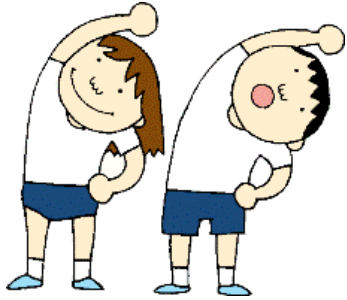


# Warm-Up!

- You may have to use R interpreter from the terminal. Type "R" at the terminal and copy and paste in your code from your editor.
- General Question: What correlations exist in the BFI data concerning the factors of one's personality?
- Use **with()** and **corPlot()** to study correlations in the BFI dataset. Now Find:
  - The top three most positively-correlated columns
  - The top three most negatively-correlated columns
  - The top three least-correlated columns.

Ideas? See File: [warmUp\\_correlations.r](#)



# Warm-Up!

- Returning to the codebook, working with your group, can you offer a suggestions to explain the typeess of correlations that you found?
- Use GGplot to graph some of your correlations. Can you tell from the graph what the correlation is?

Ideas? See File: [warmUp\\_correlations.r](#)

# **Data Analytics**

## **CS301**

### **Modeling: Formal Basics**

**Fall 2018**  
**Oliver Bonham-Carter**





# Modeling Basics

- What are models?
  - Data does not provide much insight unless something can be learned from it.
  - The ability to use data to extract meaning and extra value (the learning)
- Let's talk about...
  - How to extract some meaning from your data
  - How to make predictions using your data as training



# Modeling Basics

- Topics include
  - Modeling
  - Linear regression
  - Multivariate regression
  - Interaction terms



# Types of Models (i)

- **Support Vector Machines**

- Supervised learning models with associated learning algorithms that analyze data used for classification and regression analysis.

- **Generalized Linear Models**

- Flexible generalization of ordinary linear regression that allows for response variables that have error distribution models other than a normal distribution

- **Generalized additive models**

- Generalized linear model in which the linear predictor depends linearly on unknown smooth functions of some predictor variables, and interest focuses on inference about these smooth functions



# Types of Models (ii)

- **Linear Regression**

- Linear approach for modeling the relationship between a scalar dependent variable  $y$  and one or more explanatory variables (or independent variables) denoted  $X$
- *(we have begun this study)*

- **LOESS Regression**

- Combining much of the simplicity of linear least squares regression, but building with the flexibility of nonlinear regression.

- **Logistic Regression**

- Models where the dependent variable is categorical (i.e., 0's or 1's as factors)



# Let's Begin Our Discussion...

- Working with models begins with a basic question to answer from the analysis of data.
- We will walk through each of these with a formal discussion

Q1: Do taller people  
make more money?

Q2: Do hotter places  
have more crime?





# How Do we Answer The Question?

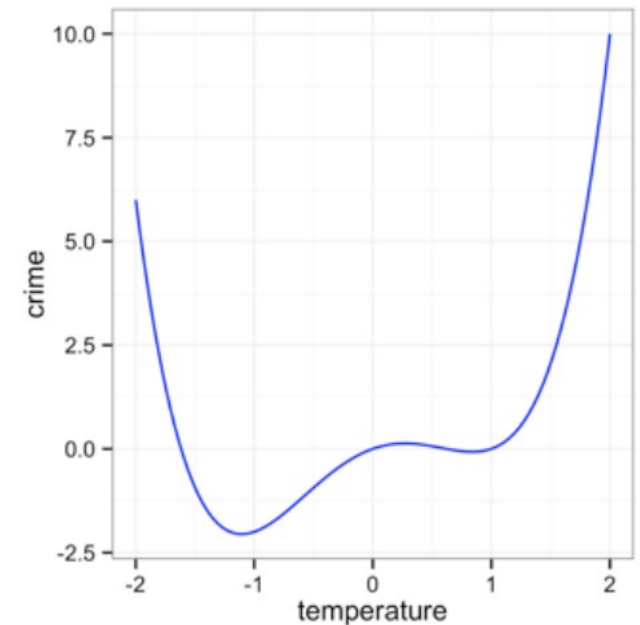
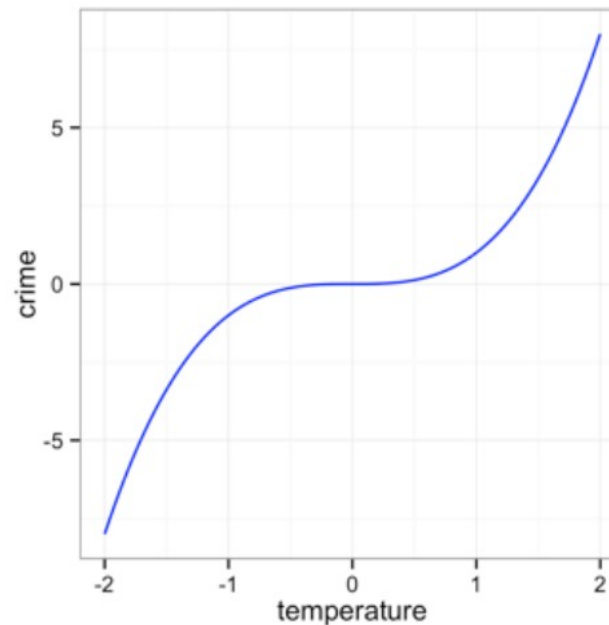
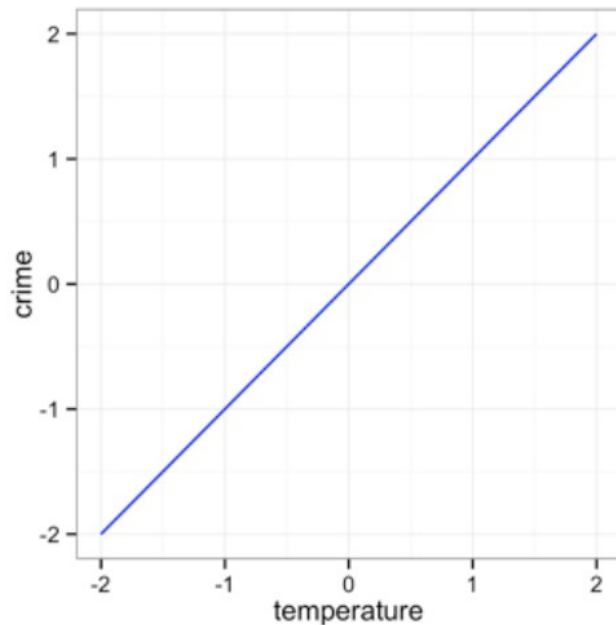
- Modeling: We employ a computational framework which we used data to build (for training).
- Play with the model to see what happens when we change a part of the data ...

***What if...***



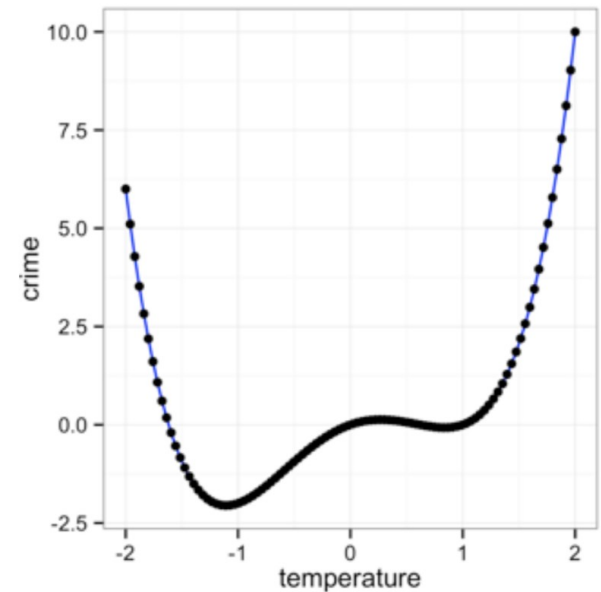
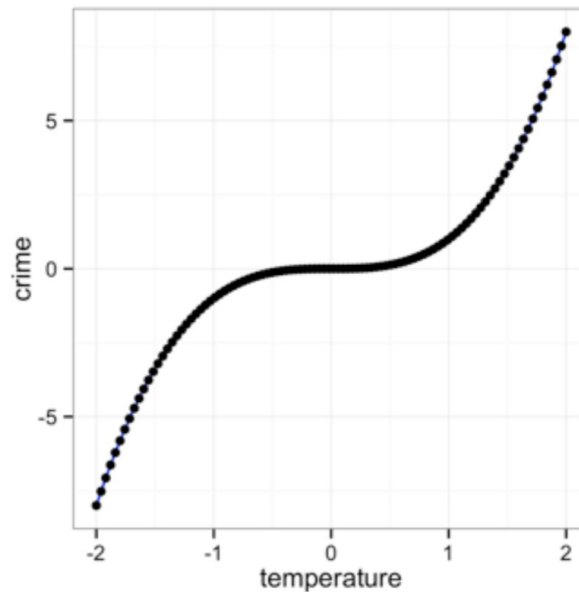
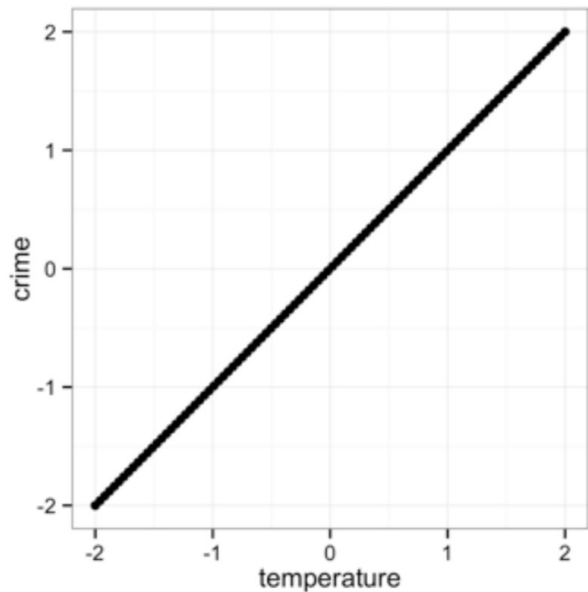
# Functions: the *stuff* behind the models

- A function is a mathematical description of a relationship.



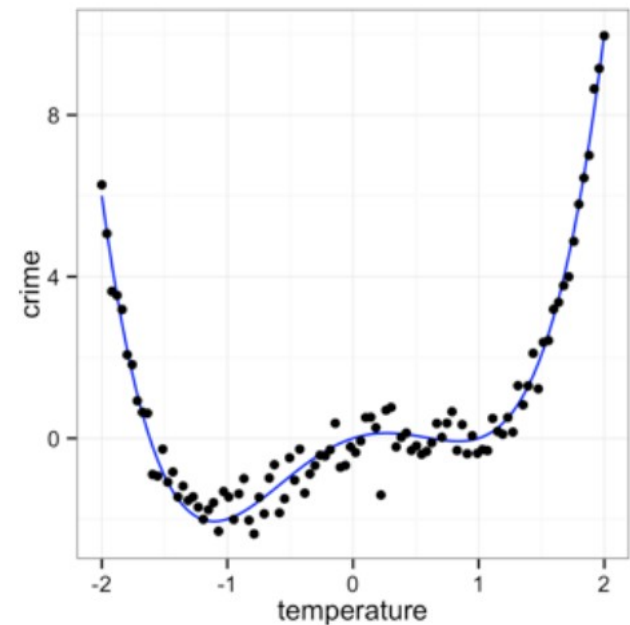
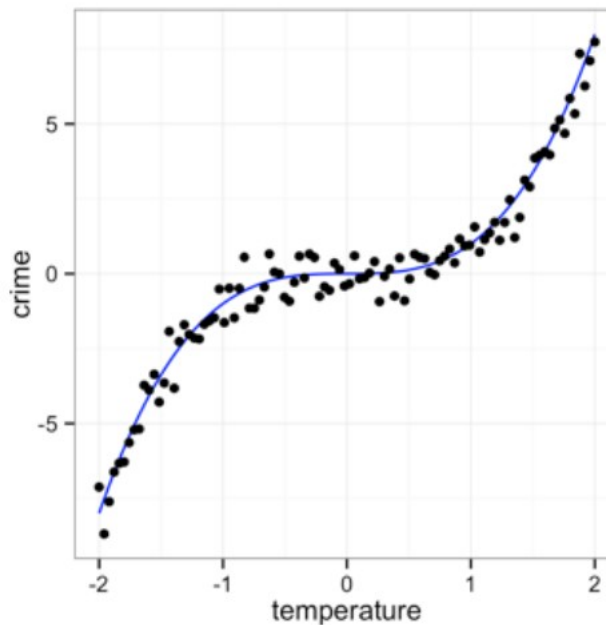
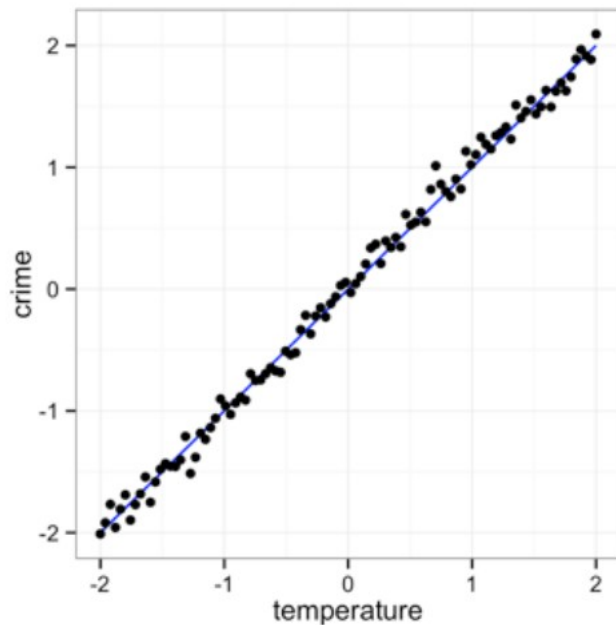
# Functions: the *stuff* behind the models

- If one variable completely determines another, every  $(x, y)$  data point will fall on the **function** line.



# Relationships Between Variables Is Messy

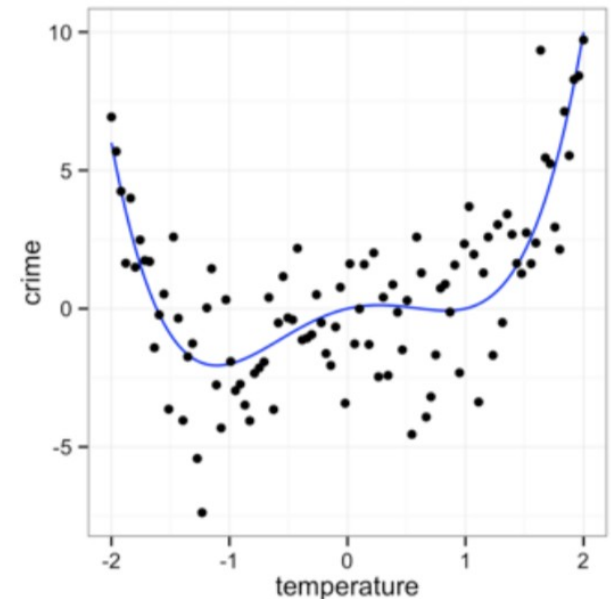
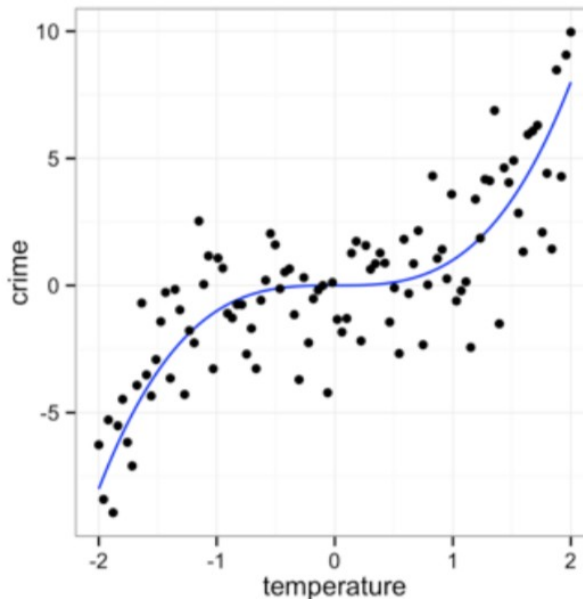
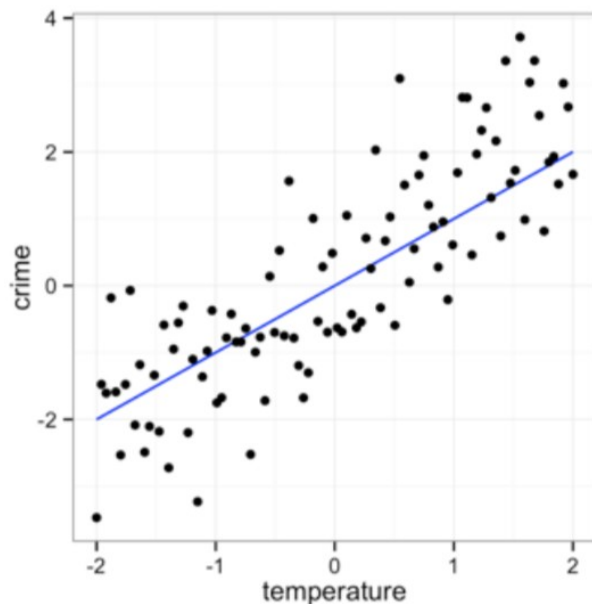
- This is what real data looks like on a good day!





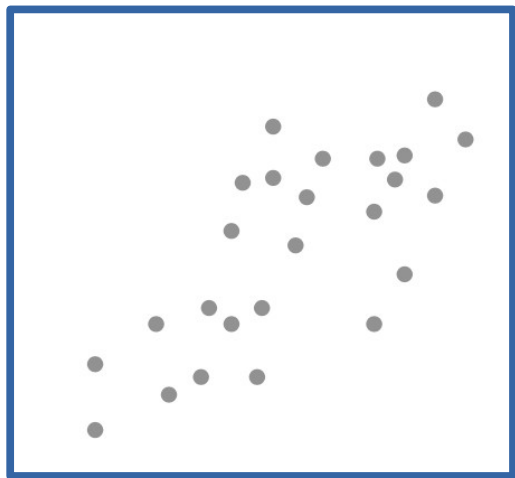
# Relationships Between Variables

- If the actual relationship is affected by other variables, data points may not fall directly on the function line.
- **Noise**: The greater the effect of other variables, the weaker the relationship. This is normally the situation with real data.



# So, A Model, Then?

- Noise is what we get in data when not every point does *what it is supposed to do*.
- Modeling *attempts* to *more-correctly* identify relationships in noisy data.



Data

Algorithm

Ask  
What  
If ... ?

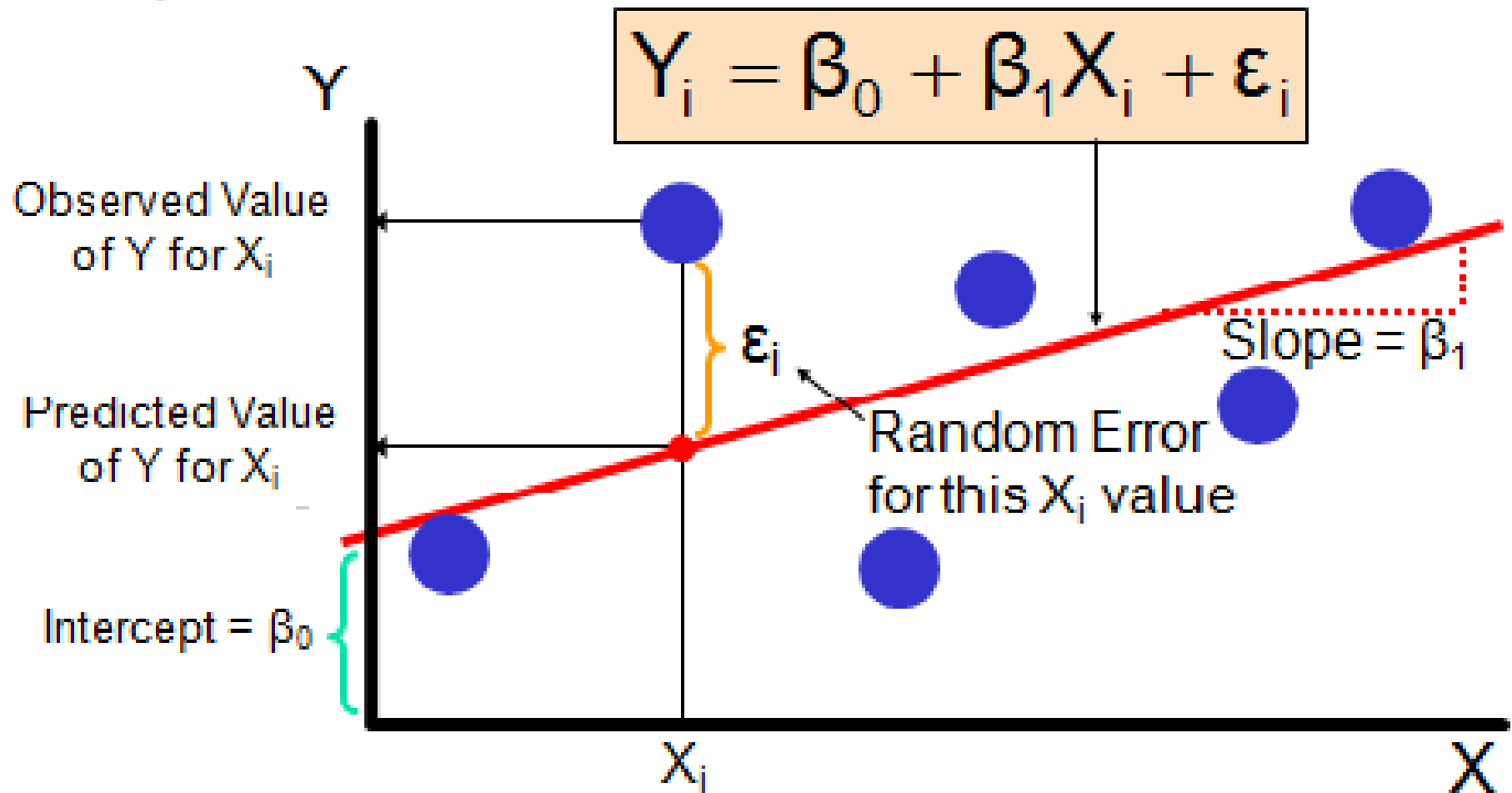
Model



# Let's Talk Linear Models

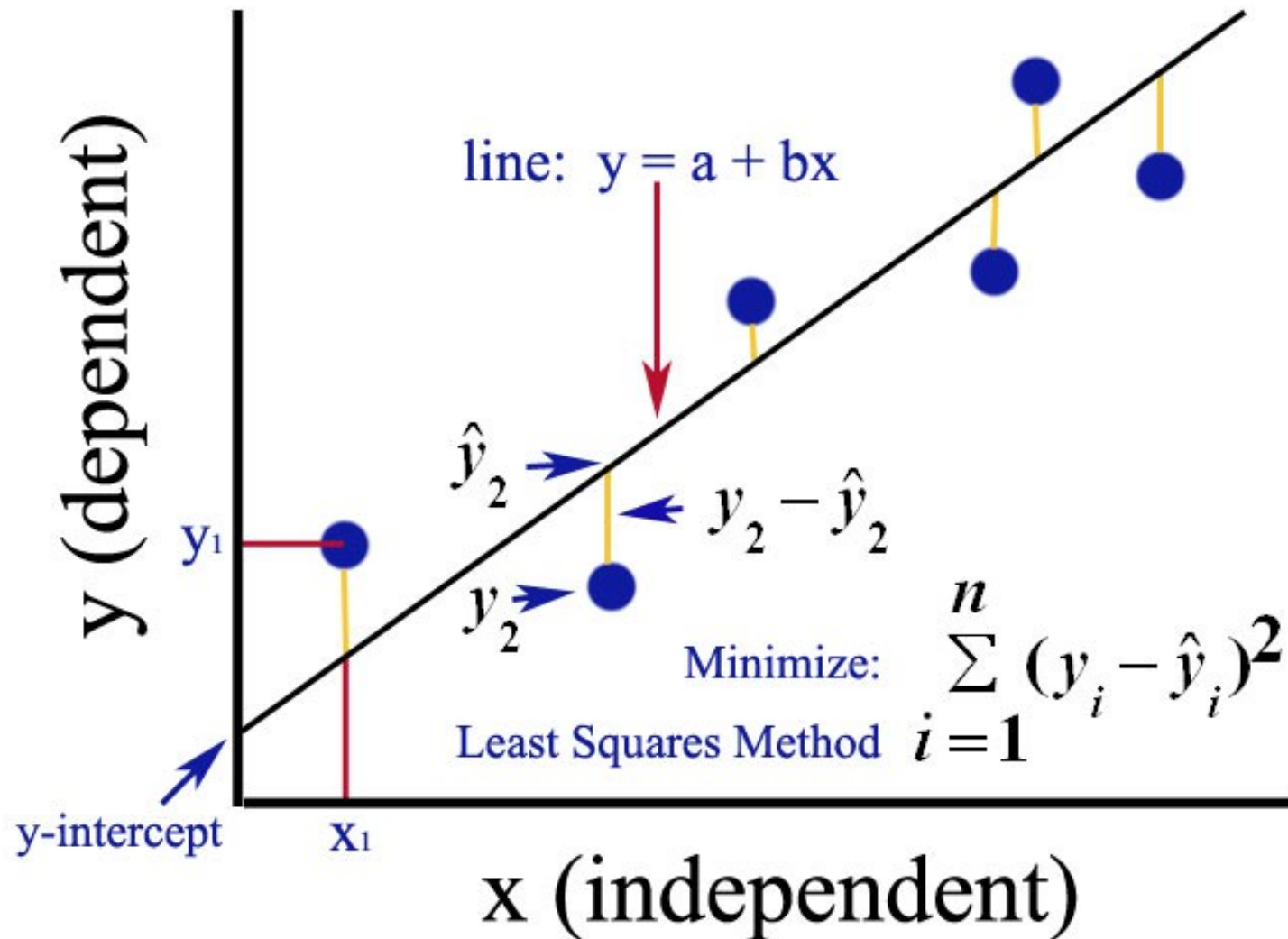
- Linear regression, formally is:
- The linear regression algorithm constrains  $f(x)$  to have the form:
- $f(x) = \alpha + \beta x + \epsilon$ 
  - Line formula alpha: intercept.
  - Beta: slope
  - Epsilon: account for the error
- *Note:*  $f(x)$  will be a straight line in  $x$

# Let's Talk Linear Models



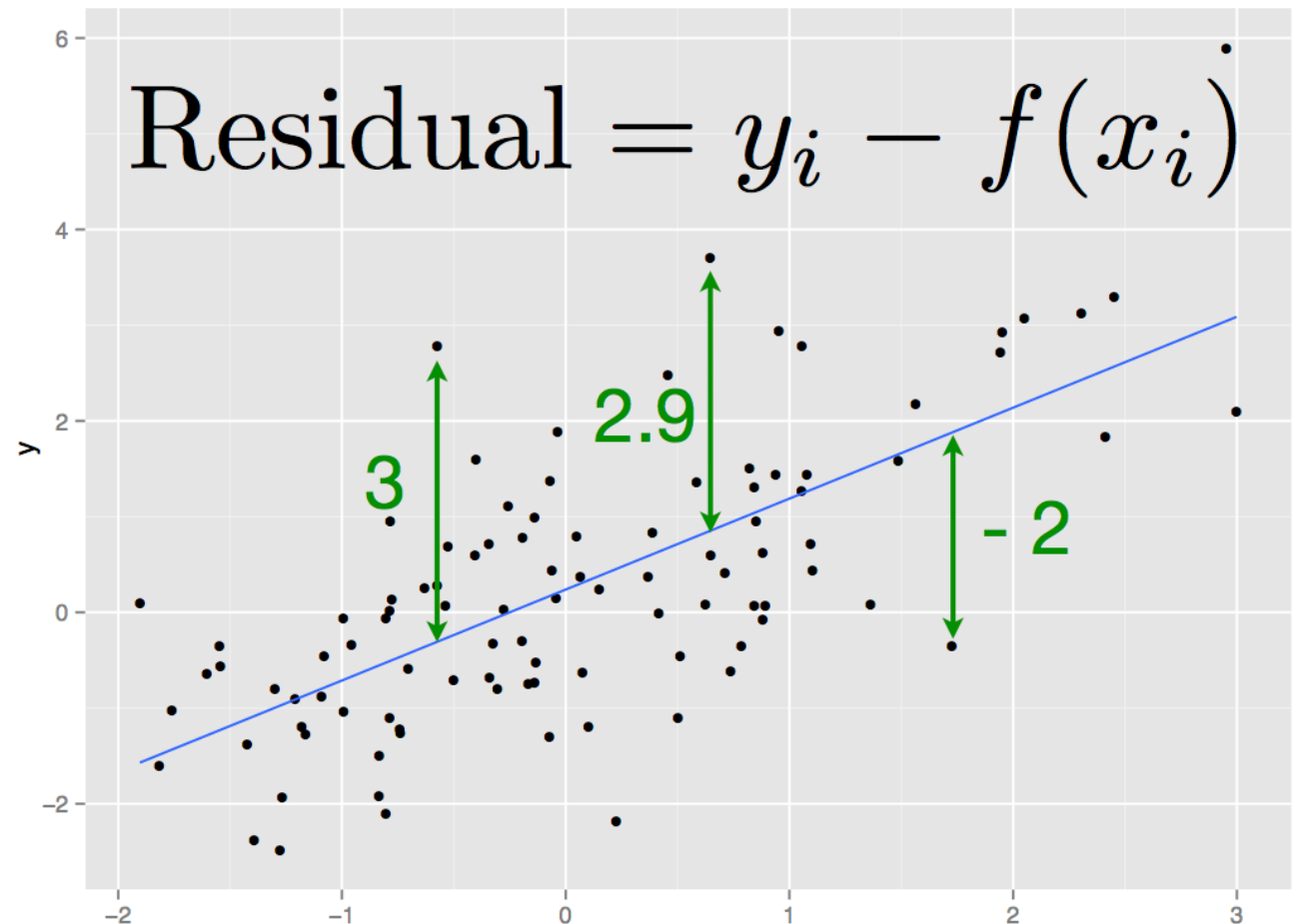


# Another Linear Model



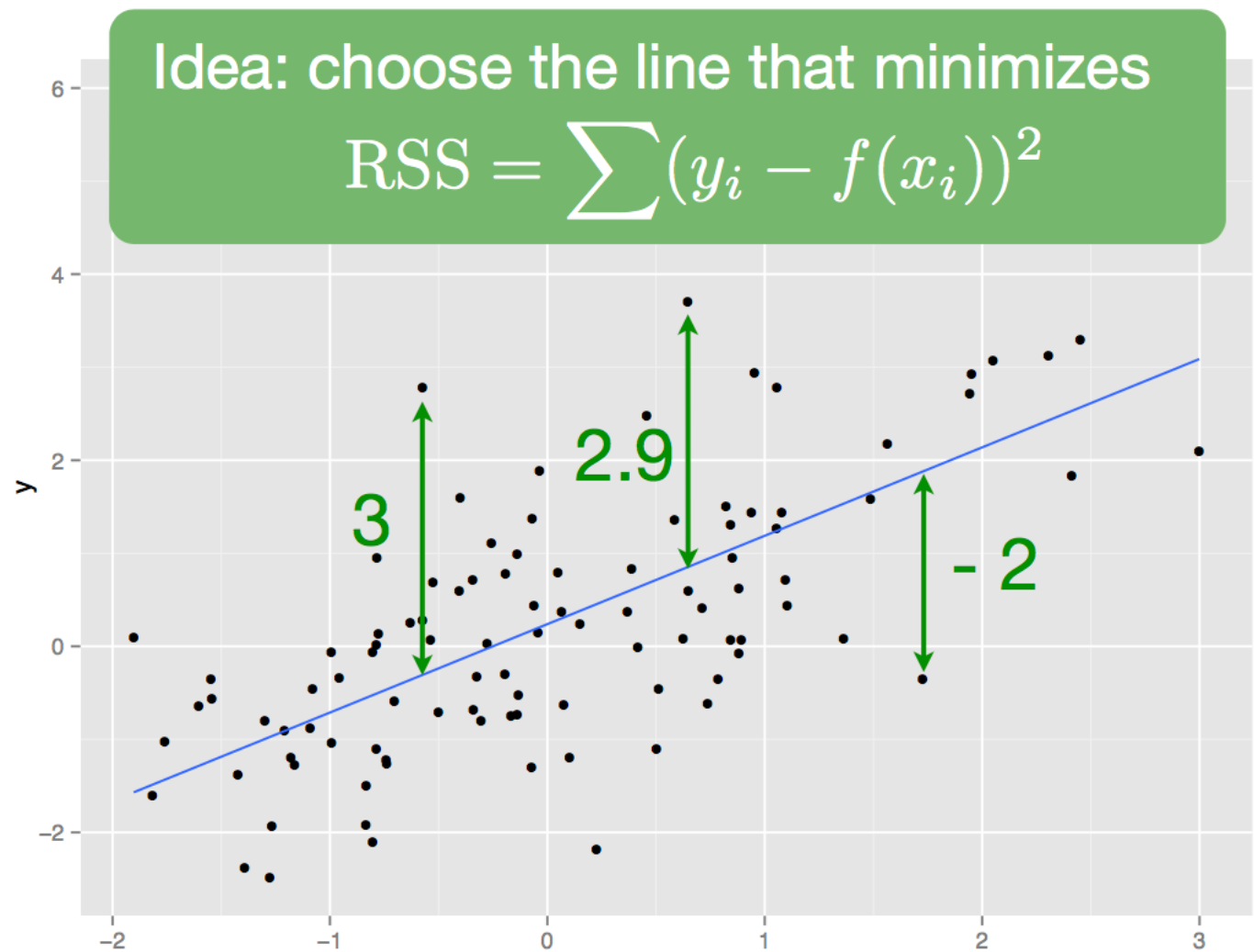
# How To Best Draw a Line Through The Data?

- A *residual* of an observed value is the difference between the observed value and the estimated value of the quantity of interest



# How To Best Draw a Line Through The Data?

- Residual sum of squares (RSS), also known as the sum of squared residuals (SSR) or the sum of squared errors of prediction (SSE)
- The sum of the squares of residuals (deviations predicted from actual empirical values of data).



# Types of Questions to Address With Data

Do you think that hotter places have more crime?

File: [crime.csv](#)



Do you think that taller people make more money?

File: [wages.csv](#)

# Crime Data Set



- Is there a relationship between crime and temperature?  
State statistics from 2009.

```
# open the crime dataset from the data.  
c <- file.choose() # set the filename  
crime <- read.csv(c) # load and read the data.
```



# Crime Data Set

```
View(crime) #or  
tbl_df(crime)
```

	state	abbr	low	murder	tc2009
	<chr>	<chr>	<int>	<dbl>	<dbl>
1	Alabama	AL	-27	7.1	4337.5
2	Alaska	AK	-80	3.2	3567.1
3	Arizona	AZ	-40	5.5	3725.2
4	Arkansas	AR	-29	6.3	4415.4
5	California	CA	-45	5.4	3201.6
6	Colorado	CO	-61	3.2	3024.5
7	Connecticut	CT	-32	3.0	2646.3
8	Delaware	DE	-17	4.6	3996.8
9	Florida	FL	-2	5.5	4453.7
10	Georgia	GA	-17	6.0	4180.6
...					

Yearly low temp

Murder rate

Training data



# Let's Hit the Code

- How much *low (indep)* influence *tc2009 (dep)*
- Linear model syntax

lm

Model formula:  
response ~ predictor(s)

data

```
mod <- lm(tc2009 ~ low, data = crime)
```



# Formulas

- R formulas are expressions built with ~ (tilda)

```
tc2009 ~ low
```

```
# gives: tc2009 ~ low
```

```
class(tc2009 ~ low)
```

```
# gives: [1] "formula"
```





# Formulas

- Formulas only need to include the response and predictor variables

$$y = f(x) = \alpha + \beta x + \epsilon$$

#Syntax to Build the linear model:

$$y \sim x$$



# Formulas

response ~ explanatory

dependent ~ independent

outcome ~ predictors

# Make a model called, *mod*

```
mod <- lm(tc2009 ~ low, data = crime)
```



# Results: summary(mod)

mod

Call:

```
lm(formula = tc2009 ~ low, data = crime)
```

Coefficients:

(Intercept)	low
4256.86	21.65



# Results: summary(mod)

## summary(mod)

Call:

```
lm(formula = tc2009 ~ low, data = crime)
```

Residuals:

Min	1Q	Median	3Q	Max
-1134.36	-647.13	98.03	533.62	1344.30

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	4256.86	233.44	18.236	< 2e-16	***
low	21.65	5.33	4.061	0.000188	***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 649.9 on 46 degrees of freedom

Multiple R-squared: 0.2639, Adjusted R-squared: 0.2479

F-statistic: 16.49 on 1 and 46 DF, p-value: 0.000188



# Extracting Info

- Create model object
- Run functions on model object to get details

Try these commands

```
summary(mod)
```

```
predict(mod) # predictions at original vals
```

```
resid(mod) # residuals
```



# Consider This!

- Fit a linear model to the crime data set.
- Predict **tc2009** (dep) with **low** (ind).  
What are the model's **A** and **B** variables? Hint: use `lm()`

$$Y = \underline{A} + \underline{B} * X + \epsilon$$

THINK



# Let's Hit the Code

- We run the code
- Next time, we interpret these results.