

Vectors and Matrices

1. Write a program that reads a 3x3 matrix of integers and multiplies the elements of the main diagonal of the matrix by a number k. Print the matrix on the screen before and after the multiplication.
2. Write a program that reads two 2x2 matrices A and B of integers and prints the matrix C which is the sum of matrices A and B.
3. Write a program that reads the dimensions of two matrices A and B, and then reads the two matrices (the elements must be integers). If the matrices are of compatible sizes for multiplication, multiply the matrices. Print the matrices A, B and the matrix resulting from the multiplication.
4. Write a program that reads a 3x3 matrix of integers and returns the row with the largest sum. Print the matrix, the row with the largest sum and the sum on the screen.
5. Write a program that reads the order of a square matrix A (up to 100), then reads its values and writes its transpose AT, where $AT[i][j] = A[j][i]$
6. A go-kart track allows 10 laps for each of 6 racers. Write a program that reads the names and times (in seconds) of each lap of each race and stores the information in a matrix. At the end, the program should inform:
 - A. Who had the best lap of the race, and in which lap
 - B. Final classification in order (1st, the champion)
 - C. Which lap had the fastest average
7. Write a program that reads a 6x3 matrix with real numbers, calculates and displays:
 - (a) the largest element of the matrix and its respective position (row and column);

(b) the smallest element of the matrix and its respective position. 8. Write a program that reads two matrices A and B of integers and checks if both are inverses (i.e., if the multiplication of A by B is the identity matrix). 9. Write a program that reads a 3x3 matrix that represents a tic-tac-toe board and indicates which position should be played to win the game (if possible) or at least avoid a defeat. 10. Write a program that reads two grades for each student in two classes. Each class has 3 students. Store the data in a matrix M. Each student must have three grades (the two entered and the average of these two). Calculate the average of each class and store it in a vector CLASS. Report which class has the highest average, and which students had an average higher than the average of their class.