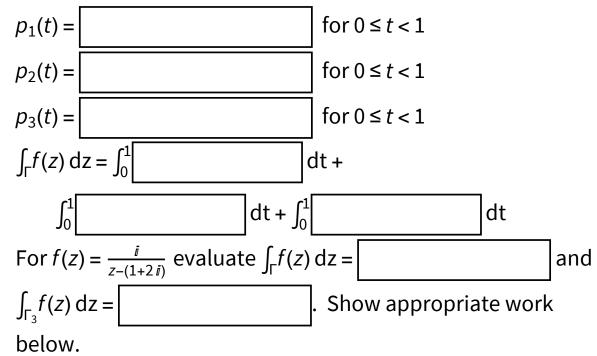
**11.** For the closed counter clockwise contour  $\Gamma$  shown below

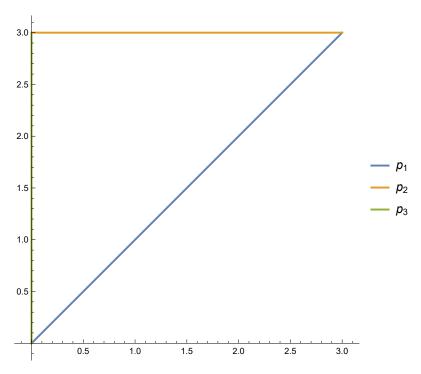






**12.** For the closed counter clockwise contour  $\Gamma$  shown below





**13.** Compute 
$$\int_{\Gamma} \frac{e^z}{(z^2+4)(z-1)} dz = \boxed{}$$
 for the counter clockwise contour  $\Gamma$ . Show appropriate work.

 $p1[t_] := (E^{2\pi it} + 1.2)^2$ 

 $ParametricPlot[ReIm[p1[t]], \{t, 0, 1\}, PlotLegends \rightarrow \{"\Gamma"\}]$ 



