

CS202 - Algorithm Analysis

Graph Algorithms Module-2

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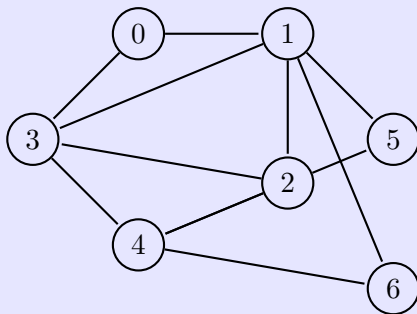
Sedgewick 4.1, 4.2

Graph Traversals

- **Graph traversal** is a process used to visit each node or vertex in a connected graph.
- Two popular algorithms are generally used for the traversal of a graph, namely, Depth First Search (DFS) and Breadth First Search (BFS).

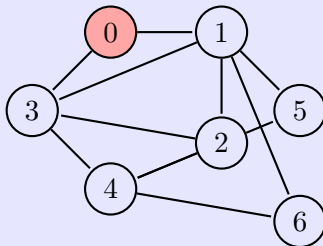
An important: application of graph traversal is to detect cycles in a Graph.

BFS example



Traverse graph by starting from 0

BFS example (1)

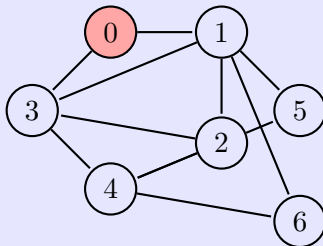


Queue

0

Result

BFS example (1)



Queue

\emptyset

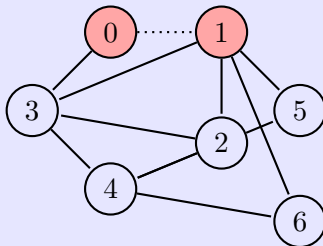
1

3

Result

0

BFS example (1)



Queue

4

3

2

5

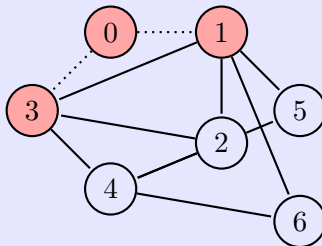
6

Result

0

1

BFS example (1)



Queue

3

2

5

6

4

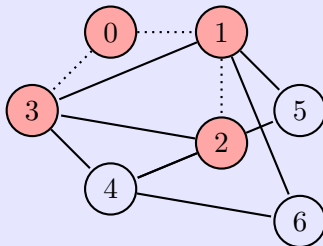
Result

0

1

3

BFS example (1)



Queue

2

5

6

4

Result

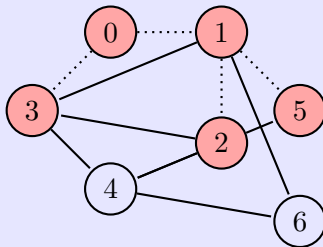
0

1

3

2

BFS example (1)



Queue

5

6

4

Result

0

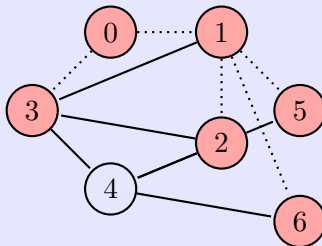
1

3

2

5

BFS example (1)



Queue

6

4

Result

0

1

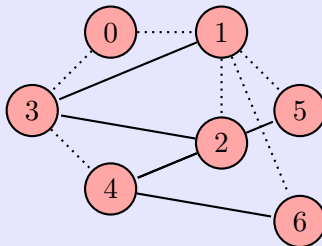
3

2

5

6

BFS example (1)



Queue

4

Result

0

1

3

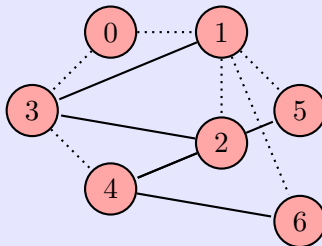
2

5

6

4

BFS example (1)



Queue

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Result

0	1	3	2	5	6	4
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Breadth First Search (BFS) Algorithm

BFS(G, u)

Input: Graph $G = (V, E)$ directed or undirected, vertex u (element of) V

Output: BFS traversal order from node u

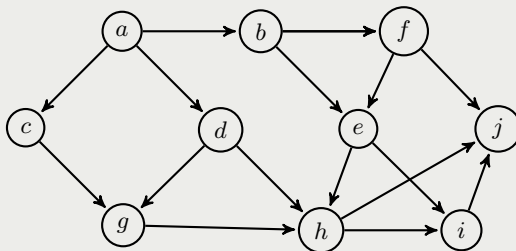
```
create a Queue Q
enqueue(Q, u)
while(Q is not empty)
    s = Dequeue(Q)
    if (visited of vertex s == false)
        result.add(s)
        visited of vertex s = true
    end if
    for all m (element of) neighbours of s
        if (visited of vertex m == false)
            enqueue(Q, m)
        end if
    end for
end while
return result
```

Complexity Analysis

Time Complexity - $O(V + E)$

Try out 1

- **Compute** the BFS traversal order in the Graph provided below, starting from vertex **a**. Show the Queue and Result array in your solution.



Reading Assignment

Sedgewick 4.1, 4.2

Questions?

Please ask if there are any Questions!